# NumPy Reference 

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## Written by the NumPy community

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## Release

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This reference manual details functions, modules, and objects included in Numpy, describing what they are and what they do. For learning how to use NumPy, see also user.

## CHAPTER

ONE

## ARRAY OBJECTS

NumPy provides an N-dimensional array type, the ndarray, which describes a collection of "items" of the same type. The items can be indexed using for example N integers.

All ndarrays are homogenous: every item takes up the same size block of memory, and all blocks are interpreted in exactly the same way. How each item in the array is to be interpreted is specified by a separate data-type object, one of which is associated with every array. In addition to basic types (integers, floats, etc.), the data type objects can also represent data structures.

An item extracted from an array, e.g., by indexing, is represented by a Python object whose type is one of the array scalar types built in Numpy. The array scalars allow easy manipulation of also more complicated arrangements of data.


Figure 1.1: Figure Conceptual diagram showing the relationship between the three fundamental objects used to describe the data in an array: 1) the ndarray itself, 2) the data-type object that describes the layout of a single fixed-size element of the array, 3) the array-scalar Python object that is returned when a single element of the array is accessed.

### 1.1 The N -dimensional array (ndarray)

An ndarray is a (usually fixed-size) multidimensional container of items of the same type and size. The number of dimensions and items in an array is defined by its shape, which is a tuple of $N$ positive integers that specify the sizes of each dimension. The type of items in the array is specified by a separate data-type object (dtype), one of which is associated with each ndarray.

As with other container objects in Python, the contents of an ndarray can be accessed and modified by indexing or slicing the array (using, for example, $N$ integers), and via the methods and attributes of the ndarray. Different
ndarrays can share the same data, so that changes made in one ndarray may be visible in another. That is, an ndarray can be a "view" to another ndarray, and the data it is referring to is taken care of by the "base" ndarray. ndarrays can also be views to memory owned by Python strings or objects implementing the buffer or array interfaces.

## Example

A 2-dimensional array of size $2 \times 3$, composed of 4-byte integer elements:

```
>>> x = np.array([[1, 2, 3], [4, 5, 6]], np.int32)
>>> type(x)
<type 'numpy.ndarray'>
>>> x.shape
(2, 3)
>>> x.dtype
dtype('int32')
```

The array can be indexed using Python container-like syntax:

```
>>> x[1,2] # i.e., the element of x in the *second* row, *third*
column, namely, 6.
```

For example slicing can produce views of the array:

```
>>> y = x[:,1]
>>> y
array([2, 5])
>>> y[0] = 9 # this also changes the corresponding element in x
>>> y
array([9, 5])
>>> x
array([[1, 9, 3],
    [4, 5, 6]])
```


### 1.1.1 Constructing arrays

New arrays can be constructed using the routines detailed in Array creation routines, and also by using the low-level ndarray constructor:
ndarray An array object represents a multidimensional, homogeneous array of fixed-size items.
class numpy. ndarray
An array object represents a multidimensional, homogeneous array of fixed-size items. An associated data-type object describes the format of each element in the array (its byte-order, how many bytes it occupies in memory, whether it is an integer, a floating point number, or something else, etc.)

Arrays should be constructed using array, zeros or empty (refer to the See Also section below). The parameters given here refer to a low-level method (ndarray(...)) for instantiating an array.

For more information, refer to the numpy module and examine the the methods and attributes of an array.

```
Parameters
    (for the __new__ method; see Notes below) :
    shape : tuple of ints
```

        Shape of created array.
    dtype : data-type, optional
    Any object that can be interpreted as a numpy data type.
buffer : object exposing buffer interface, optional
Used to fill the array with data.
offset : int, optional
Offset of array data in buffer.
strides : tuple of ints, optional
Strides of data in memory.
order : \{ 'C', 'F'\}, optional
Row-major or column-major order.

## See Also:

```
array
```

Construct an array.

```
zeros
```

Create an array, each element of which is zero.
empty
Create an array, but leave its allocated memory unchanged (i.e., it contains "garbage").
dtype
Create a data-type.

## Notes

There are two modes of creating an array using $\qquad$ new $\qquad$ :
1.If buffer is None, then only shape, dtype, and order are used.
2.If buffer is an object exposing the buffer interface, then all keywords are interpreted.

No $\qquad$ init $\qquad$ method is needed because the array is fully initialized after the $\qquad$ new_ method.

## Examples

These examples illustrate the low-level ndarray constructor. Refer to the See Also section above for easier ways of constructing an ndarray.
First mode, buffer is None:

```
>>> np.ndarray(shape=(2,2), dtype=float, order='F')
array([[ -1.13698227e+002, 4.25087011e-303],
    [ 2.88528414e-306, 3.27025015e-309]]) #random
```

Second mode:

```
>>> np.ndarray((2,), buffer=np.array([1,2,3]),
... offset=np.int_().itemsize,
... dtype=int) # offset = I*itemsize, i.e. skip first element
array([2, 3])
```


## Attributes

| T |  |
| :--- | :--- |
| data |  |
| dtype | Create a data type object. |
| flags |  |
| flat |  |
| imag(val) | Return the imaginary part of the elements of the array. |
| real(val) | Return the real part of the elements of the array. |
| size(a[, axis]) | Return the number of elements along a given axis. |
| itemsize | Base object for a dictionary for look-up with any alias for an array dtype. |
| nbytes | Return the number of dimensions of an array. |
| ndim(a) | Return the shape of an array. |
| shape(a) |  |
| strides | create and manipulate C data types in Python |
| ctypes |  |

class numpy. dtype
Create a data type object.
A numpy array is homogeneous, and contains elements described by a dtype object. A dtype object can be constructed from different combinations of fundamental numeric types.

## Parameters <br> obj :

Object to be converted to a data type object.
align : bool, optional
Add padding to the fields to match what a C compiler would output for a similar C -
struct. Can be True only if $o b j$ is a dictionary or a comma-separated string.
copy : bool, optional
Make a new copy of the data-type object. If False, the result may just be a reference to a built-in data-type object.

## Examples

Using array-scalar type:

```
>>> np.dtype(np.int16)
dtype('int16')
```

Record, one field name ' f 1 ', containing int 16 :

```
>>> np.dtype([('f1', np.int16)])
dtype([('f1', '<i2')])
```

Record, one field named ' f 1 ', in itself containing a record with one field:

```
>>> np.dtype([('f1', [('f1', np.int16)])])
dtype([('f1', [('f1', '<i2')])])
```

Record, two fields: the first field contains an unsigned int, the second an int32:

```
>>> np.dtype([('f1', np.uint), ('f2', np.int32)])
dtype([('f1', '<u4'), ('f2', '<i4')])
```

Using array-protocol type strings:

```
>>> np.dtype([('a','f8'),('b','S10')])
dtype([('a', '<f8'), ('b', '|S10')])
```

Using comma-separated field formats. The shape is $(2,3)$ :

```
>>> np.dtype("i4, (2,3)f8")
dtype([('f0', '<i4'), ('f1', '<f8', (2, 3))])
```

Using tuples. int is a fixed type, 3 the field's shape. void is a flexible type, here of size 10 :

```
>>> np.dtype([('hello',(np.int,3)),('world',np.void,10)])
dtype([('hello', '<i4', 3), ('world', '|V10')])
```

Subdivide int 16 into 2 int 8 's, called $x$ and $y .0$ and 1 are the offsets in bytes:

```
>>> np.dtype((np.int16, {'x':(np.int8,0), 'y':(np.int8,1)}))
dtype(('<i2', [('x', '|i1'), ('y', '|i1')]))
```

Using dictionaries. Two fields named 'gender' and 'age':

```
>>> np.dtype({'names':['gender','age'], 'formats':['S1',np.uint8]})
dtype([('gender', '|S1'), ('age', '|u1')])
```

Offsets in bytes, here 0 and 25:

```
>>> np.dtype({'surname':('S25',0),'age':(np.uint8,25)})
dtype([('surname', '|S25'), ('age', '|u1')])
```


## Methods

```
newbyteorder
```

numpy.imag (val)
Return the imaginary part of the elements of the array.

## Parameters

val : array_like
Input array.

## Returns

out : ndarray
Output array. If val is real, the type of val is used for the output. If $v a l$ has complex elements, the returned type is float.

## See Also:

real, angle, real_if_close

## Examples

```
>>> a = np.array([1+2j, 3+4j, 5+6j])
>>> a.imag
array([ 2., 4., 6.])
>>> a.imag = np.array([8, 10, 12])
>>> a
array([ 1. +8.j, 3.+10.j, 5.+12.j])
```

numpy.real (val)
Return the real part of the elements of the array.

## Parameters

val : array_like
Input array.

## Returns

out : ndarray
Output array. If val is real, the type of val is used for the output. If val has complex elements, the returned type is float.

## See Also:

```
real_if_close,imag, angle
Examples
```

```
>>> a = np.array([1+2j, 3+4j, 5+6j])
>>> a.real
array([ 1., 3., 5.])
>>> a.real = 9
>>> a
array([ 9.+2.j, 9.+4.j, 9.+6.j])
>>> a.real = np.array([9, 8, 7])
>>> a
array([ 9.+2.j, 8.+4.j, 7.+6.j])
```


## Methods



Table 1.1 - continued from previous page

```
newbyteorder
nonzero(a) Return the indices of the elements that are non-zero.
prod(a[, axis, dtype, out]) Return the product of array elements over a given axis.
ptp(a[, axis, out]) Range of values (maximum - minimum) along an axis.
put(a, ind, v[, mode]) Replaces specified elements of an array with given values.
ravel(a[, order]) Return a flattened array.
repeat(a, repeats[, axis]) Repeat elements of an array.
reshape(a, newshape[, order]) Gives a new shape to an array without changing its data.
resize(a, new_shape)
round(a[, decimals, out])
searchsorted(a, v[, side]) Find indices where elements should be inserted to maintain order.
setasflat
setfield
setflags
sort(a[, axis, kind, order]) Return a sorted copy of an array.
squeeze(a)
std(a[, axis, dtype, out, ddof])
```



```
take(a, indices[, axis, out, mode]) Take elements from an array along an axis.
tofile
tolist
tostring
trace(a[,offset, axis1, axis2, dtype, out]) Return the sum along diagonals of the array.
transpose(a[, axes]) Permute the dimensions of an array.
var(a[, axis, dtype, out, ddof]) Compute the variance along the specified axis.
view
```

numpy.all (a, axis=None, out=None)
Test whether all array elements along a given axis evaluate to True.

## Parameters

a : array_like
Input array or object that can be converted to an array.
axis : int, optional
Axis along which a logical AND is performed. The default (axis = None) is to perform a logical AND over a flattened input array. axis may be negative, in which case it counts from the last to the first axis.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output and its type is preserved (e.g., if dtype (out) is float, the result will consist of 0.0 's and 1.0 's). See doc.ufuncs (Section "Output arguments") for more details.

## Returns

all : ndarray, bool
A new boolean or array is returned unless out is specified, in which case a reference to out is returned.

## See Also:

ndarray.all
equivalent method
any
Test whether any element along a given axis evaluates to True.

## Notes

Not a Number (NaN), positive infinity and negative infinity evaluate to True because these are not equal to zero.

Examples

```
>>> np.all([[True,False],[True,True]])
False
>>> np.all([[True,False],[True,True]], axis=0)
array([ True, False], dtype=bool)
>>> np.all([-1, 4, 5])
True
>>> np.all([1.0, np.nan])
True
>>> o=np.array([False])
>>> z=np.all([-1, 4, 5], out=0)
>>> id(z), id(o), z
(28293632, 28293632, array([ True], dtype=bool))
```

numpy . any ( $a$, axis=None, out=None)
Test whether any array element along a given axis evaluates to True.
Returns single boolean unless axis is not None

## Parameters

a : array_like
Input array or object that can be converted to an array.
axis : int, optional
Axis along which a logical OR is performed. The default (axis $=$ None $)$ is to perform a logical OR over a flattened input array. axis may be negative, in which case it counts from the last to the first axis.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output and its type is preserved (e.g., if it is of type float, then it will remain so, returning 1.0 for True and 0.0 for False, regardless of the type of $a$ ). See doc.ufuncs (Section "Output arguments") for details.

## Returns

any : bool or ndarray
A new boolean or ndarray is returned unless out is specified, in which case a reference to out is returned.

## See Also:

ndarray.any
equivalent method
all
Test whether all elements along a given axis evaluate to True.

## Notes

Not a Number (NaN), positive infinity and negative infinity evaluate to True because these are not equal to zero.

Examples

```
>>> np.any([[True, False], [True, True]])
True
>>> np.any([[True, False], [False, False]], axis=0)
array([ True, False], dtype=bool)
>>> np.any([-1, 0, 5])
True
>>> np.any(np.nan)
True
>>> o=np.array([False])
>>> z=np.any([-1, 4, 5], out=o)
>>> z, o
(array([ True], dtype=bool), array([ True], dtype=bool))
>>> # Check now that z is a reference to o
>>> z is O
True
>>> id(z), id(o) # identity of z and o
(191614240, 191614240)
```

numpy .argmax ( $a$, axis=None)
Indices of the maximum values along an axis.

## Parameters

a : array_like
Input array.
axis : int, optional
By default, the index is into the flattened array, otherwise along the specified axis.

## Returns

index_array : ndarray of ints
Array of indices into the array. It has the same shape as a.shape with the dimension along axis removed.

## See Also:

ndarray.argmax, argmin
amax
The maximum value along a given axis.
unravel_index
Convert a flat index into an index tuple.

## Notes

In case of multiple occurrences of the maximum values, the indices corresponding to the first occurrence are returned.

## Examples

```
>>> a = np.arange(6).reshape(2,3)
>>> a
array([[0, 1, 2],
        [3, 4, 5]])
>>> np.argmax(a)
5
>>> np.argmax(a, axis=0)
array([1, 1, 1])
>>> np.argmax(a, axis=1)
array([2, 2])
>>> b = np.arange(6)
>>> b[1] = 5
>>> b
array([0, 5, 2, 3, 4, 5])
>>> np.argmax(b) # Only the first occurrence is returned.
1
```

numpy . argmin (a, axis=None)

Return the indices of the minimum values along an axis.

## See Also:

argmax
Similar function. Please refer to numpy. argmax for detailed documentation.
numpy. argsort ( a, axis=-1, kind='quicksort', order=None)
Returns the indices that would sort an array.
Perform an indirect sort along the given axis using the algorithm specified by the kind keyword. It returns an array of indices of the same shape as $a$ that index data along the given axis in sorted order.

## Parameters

a : array_like
Array to sort.
axis : int or None, optional
Axis along which to sort. The default is -1 (the last axis). If None, the flattened array is used.
kind : \{ 'quicksort', 'mergesort', 'heapsort'\}, optional
Sorting algorithm.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## Returns

index_array : ndarray, int
Array of indices that sort $a$ along the specified axis. In other words, a [index_array] yields a sorted $a$.

## See Also:

sort
Describes sorting algorithms used.
lexsort
Indirect stable sort with multiple keys.
ndarray.sort
Inplace sort.

## Notes

See sort for notes on the different sorting algorithms.
As of NumPy 1.4.0 argsort works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

One dimensional array:

```
>>> x = np.array([3, 1, 2])
>>> np.argsort(x)
array([1, 2, 0])
```

Two-dimensional array:

```
>>> x = np.array([[0, 3], [2, 2]])
>>> x
array([[0, 3],
    [2, 2]])
>>> np.argsort(x, axis=0)
array([[0, 1],
    [1, 0]])
>>> np.argsort(x, axis=1)
array([[0, 1],
    [0, 1]])
```

Sorting with keys:

```
>>> x = np.array([(1, 0), (0, 1)], dtype=[('x', '<i4'), ('y', '<i4')])
>>> x
array([(1, 0), (0, 1)],
    dtype=[('x', '<i4'), ('y', '<i4')])
>>> np.argsort(x, order=('x','y'))
array([1, 0])
>>> np.argsort(x, order=('y',' ('))
array([0, 1])
```

numpy. choose (a, choices, out=None, mode='raise')
Construct an array from an index array and a set of arrays to choose from.
First of all, if confused or uncertain, definitely look at the Examples - in its full generality, this function is less simple than it might seem from the following code description (below ndi $=$ numpy.lib.index_tricks):
np. choose (a, c) == np.array([c[a[I]][I] for I in ndi.ndindex(a.shape)]).
But this omits some subtleties. Here is a fully general summary:
Given an "index" array ( $a$ ) of integers and a sequence of $n$ arrays (choices), $a$ and each choice array are first broadcast, as necessary, to arrays of a common shape; calling these Ba and Bchoices[i], $i=0, \ldots, n-1$ we have that, necessarily, Ba.shape $==$ Bchoices[i].shape for each $i$. Then, a new array with shape Ba. shape is created as follows:
-if mode=raise (the default), then, first of all, each element of $a$ (and thus $B a$ ) must be in the range $[0, n-1]$; now, suppose that $i$ (in that range) is the value at the $(j 0, j 1, \ldots, j m)$ position in $B a$ - then the value at the same position in the new array is the value in Bchoices [i] at that same position;
-if mode=wrap, values in $a$ (and thus $B a$ ) may be any (signed) integer; modular arithmetic is used to map integers outside the range [0, n-1] back into that range; and then the new array is constructed as above;
-if mode=clip, values in $a$ (and thus $B a$ ) may be any (signed) integer; negative integers are mapped to 0 ; values greater than $n-1$ are mapped to $n-1$; and then the new array is constructed as above.

## Parameters

a : int array
This array must contain integers in [0, n-1], where $n$ is the number of choices, unless mode=wrap or mode=clip, in which cases any integers are permissible.
choices : sequence of arrays
Choice arrays. $a$ and all of the choices must be broadcastable to the same shape. If choices is itself an array (not recommended), then its outermost dimension (i.e., the one corresponding to choices.shape [0]) is taken as defining the "sequence".
out : array, optional
If provided, the result will be inserted into this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise' (default), 'wrap', 'clip'\}, optional
Specifies how indices outside [ $0, n-1$ ] will be treated:

- 'raise' : an exception is raised
- 'wrap' : value becomes value $\bmod n$
- 'clip' : values $<0$ are mapped to 0 , values $>\mathrm{n}-1$ are mapped to $\mathrm{n}-1$


## Returns

merged_array : array
The merged result.

## Raises

## ValueError: shape mismatch :

If $a$ and each choice array are not all broadcastable to the same shape.

## See Also:

ndarray. choose
equivalent method

## Notes

To reduce the chance of misinterpretation, even though the following "abuse" is nominally supported, choices should neither be, nor be thought of as, a single array, i.e., the outermost sequence-like container should be either a list or a tuple.

## Examples

```
>>> choices = [[0, 1, 2, 3], [10, 11, 12, 13],
... [20, 21, 22, 23], [30, 31, 32, 33]]
>>> np.choose([2, 3, 1, 0], choices
... # the first element of the result will be the first element of the
... # third (2+1) "array" in choices, namely, 20; the second element
... # will be the second element of the fourth (3+1) choice array, i.e.,
... # 31, etc.
... )
array([20, 31, 12, 3])
>>> np.choose([2, 4, 1, 0], choices, mode='clip') # 4 goes to 3 (4-1)
array([20, 31, 12, 3])
>>> # because there are 4 choice arrays
>>> np.choose([2, 4, 1, 0], choices, mode='wrap') # 4 goes to (4 mod 4)
array([20, 1, 12, 3])
>>> # i.e., 0
```

A couple examples illustrating how choose broadcasts:

```
>>> a = [[1, 0, 1], [0, 1, 0], [1, 0, 1]]
>>> choices = [-10, 10]
>>> np.choose(a, choices)
array([[ 10, -10, 10],
    [-10, 10, -10],
    [ 10, -10, 10]])
>>> # With thanks to Anne Archibald
>>> a = np.array([0, 1]).reshape((2,1,1))
>>> c1 = np.array([1, 2, 3]).reshape((1,3,1))
>>> c2 = np.array([-1, -2, -3, -4, -5]).reshape((1,1,5))
>>> np.choose(a, (c1, c2)) # result is 2x3\times5, res[0,:,:]=c1, res[1,:,:]=c2
array([[[ 1, 1, 1, 1, 1],
    [ 2, 2, 2, 2, 2],
    [ 3, 3, 3, 3, 3]],
    [[-1, -2, -3, -4, -5],
        [-1, -2, -3, -4, -5],
        [-1, -2, -3, -4, -5]]])
```

numpy.clip ( $a, a \_$min, $a \_$max, out=None)
Clip (limit) the values in an array.
Given an interval, values outside the interval are clipped to the interval edges. For example, if an interval of $[0,1]$ is specified, values smaller than 0 become 0 , and values larger than 1 become 1 .

## Parameters

a : array_like
Array containing elements to clip.
a_min : scalar or array_like
Minimum value.
a_max : scalar or array_like

Maximum value. If $a \_m i n$ or $a \_m a x$ are array_like, then they will be broadcasted to the shape of $a$.
out : ndarray, optional
The results will be placed in this array. It may be the input array for in-place clipping. out must be of the right shape to hold the output. Its type is preserved.

## Returns

clipped_array : ndarray
An array with the elements of $a$, but where values $<a_{-} \min$ are replaced with $a \_m i n$, and those > a_max with $a \_m a x$.

## See Also:

numpy.doc.ufuncs
Section "Output arguments"

## Examples

```
>>> a = np.arange(10)
>>> np.clip(a, 1, 8)
array([1, 1, 2, 3, 4, 5, 6, 7, 8, 8])
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, 3, 6, out=a)
array([3, 3, 3, 3, 4, 5, 6, 6, 6, 6])
>>> a = np.arange(10)
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, [3,4,1,1,1,4,4,4,4,4], 8)
array([3, 4, 2, 3, 4, 5, 6, 7, 8, 8])
```

numpy. compress (condition, a, axis=None, out=None)
Return selected slices of an array along given axis.
When working along a given axis, a slice along that axis is returned in output for each index where condition evaluates to True. When working on a 1-D array, compress is equivalent to extract.

## Parameters

condition : 1-D array of bools
Array that selects which entries to return. If len(condition) is less than the size of $a$ along the given axis, then output is truncated to the length of the condition array.
a : array_like
Array from which to extract a part.
axis : int, optional
Axis along which to take slices. If None (default), work on the flattened array.
out : ndarray, optional
Output array. Its type is preserved and it must be of the right shape to hold the output.

## Returns

compressed_array : ndarray
A copy of $a$ without the slices along axis for which condition is false.

## See Also:

take, choose, diag, diagonal, select
ndarray. compress
Equivalent method.
numpy.doc.ufuncs
Section "Output arguments"

## Examples

```
>>> a = np.array([[1, 2], [3, 4], [5, 6]])
>>> a
array([[1, 2],
        [3, 4],
        [5, 6]])
>>> np.compress([0, 1], a, axis=0)
array([[3, 4]])
>>> np.compress([False, True, True], a, axis=0)
array([[3, 4],
    [5, 6]])
>>> np.compress([False, True], a, axis=1)
array([[2],
    [4],
    [6]])
```

Working on the flattened array does not return slices along an axis but selects elements.

```
>>> np.compress([False, True], a)
array([2])
```

numpy.conj( $x[$, out $]$ )
Return the complex conjugate, element-wise.
The complex conjugate of a complex number is obtained by changing the sign of its imaginary part.

## Parameters

$\mathbf{x}$ : array_like
Input value.

## Returns

y : ndarray
The complex conjugate of $x$, with same dtype as $y$.

## Examples

```
>>> np.conjugate(1+2j)
(1-2j)
>>> x = np.eye(2) + 1j * np.eye(2)
>>> np.conjugate(x)
array([[ 1.-1.j, 0.-0.j],
            [ 0.-0.j, 1.-1.j]])
```

numpy. copy (a)
Return an array copy of the given object.

## Parameters

a : array_like

Input data.

## Returns

arr : ndarray
Array interpretation of $a$.

## Notes

This is equivalent to

```
>>> np.array(a, copy=True)
```


## Examples

Create an array x , with a reference y and a copy z :

```
>>> x = np.array([1, 2, 3])
>>> y = x
>>> z = np.copy(x)
```

Note that, when we modify $x, y$ changes, but not $z$ :

```
>>> x[0] = 10
>>> x[0] == y[0]
True
>>> x[0] == z[0]
False
```

numpy. cumprod (a, axis=None, dtype=None, out=None)

Return the cumulative product of elements along a given axis.

## Parameters

a: array_like
Input array.
axis : int, optional
Axis along which the cumulative product is computed. By default the input is flattened.
dtype : dtype, optional
Type of the returned array, as well as of the accumulator in which the elements are multiplied. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used instead.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type of the resulting values will be cast if necessary.

## Returns

cumprod : ndarray
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

See Also:
numpy.doc.ufuncs
Section "Output arguments"

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> a = np.array([1,2,3])
>>> np.cumprod(a) # intermediate results 1, 1*2
... # total product 1*2*3 = 6
array([1, 2, 6])
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
>>> np.cumprod(a, dtype=float) # specify type of output
array([ 1., 2., 6., 24., 120., 720.])
```

The cumulative product for each column (i.e., over the rows) of $a$ :

```
>>> np.cumprod(a, axis=0)
array([[ 1, 2, 3],
    [ 4, 10, 18]])
```

The cumulative product for each row (i.e. over the columns) of $a$ :

```
>>> np.cumprod(a,axis=1)
array([[ 1, 2, 6],
    [ 4, 20, 120]])
```

numpy. cumsum ( $a$, axis=None, dtype $=$ None, out=None )
Return the cumulative sum of the elements along a given axis.

## Parameters

a : array_like
Input array.
axis : int, optional
Axis along which the cumulative sum is computed. The default (None) is to compute the cumsum over the flattened array.
dtype : dtype, optional
Type of the returned array and of the accumulator in which the elements are summed. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

cumsum_along_axis : ndarray.
A new array holding the result is returned unless out is specified, in which case a reference to out is returned. The result has the same size as $a$, and the same shape as $a$ if axis is not None or $a$ is a 1-d array.

## See Also:

sum
Sum array elements.
trapz
Integration of array values using the composite trapezoidal rule.

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> a
array([[1, 2, 3],
    [4, 5, 6]])
>>> np.cumsum(a)
array([ 1, 3, 6, 10, 15, 21])
>>> np.cumsum(a, dtype=float) # specifies type of output value(s)
array([ 1., 3., 6., 10., 15., 21.])
>>> np.cumsum(a,axis=0) # sum over rows for each of the 3 columns
array([[1, 2, 3],
    [5, 7, 9]])
>>> np.cumsum(a,axis=1) # sum over columns for each of the 2 rows
array([[ 1, 3, 6],
    [ 4, 9, 15]])
```

numpy.diagonal (a, offset $=0$, axis $1=0$, axis $2=1$ )
Return specified diagonals.
If $a$ is 2-D, returns the diagonal of $a$ with the given offset, i.e., the collection of elements of the form a [i, i+offset]. If $a$ has more than two dimensions, then the axes specified by axisl and axis 2 are used to determine the 2-D sub-array whose diagonal is returned. The shape of the resulting array can be determined by removing axisl and axis 2 and appending an index to the right equal to the size of the resulting diagonals.

## Parameters

a : array_like
Array from which the diagonals are taken.
offset : int, optional
Offset of the diagonal from the main diagonal. Can be positive or negative. Defaults to main diagonal (0).
axis1 : int, optional
Axis to be used as the first axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults to first axis (0).
axis2 : int, optional
Axis to be used as the second axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults to second axis (1).

## Returns

```
array_of_diagonals : ndarray
```

If $a$ is 2-D, a 1-D array containing the diagonal is returned. If the dimension of $a$ is larger, then an array of diagonals is returned, "packed" from left-most dimension to right-most (e.g., if $a$ is 3-D, then the diagonals are "packed" along rows).

## Raises

## ValueError :

If the dimension of $a$ is less than 2 .

## See Also:

diag
MATLAB work-a-like for 1-D and 2-D arrays.
diagflat
Create diagonal arrays.
trace
Sum along diagonals.

## Examples

```
>>> a = np.arange(4).reshape(2,2)
>>> a
array([[0, 1],
    [2, 3]])
>>> a.diagonal()
array([0, 3])
>>> a.diagonal(1)
array([1])
```

A 3-D example:

```
>>> a = np.arange(8).reshape(2,2,2); a
array([[[0, 1],
            [2, 3]],
            [[4, 5],
            [6, 7]]])
>>> a.diagonal(0, # Main diagonals of two arrays created by skipping
... 0, # across the outer(left)-most axis last and
... 1) # the "middle" (row) axis first.
array([[0, 6],
    [1, 7]])
```

The sub-arrays whose main diagonals we just obtained; note that each corresponds to fixing the right-most (column) axis, and that the diagonals are "packed" in rows.

```
>>> a[:,:,0] # main diagonal is [0 6]
array([[0, 2],
    [4, 6]])
>>> a[:,:,1] # main diagonal is [1 7]
array([[1, 3],
    [5, 7]])
```

numpy.dot ( $a, b$, out $=$ None)
Dot product of two arrays.
For 2-D arrays it is equivalent to matrix multiplication, and for 1-D arrays to inner product of vectors (without complex conjugation). For N dimensions it is a sum product over the last axis of $a$ and the second-to-last of $b$ :

```
dot(a, b)[i,j,k,m] = sum(a[i,j,:] * b[k,:,m])
```


## Parameters

a : array_like
First argument.
b : array_like
Second argument.
out : ndarray, optional
Output argument. This must have the exact kind that would be returned if it was not used. In particular, it must have the right type, must be C-contiguous, and its dtype must be the dtype that would be returned for $\operatorname{dot}(a, b)$. This is a performance feature. Therefore, if these conditions are not met, an exception is raised, instead of attempting to be flexible.

## Returns

output : ndarray
Returns the dot product of $a$ and $b$. If $a$ and $b$ are both scalars or both 1-D arrays then a scalar is returned; otherwise an array is returned. If out is given, then it is returned.

## Raises

## ValueError :

If the last dimension of $a$ is not the same size as the second-to-last dimension of $b$.

## See Also:

```
vdot
```

Complex-conjugating dot product.

```
tensordot
```

Sum products over arbitrary axes.
einsum
Einstein summation convention.

## Examples

```
>>> np.dot(3, 4)
12
```

Neither argument is complex-conjugated:

```
>>> np.dot([2j, 3j], [2j, 3j])
(-13+0j)
```

For 2-D arrays it's the matrix product:

```
>>>a=[[1, 0], [0, 1]]
>>> b = [[4, 1], [2, 2]]
>>> np.dot(a, b)
array([[4, 1],
    [2, 2]])
>>> a = np.arange( }3*4*5*6).reshape( (3,4,5,6)
>>> b = np.arange( }3*4*5*6) [::-1].reshape((5,4,6,3)
>>>np.dot(a, b) [2,3,2,1,2,2]
499128
```

```
>>> sum(a[2,3,2,:] * b[1,2,:,2])
499128
```

numpy .mean ( $a$, axis=None, dtype=None, out=None)
Compute the arithmetic mean along the specified axis.
Returns the average of the array elements. The average is taken over the flattened array by default, otherwise over the specified axis. float64 intermediate and return values are used for integer inputs.

## Parameters

a : array_like
Array containing numbers whose mean is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the means are computed. The default is to compute the mean of the flattened array.
dtype : data-type, optional
Type to use in computing the mean. For integer inputs, the default is float64; for floating point inputs, it is the same as the input dtype.
out : ndarray, optional
Alternate output array in which to place the result. The default is None; if provided, it must have the same shape as the expected output, but the type will be cast if necessary. See doc.ufuncs for details.

## Returns

$\mathbf{m}$ : ndarray, see dtype parameter above
If out=None, returns a new array containing the mean values, otherwise a reference to the output array is returned.

## See Also:

average
Weighted average

## Notes

The arithmetic mean is the sum of the elements along the axis divided by the number of elements.
Note that for floating-point input, the mean is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-precision accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.mean(a)
2.5
>>> np.mean(a, axis=0)
array([ 2., 3.])
>>> np.mean(a, axis=1)
array([ 1.5, 3.5])
```

In single precision, mean can be inaccurate:

```
>>> a = np.zeros((2, 512*512), dtype=np.float 32)
>>> a[0, :] = 1.0
>>> a[1, :] = 0.1
>>> np.mean(a)
0.546875
```

Computing the mean in float64 is more accurate:

```
>>> np.mean(a, dtype=np.float64)
0.55000000074505806
```

numpy. nonzero (a)
Return the indices of the elements that are non-zero.
Returns a tuple of arrays, one for each dimension of $a$, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

```
a[nonzero(a)]
```

To group the indices by element, rather than dimension, use:

```
transpose(nonzero(a))
```

The result of this is always a 2-D array, with a row for each non-zero element.

## Parameters

a: array_like
Input array.

## Returns

tuple_of_arrays : tuple
Indices of elements that are non-zero.

## See Also:

## flatnonzero

Return indices that are non-zero in the flattened version of the input array.

```
ndarray.nonzero
```

Equivalent ndarray method.
count_nonzero
Counts the number of non-zero elements in the input array.

## Examples

```
>>> x = np.eye(3)
>>> x
array([[ 1., 0., 0.],
    [ 0., 1., 0.],
    [ 0., 0., 1.]])
>>> np.nonzero(x)
(array([0, 1, 2]), array([0, 1, 2]))
>>> x[np.nonzero(x)]
array([ 1., 1., 1.])
>>> np.transpose(np.nonzero(x))
array([[0, 0],
    [1, 1],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , np.nonzero( $a>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a = np.array([[1,2,3],[4,5,6],[7, 8,9]])
>>> a > 3
array([[False, False, False],
    [ True, True, True],
    [ True, True, True]], dtype=bool)
>>> np.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the boolean array can also be called.

```
>>> (a > 3).nonzero()
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

numpy $\cdot \operatorname{prod}(a$, axis=None, dtype=None, out=None)
Return the product of array elements over a given axis.

## Parameters

a : array_like
Input data.
axis : int, optional
Axis over which the product is taken. By default, the product of all elements is calculated.
dtype : data-type, optional
The data-type of the returned array, as well as of the accumulator in which the elements are multiplied. By default, if $a$ is of integer type, dtype is the default platform integer. (Note: if the type of $a$ is unsigned, then so is dtype.) Otherwise, the dtype is the same as that of $a$.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output, but the type of the output values will be cast if necessary.

## Returns

product_along_axis : ndarray, see dtype parameter above.
An array shaped as $a$ but with the specified axis removed. Returns a reference to out if specified.

## See Also:

ndarray.prod
equivalent method
numpy. doc. ufuncs
Section "Output arguments"

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow. That means that, on a 32-bit platform:

```
>>> x = np.array([536870910, 536870910, 536870910, 536870910])
>>> np.prod(x) #random
16
```


## Examples

By default, calculate the product of all elements:

```
>>> np.prod([1.,2.])
2.0
```

Even when the input array is two-dimensional:

```
>>> np.prod([[1.,2.],[3.,4.]])
24.0
```

But we can also specify the axis over which to multiply:

```
>>> np.prod([[1.,2.],[3.,4.]], axis=1)
array([ 2., 12.])
```

If the type of $x$ is unsigned, then the output type is the unsigned platform integer:

```
>>> x = np.array([1, 2, 3], dtype=np.uint8)
>>> np.prod(x).dtype == np.uint
True
```

If $x$ is of a signed integer type, then the output type is the default platform integer:

```
>>> x = np.array([1, 2, 3], dtype=np.int8)
>>> np.prod(x).dtype == np.int
True
```

numpy.ptp ( $a$, axis=None, out=None)

Range of values (maximum - minimum) along an axis.
The name of the function comes from the acronym for 'peak to peak'.

## Parameters

a : array_like
Input values.
axis : int, optional
Axis along which to find the peaks. By default, flatten the array.
out : array_like
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output, but the type of the output values will be cast if necessary.

## Returns

 ptp : ndarrayA new array holding the result, unless out was specified, in which case a reference to out is returned.

## Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
        [2, 3]])
>>> np.ptp(x, axis=0)
array([2, 2])
>>> np.ptp(x, axis=1)
array([1, 1])
numpy . put (a, ind, v, mode='raise')
Replaces specified elements of an array with given values.
The indexing works on the flattened target array. put is roughly equivalent to:
```

```
a.flat[ind] = v
```


## Parameters

a: ndarray
Target array.
ind : array_like
Target indices, interpreted as integers.
v: array_like
Values to place in $a$ at target indices. If $v$ is shorter than ind it will be repeated as necessary.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## See Also:

putmask, place

## Examples

```
>>> a = np.arange(5)
>>> np.put(a, [0, 2], [-44, -55])
>>> a
array([-44, 1, -55, 3, 4])
>>> a = np.arange(5)
>>> np.put(a, 22, -5, mode='clip')
>>> a
array([ 0, 1, 2, 3, -5])
```

numpy. ravel ( $a$, order=' $C^{\prime}$ )
Return a flattened array.
A 1-D array, containing the elements of the input, is returned. A copy is made only if needed.

## Parameters

a : array_like
Input array. The elements in a are read in the order specified by order, and packed as a 1-D array.
order : \{ 'C','F', 'A', 'K' , optional
The elements of a are read in this order. ' C ' means to view the elements in C (rowmajor) order. ' $F$ ' means to view the elements in Fortran (column-major) order. 'A' means to view the elements in ' $F$ ' order if a is Fortran contiguous, ' $C$ ' order otherwise. ' K ' means to view the elements in the order they occur in memory, except for reversing the data when strides are negative. By default, 'C' order is used.

## Returns

1d_array : ndarray
Output of the same dtype as $a$, and of shape (a.size(), ).

## See Also:

ndarray.flat
1-D iterator over an array.
ndarray.flatten
1-D array copy of the elements of an array in row-major order.

## Notes

In row-major order, the row index varies the slowest, and the column index the quickest. This can be generalized to multiple dimensions, where row-major order implies that the index along the first axis varies slowest, and the index along the last quickest. The opposite holds for Fortran-, or column-major, mode.

## Examples

It is equivalent to reshape ( -1 , order=order).

```
>>> x = np.array([[1, 2, 3], [4, 5, 6]])
>>> print np.ravel(x)
[1 2 3 4 5 5 6]
>>> print x.reshape(-1)
[1 2 3 4 4 5 6]
>>> print np.ravel(x, order='F')
[1 4 2 5 3 6]
```

When order is ' $A$ ', it will preserve the array's ' $C$ ' or ' $F$ ' ordering:

```
>>> print np.ravel(x.T)
[1 4 2 5 3 6]
>>> print np.ravel(x.T, order='A')
[1 2 3 4 5 6]
```

When order is ' $K$ ', it will preserve orderings that are neither ' $C$ ' nor ' $F$ ', but won't reverse axes:

```
>>> a = np.arange(3)[::-1]; a
array([2, 1, 0])
>>> a.ravel(order=' C')
array([2, 1, 0])
>>> a.ravel(order=' K')
array([2, 1, 0])
>>> a = np.arange(12).reshape(2,3,2).swapaxes(1,2); a
array([[[ 0, 2, 4],
            [ 1, 3, 5]],
            [[ 6, 8, 10],
            [ 7, 9, 11]]])
>>> a.ravel(order=' C')
array([ 0, 2, 4, 1, 3, 5, 6, 8, 10, 7, 9, 11])
>>> a.ravel(order='K')
array([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11])
```

numpy. repeat (a, repeats, axis=None)
Repeat elements of an array.

## Parameters

a : array_like
Input array.
repeats: \{int, array of ints \}
The number of repetitions for each element. repeats is broadcasted to fit the shape of the given axis.
axis : int, optional
The axis along which to repeat values. By default, use the flattened input array, and return a flat output array.

## Returns

 repeated_array : ndarrayOutput array which has the same shape as $a$, except along the given axis.

## See Also:

tile
Tile an array.
Examples

```
>>> x = np.array([[1,2], [3,4]])
>>> np.repeat (x, 2)
array([1, 1, 2, 2, 3, 3, 4, 4])
>>> np.repeat (x, 3, axis=1)
array([[1, 1, 1, 2, 2, 2],
            [3, 3, 3, 4, 4, 4]])
>>> np.repeat(x, [1, 2], axis=0)
array([[1, 2],
            [3, 4],
            [3, 4]])
```

numpy. reshape ( $a$, newshape, order=' $C$ ')
Gives a new shape to an array without changing its data.

## Parameters

a : array_like
Array to be reshaped.
newshape : int or tuple of ints
The new shape should be compatible with the original shape. If an integer, then the result will be a 1-D array of that length. One shape dimension can be -1 . In this case, the value is inferred from the length of the array and remaining dimensions.
order : \{ 'C', 'F', 'A'\}, optional
Determines whether the array data should be viewed as in C (row-major) order, FORTRAN (column-major) order, or the C/FORTRAN order should be preserved.

## Returns

reshaped_array : ndarray
This will be a new view object if possible; otherwise, it will be a copy.

## See Also:

ndarray.reshape
Equivalent method.

## Notes

It is not always possible to change the shape of an array without copying the data. If you want an error to be raise if the data is copied, you should assign the new shape to the shape attribute of the array:

```
>>> a = np.zeros((10, 2))
# A transpose make the array non-contiguous
>>> b = a.T
# Taking a view makes it possible to modify the shape without modiying the
# initial object.
>>> c = b.view()
>>> c.shape = (20)
AttributeError: incompatible shape for a non-contiguous array
```


## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> np.reshape(a, 6)
array([1, 2, 3, 4, 5, 6])
>>> np.reshape(a, 6, order=' F')
array([1, 4, 2, 5, 3, 6])
>>> np.reshape(a, (3,-1)) # the unspecified value is inferred to be 2
array([[1, 2],
    [3, 4],
    [5, 6]])
```

numpy.resize ( $a$, new_shape)
Return a new array with the specified shape.
If the new array is larger than the original array, then the new array is filled with repeated copies of $a$. Note that this behavior is different from a.resize(new_shape) which fills with zeros instead of repeated copies of $a$.

## Parameters

a : array_like

Array to be resized. new_shape : int or tuple of int

Shape of resized array.

## Returns

 reshaped_array : ndarrayThe new array is formed from the data in the old array, repeated if necessary to fill out the required number of elements. The data are repeated in the order that they are stored in memory.

See Also:
ndarray.resize
resize an array in-place.
Examples

```
>>> a=np.array([[0,1],[2,3]])
>>> np.resize(a, (1,4))
array([[0, 1, 2, 3]])
>>> np.resize(a, (2,4))
array([[0, 1, 2, 3],
    [0, 1, 2, 3]])
```

numpy. searchsorted ( $a, v$, side='left')
Find indices where elements should be inserted to maintain order.
Find the indices into a sorted array $a$ such that, if the corresponding elements in $v$ were inserted before the indices, the order of $a$ would be preserved.

## Parameters

a: 1-D array_like
Input array, sorted in ascending order.
$\mathbf{v}$ : array_like
Values to insert into $a$.
side : \{'left', 'right' \}, optional
If 'left', the index of the first suitable location found is given. If 'right', return the last such index. If there is no suitable index, return either 0 or N (where N is the length of $a)$.

## Returns

indices : array of ints
Array of insertion points with the same shape as $v$.

## See Also:

sort
Return a sorted copy of an array.
histogram
Produce histogram from 1-D data.

## Notes

Binary search is used to find the required insertion points.
As of Numpy 1.4.0 searchsorted works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

```
>>> np.searchsorted([1,2,3,4,5], 3)
2
>>> np.searchsorted([1,2,3,4,5], 3, side='right')
3
>>> np.searchsorted([1,2,3,4,5], [-10, 10, 2, 3])
array([0, 5, 1, 2])
```

numpy. sort ( $a$, axis=-1, kind='quicksort', order=None )

Return a sorted copy of an array.

## Parameters

a : array_like
Array to be sorted.
axis : int or None, optional
Axis along which to sort. If None, the array is flattened before sorting. The default is -1 , which sorts along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort'\}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is a structured array, this argument specifies which fields to compare first, second, and so on. This list does not need to include all of the fields.

## Returns

sorted_array : ndarray
Array of the same type and shape as $a$.

## See Also:

ndarray.sort
Method to sort an array in-place.
argsort
Indirect sort.
lexsort
Indirect stable sort on multiple keys.
searchsorted
Find elements in a sorted array.

## Notes

The various sorting algorithms are characterized by their average speed, worst case performance, work space size, and whether they are stable. A stable sort keeps items with the same key in the same relative order. The three available algorithms have the following properties:

| kind | speed | worst case | work space | stable |
| :--- | :--- | :--- | :--- | :--- |
| 'quicksort' | 1 | $\mathrm{O}\left(\mathrm{n}^{\wedge} 2\right)$ | 0 | no |
| 'mergesort' | 2 | $\mathrm{O}\left(\mathrm{n}^{*} \log (\mathrm{n})\right)$ | $\sim \mathrm{n} / 2$ | yes |
| 'heapsort' | 3 | $\mathrm{O}(\mathrm{n} * \log (\mathrm{n}))$ | 0 | no |

All the sort algorithms make temporary copies of the data when sorting along any but the last axis. Consequently, sorting along the last axis is faster and uses less space than sorting along any other axis.

The sort order for complex numbers is lexicographic. If both the real and imaginary parts are non-nan then the order is determined by the real parts except when they are equal, in which case the order is determined by the imaginary parts.

Previous to numpy 1.4.0 sorting real and complex arrays containing nan values led to undefined behaviour. In numpy versions $>=1.4 .0$ nan values are sorted to the end. The extended sort order is:
-Real: [R, nan]
-Complex: [ $\mathrm{R}+\mathrm{Rj}, \mathrm{R}+$ nanj, nan +Rj , nan + nanj]
where R is a non-nan real value. Complex values with the same nan placements are sorted according to the non-nan part if it exists. Non-nan values are sorted as before.

## Examples

```
>>> a = np.array([[1,4],[3,1]])
>>> np.sort(a) # sort along the last axis
array([[1, 4],
    [1, 3]])
>>>n.sort(a, axis=None) # sort the flattened array
array([1, 1, 3, 4])
mp.sort(a, axis=0) # sort along the first axis
array([[1, 1],
    [3, 4]])
```

Use the order keyword to specify a field to use when sorting a structured array:

```
>>> dtype = [('name', 'S10'), ('height', float), ('age', int)]
>>> values = [('Arthur', 1.8, 41), ('Lancelot', 1.9, 38),
... ('Galahad', 1.7, 38)]
>>> a = np.array(values, dtype=dtype) # create a structured array
>>> np.sort(a, order='height')
array([('Galahad', 1.7, 38), ('Arthur', 1.8, 41),
    ('Lancelot', 1.8999999999999999, 38)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

Sort by age, then height if ages are equal:

```
>>> np.sort(a, order=['age', 'height'])
array([('Galahad', 1.7, 38), ('Lancelot', 1.89999999999999999, 38),
    ('Arthur', 1.8, 41)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

numpy.squeeze (a)
Remove single-dimensional entries from the shape of an array.

## Parameters

a : array_like
Input data.

## Returns

squeezed : ndarray

The input array, but with with all dimensions of length 1 removed. Whenever possible, a view on $a$ is returned.

## Examples

```
>>> x = np.array([[[0], [1], [2]]])
```

>>> x.shape
(1, 3, 1)
>>> np.squeeze(x).shape
(3, )
numpy.std ( $a$, axis=None, dtype $=$ None, out=None, $d d o f=0$ )
Compute the standard deviation along the specified axis.
Returns the standard deviation, a measure of the spread of a distribution, of the array elements. The standard deviation is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Calculate the standard deviation of these values.
axis : int, optional
Axis along which the standard deviation is computed. The default is to compute the standard deviation of the flattened array.
dtype : dtype, optional
Type to use in computing the standard deviation. For arrays of integer type the default is float64, for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type (of the calculated values) will be cast if necessary.
ddof : int, optional
Means Delta Degrees of Freedom. The divisor used in calculations is N - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

standard_deviation : ndarray, see dtype parameter above.
If out is None, return a new array containing the standard deviation, otherwise return a reference to the output array.

## See Also:

var, mean
numpy.doc.ufuncs
Section "Output arguments"

## Notes

The standard deviation is the square root of the average of the squared deviations from the mean, i.e., std $=\operatorname{sqrt}(\operatorname{mean}(\operatorname{abs}(x-x . m e a n()) * * 2))$.

The average squared deviation is normally calculated as $x \cdot \operatorname{sum}() / N$, where $N=$ len(x). If, however, $d d o f$ is specified, the divisor $N$ - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of the infinite population. ddof=0 provides a maximum likelihood estimate of the variance for normally distributed variables. The standard deviation computed in
this function is the square root of the estimated variance, so even with ddof $=1$, it will not be an unbiased estimate of the standard deviation per se.

Note that, for complex numbers, std takes the absolute value before squaring, so that the result is always real and nonnegative.

For floating-point input, the $s t d$ is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.std(a)
1.1180339887498949
>>> np.std(a, axis=0)
array([ 1., 1.])
>>> np.std(a, axis=1)
array([ 0.5, 0.5])
```

In single precision, $\operatorname{std}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.std(a)
0.45172946707416706
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.std(a, dtype=np.float64)
0.449999999925552653
```

numpy. sum ( $a$, axis=None, dtype $=$ None, out $=$ None )
Sum of array elements over a given axis.

## Parameters

a : array_like
Elements to sum.
axis : integer, optional
Axis over which the sum is taken. By default axis is None, and all elements are summed.
dtype : dtype, optional
The type of the returned array and of the accumulator in which the elements are summed. By default, the dtype of $a$ is used. An exception is when $a$ has an integer type with less precision than the default platform integer. In that case, the default platform integer is used instead.
out : ndarray, optional
Array into which the output is placed. By default, a new array is created. If out is given, it must be of the appropriate shape (the shape of $a$ with axis removed, i.e., numpy.delete(a.shape, axis)). Its type is preserved. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

sum_along_axis : ndarray

An array with the same shape as $a$, with the specified axis removed. If $a$ is a $0-\mathrm{d}$ array, or if axis is None, a scalar is returned. If an output array is specified, a reference to out is returned.

## See Also:

ndarray.sum
Equivalent method.
cumsum
Cumulative sum of array elements.
trapz
Integration of array values using the composite trapezoidal rule.
mean, average

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> np.sum([0.5, 1.5])
2.0
>>> np.sum([0.5, 0.7, 0.2, 1.5], dtype=np.int32)
1
>>> np.sum([[0, 1], [0, 5]])
6
>>> np.sum([[0, 1], [0, 5]], axis=0)
array([0, 6])
>>> np.sum([[0, 1], [0, 5]], axis=1)
array([1, 5])
```

If the accumulator is too small, overflow occurs:

```
>>> np.ones(128, dtype=np.int8).sum(dtype=np.int8)
-128
```

numpy.swapaxes (a, axis1, axis2)

Interchange two axes of an array.

## Parameters

a : array_like
Input array.
axis1 : int
First axis.
axis2 : int
Second axis.

## Returns

a_swapped : ndarray
If $a$ is an ndarray, then a view of $a$ is returned; otherwise a new array is created.

## Examples

```
>>> x = np.array([[1,2,3]])
>>> np.swapaxes(x,0,1)
array([[1],
[2],
    [3]])
>>> x = np.array([[[0,1],[2,3]],[[4,5],[6,7]]])
>>> x
array([[[0, 1],
    [2, 3]],
    [[4, 5],
    [6, 7]]])
>>> np.swapaxes(x,0,2)
array([[[0, 4],
    [2, 6]],
    [[1, 5],
    [3, 7]]])
```

numpy.take ( $a$, indices, axis=None, out=None, mode='raise')
Take elements from an array along an axis.
This function does the same thing as "fancy" indexing (indexing arrays using arrays); however, it can be easier to use if you need elements along a given axis.

## Parameters

a : array_like
The source array.
indices : array_like
The indices of the values to extract.
axis : int, optional
The axis over which to select values. By default, the flattened input array is used.
out : ndarray, optional
If provided, the result will be placed in this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## Returns

subarray : ndarray
The returned array has the same type as $a$.

## See Also:

ndarray.take
equivalent method
Examples

```
>>> a = [4, 3, 5, 7, 6, 8]
>>> indices = [0, 1, 4]
>>> np.take(a, indices)
array([4, 3, 6])
```

In this example if $a$ is an ndarray, "fancy" indexing can be used.

```
>>> a = np.array(a)
>>> a[indices]
array([4, 3, 6])
```

numpy.trace $(a$, offset $=0$, axis $1=0$, axis $2=1$, dtype $=$ None, out $=$ None $)$
Return the sum along diagonals of the array.
If $a$ is $2-D$, the sum along its diagonal with the given offset is returned, i.e., the sum of elements a [i,i+offset] for all i.

If $a$ has more than two dimensions, then the axes specified by axis1 and axis 2 are used to determine the 2-D sub-arrays whose traces are returned. The shape of the resulting array is the same as that of $a$ with axis1 and axis2 removed.

## Parameters

a : array_like
Input array, from which the diagonals are taken.
offset : int, optional
Offset of the diagonal from the main diagonal. Can be both positive and negative. Defaults to 0 .
axis1, axis2 : int, optional
Axes to be used as the first and second axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults are the first two axes of $a$.
dtype : dtype, optional
Determines the data-type of the returned array and of the accumulator where the elements are summed. If dtype has the value None and $a$ is of integer type of precision less than the default integer precision, then the default integer precision is used. Otherwise, the precision is the same as that of $a$.
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

sum_along_diagonals : ndarray
If $a$ is 2-D, the sum along the diagonal is returned. If $a$ has larger dimensions, then an array of sums along diagonals is returned.

## See Also:

diag, diagonal, diagflat

## Examples

```
>>> np.trace(np.eye(3))
3.0
>>> a = np.arange(8).reshape((2,2,2))
>>> np.trace(a)
array([6, 8])
>>> a = np.arange(24).reshape((2,2,2,3))
>>> np.trace(a).shape
(2, 3)
```

numpy.transpose ( $a$, axes=None)
Permute the dimensions of an array.

## Parameters

a : array_like
Input array.
axes : list of ints, optional
By default, reverse the dimensions, otherwise permute the axes according to the values given.

## Returns

p: ndarray
$a$ with its axes permuted. A view is returned whenever possible.

## See Also:

rollaxis
Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
                [2, 3]])
>>> np.transpose(x)
array([[0, 2],
            [1, 3]])
>>> x = np.ones((1, 2, 3))
>>> np.transpose(x, (1, 0, 2)).shape
(2, 1, 3)
```

numpy . var ( $a$, axis $=$ None, dtype $=$ None, out $=$ None, , ddof=0)
Compute the variance along the specified axis.
Returns the variance of the array elements, a measure of the spread of a distribution. The variance is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Array containing numbers whose variance is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional

Axis along which the variance is computed. The default is to compute the variance of the flattened array.
dtype : data-type, optional
Type to use in computing the variance. For arrays of integer type the default is float32; for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output, but the type is cast if necessary.
ddof : int, optional
"Delta Degrees of Freedom": the divisor used in the calculation is N - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

variance : ndarray, see dtype parameter above
If out=None, returns a new array containing the variance; otherwise, a reference to the output array is returned.

## See Also:

## std

Standard deviation
mean
Average
numpy.doc.ufuncs
Section "Output arguments"

## Notes

The variance is the average of the squared deviations from the mean, i.e., var $=$ mean (abs (x x.mean()) **2).

The mean is normally calculated as x . sum () / N , where $\mathrm{N}=$ len ( x ). If, however, $d d o f$ is specified, the divisor $N$ - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of a hypothetical infinite population. $\mathrm{ddof}=0$ provides a maximum likelihood estimate of the variance for normally distributed variables.

Note that for complex numbers, the absolute value is taken before squaring, so that the result is always real and nonnegative.

For floating-point input, the variance is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1,2],[3,4]])
>>> np.var(a)
1.25
>>> np.var(a,0)
array([ 1., 1.])
>>> np.var(a,1)
array([ 0.25, 0.25])
```

In single precision, $\operatorname{var}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.var(a)
0.20405951142311096
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.var(a, dtype=np.float64)
0.20249999932997387
>>> ((1-0.55)**2 + (0.1-0.55)**2)/2
0.20250000000000001
```


### 1.1.2 Indexing arrays

Arrays can be indexed using an extended Python slicing syntax, array[selection]. Similar syntax is also used for accessing fields in a record array.

## See Also:

Array Indexing.

### 1.1.3 Internal memory layout of an ndarray

An instance of class ndarray consists of a contiguous one-dimensional segment of computer memory (owned by the array, or by some other object), combined with an indexing scheme that maps $N$ integers into the location of an item in the block. The ranges in which the indices can vary is specified by the shape of the array. How many bytes each item takes and how the bytes are interpreted is defined by the data-type object associated with the array. A segment of memory is inherently 1-dimensional, and there are many different schemes for arranging the items of an $N$-dimensional array in a 1-dimensional block. Numpy is flexible, and ndarray objects can accommodate any strided indexing scheme. In a strided scheme, the N -dimensional index $\left(n_{0}, n_{1}, \ldots, n_{N-1}\right)$ corresponds to the offset (in bytes):

$$
n_{\mathrm{offset}}=\sum_{k=0}^{N-1} s_{k} n_{k}
$$

from the beginning of the memory block associated with the array. Here, $s_{k}$ are integers which specify the strides of the array. The column-major order (used, for example, in the Fortran language and in Matlab) and row-major order (used in C) schemes are just specific kinds of strided scheme, and correspond to the strides:

$$
s_{k}^{\text {column }}=\prod_{j=0}^{k-1} d_{j}, \quad s_{k}^{\mathrm{row}}=\prod_{j=k+1}^{N-1} d_{j}
$$

where $d_{j}=$ self.itemsize $*$ self.shape $[j]$.
Both the C and Fortran orders are contiguous, i.e., single-segment, memory layouts, in which every part of the memory block can be accessed by some combination of the indices.

Data in new ndarrays is in the row-major (C) order, unless otherwise specified, but, for example, basic array slicing often produces views in a different scheme.

Note: Several algorithms in NumPy work on arbitrarily strided arrays. However, some algorithms require singlesegment arrays. When an irregularly strided array is passed in to such algorithms, a copy is automatically made.

### 1.1.4 Array attributes

Array attributes reflect information that is intrinsic to the array itself. Generally, accessing an array through its attributes allows you to get and sometimes set intrinsic properties of the array without creating a new array. The exposed attributes are the core parts of an array and only some of them can be reset meaningfully without creating a new array. Information on each attribute is given below.

## Memory layout

The following attributes contain information about the memory layout of the array:

| ndarray.flags | Information about the memory layout of the array. |
| :--- | :--- |
| ndarray.shape | Tuple of array dimensions. |
| ndarray.strides | Tuple of bytes to step in each dimension when traversing an array. |
| ndarray. ndim | Number of array dimensions. |
| ndarray.data | Python buffer object pointing to the start of the array’s data. |
| ndarray.size | Number of elements in the array. |
| ndarray.itemsize | Length of one array element in bytes. |
| ndarray.nbytes | Total bytes consumed by the elements of the array. |
| ndarray.base | Base object if memory is from some other object. |
| ndarray.flags |  |
| Information about the memory layout of the array. |  |
| Notes |  |

The flags object can be accessed dictionary-like (as in a.flags ['WRITEABLE' ]), or by using lowercased attribute names (as in a.flags.writeable). Short flag names are only supported in dictionary access.

Only the UPDATEIFCOPY, WRITEABLE, and ALIGNED flags can be changed by the user, via direct assignment to the attribute or dictionary entry, or by calling ndarray.setflags.

The array flags cannot be set arbitrarily:
-UPDATEIFCOPY can only be set False.

- ALIGNED can only be set True if the data is truly aligned.
-WRITEABLE can only be set True if the array owns its own memory or the ultimate owner of the memory exposes a writeable buffer interface or is a string.


## Attributes

ndarray.shape
Tuple of array dimensions.

## Notes

May be used to "reshape" the array, as long as this would not require a change in the total number of elements

## Examples

```
>>> x = np.array([1, 2, 3, 4])
>>> x.shape
(4,)
>>> y = np.zeros((2, 3, 4))
>>> y.shape
(2, 3, 4)
>>> y.shape = (3, 8)
>>> y
```

```
array([[ 0., 0., 0., 0., 0., 0., 0., 0.],
    [ 0., 0., 0., 0., 0., 0., 0., 0.],
    [ 0., 0., 0., 0., 0., 0., 0., 0.]])
>>> y.shape = (3, 6)
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
ValueError: total size of new array must be unchanged
ndarray.strides
```

Tuple of bytes to step in each dimension when traversing an array.
The byte offset of element (i[0], i[1], ..., $i[n]$ ) in an array $a$ is:

```
offset = sum(np.array(i) * a.strides)
```

A more detailed explanation of strides can be found in the "ndarray.rst" file in the NumPy reference guide.
See Also:

```
numpy.lib.stride_tricks.as_strided
```


## Notes

Imagine an array of 32-bit integers (each 4 bytes):

```
x = np.array([[0, 1, 2, 3, 4],
    [5, 6, 7, 8, 9]], dtype=np.int32)
```

This array is stored in memory as 40 bytes, one after the other (known as a contiguous block of memory). The strides of an array tell us how many bytes we have to skip in memory to move to the next position along a certain axis. For example, we have to skip 4 bytes ( 1 value) to move to the next column, but 20 bytes ( 5 values) to get to the same position in the next row. As such, the strides for the array $x$ will be $(20,4)$.

## Examples

```
>>> y = np.reshape(np.arange (2*3*4), (2, 3, 4))
>>> y
array([[[ 0, 1, 2, 3],
            [4, 5, 6, 7],
            [ 8, 9, 10, 11]],
            [[12, 13, 14, 15],
            [16, 17, 18, 19],
            [20, 21, 22, 23]]])
>>> y.strides
(48, 16, 4)
>>> y[1,1,1]
17
>>> offset=sum(y.strides * np.array((1,1,1)))
>>> offset/y.itemsize
1 7
>>> x = np.reshape(np.arange(5* 6*7*8), (5,6,7,8)).transpose(2,3,1,0)
>>> x.strides
(32, 4, 224, 1344)
>>> i = np.array([3,5,2,2])
>>> offset = sum(i * x.strides)
>>> x[3,5,2,2]
813
>>> offset / x.itemsize
813
```

ndarray.ndim
Number of array dimensions.

## Examples

```
>>> x = np.array([1, 2, 3])
>>> x.ndim
1
>>> y = np.zeros((2, 3, 4))
>>> y.ndim
3
```

ndarray.data

Python buffer object pointing to the start of the array's data.

```
ndarray.size
```

Number of elements in the array.
Equivalent to np.prod (a.shape), i.e., the product of the array's dimensions.

## Examples

```
>>> x = np.zeros((3, 5, 2), dtype=np.complex128)
>>> x.size
30
>>> np.prod(x.shape)
30
```

ndarray.itemsize

Length of one array element in bytes.

## Examples

```
>>> x = np.array([1,2,3], dtype=np.float64)
>>> x.itemsize
8
>>> x = np.array([1,2,3], dtype=np.complex128)
>>> x.itemsize
16
```

ndarray.nbytes
Total bytes consumed by the elements of the array.

## Notes

Does not include memory consumed by non-element attributes of the array object.

## Examples

```
>>> x = np.zeros((3,5,2), dtype=np.complex128)
>>> x.nbytes
480
>>> np.prod(x.shape) * x.itemsize
480
Base object if memory is from some other object.
```


## Examples

ndarray.base

The base of an array that owns its memory is None:

```
>>> x = np.array([1,2,3,4])
>>> x.base is None
True
```

Slicing creates a view, whose memory is shared with x :

```
>>> y = x[2:]
>>> y.base is x
True
```


## Data type

## See Also:

Data type objects
The data type object associated with the array can be found in the dtype attribute:

```
ndarray.dtype Data-type of the array's elements.
ndarray.dtype
    Data-type of the array's elements.
```


## Parameters

None :

## Returns

d : numpy dtype object

## See Also:

numpy.dtype

## Examples

>> $x$
array ([[0, 1],
$[2,3]])$
>>> x.dtype
dtype('int32')
>>> type(x.dtype)
<type 'numpy.dtype'>

Other attributes

| ndarray.T | Same as self.transpose(), except that self is returned if self.ndim $<2$. <br> ndarray.real <br> ndarray.imag <br> ndarray.flat |
| :--- | :--- |
| The real part of the array. |  |
| ndarray.ctypes | The imaginary part of the array. |
| An iterator over the array. |  |
| ndarray. $\mathbf{T}$ | An object to simplify the interaction of the array with the ctypes module. |
| Same as self.transpose(), except that self is returned if self.ndim $<2$. |  |
| Examples |  |

```
>>> x = np.array([[1.,2.],[3.,4.]])
>>> x
array([[ 1., 2.],
    [ 3., 4.]])
>>> x.T
array([[ 1., 3.],
    [ 2., 4.]])
>>> x = np.array([1.,2.,3.,4.])
>>> x
array([ 1., 2., 3., 4.])
>>> x.T
array([ 1., 2., 3., 4.])
```

ndarray.real

The real part of the array.

## See Also:

numpy.real
equivalent function

## Examples

```
>>> x = np.sqrt([1+0j, 0+1j])
>>> x.real
array([ 1. , 0.70710678])
>>> x.real.dtype
dtype('float64')
```

ndarray.imag

The imaginary part of the array.

## Examples

```
>>> x = np.sqrt([1+0j, 0+1j])
>>> x.imag
array([ 0. , 0.70710678])
>>> x.imag.dtype
dtype('float64')
```

ndarray.flat

A 1-D iterator over the array.
This is a numpy.flat iter instance, which acts similarly to, but is not a subclass of, Python's built-in iterator object.
See Also:

## flatten

Return a copy of the array collapsed into one dimension.
flatiter

## Examples

```
>>> x = np.arange(1, 7).reshape(2, 3)
>>> x
array([[1, 2, 3],
                    [4, 5, 6]])
```

```
>>> x.flat[3]
4
>>> x.T
array([[1, 4],
    [2, 5],
    [3, 6]])
>>> x.T.flat[3]
5
>>> type(x.flat)
<type 'numpy.flatiter'>
```

An assignment example:

```
>>> x.flat = 3; x
array([[3, 3, 3],
    [3, 3, 3]])
>>> x.flat[[1,4]] = 1; x
array([[3, 1, 3],
    [3, 1, 3]])
```


## ndarray.ctypes

An object to simplify the interaction of the array with the ctypes module.
This attribute creates an object that makes it easier to use arrays when calling shared libraries with the ctypes module. The returned object has, among others, data, shape, and strides attributes (see Notes below) which themselves return ctypes objects that can be used as arguments to a shared library.

## Parameters

None :

## Returns

c: Python object
Possessing attributes data, shape, strides, etc.

## See Also:

numpy.ctypeslib

## Notes

Below are the public attributes of this object which were documented in "Guide to NumPy" (we have omitted undocumented public attributes, as well as documented private attributes):
-data: A pointer to the memory area of the array as a Python integer. This memory area may contain data that is not aligned, or not in correct byte-order. The memory area may not even be writeable. The array flags and data-type of this array should be respected when passing this attribute to arbitrary C-code to avoid trouble that can include Python crashing. User Beware! The value of this attribute is exactly the same as self._array_interface_['data'][0].
-shape (c_intp*self.ndim): A ctypes array of length self.ndim where the basetype is the C-integer corresponding to dtype(' p ') on this platform. This base-type could be c _int, c _long, or c_longlong depending on the platform. The c_intp type is defined accordingly in numpy.ctypeslib. The ctypes array contains the shape of the underlying array.
-strides (c_intp*self.ndim): A ctypes array of length self.ndim where the basetype is the same as for the shape attribute. This ctypes array contains the strides information from the underlying array. This strides information is important for showing how many bytes must be jumped to get to the next element in the array.
-data_as(obj): Return the data pointer cast to a particular c-types object. For example, calling self._as_parameter_ is equivalent to self.data_as(ctypes.c_void_p). Perhaps you want to use the data as a pointer to a ctypes array of floating-point data: self.data_as(ctypes.POINTER(ctypes.c_double)).
-shape_as(obj): Return the shape tuple as an array of some other c-types type. For example: self.shape_as(ctypes.c_short).
-strides_as(obj): Return the strides tuple as an array of some other c-types type. For example: self.strides_as(ctypes.c_longlong).

Be careful using the ctypes attribute - especially on temporary arrays or arrays constructed on the fly. For example, calling ( $a+b$ ).ctypes.data_as (ctypes.c_void_p) returns a pointer to memory that is invalid because the array created as $(a+b)$ is deallocated before the next Python statement. You can avoid this problem using either $c=a+b$ or $c t=(a+b) . c t y p e s$. In the latter case, ct will hold a reference to the array until ct is deleted or re-assigned.

If the ctypes module is not available, then the ctypes attribute of array objects still returns something useful, but ctypes objects are not returned and errors may be raised instead. In particular, the object will still have the as parameter attribute which will return an integer equal to the data attribute.

## Examples

```
>>> import ctypes
>>> x
array([[0, 1],
    [2, 3]])
>>> x.ctypes.data
30439712
>>> x.ctypes.data_as(ctypes.POINTER(ctypes.c_long))
<ctypes.LP_c_long object at 0x01F01300>
>>> x.ctypes.data_as(ctypes.POINTER(ctypes.c_long)).contents
c_long(0)
>>> x.ctypes.data_as(ctypes.POINTER(ctypes.c_longlong)).contents
c_longlong(4294967296L)
>>> x.ctypes.shape
<numpy.core._internal.c_long_Array_2 object at 0x01FFD580>
>>> x.ctypes.shape_as(ctypes.c_long)
<numpy.core._internal.c_long_Array_2 object at 0x01FCE620>
>>> x.ctypes.strides
<numpy.core._internal.c_long_Array_2 object at 0x01FCE620>
>>> x.ctypes.strides_as(ctypes.c_longlong)
<numpy.core._internal.c_longlong_Array_2 object at 0x01F01300>
```


## Array interface

## See Also:

The Array Interface.


## ctypes foreign function interface

ndarray.ctypes An object to simplify the interaction of the array with the ctypes module.
ndarray.ctypes
An object to simplify the interaction of the array with the ctypes module.

This attribute creates an object that makes it easier to use arrays when calling shared libraries with the ctypes module. The returned object has, among others, data, shape, and strides attributes (see Notes below) which themselves return ctypes objects that can be used as arguments to a shared library.

## Parameters

None :

## Returns

c: Python object
Possessing attributes data, shape, strides, etc.

## See Also:

numpy.ctypeslib

## Notes

Below are the public attributes of this object which were documented in "Guide to NumPy" (we have omitted undocumented public attributes, as well as documented private attributes):
-data: A pointer to the memory area of the array as a Python integer. This memory area may contain data that is not aligned, or not in correct byte-order. The memory area may not even be writeable. The array flags and data-type of this array should be respected when passing this attribute to arbitrary C-code to avoid trouble that can include Python crashing. User Beware! The value of this attribute is exactly the same as self._array_interface_['data'][0].
-shape (c_intp*self.ndim): A ctypes array of length self.ndim where the basetype is the C-integer corresponding to dtype(' p ') on this platform. This base-type could be c _int, $\mathrm{c} \_$long, or c _longlong depending on the platform. The c_intp type is defined accordingly in numpy.ctypeslib. The ctypes array contains the shape of the underlying array.
-strides (c_intp*self.ndim): A ctypes array of length self.ndim where the basetype is the same as for the shape attribute. This ctypes array contains the strides information from the underlying array. This strides information is important for showing how many bytes must be jumped to get to the next element in the array.
-data_as(obj): Return the data pointer cast to a particular c-types object. For example, calling self._as_parameter_is equivalent to self.data_as(ctypes.c_void_p). Perhaps you want to use the data as a pointer to a ctypes array of floating-point data: self.data_as(ctypes.POINTER(ctypes.c_double)).
-shape_as(obj): Return the shape tuple as an array of some other c-types type. For example: self.shape_as(ctypes.c_short).
-strides_as(obj): Return the strides tuple as an array of some other c-types type. For example: self.strides_as(ctypes.c_longlong).

Be careful using the ctypes attribute - especially on temporary arrays or arrays constructed on the fly. For example, calling ( $a+b$ ).ctypes.data_as (ctypes.c_void_p) returns a pointer to memory that is invalid because the array created as $(a+b)$ is deallocated before the next Python statement. You can avoid this problem using either $c=a+b$ or $c t=(a+b) . c t y p e s$. In the latter case, ct will hold a reference to the array until ct is deleted or re-assigned.

If the ctypes module is not available, then the ctypes attribute of array objects still returns something useful, but ctypes objects are not returned and errors may be raised instead. In particular, the object will still have the as parameter attribute which will return an integer equal to the data attribute.

## Examples

```
>>> import ctypes
>>> x
```

```
array([[0, 1],
    [2, 3]])
>>> x.ctypes.data
30439712
>>> x.ctypes.data_as(ctypes.POINTER(ctypes.c_long))
<ctypes.LP_c_long object at 0x01F01300>
>>> x.ctypes.data_as(ctypes.POINTER(ctypes.c_long)).contents
c_long(0)
>>> x.ctypes.data_as(ctypes.POINTER(ctypes.c_longlong)).contents
c_longlong(4294967296L)
>>> x.ctypes.shape
<numpy.core._internal.c_long_Array_2 object at 0x01FFD580>
>>> x.ctypes.shape_as(ctypes.c_long)
<numpy.core._internal.c_long_Array_2 object at 0x01FCE620>
>>> x.ctypes.strides
<numpy.core._internal.c_long_Array_2 object at 0x01FCE620>
>>> x.ctypes.strides_as(ctypes.c_longlong)
<numpy.core._internal.c_longlong_Array_2 object at 0x01F01300>
```


### 1.1.5 Array methods

An ndarray object has many methods which operate on or with the array in some fashion, typically returning an array result. These methods are briefly explained below. (Each method's docstring has a more complete description.)

For the following methods there are also corresponding functions in numpy: all, any, argmax, argmin, argsort, choose, clip, compress, copy, cumprod, cumsum, diagonal, imag, max, mean, min, nonzero, prod, ptp, put, ravel, real, repeat, reshape, round, searchsorted, sort, squeeze, std, sum, swapaxes, take, trace, transpose, var.

## Array conversion

| ndarray.item(*args) | Copy an element of an array to a standard Python scalar and return it. |
| :--- | :--- |
| ndarray.tolist() | Return the array as a (possibly nested) list. |
| ndarray.itemset(*args) | Insert scalar into an array (scalar is cast to array’s dtype, if possible) |
| ndarray.setasflat(arr) | Equivalent to a.flat = arr.flat, but is generally more efficient. |
| ndarray.tostring([order]) | Construct a Python string containing the raw data bytes in the array. |
| ndarray.tofile(fid[, sep, | Write array to a file as text or binary (default). |
| format]) |  |
| ndarray.dump(file) | Dump a pickle of the array to the specified file. |
| ndarray.dumps() | Returns the pickle of the array as a string. |
| ndarray.astype(t) | Copy of the array, cast to a specified type. |
| ndarray.byteswap(inplace) | Swap the bytes of the array elements |
| ndarray.copy([order]) | Return a copy of the array. |
| ndarray.view([dtype, type]) | New view of array with the same data. |
| ndarray.getfield(dtype, offset) | Returns a field of the given array as a certain type. |
| ndarray.setflags([write, align, | Set array flags WRITEABLE, ALIGNED, and UPDATEIFCOPY, |
| uic]) | respectively. |
| ndarray.fill(value) | Fill the array with a scalar value. |

## ndarray.item(*args)

Copy an element of an array to a standard Python scalar and return it.

## Parameters

*args : Arguments (variable number and type)

- none: in this case, the method only works for arrays with one element (a.size $==1$ ), which element is copied into a standard Python scalar object and returned.
- int_type: this argument is interpreted as a flat index into the array, specifying which element to copy and return.
- tuple of int_types: functions as does a single int_type argument, except that the argument is interpreted as an nd-index into the array.


## Returns

z: Standard Python scalar object
A copy of the specified element of the array as a suitable Python scalar

## Notes

When the data type of $a$ is longdouble or clongdouble, item() returns a scalar array object because there is no available Python scalar that would not lose information. Void arrays return a buffer object for item(), unless fields are defined, in which case a tuple is returned.
item is very similar to a[args], except, instead of an array scalar, a standard Python scalar is returned. This can be useful for speeding up access to elements of the array and doing arithmetic on elements of the array using Python's optimized math.

## Examples

```
>>> x = np.random.randint(9, size=(3, 3))
>>> x
array([[3, 1, 7],
[2, 8, 3],
[8, 5, 3]])
>>> x.item(3)
2
>>> x.item(7)
5
>>> x.item((0, 1))
1
>>> x.item((2, 2))
3
```

ndarray.tolist()

Return the array as a (possibly nested) list.
Return a copy of the array data as a (nested) Python list. Data items are converted to the nearest compatible Python type.

## Parameters

none :

## Returns

$\mathbf{y}$ : list
The possibly nested list of array elements.

## Notes

The array may be recreated, $a=n p . \operatorname{array}(a . t o l i s t())$.

## Examples

```
>>> a = np.array([1, 2])
>>> a.tolist()
[1, 2]
>>> a = np.array([[1, 2], [3, 4]])
>>> list(a)
[array([1, 2]), array([3, 4])]
>>> a.tolist()
[[1, 2], [3, 4]]
```

ndarray.itemset (*args)
Insert scalar into an array (scalar is cast to array's dtype, if possible)
There must be at least 1 argument, and define the last argument as item. Then, a.itemset (*args) is
equivalent to but faster than a [args] = item. The item should be a scalar value and args must select a
single item in the array $a$.

## Parameters

*args : Arguments
If one argument: a scalar, only used in case $a$ is of size 1 . If two arguments: the last argument is the value to be set and must be a scalar, the first argument specifies a single array element location. It is either an int or a tuple.

## Notes

Compared to indexing syntax, itemset provides some speed increase for placing a scalar into a particular location in an ndarray, if you must do this. However, generally this is discouraged: among other problems, it complicates the appearance of the code. Also, when using itemset (and item) inside a loop, be sure to assign the methods to a local variable to avoid the attribute look-up at each loop iteration.

## Examples

```
>>> x = np.random.randint(9, size=(3, 3))
>>> x
array([[3, 1, 7],
    [2, 8, 3],
    [8, 5, 3]])
>>> x.itemset (4, 0)
>>> x.itemset((2, 2), 9)
>>> x
array([[3, 1, 7],
            [2, 0, 3],
            [8, 5, 9]])
```

ndarray.setasflat (arr)

Equivalent to a.flat = arr.flat, but is generally more efficient. This function does not check for overlap, so if arr and a are viewing the same data with different strides, the results will be unpredictable.

## Parameters

arr : array_like
The array to copy into a.

## Examples

```
>>> a = np.arange(2*4).reshape(2,4)[:,:-1]; a
array([[0, 1, 2],
                    [4, 5, 6]])
>>> b = np.arange(3*3, dtype='f4').reshape(3,3).T[::-1,:-1]; b
array([[ 2., 5.],
```

```
    [ 1., 4.],
    [ 0., 3.]], dtype=float32)
>>> a.setasflat(b)
>>> a
array([[2, 5, 1],
    [4, 0, 3]])
```

ndarray.tostring (order='C')

Construct a Python string containing the raw data bytes in the array.
Constructs a Python string showing a copy of the raw contents of data memory. The string can be produced in either ' C ' or 'Fortran', or 'Any' order (the default is ' C '-order). 'Any' order means C -order unless the F_CONTIGUOUS flag in the array is set, in which case it means 'Fortran' order.

## Parameters

order : \{ 'C', 'F', None \}, optional
Order of the data for multidimensional arrays: C, Fortran, or the same as for the original array.

## Returns

s: str
A Python string exhibiting a copy of $a^{\text {s }}$ s raw data.

## Examples

```
>>> x = np.array([[0, 1], [2, 3]])
>>> x.tostring()
'\x00\x00\x00\x00\x01\x00\x00\x00\x02\x00\x00\x00\x03\x00\x00\x00'
>>> x.tostring('C') == x.tostring()
True
>>> x.tostring('F')
'\x00\x00\x00\x00\x02\x00\x00\x00\x01 \x00\x00\x00\x03\x00\x00\x00'
```

ndarray.tofile (fid, sep="", format="\%s")

Write array to a file as text or binary (default).
Data is always written in ' $C$ ' order, independent of the order of $a$. The data produced by this method can be recovered using the function fromfile().

## Parameters

fid : file or str
An open file object, or a string containing a filename.
sep : str
Separator between array items for text output. If "" (empty), a binary file is written, equivalent to file.write(a.tostring()).
format : str
Format string for text file output. Each entry in the array is formatted to text by first converting it to the closest Python type, and then using "format" \% item.

## Notes

This is a convenience function for quick storage of array data. Information on endianness and precision is lost, so this method is not a good choice for files intended to archive data or transport data between machines with different endianness. Some of these problems can be overcome by outputting the data as text files, at the expense of speed and file size.
ndarray.dump (file)
Dump a pickle of the array to the specified file. The array can be read back with pickle.load or numpy.load.

## Parameters

file : str
A string naming the dump file.
ndarray. dumps ()
Returns the pickle of the array as a string. pickle.loads or numpy.loads will convert the string back to an array.

## Parameters

## None :

ndarray.astype ( $t$ )
Copy of the array, cast to a specified type.

## Parameters

$\mathbf{t}$ : str or dtype
Typecode or data-type to which the array is cast.

## Raises

## ComplexWarning : :

When casting from complex to float or int. To avoid this, one should use a.real.astype(t).

## Examples

```
>>> x = np.array([1, 2, 2.5])
>>> x
array([ 1. , 2. , 2.5])
>>> x.astype(int)
array([1, 2, 2])
```

ndarray.byteswap (inplace)

Swap the bytes of the array elements
Toggle between low-endian and big-endian data representation by returning a byteswapped array, optionally swapped in-place.

## Parameters

inplace: bool, optional :
If True, swap bytes in-place, default is False.

## Returns

out: ndarray :
The byteswapped array. If inplace is True, this is a view to self.

## Examples

```
>>> A = np.array([1, 256, 8755], dtype=np.int16)
>>> map (hex, A)
['0x1', '0x100', '0x2233']
>>> A.byteswap(True)
array([ 256, 1, 13090], dtype=int16)
>>> map (hex, A)
['0x100', '0x1', '0x3322']
```

Arrays of strings are not swapped

```
>>> A = np.array(['ceg', 'fac'])
>>> A.byteswap()
array(['ceg', 'fac'],
    dtype='|S3')
ndarray.copy (order='C')
    Return a copy of the array.
        Parameters
            order : { 'C', 'F', 'A'}, optional
                has the same order as the input.
    Examples
        >>> x = np.array([[1,2,3],[4,5,6]], order='F')
        >>> y = x.copy()
        >>> x.fill(0)
        >>> x
        array([[0, 0, 0],
            [0, 0, 0]])
        >>> y
        array([[1, 2, 3],
            [4, 5, 6]])
        >>> y.flags['C_CONTIGUOUS']
        True
ndarray.view (dtype=None, type=None)
    New view of array with the same data.
```


## Parameters

```
dtype : data-type, optional
```

            By default, the result is stored in C-contiguous (row-major) order in memory. If order is
                \(F\), the result has 'Fortran' (column-major) order. If order is ' \(A\) ' ('Any'), then the result
    Data-type descriptor of the returned view, e.g., float 32 or int 16 . The default, None, results in the view having the same data-type as $a$.
type : Python type, optional
Type of the returned view, e.g., ndarray or matrix. Again, the default None results in type preservation.

## Notes

a.view () is used two different ways:
a.view (some_dtype) or a.view (dtype=some_dtype) constructs a view of the array's memory with a different data-type. This can cause a reinterpretation of the bytes of memory.
a.view (ndarray_subclass) or a.view(type=ndarray_subclass) just returns an instance of ndarray_subclass that looks at the same array (same shape, dtype, etc.) This does not cause a reinterpretation of the memory.

## Examples

```
>>> x = np.array([(1, 2)], dtype=[('a', np.int8), ('b', np.int8)])
```

Viewing array data using a different type and dtype:

```
>>> y = x.view(dtype=np.int16, type=np.matrix)
>>> y
matrix([[513]], dtype=int16)
>>> print type(y)
<class 'numpy.matrixlib.defmatrix.matrix'>
```

Creating a view on a structured array so it can be used in calculations

```
>>> x = np.array([(1, 2), (3,4)], dtype=[('a', np.int8), ('b', np.int8)])
>>> xv = x.view(dtype=np.int8).reshape(-1,2)
>>> xv
array([[1, 2],
    [3, 4]], dtype=int8)
>>> xv.mean(0)
array([ 2., 3.])
```

Making changes to the view changes the underlying array

```
>>> xv[0,1] = 20
>>> print x
[(1, 20) (3, 4)]
```

Using a view to convert an array to a record array:

```
>>> z = x.view(np.recarray)
>>> Z.a
array([1], dtype=int8)
```

Views share data:

```
>>> x[0] = (9, 10)
>>> z[0]
(9, 10)
```


## ndarray.getfield (dtype, offset)

Returns a field of the given array as a certain type.
A field is a view of the array data with each itemsize determined by the given type and the offset into the current array, i.e. from offset * dtype.itemsize to (offset+1) * dtype.itemsize.

## Parameters

dtype : str
String denoting the data type of the field.
offset : int
Number of dtype.itemsize's to skip before beginning the element view.

## Examples

```
>>> x = np.diag([1.+1.j]*2)
>>> x
array([[ 1.+1.j, 0.+0.j],
    [ 0.+0.j, 1.+1.j]])
```

```
>>> x.dtype
dtype('complex128')
>>> x.getfield('complex64', 0) # Note how this != x
array([[ 0.+1.875j, 0.+0.j ],
    [ 0.+0.j , 0.+1.875j]], dtype=complex64)
>>> x.getfield('complex64',1) # Note how different this is than x
array([[ 0. +5.87173204e-39j, 0. +0.00000000e+00j],
    [ 0. +0.00000000e+00j, 0. +5.87173204e-39j]], dtype=complex64)
>>> x.getfield('complex128', 0) # == x
array([[ 1.+1.j, 0.+0.j],
    [ 0.+0.j, 1.+1.j]])
```

If the argument dtype is the same as x.dtype, then offset $!=0$ raises a ValueError:

```
>>> x.getfield('complex128', 1)
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
ValueError: Need 0 <= offset <= 0 for requested type but received offset = 1
>>> x.getfield('float64', 0)
array([[ 1., 0.],
    [ 0., 1.]])
>>> x.getfield('float64', 1)
array([[ 1.77658241e-307, 0.00000000e+000],
    [ 0.00000000e+000, 1.77658241e-307]])
```

ndarray.setflags (write=None, align=None, uic=None)
Set array flags WRITEABLE, ALIGNED, and UPDATEIFCOPY, respectively.
These Boolean-valued flags affect how numpy interprets the memory area used by $a$ (see Notes below). The ALIGNED flag can only be set to True if the data is actually aligned according to the type. The UPDATEIFCOPY flag can never be set to True. The flag WRITEABLE can only be set to True if the array owns its own memory, or the ultimate owner of the memory exposes a writeable buffer interface, or is a string. (The exception for string is made so that unpickling can be done without copying memory.)

## Parameters

write : bool, optional
Describes whether or not $a$ can be written to.
align : bool, optional
Describes whether or not $a$ is aligned properly for its type.
uic : bool, optional
Describes whether or not $a$ is a copy of another "base" array.

## Notes

Array flags provide information about how the memory area used for the array is to be interpreted. There are 6 Boolean flags in use, only three of which can be changed by the user: UPDATEIFCOPY, WRITEABLE, and ALIGNED.

WRITEABLE (W) the data area can be written to;
ALIGNED (A) the data and strides are aligned appropriately for the hardware (as determined by the compiler);

UPDATEIFCOPY (U) this array is a copy of some other array (referenced by .base). When this array is deallocated, the base array will be updated with the contents of this array.
All flags can be accessed using their first (upper case) letter as well as the full name.

## Examples

```
>>> y
array([[3, 1, 7],
            [2, 0, 0],
            [8, 5, 9]])
>>> y.flags
    C_CONTIGUOUS : True
    F_CONTIGUOUS : False
    OWNDATA : True
    WRITEABLE : True
    ALIGNED : True
    UPDATEIFCOPY : False
>>> y.setflags(write=0, align=0)
>>> y.flags
    C_CONTIGUOUS : True
    F_CONTIGUOUS : False
    OWNDATA : True
    WRITEABLE : False
    ALIGNED : False
    UPDATEIFCOPY : False
>>> y.setflags(uic=1)
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
ValueError: cannot set UPDATEIFCOPY flag to True
```

ndarray.fill (value)

Fill the array with a scalar value.

## Parameters

value : scalar
All elements of $a$ will be assigned this value.

## Examples

```
>>> a = np.array([1, 2])
>>> a.fill(0)
>>> a
array([0, 0])
>>> a = np.empty(2)
>>> a.fill(1)
>>> a
array([ 1., 1.])
```


## Shape manipulation

For reshape, resize, and transpose, the single tuple argument may be replaced with n integers which will be interpreted as an n-tuple.

```
ndarray.reshape(shape[, order]) Returns an array containing the same data with a new shape.
ndarray.resize(new_shape[, refcheck]) Change shape and size of array in-place.
ndarray.transpose(*axes)
ndarray.swapaxes(axis1, axis2)
ndarray.flatten([order])
ndarray.ravel()
Returns an array containing the same data with a new shape.
```

ndarray.reshape(shape[, order])
ndarray.resize(new_shape[, refcheck])
ndarray.transpose(*axes)
ndarray.swapaxes(axis1, axis2)
ndarray.flatten([order])
ndarray.ravel()
ndarray.squeeze()

Change shape and size of array in-place.
Returns a view of the array with axes transposed.
Return a view of the array with axis1 and axis2 interchanged.
Return a copy of the array collapsed into one dimension.
Return a flattened array.
Remove single-dimensional entries from the shape of $a$.

```
ndarray. reshape (shape, order='C')
Returns an array containing the same data with a new shape.
Refer to numpy . reshape for full documentation.
```


## See Also:

numpy.reshape
equivalent function
ndarray.resize (new_shape, refcheck=True)
Change shape and size of array in-place.

## Parameters

new_shape : tuple of ints, or $n$ ints
Shape of resized array.
refcheck: bool, optional
If False, reference count will not be checked. Default is True.

## Returns

None :

## Raises

ValueError :
If $a$ does not own its own data or references or views to it exist, and the data memory must be changed.

## SystemError :

If the order keyword argument is specified. This behaviour is a bug in NumPy.

## See Also:

resize
Return a new array with the specified shape.

## Notes

This reallocates space for the data area if necessary.
Only contiguous arrays (data elements consecutive in memory) can be resized.
The purpose of the reference count check is to make sure you do not use this array as a buffer for another Python object and then reallocate the memory. However, reference counts can increase in other ways so if you are sure that you have not shared the memory for this array with another Python object, then you may safely set refcheck to False.

## Examples

Shrinking an array: array is flattened (in the order that the data are stored in memory), resized, and reshaped:

```
>>> a = np.array([[0, 1], [2, 3]], order=' C')
>>> a.resize((2, 1))
>>> a
array([[0],
    [1]])
>>> a = np.array([[0, 1], [2, 3]], order=' F')
>>> a.resize((2, 1))
>>> a
array([[0],
    [2]])
```

Enlarging an array: as above, but missing entries are filled with zeros:

```
>>> b = np.array([[0, 1], [2, 3]])
>>> b.resize(2, 3) # new_shape parameter doesn't have to be a tuple
>>> b
array([[0, 1, 2],
    [3, 0, 0]])
```

Referencing an array prevents resizing...

```
>>> c = a
>>> a.resize((1, 1))
Traceback (most recent call last):
ValueError: cannot resize an array that has been referenced ...
```

Unless refcheck is False:

```
>>> a.resize((1, 1), refcheck=False)
>>> a
array([[0]])
>>> c
array([[0]])
ndarray.transpose (*axes)
```

Returns a view of the array with axes transposed.
For a 1-D array, this has no effect. (To change between column and row vectors, first cast the 1-D array into a matrix object.) For a 2-D array, this is the usual matrix transpose. For an n-D array, if axes are given, their order indicates how the axes are permuted (see Examples). If axes are not provided and a.shape = (i[0], i[1], ... i[n-2], $i[n-1])$, then a.transpose().shape $=(i[n-1], i[n-2], \ldots i[1]$, i [0]).

## Parameters

axes: None, tuple of ints, or $n$ ints

- None or no argument: reverses the order of the axes.
- tuple of ints: $i$ in the $j$-th place in the tuple means $a$ 's $i$-th axis becomes a.transpose() ${ }^{\bullet} j$-th axis.
- $n$ ints: same as an n-tuple of the same ints (this form is intended simply as a "convenience" alternative to the tuple form)


## Returns

out : ndarray

View of $a$, with axes suitably permuted.
See Also:
ndarray. T
Array property returning the array transposed.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> a
array([[1, 2],
    [3, 4]])
>>> a.transpose()
array([[1, 3],
    [2, 4]])
>>> a.transpose((1, 0))
array([[1, 3],
    [2, 4]])
>>> a.transpose(1, 0)
array([[1, 3],
    [2, 4]])
```

ndarray.swapaxes (axis1, axis2)
Return a view of the array with axis1 and axis 2 interchanged.
Refer to numpy. swapaxes for full documentation.

## See Also:

numpy.swapaxes
equivalent function

```
ndarray.flatten(order='C')
```

Return a copy of the array collapsed into one dimension.

## Parameters

order : \{ ' $C$ ', ' $F$ ', 'A' $\}$, optional
Whether to flatten in C (row-major), Fortran (column-major) order, or preserve the $\mathrm{C} /$ Fortran ordering from $a$. The default is ' C '.

## Returns

$\mathbf{y}$ : ndarray
A copy of the input array, flattened to one dimension.

## See Also:

ravel
Return a flattened array.
flat
A 1-D flat iterator over the array.

## Examples

```
>>> a = np.array([[1,2], [3,4]])
>>> a.flatten()
array([1, 2, 3, 4])
```

```
>>> a.flatten('F')
array([1, 3, 2, 4])
```

ndarray.ravel ([order])

Return a flattened array.
Refer to numpy. ravel for full documentation.

## See Also:

numpy. ravel equivalent function
ndarray.flat
a flat iterator on the array.
ndarray.squeeze ()
Remove single-dimensional entries from the shape of $a$.
Refer to numpy. squeeze for full documentation.

## See Also:

numpy.squeeze equivalent function

## Item selection and manipulation

For array methods that take an axis keyword, it defaults to None. If axis is None, then the array is treated as a 1-D array. Any other value for axis represents the dimension along which the operation should proceed.

```
ndarray.take(indices[, axis, out, Return an array formed from the elements of a at the given indices.
mode])
ndarray.put(indices, values[, mode]) Seta.flat[n] = values[n] for all n in indices.
ndarray.repeat(repeats[, axis]) Repeat elements of an array.
ndarray.choose(choices[, out, Use an index array to construct a new array from a set of choices.
mode])
ndarray.sort([axis, kind, order])
ndarray.argsort([axis, kind, order])
ndarray.searchsorted(v[, side])
ndarray.nonzero()
ndarray.compress(condition[, axis,
out])
ndarray.diagonal([offset, axis1,
axis2])
ndarray.take (indices, axis=None,out=None, mode='raise')
Return an array formed from the elements of \(a\) at the given indices.
Refer to numpy . take for full documentation.
```


## See Also:

```
numpy.take equivalent function
```

```
ndarray.put (indices, values, mode='raise')
```

Seta.flat [ n ] = values [ n ] for all $n$ in indices.
Refer to numpy . put for full documentation.

## See Also:

numpy.put
equivalent function
ndarray.repeat (repeats, axis=None)
Repeat elements of an array.
Refer to numpy . repeat for full documentation.
See Also:
numpy.repeat
equivalent function
ndarray. choose (choices, out=None, mode='raise')
Use an index array to construct a new array from a set of choices.
Refer to numpy. choose for full documentation.
See Also:
numpy. choose
equivalent function
ndarray. sort (axis=-1, kind='quicksort', order=None)
Sort an array, in-place.

## Parameters

axis : int, optional
Axis along which to sort. Default is -1 , which means sort along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## See Also:

numpy.sort
Return a sorted copy of an array.
argsort
Indirect sort.
lexsort
Indirect stable sort on multiple keys.
searchsorted
Find elements in sorted array.

## Notes

See sort for notes on the different sorting algorithms.

## Examples

```
>>> a = np.array([[1,4], [3,1]])
>>> a.sort(axis=1)
>>> a
array([[1, 4],
    [1, 3]])
>>> a.sort(axis=0)
>>> a
array([[1, 3],
    [1, 4]])
```

Use the order keyword to specify a field to use when sorting a structured array:

```
>>> a = np.array([('a', 2), ('c', 1)], dtype=[('x', 'S1'), ('y', int)])
>>> a.sort(order=' y')
>>> a
array([('c', 1), ('a', 2)],
    dtype=[('x', '|S1'), ('y', '<i4')])
```

ndarray. argsort (axis=-1, kind='quicksort', order=None)

Returns the indices that would sort this array.
Refer to numpy. argsort for full documentation.

## See Also:

numpy.argsort
equivalent function
ndarray. searchsorted ( $v$, side $=$ 'left')
Find indices where elements of v should be inserted in a to maintain order.
For full documentation, see numpy. searchsorted

## See Also:

numpy.searchsorted equivalent function
ndarray.nonzero()
Return the indices of the elements that are non-zero.
Refer to numpy. nonzero for full documentation.

## See Also:

numpy.nonzero equivalent function
ndarray. compress (condition, axis=None, out=None)
Return selected slices of this array along given axis.
Refer to numpy. compress for full documentation.
See Also:
numpy.compress
equivalent function
ndarray.diagonal (offset $=0$, axis $1=0$, axis $2=1$ )
Return specified diagonals.
Refer to numpy. diagonal for full documentation.

## See Also:

numpy.diagonal
equivalent function

## Calculation

Many of these methods take an argument named axis. In such cases,

- If axis is None (the default), the array is treated as a 1-D array and the operation is performed over the entire array. This behavior is also the default if self is a 0-dimensional array or array scalar. (An array scalar is an instance of the types/classes float32, float64, etc., whereas a 0 -dimensional array is an ndarray instance containing precisely one array scalar.)
- If axis is an integer, then the operation is done over the given axis (for each 1-D subarray that can be created along the given axis).


## Example of the axis argument

A 3-dimensional array of size $3 \times 3 \times 3$, summed over each of its three axes

```
>>> x
array([[[ 0, 1, 2],
    [ 3, 4, 5],
    [6, 7, 8]],
    [[ 9, 10, 11],
    [12, 13, 14],
    [15, 16, 17]],
    [[18, 19, 20],
    [21, 22, 23],
    [24, 25, 26]]])
>>> x.sum(axis=0)
array([[27, 30, 33],
    [36, 39, 42],
    [45, 48, 51]])
>>> # for sum, axis is the first keyword, so we may omit it,
>>> # specifying only its value
>>> x.sum(0), x.sum(1), x.sum(2)
(array([[27, 30, 33],
    [36, 39, 42],
    [45, 48, 51]]),
    array([[ 9, 12, 15],
    [36, 39, 42],
    [63, 66, 69]]),
array([[ 3, 12, 21],
    [30, 39, 48],
    [57, 66, 75]]))
```

The parameter dtype specifies the data type over which a reduction operation (like summing) should take place. The default reduce data type is the same as the data type of self. To avoid overflow, it can be useful to perform the reduction using a larger data type.

For several methods, an optional out argument can also be provided and the result will be placed into the output array given. The out argument must be an ndarray and have the same number of elements. It can have a different data type in which case casting will be performed.

| ndarray.argmax([axis, out]) | Return indices of the maximum values along the given axis. |
| :---: | :---: |
| ndarray.min([axis, out]) | Return the minimum along a given axis. |
| ndarray.argmin([axis, out]) | Return indices of the minimum values along the given axis of $a$. |
| ndarray.ptp([axis, out]) | Peak to peak (maximum - minimum) value along a given axis. |
| ndarray.clip(a_min, a_max[,out]) | Return an array whose values are limited to [a_min, a_max]. |
| ndarray.conj() | Complex-conjugate all elements. |
| ndarray.round([decimals, out]) | Return $a$ with each element rounded to the given number of decimals. |
| ndarray.trace([offset, axis1, axis2, dtype, out]) | Return the sum along diagonals of the array. |
| ndarray.sum([axis, dtype, out]) | Return the sum of the array elements over the given axis. |
| ndarray.cumsum([axis, dtype, out]) | Return the cumulative sum of the elements along the given axis. |
| ndarray.mean([axis | Returns the average of the array elements along given axis. |
| ndarray.var([axis, dtype, out, ddof]) | Returns the variance of the array elements, along given axis. |
| ndarray.std([axis, dtype, out, ddof]) | Returns the standard deviation of the array elements along given axis. |
| ndarray.prod([axis, dtype, out]) | Return the product of the array elements over the given axis |
| ndarray. cumprod([axis, dtype, out]) | Return the cumulative product of the elements along the given axis. |
| ndarray.all([axis, out]) | Returns True if all elements evaluate to True. |
| ndarray.any([axis, out]) | Returns True if any of the elements of $a$ evaluate to True. |

ndarray. argmax (axis=None, out=None)
Return indices of the maximum values along the given axis.
Refer to numpy . argmax for full documentation.

## See Also:

numpy.argmax equivalent function
ndarray.min (axis=None, out=None)
Return the minimum along a given axis.
Refer to numpy. amin for full documentation.

## See Also:

numpy.amin equivalent function
ndarray.argmin (axis=None, out=None)
Return indices of the minimum values along the given axis of $a$.
Refer to numpy . argmin for detailed documentation.

## See Also:

numpy. argmin
equivalent function
ndarray.ptp (axis=None, out=None)
Peak to peak (maximum - minimum) value along a given axis.
Refer to numpy.ptp for full documentation.

## See Also:

numpy.ptp
equivalent function
ndarray.clip (a_min, a_max, out=None)
Return an array whose values are limited to [a_min, a_max].
Refer to numpy.clip for full documentation.
See Also:
numpy.clip
equivalent function
ndarray.conj()
Complex-conjugate all elements.
Refer to numpy. conjugate for full documentation.
See Also:
numpy.conjugate
equivalent function
ndarray. round (decimals=0, out=None)
Return $a$ with each element rounded to the given number of decimals.
Refer to numpy . around for full documentation.
See Also:
numpy.around
equivalent function
ndarray.trace $($ offset $=0$, axis $1=0$, axis $2=1$, dtype $=$ None, out $=$ None $)$
Return the sum along diagonals of the array.
Refer to numpy. trace for full documentation.

## See Also:

numpy.trace
equivalent function
ndarray.sum (axis=None, dtype=None, out=None)
Return the sum of the array elements over the given axis.
Refer to numpy. sum for full documentation.
See Also:
numpy.sum
equivalent function
ndarray. cumsum (axis=None, dtype=None, out=None)
Return the cumulative sum of the elements along the given axis.
Refer to numpy. cumsum for full documentation.

## See Also:

numpy. cumsum
equivalent function
ndarray .mean (axis=None, dtype=None, out=None)
Returns the average of the array elements along given axis.
Refer to numpy.mean for full documentation.
See Also:
numpy.mean equivalent function
ndarray. var $($ axis=None, dtype=None, out=None, $d d o f=0)$
Returns the variance of the array elements, along given axis.
Refer to numpy . var for full documentation.
See Also:
numpy.var
equivalent function
ndarray.std (axis=None, dtype=None, out=None, ddof=0)
Returns the standard deviation of the array elements along given axis.
Refer to numpy. std for full documentation.
See Also:
numpy.std
equivalent function
ndarray.prod (axis=None, dtype=None, out=None)
Return the product of the array elements over the given axis
Refer to numpy.prod for full documentation.

## See Also:

numpy.prod
equivalent function
ndarray. cumprod (axis=None, dtype=None, out=None)
Return the cumulative product of the elements along the given axis.
Refer to numpy. cumprod for full documentation.
See Also:
numpy. cumprod
equivalent function
ndarray.all (axis=None, out=None)
Returns True if all elements evaluate to True.
Refer to numpy. all for full documentation.

## See Also:

numpy.all
equivalent function
ndarray. any (axis=None, out=None)
Returns True if any of the elements of $a$ evaluate to True.
Refer to numpy . any for full documentation.
See Also:
numpy. any equivalent function

### 1.1.6 Arithmetic and comparison operations

Arithmetic and comparison operations on ndarrays are defined as element-wise operations, and generally yield ndarray objects as results.

Each of the arithmetic operations (+, $-, *, /, / /, \circ, \operatorname{divmod}(), * *$ or pow (), $\langle<, \gg, \&, \wedge|,, \sim)$ and the comparisons ( $==,\langle\rangle,,\langle=,>=,!=$ ) is equivalent to the corresponding universal function (or ufunc for short) in Numpy. For more information, see the section on Universal Functions.

Comparison operators:

```
ndarray.__lt___ x.__lt__(y)<==> x < y
ndarray.__le___ x.__le__(y)<==> x<=y
ndarray.__gt__ x.__gt__(y) <==> x>y
ndarray.__ge__ x.__ge__(y)<==> x>=y
ndarray.__eq__ x.__eq__(y)<==> x==y
ndarray.__ne___ x.__ne__(y)<==> x!=y
ndarray.__lt__()
    x.__lt__(y)<==> x<y
ndarray.__le__()
    x.__le__(y)<==>> x<=y
ndarray.__gt__()
    x.__gt__(y)<==> x>y
ndarray.__ge__()
    x.__ge__(y)<==> x>=y
ndarray.__eq_()
    x.__eq__(y) <==> x==y
ndarray.__ne__()
    x.__ne__(y) <==> x!=y
```

Truth value of an array ( $\mathrm{b} \circ \circ \mathrm{l}$ ):

```
ndarray.__nonzero__ x.__nonzero__()<==>x \(!=0\)
```

```
ndarray.__nonzero__()
    x.__nonzero__()<==> x != 0
```

Note: Truth-value testing of an array invokes ndarray.__nonzero__ which raises an error if the number of elements in the the array is larger than 1, because the truth value of such arrays is ambiguous. Use . any () and . all () instead to be clear about what is meant in such cases. (If the number of elements is 0 , the array evaluates to False.)

Unary operations:

```
ndarray.__neg___ x.__neg__()<==> -x
ndarray.__pos___ x.__pos__()<==> +x
ndarray.___abs__(x)
ndarray.__invert___ x.__invert__()<==> ~x
ndarray.__neg__()
    x.__neg__() <==> -x
ndarray.__pos__()
    x.__pos__() <==> +x
ndarray.__abs__() <==> abs(x)
ndarray.__invert__()
    x.__invert__() <==> ~x
```


## Arithmetic:

```
ndarray.___add___ x.__add__(y) <==> x+y
    ndarray.__sub___ x.__sub__(y)<==> x-y
    ndarray.__mul__ x.__mul__(y)<==> x*y
    ndarray.__div___ x.__div__(y)<==> x/y
    ndarray.__truediv___ x.__truediv__(y)<==> x/y
    ndarray.__floordiv___ x.__floordiv__(y)<==> x//y
    ndarray.__mod___ x.__mod__(y)<==> x%y
    ndarray.__divmod__(x, y)
    ndarray.__pow__(x)
    ndarray.__lshift___ x.__lshift__(y)<==> x<<< 
    ndarray.__rshift___ x.__rshift__(y)<==> x>>y
    ndarray.__and___ x.__and__(y) <==> x&y
    ndarray.__or__ x.__or__(y)<==> xly
    ndarray.__xor___ x.__xor__(y)<==> x^y
ndarray.__add___()
    x.__add__(y) <==> x+y
ndarray.__sub__()
    x.__sub__(y)<==> x-y
ndarray.__mul__()
    x.__mul__(y)<==> x*y
ndarray.__div__()
    x.__div__(y)<==> x/y
ndarray.__truediv__()
    x.__truediv__(y) <==> x/y
ndarray.__floordiv__()
    x.__floordiv__(y) <==> x//y
```

```
ndarray.__mod__()
    x.__mod__(y)<==> x%y
ndarray.___divmod__ (y)<==> divmod}(x,y
ndarray.__pow__ (y[,z])<==> pow(x,y[,z])
ndarray.__lshift__()
    x.__lshift__(y)<==> x<<<y
ndarray.__rshift__()
    x.__rshift__(y)<==> x>>y
ndarray.__and__()
    x.__and__(y) <==> x&y
ndarray.__or__()
    x.__or__(y)<==>> xly
ndarray.__xor__()
    x.__xor__(y)<==> x^y
```


## Note:

- Any third argument to pow is silently ignored, as the underlying ufunc takes only two arguments.
- The three division operators are all defined; div is active by default, truediv is active when $\qquad$ future_ division is in effect.
- Because ndarray is a built-in type (written in C), the $\qquad$ r $\{o p\}$ $\qquad$ special methods are not directly defined.
- The functions called to implement many arithmetic special methods for arrays can be modified using set_numeric_ops.

Arithmetic, in-place:

```
ndarray.__iadd___ x.__iadd__(y)<==> x+y
ndarray.__isub___ x.__isub__(y)<==> x-y
ndarray.__imul___ x.__imul__(y)<==> x*y
ndarray.__idiv__ x.__idiv__(y)<==> x/y
ndarray.__itruediv__ x.__itruediv__(y)<==> x/y
ndarray.__ifloordiv__ x.__ifloordiv__(y) <==> x//y
ndarray.__imod___ x.__imod__(y)<==> x%y
ndarray.__ipow___ x.__ipow__(y)<==> x**y
ndarray.__ilshift___ x.__ilshift__(y)<==> x<<y
ndarray.__irshift__ x.__irshift__(y)<==> x>>y
ndarray.__iand___ x.__iand__(y)<==> x&y
ndarray.__ior___ x.__ior__(y)<==> xly
ndarray.__ixor__ x.__ixor__(y)<==> x^y
ndarray.__iadd__()
    x.__iadd__(y) <==> x+y
ndarray.__isub__()
    x.__isub__(y)<==> x-y
ndarray.__imul__()
    x.__imul__(y) <==> x*y
ndarray.__idiv__()
    x.__idiv__(y)<==> x/y
```

```
ndarray.__itruediv__()
    x.__itruediv__(y)<==> x/y
ndarray.__ifloordiv__()
    x.__ifloordiv__(y) <==> x//y
ndarray.__imod__()
    x.__imod__(y) <==> x%y
ndarray.__ipow__()
    x.__ipow__(y)<==> x**y
ndarray.__ilshift__()
    x.__ilshift__(y)<==> x<<<y
ndarray.__irshift__()
    x.__irshift__(y)<==> x>>y
ndarray.__iand__()
    x.__iand__(y)<==> x&y
ndarray.__ior__()
    x.__ior__(y)<==> xly
ndarray.__ixor__()
    x.__ixor__(y)<==>> x^y
```

Warning: In place operations will perform the calculation using the precision decided by the data type of the two operands, but will silently downcast the result (if necessary) so it can fit back into the array. Therefore, for mixed precision calculations, $A \quad\{o p\}=B$ can be different than $A=A \quad\{o p\}$ B. For example, suppose $a=$ ones $((3,3))$. Then, $a+=3 j$ is different than $a=a+3 j$ : while they both perform the same computation, $a+=3$ casts the result to fit back in $a$, whereas $a=a+3 j$ re-binds the name $a$ to the result.

### 1.1.7 Special methods

For standard library functions:

```
ndarray.__copy__() Return a copy of the array.
ndarray.__deepcopy__ a.__deepcopy__() -> Deep copy of array.
ndarray.__reduce__() For pickling.
ndarray.__setstate__(version, shape, dtype, ...) For unpickling.
ndarray.__copy__([order])
    Return a copy of the array.
```


## Parameters

```
order : \{ 'C', 'F', 'A'\}, optional
If order is 'C' (False) then the result is contiguous (default). If order is 'Fortran' (True) then the result has fortran order. If order is 'Any' (None) then the result has fortran order only if the array already is in fortran order.
```

ndarray.__deepcopy__()
a.__deepcopy__() -> Deep copy of array.

Used if copy.deepcopy is called on an array.
ndarray.__reduce__()
For pickling.

```
ndarray.___setstate___(version, shape,dtype,isfortran, rawdata)
```

For unpickling.

## Parameters <br> version : int

optional pickle version. If omitted defaults to 0 .
shape : tuple
dtype : data-type
isFortran : bool
rawdata : string or list
a binary string with the data (or a list if ' $a$ ' is an object array)
Basic customization:

```
ndarray.__new__
ndarray.__array__ a.__array__(Idtype) -> reference if type unchanged, copy otherwise.
ndarray.__array_wrap___ a.__array_wrap__(obj) -> Object of same type as ndarray object a.
ndarray.__array__()
a.__array__(Idtype) -> reference if type unchanged, copy otherwise.
```

Returns either a new reference to self if dtype is not given or a new array of provided data type if dtype is different from the current dtype of the array.

```
ndarray.___array_wrap__()
    a.__array_wrap__(obj) -> Object of same type as ndarray object a.
```

Container customization: (see Indexing)

```
ndarray.__len__(x)
ndarray.__getitem__ x.__getitem__(y)<==> x[y]
ndarray.__setitem__ x.__setitem__(i, y)<==> x[i]=y
ndarray.__getslice__ x.__getslice__(i,j)<==> x[i:j]
ndarray.__setslice___ x.__setslice__(i, j, y)<==> x[i:j]=y
ndarray.__contains___ x.__contains__(y)<==> y in x
ndarray.__len__()<==> len(x)
ndarray.__getitem__()
    x.__getitem__(y)<==> x[y]
ndarray.__setitem__()
    x.__setitem__(i, y) <==> x[i]=y
ndarray.__getslice__()
    x.__getslice__(i,j) <==> x[i:j]
```

Use of negative indices is not supported.
ndarray.__setslice__()
$x . \ldots$ setslice__(i, $, \mathrm{j}, \mathrm{y})<==>x[i: j]=y$

Use of negative indices is not supported.

```
ndarray.__contains__()
    x.__contains__(y)<==> y in x
```

Conversion; the operations complex, int, long, float, oct, and hex. They work only on arrays that have one element in them and return the appropriate scalar.

```
ndarray.__int__(x)
ndarray.__long__(x)
ndarray.__float___(x)
ndarray.__oct__(x)
ndarray.__hex__(x)
ndarray.___int__()<==> int(x)
ndarray.__long__() <==> long(x)
ndarray.__float__()<==> float(x)
ndarray.__oct___()<==> oct(x)
ndarray.__hex__()<==> hex(x)
```

String representations:

```
    ndarray.__str__(x)
    ndarray.__repr__(x)
ndarray.__str___() <==> str(x)
ndarray.__repr__() <==> repr(x)
```


### 1.2 Scalars

Python defines only one type of a particular data class (there is only one integer type, one floating-point type, etc.). This can be convenient in applications that don't need to be concerned with all the ways data can be represented in a computer. For scientific computing, however, more control is often needed.

In NumPy, there are 24 new fundamental Python types to describe different types of scalars. These type descriptors are mostly based on the types available in the C language that CPython is written in, with several additional types compatible with Python's types.
Array scalars have the same attributes and methods as ndarrays. ${ }^{1}$ This allows one to treat items of an array partly on the same footing as arrays, smoothing out rough edges that result when mixing scalar and array operations.

Array scalars live in a hierarchy (see the Figure below) of data types. They can be detected using the hierarchy: For example, isinstance (val, np.generic) will return True if val is an array scalar object. Alternatively, what kind of array scalar is present can be determined using other members of the data type hierarchy. Thus, for example isinstance (val, np.complexfloating) will return True if $v a l$ is a complex valued type, while isinstance (val, np.flexible) will return true if val is one of the flexible itemsize array types (string, unicode, void).

[^0]

Figure 1.2: Figure: Hierarchy of type objects representing the array data types. Not shown are the two integer types intp and uintp which just point to the integer type that holds a pointer for the platform. All the number types can be obtained using bit-width names as well.

### 1.2.1 Built-in scalar types

The built-in scalar types are shown below. Along with their (mostly) C-derived names, the integer, float, and complex data-types are also available using a bit-width convention so that an array of the right size can always be ensured (e.g. int8, float64, complex128). Two aliases (intp and uintp) pointing to the integer type that is sufficiently large to hold a C pointer are also provided. The C -like names are associated with character codes, which are shown in the table. Use of the character codes, however, is discouraged.
Five of the scalar types are essentially equivalent to fundamental Python types and therefore inherit from them as well as from the generic array scalar type:

| Array scalar type | Related Python type |
| :--- | :--- |
| int_ | IntType |
| float_- | FloatType |
| complex_- | ComplexType |
| str_- | StringType |
| unicode_ | UnicodeType |

The bool_ data type is very similar to the Python BooleanType but does not inherit from it because Python's BooleanType does not allow itself to be inherited from, and on the C-level the size of the actual bool data is not the same as a Python Boolean scalar.

Warning: The bool_ type is not a subclass of the int_ type (the bool_ is not even a number type). This is different than Python's default implementation of bool as a sub-class of int.

Tip: The default data type in Numpy is float_.
In the tables below, plat form? means that the type may not be available on all platforms. Compatibility with different C or Python types is indicated: two types are compatible if their data is of the same size and interpreted in the same way.

## Booleans:

| Type | Remarks | Character code |
| :--- | :--- | :--- |
| bool $_{-}$ | compatible: Python bool <br> bool 8 | $'^{\prime} ?^{\prime}$ |
| 8 bits |  |  |

Integers:

| byte | compatible: C char | $\prime \mathrm{b}^{\prime}$ |
| :--- | :--- | :--- |
| short | compatible: C short | $\prime \mathrm{h}$ |
| intc | compatible: C int | $\mathrm{h}^{\prime}$ |
| int_ | compatible: Python int | $\mathrm{i}^{\prime}$ |
| longlong | compatible: C long long | $\prime \mathrm{q}^{\prime}$ |
| intp | large enough to fit a pointer | $\prime \mathrm{p}^{\prime}$ |
| int8 | 8 bits |  |
| int16 | 16 bits |  |
| int32 | 32 bits |  |
| int 64 | 64 bits |  |

Unsigned integers:

| ubyte | compatible: C unsigned char | $\prime \mathrm{B}^{\prime}$ |
| :--- | :--- | :--- |
| ushort | compatible: C unsigned short | $\mathrm{H}^{\prime}$ |
| uintc | compatible: C unsigned int | $\mathrm{I}^{\prime}$ |
| uint | compatible: Python int | $\prime \mathrm{L}^{\prime}$ |
| ulonglong | compatible: C long long | $\mathrm{Q}^{\prime}$ |
| uintp | large enough to fit a pointer | $\mathrm{I}^{\prime}$ |
| uint8 | 8 bits |  |
| uint16 | 16 bits |  |
| uint 32 | 32 bits |  |
| uint 64 | 64 bits |  |

Floating-point numbers:

| half |  | ' ${ }^{\prime}$ |
| :---: | :---: | :---: |
| single | compatible: C float | 'f' |
| double | compatible: C double |  |
| float_ | compatible: Python float | ' d' |
| longfloat | compatible: C long float | ' g' |
| float16 | 16 bits |  |
| float 32 | 32 bits |  |
| float 64 | 64 bits |  |
| float96 | 96 bits, platform? |  |
| float128 | 128 bits, platform? |  |

Complex floating-point numbers:

| csingle <br> complex_ <br> clongfloat | compatible: Python complex | ' $^{\prime}$ |
| :--- | :--- | :--- |
| complex64 <br> complex128 | two 32-bit floats | two 64-bit floats |
| complex192 | two 96-bit floats, platform? |  |
| complex256 | two 128-bit floats, platform? |  |

Any Python object:

| object_ | any Python object | $O^{\prime}$ |
| :--- | :--- | :--- |

Note: The data actually stored in object arrays (i.e., arrays having dtype object_) are references to Python objects, not the objects themselves. Hence, object arrays behave more like usual Python lists, in the sense that their contents need not be of the same Python type.

The object type is also special because an array containing ob ject_ items does not return an object_ object on item access, but instead returns the actual object that the array item refers to.

The following data types are flexible. They have no predefined size: the data they describe can be of different length in different arrays. (In the character codes \# is an integer denoting how many elements the data type consists of.)

| str_ <br> unicode_ <br> void | compatible: Python str compatible: Python unicode | $\begin{aligned} & \text { 'S\#' } \\ & \text { 'U\#' } \\ & \text { 'V\#' } \end{aligned}$ |
| :---: | :---: | :---: |

Warning: Numeric Compatibility: If you used old typecode characters in your Numeric code (which was never recommended), you will need to change some of them to the new characters. In particular, the needed changes are c -> S1, b -> B, 1 -> b, s -> h, w -> H, and u -> I. These changes make the type character convention more consistent with other Python modules such as the struct module.

### 1.2.2 Attributes

The array scalar objects have an array priority of NPY_SCALAR_PRIORITY (-1,000,000.0). They also do not (yet) have a ctypes attribute. Otherwise, they share the same attributes as arrays:

```
generic.flags integer value of flags
generic.shape tuple of array dimensions
generic.strides tuple of bytes steps in each dimension
generic.ndim number of array dimensions
generic.data pointer to start of data
generic.size number of elements in the gentype
generic.itemsize length of one element in bytes
generic.base base object
generic.dtype get array data-descriptor
generic.real real part of scalar
generic.imag imaginary part of scalar
generic.flat a 1-d view of scalar
generic.T transpose
generic.__array_interface__ Array protocol: Python side
generic.__array_struct__ Array protocol: struct
generic.__array_priority__ Array priority.
generic.__array_wrap___ sc.__array_wrap__(obj) return scalar from array
generic.flags
    integer value of flags
generic.shape
    tuple of array dimensions
generic.strides
    tuple of bytes steps in each dimension
generic.ndim
    number of array dimensions
generic.data
    pointer to start of data
generic.size
    number of elements in the gentype
generic.itemsize
    length of one element in bytes
generic.base
    base object
generic.dtype
    get array data-descriptor
generic.real
    real part of scalar
generic.imag
    imaginary part of scalar
generic.flat
    a 1-d view of scalar
generic.T
    transpose
```

```
generic.__array_interface__
Array protocol: Python side
generic.__array_struct__
    Array protocol: struct
generic.__array_priority__
    Array priority.
generic.___array_wrap__()
    sc.__array_wrap__(obj) return scalar from array
```


### 1.2.3 Indexing

## See Also:

Indexing, Data type objects (dtype)
Array scalars can be indexed like 0 -dimensional arrays: if $x$ is an array scalar,

- $x[()]$ returns a 0 -dimensional ndarray
- $\mathrm{x}[$ 'field-name'] returns the array scalar in the field field-name. ( $x$ can have fields, for example, when it corresponds to a record data type.)


### 1.2.4 Methods

Array scalars have exactly the same methods as arrays. The default behavior of these methods is to internally convert the scalar to an equivalent 0 -dimensional array and to call the corresponding array method. In addition, math operations on array scalars are defined so that the same hardware flags are set and used to interpret the results as for ufunc, so that the error state used for ufuncs also carries over to the math on array scalars.

The exceptions to the above rules are given below:

| generic | Base class for numpy scalar types. |
| :--- | :--- |
| generic.__array__ | sc.__array__(Itype) return 0-dim array |
| generic.__array_wrap__ | sc.__array_wrap__(obj) return scalar from array |
| generic.squeeze | Not implemented (virtual attribute) |
| generic.byteswap | Not implemented (virtual attribute) |
| generic.__reduce___ <br> generic.__setstate__ <br> generic.setflags |  |

class numpy.generic
Base class for numpy scalar types.
Class from which most (all?) numpy scalar types are derived. For consistency, exposes the same API as ndarray, despite many consequent attributes being either "get-only," or completely irrelevant. This is the class from which it is strongly suggested users should derive custom scalar types.

## Methods



Table 1.2 - continued from previous page
astype
byteswap
choose(a, choices[, out, mode]) Construct an array from an index array and a set of arrays to choose from.
$\operatorname{clip}(a$, a_min, a_max[, out]) Clip (limit) the values in an array.
compress(condition, a[, axis, out]) Return selected slices of an array along given axis.
conj()
conjugate()
copy(a)
Return the complex conjugate, element-wise.
Return the complex conjugate, element-wise.
cumprod(a[, axis, dtype, out $]$ ) Return the cumulative product of elements along a given axis.
cumsum(a[, axis, dtype, out $]$ ) Return the cumulative sum of the elements along a given axis.
diagonal(a[, offset, axis1, axis2]) Return specified diagonals.
dump
dumps
fill
flatten
getfield
item
itemset
$\max (\mathrm{a}[$ axis, out $]) \quad$ Return the maximum of an array or maximum along an axis.
$\operatorname{mean}(\mathrm{a}[$, axis, dtype, out $])$ Compute the arithmetic mean along the specified axis.
$\min (\mathrm{a}[$ axis, out $]$ Return the minimum of an array or minimum along an axis.
newbyteorder
nonzero(a)
$\operatorname{prod}(a[$ axis, dtype, out $])$
$\operatorname{ptp}(\mathrm{a}[, \quad$ axis, out $])$
put(a, ind, $\mathrm{v}[$, mode $]$ )
ravel(a[, order])
repeat(a, repeats[, axis])
Return the indices of the elements that are non-zero.
Return the product of array elements over a given axis.
Range of values (maximum - minimum) along an axis.
Replaces specified elements of an array with given values.
Return a flattened array.
reshape(a, newshape[, order])
Repeat elements of an array.
Gives a new shape to an array without changing its data.
resize(a, new_shape)
round(a[, decimals, out])
Return a new array with the specified shape.
searchsorted $(a, \quad \mathrm{v}[$, side $]) \quad$ Find indices where elements should be inserted to maintain order.
setfield
setflags
sort(a[, axis, kind, order]) Return a sorted copy of an array.
squeeze(a)
std(a[, axis, dtype, out, ddof])
$\operatorname{sum}(\mathrm{a}[$ axis, dtype, out $])$
Remove single-dimensional entries from the shape of an array.
Compute the standard deviation along the specified axis.

Interchange two axes of an array.
take(a, indices[, axis, out, mode]) Take elements from an array along an axis.
tofile
tolist
tostring
trace (a[, offset, axis1, axis2, dtype, out $]$ ) Return the sum along diagonals of the array.
transpose(a[, axes]) Permute the dimensions of an array.
$\operatorname{var}(\mathrm{a}[$, axis, dtype, out, ddof $])$ Compute the variance along the specified axis.
view
numpy.all (a, axis=None, out=None)
Test whether all array elements along a given axis evaluate to True.

## Parameters

a: array_like

Input array or object that can be converted to an array.
axis : int, optional
Axis along which a logical AND is performed. The default (axis $=$ None) is to perform a logical AND over a flattened input array. axis may be negative, in which case it counts from the last to the first axis.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output and its type is preserved (e.g., if dtype (out) is float, the result will consist of 0.0 's and 1.0 's). See doc.ufuncs (Section "Output arguments") for more details.

## Returns

all : ndarray, bool
A new boolean or array is returned unless out is specified, in which case a reference to out is returned.

## See Also:

ndarray.all
equivalent method
any
Test whether any element along a given axis evaluates to True.

## Notes

Not a Number (NaN), positive infinity and negative infinity evaluate to True because these are not equal to zero.

Examples

```
>>> np.all([[True,False],[True,True]])
False
>>> np.all([[True,False],[True,True]], axis=0)
array([ True, False], dtype=bool)
>>> np.all([-1, 4, 5])
True
>>> np.all([1.0, np.nan])
True
>>> o=np.array([False])
>>> z=np.all([-1, 4, 5], out=0)
>>> id(z), id(o), z
(28293632, 28293632, array([ True], dtype=bool))
```

numpy . any ( $a$, axis=None, out=None)
Test whether any array element along a given axis evaluates to True.
Returns single boolean unless axis is not None

## Parameters

a : array_like
Input array or object that can be converted to an array.
axis : int, optional
Axis along which a logical OR is performed. The default (axis $=$ None) is to perform a logical OR over a flattened input array. axis may be negative, in which case it counts from the last to the first axis.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output and its type is preserved (e.g., if it is of type float, then it will remain so, returning 1.0 for True and 0.0 for False, regardless of the type of $a$ ). See doc.ufuncs (Section "Output arguments") for details.

## Returns

any : bool or ndarray
A new boolean or ndarray is returned unless out is specified, in which case a reference to out is returned.

## See Also:

ndarray.any
equivalent method
all
Test whether all elements along a given axis evaluate to True.

## Notes

Not a Number (NaN), positive infinity and negative infinity evaluate to True because these are not equal to zero.

Examples

```
>>> np.any([[True, False], [True, True]])
True
>>> np.any([[True, False], [False, False]], axis=0)
array([ True, False], dtype=bool)
>>> np.any([-1, 0, 5])
True
>>> np.any(np.nan)
True
>>> o=np.array([False])
>>> z=np.any([-1, 4, 5], out=0)
>>> z, O
(array([ True], dtype=bool), array([ True], dtype=bool))
>>> # Check now that z is a reference to o
>>> z is o
True
>>> id(z), id(o) # identity of z and o
(191614240, 191614240)
```

numpy .argmax (a, axis=None)

Indices of the maximum values along an axis.

## Parameters

a : array_like

Input array.
axis : int, optional
By default, the index is into the flattened array, otherwise along the specified axis.

## Returns

index_array : ndarray of ints
Array of indices into the array. It has the same shape as a.shape with the dimension along axis removed.

## See Also:

ndarray.argmax, argmin
amax
The maximum value along a given axis.

```
unravel_index
```

Convert a flat index into an index tuple.

## Notes

In case of multiple occurrences of the maximum values, the indices corresponding to the first occurrence are returned.

## Examples

```
>>> a = np.arange(6).reshape(2,3)
>>> a
array([[0, 1, 2],
    [3, 4, 5]])
>>> np.argmax(a)
5
>>> np.argmax(a, axis=0)
array([1, 1, 1])
>>> np.argmax(a, axis=1)
array([2, 2])
>>> b = np.arange(6)
>>> b[1] = 5
>>> b
array([0, 5, 2, 3, 4, 5])
>>> np.argmax(b) # Only the first occurrence is returned.
1
```

numpy. argmin (a, axis=None)

Return the indices of the minimum values along an axis.
See Also:
argmax
Similar function. Please refer to numpy . argmax for detailed documentation.
numpy.argsort (a, axis=-1, kind='quicksort', order=None)
Returns the indices that would sort an array.
Perform an indirect sort along the given axis using the algorithm specified by the kind keyword. It returns an array of indices of the same shape as $a$ that index data along the given axis in sorted order.

## Parameters

a : array_like
Array to sort.
axis : int or None, optional
Axis along which to sort. The default is -1 (the last axis). If None, the flattened array is used.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## Returns

index_array : ndarray, int
Array of indices that sort $a$ along the specified axis. In other words, a [index_array] yields a sorted $a$.

## See Also:

sort
Describes sorting algorithms used.

## lexsort

Indirect stable sort with multiple keys.

```
ndarray.sort
```

Inplace sort.

## Notes

See sort for notes on the different sorting algorithms.
As of NumPy 1.4.0 argsort works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

One dimensional array:

```
>>> x = np.array([3, 1, 2])
>>> np.argsort(x)
array([1, 2, 0])
```

Two-dimensional array:

```
>>> x = np.array([[0, 3], [2, 2]])
>>> x
array([[0, 3],
    [2, 2]])
>>> np.argsort(x, axis=0)
array([[0, 1],
    [1, 0]])
```

```
>>> np.argsort(x, axis=1)
array([[0, 1],
    [0, 1]])
```

Sorting with keys:

```
>>> x = np.array([(1, 0), (0, 1)], dtype=[('x', '<i4'), ('y', '<i4')])
>>> x
array([(1, 0), (0, 1)],
    dtype=[('x', '<i4'), ('y', '<i4')])
>>> np.argsort(x, order=(' x',' y'))
array([1, 0])
>>> np.argsort(x, order=(' y',' x'))
array([0, 1])
```

numpy. choose (a, choices, out=None, mode='raise')
Construct an array from an index array and a set of arrays to choose from.
First of all, if confused or uncertain, definitely look at the Examples - in its full generality, this function is less simple than it might seem from the following code description (below ndi $=$ numpy.lib.index_tricks):
np.choose(a,c) == np.array([c[a[I]][I] for I in ndi.ndindex(a.shape)]).
But this omits some subtleties. Here is a fully general summary:
Given an "index" array ( $a$ ) of integers and a sequence of $n$ arrays (choices), $a$ and each choice array are first broadcast, as necessary, to arrays of a common shape; calling these Ba and Bchoices $[i], i=0, \ldots, n-1$ we have that, necessarily, Ba.shape == Bchoices[i].shape for each $i$. Then, a new array with shape Ba . shape is created as follows:
-if mode=raise (the default), then, first of all, each element of $a$ (and thus $B a$ ) must be in the range $[0, n-1]$; now, suppose that $i$ (in that range) is the value at the $(j 0, j 1, \ldots, j m)$ position in $B a$ - then the value at the same position in the new array is the value in Bchoices $[i]$ at that same position;
-if mode=wrap, values in $a$ (and thus $B a$ ) may be any (signed) integer; modular arithmetic is used to map integers outside the range [ $0, n-1]$ back into that range; and then the new array is constructed as above;
-if mode $=$ clip, values in $a$ (and thus $B a$ ) may be any (signed) integer; negative integers are mapped to 0 ; values greater than $n-1$ are mapped to $n-1$; and then the new array is constructed as above.

## Parameters

a : int array
This array must contain integers in $[0, n-1]$, where $n$ is the number of choices, unless mode=wrap or mode=clip, in which cases any integers are permissible.
choices : sequence of arrays
Choice arrays. $a$ and all of the choices must be broadcastable to the same shape. If choices is itself an array (not recommended), then its outermost dimension (i.e., the one corresponding to choices.shape [0]) is taken as defining the "sequence".
out : array, optional
If provided, the result will be inserted into this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise' (default), 'wrap', 'clip'\}, optional

Specifies how indices outside [ $0, n-1$ ] will be treated:

- 'raise' : an exception is raised
- 'wrap' : value becomes value $\bmod n$
- 'clip' : values $<0$ are mapped to 0 , values $>\mathrm{n}-1$ are mapped to $\mathrm{n}-1$


## Returns

merged_array : array
The merged result.

## Raises

ValueError: shape mismatch :
If $a$ and each choice array are not all broadcastable to the same shape.

## See Also:

ndarray. choose
equivalent method

## Notes

To reduce the chance of misinterpretation, even though the following "abuse" is nominally supported, choices should neither be, nor be thought of as, a single array, i.e., the outermost sequence-like container should be either a list or a tuple.

## Examples

```
>>> choices = [[0, 1, 2, 3], [10, 11, 12, 13],
... [20, 21, 22, 23], [30, 31, 32, 33]]
>>> np.choose([2, 3, 1, 0], choices
... # the first element of the result will be the first element of the
... # third (2+1) "array" in choices, namely, 20; the second element
... # will be the second element of the fourth (3+1) choice array, i.e.,
... # 31, etc.
... )
array([20, 31, 12, 3])
>>> np.choose([2, 4, 1, 0], choices, mode='clip') # 4 goes to 3 (4-1)
array([20, 31, 12, 3])
>>> # because there are 4 choice arrays
>>> np.choose([2, 4, 1, 0], choices, mode='wrap') # 4 goes to (4 mod 4)
array([20, 1, 12, 3])
>>> # i.e., 0
```

A couple examples illustrating how choose broadcasts:

```
>>> a = [[1, 0, 1], [0, 1, 0], [1, 0, 1]]
>>> choices = [-10, 10]
>>> np.choose(a, choices)
array([[ 10, -10, 10],
    [-10, 10, -10],
    [ 10, -10, 10]])
>>> # With thanks to Anne Archibald
>>> a = np.array([0, 1]).reshape((2,1,1))
>>> c1 = np.array([1, 2, 3]).reshape((1,3,1))
>>> c2 = np.array([-1, -2, -3, -4, -5]).reshape((1,1,5))
>>> np.choose(a, (c1, c2)) # result is 2x3\times5, res[0,:,:]=c1, res[1,:,:]=c2
```

```
array([[[[ 1, 1, 1, 1, 1],
    [2, 2, 2, 2, 2],
    [ 3, 3, 3, 3, 3]],
    [[[-1, -2, -3, -4, -5],
    [-1, -2, -3, -4, -5],
    [-1, -2, -3, -4, -5]]])
```

numpy.clip (a, a_min, a_max, out=None)
Clip (limit) the values in an array.
Given an interval, values outside the interval are clipped to the interval edges. For example, if an interval of $[0,1]$ is specified, values smaller than 0 become 0 , and values larger than 1 become 1 .

## Parameters

a : array_like
Array containing elements to clip.
a_min : scalar or array_like
Minimum value.
a_max : scalar or array_like
Maximum value. If $a \_$min or $a \_m a x$ are array_like, then they will be broadcasted to the shape of $a$.
out : ndarray, optional
The results will be placed in this array. It may be the input array for in-place clipping. out must be of the right shape to hold the output. Its type is preserved.

## Returns

clipped_array : ndarray
An array with the elements of $a$, but where values < $a_{-} \min$ are replaced with $a_{-}$min, and those >a_max with $a_{-}$max.

## See Also:

numpy.doc. ufuncs
Section "Output arguments"
Examples

```
>>> a = np.arange(10)
>>> np.clip(a, 1, 8)
array([1, 1, 2, 3, 4, 5, 6, 7, 8, 8])
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, 3, 6, out=a)
array([3, 3, 3, 3, 4, 5, 6, 6, 6, 6])
>>> a = np.arange(10)
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, [3,4,1,1,1,4,4,4,4,4], 8)
array([3, 4, 2, 3, 4, 5, 6, 7, 8, 8])
```

numpy. compress (condition, a, axis=None, out=None)
Return selected slices of an array along given axis.

When working along a given axis, a slice along that axis is returned in output for each index where condition evaluates to True. When working on a 1-D array, compress is equivalent to extract.

## Parameters

condition : 1-D array of bools
Array that selects which entries to return. If len(condition) is less than the size of $a$ along the given axis, then output is truncated to the length of the condition array.
a : array_like
Array from which to extract a part.
axis : int, optional
Axis along which to take slices. If None (default), work on the flattened array.
out : ndarray, optional
Output array. Its type is preserved and it must be of the right shape to hold the output.

## Returns

compressed_array : ndarray
A copy of $a$ without the slices along axis for which condition is false.

## See Also:

```
take, choose, diag, diagonal, select
```

ndarray. compress

Equivalent method.

## numpy.doc.ufuncs

Section "Output arguments"

## Examples

```
>>> a = np.array([[1, 2], [3, 4], [5, 6]])
>>> a
array([[1, 2],
        [3, 4],
        [5, 6]])
>>> np.compress([0, 1], a, axis=0)
array([[3, 4]])
>>> np.compress([False, True, True], a, axis=0)
array([[3, 4],
            [5, 6]])
>>> np.compress([False, True], a, axis=1)
array([[2],
    [4],
    [6]])
```

Working on the flattened array does not return slices along an axis but selects elements.

```
>>> np.compress([False, True], a)
array([2])
```

numpy. conj ( $x[$, out $]$ )
Return the complex conjugate, element-wise.
The complex conjugate of a complex number is obtained by changing the sign of its imaginary part.

## Parameters

$\mathbf{x}$ : array_like
Input value.

## Returns

$\mathbf{y}$ : ndarray
The complex conjugate of $x$, with same dtype as $y$.

## Examples

```
>>> np.conjugate(1+2j)
(1-2j)
>>> x = np.eye(2) + 1j * np.eye(2)
>>> np.conjugate(x)
array([[ 1.-1.j, 0.-0.j],
            [ 0.-0.j, 1.-1.j]])
```

numpy. copy (a)
Return an array copy of the given object.

## Parameters

a : array_like
Input data.

## Returns

arr : ndarray
Array interpretation of $a$.

## Notes

This is equivalent to

```
>>> np.array(a, copy=True)
```


## Examples

Create an array $x$, with a reference $y$ and a copy $z$ :

```
>>> x = np.array([1, 2, 3])
>>> y = x
>>> z = np.copy(x)
```

Note that, when we modify $\mathrm{x}, \mathrm{y}$ changes, but not z :

```
>>> x[0] = 10
>>> x[0] == y[0]
True
>>> x[0] == z[0]
False
```

numpy. cumprod ( $a$, axis=None, dtype=None, out=None)
Return the cumulative product of elements along a given axis.

## Parameters

a : array_like
Input array.
axis : int, optional
Axis along which the cumulative product is computed. By default the input is flattened.
dtype : dtype, optional
Type of the returned array, as well as of the accumulator in which the elements are multiplied. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used instead.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type of the resulting values will be cast if necessary.

## Returns

cumprod : ndarray
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## See Also:

## numpy.doc.ufuncs

Section "Output arguments"

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> a = np.array([1,2,3])
>>> np.cumprod(a) # intermediate results 1, 1*2
... # total product 1*2*3 = 6
array([1, 2, 6])
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
>>> np.cumprod(a, dtype=float) # specify type of output
array([ 1., 2., 6., 24., 120., 720.])
```

The cumulative product for each column (i.e., over the rows) of $a$ :

```
>>> np.cumprod(a, axis=0)
array([[ 1, 2, 3],
    [ 4, 10, 18]])
```

The cumulative product for each row (i.e. over the columns) of $a$ :

```
>>> np.cumprod(a,axis=1)
array([[ 1, 2, 6],
    [ 4, 20, 120]])
```

numpy. cumsum (a, axis=None, dtype=None, out=None)
Return the cumulative sum of the elements along a given axis.

## Parameters

a : array_like
Input array.
axis : int, optional

Axis along which the cumulative sum is computed. The default (None) is to compute the cumsum over the flattened array.

```
dtype : dtype, optional
```

Type of the returned array and of the accumulator in which the elements are summed. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used.

```
out : ndarray, optional
```

Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

```
        cumsum_along_axis : ndarray.
```

A new array holding the result is returned unless out is specified, in which case a reference to out is returned. The result has the same size as $a$, and the same shape as $a$ if axis is not None or $a$ is a 1-d array.

## See Also:

sum
Sum array elements.
trapz
Integration of array values using the composite trapezoidal rule.

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> a
array([[1, 2, 3],
    [4, 5, 6]])
>>> np.cumsum(a)
array([ 1, 3, 6, 10, 15, 21])
>>> np.cumsum(a, dtype=float) # specifies type of output value(s)
array([ 1., 3., 6., 10., 15., 21.])
>>> np.cumsum(a,axis=0) # sum over rows for each of the 3 columns
array([[1, 2, 3],
            [5, 7, 9]])
>>> np.cumsum(a,axis=1) # sum over columns for each of the 2 rows
array([[ 1, 3, 6],
    [ 4, 9, 15]])
```

numpy.diagonal (a, offset $=0$, axis $1=0$, axis $2=1$ )
Return specified diagonals.
If $a$ is 2-D, returns the diagonal of $a$ with the given offset, i.e., the collection of elements of the form a [i, i+offset]. If $a$ has more than two dimensions, then the axes specified by axisl and axis 2 are used to determine the 2-D sub-array whose diagonal is returned. The shape of the resulting array can be determined by removing axisl and axis 2 and appending an index to the right equal to the size of the resulting diagonals.

## Parameters

a : array_like
Array from which the diagonals are taken.
offset : int, optional
Offset of the diagonal from the main diagonal. Can be positive or negative. Defaults to main diagonal (0).
axis1 : int, optional
Axis to be used as the first axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults to first axis (0).
axis2 : int, optional
Axis to be used as the second axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults to second axis (1).

## Returns

array_of_diagonals : ndarray
If $a$ is $2-\mathrm{D}$, a $1-\mathrm{D}$ array containing the diagonal is returned. If the dimension of $a$ is larger, then an array of diagonals is returned, "packed" from left-most dimension to right-most (e.g., if $a$ is 3-D, then the diagonals are "packed" along rows).

## Raises

ValueError :
If the dimension of $a$ is less than 2 .

## See Also:

diag
MATLAB work-a-like for 1-D and 2-D arrays.
diagflat
Create diagonal arrays.
trace
Sum along diagonals.

## Examples

```
>>> a = np.arange(4).reshape(2,2)
>>> a
array([[0, 1],
            [2, 3]])
>>> a.diagonal()
array([0, 3])
>>> a.diagonal(1)
array([1])
```

A 3-D example:

```
>>> a = np.arange(8).reshape(2,2,2); a
array([[[0, 1],
            [2, 3]],
            [[4, 5],
            [6, 7]]])
>>> a.diagonal(0, # Main diagonals of two arrays created by skipping
... 0, # across the outer(left)-most axis last and
```

```
1) # the "middle" (row) axis first.
array([[0, 6],
    [1, 7]])
```

The sub-arrays whose main diagonals we just obtained; note that each corresponds to fixing the right-most (column) axis, and that the diagonals are "packed" in rows.

```
>>> a[:,:,0] # main diagonal is [0 6]
array([[0, 2],
    [4, 6]])
>>> a[:,:,1] # main diagonal is [1 7]
array([[1, 3],
    [5, 7]])
```

numpy .mean ( $a$, axis=None, dtype=None, out=None)
Compute the arithmetic mean along the specified axis.
Returns the average of the array elements. The average is taken over the flattened array by default, otherwise over the specified axis. float64 intermediate and return values are used for integer inputs.

## Parameters

a : array_like
Array containing numbers whose mean is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the means are computed. The default is to compute the mean of the flattened array.
dtype : data-type, optional
Type to use in computing the mean. For integer inputs, the default is float64; for floating point inputs, it is the same as the input dtype.

```
out : ndarray, optional
```

Alternate output array in which to place the result. The default is None; if provided, it must have the same shape as the expected output, but the type will be cast if necessary. See doc.ufuncs for details.

## Returns

m : ndarray, see dtype parameter above
If out=None, returns a new array containing the mean values, otherwise a reference to the output array is returned.

## See Also:

average
Weighted average

## Notes

The arithmetic mean is the sum of the elements along the axis divided by the number of elements.
Note that for floating-point input, the mean is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-precision accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.mean(a)
2.5
>>> np.mean(a, axis=0)
array([ 2., 3.])
>>> np.mean(a, axis=1)
array([ 1.5, 3.5])
```

In single precision, mean can be inaccurate:

```
>>> a = np.zeros((2, 512*512), dtype=np.float32)
>>> a[0, :] = 1.0
>>> a[1, :] = 0.1
>>> np.mean(a)
0.546875
```

Computing the mean in float64 is more accurate:

```
>>> np.mean(a, dtype=np.float64)
0.550000000074505806
```

numpy.nonzero (a)
Return the indices of the elements that are non-zero.
Returns a tuple of arrays, one for each dimension of $a$, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

```
a[nonzero(a)]
```

To group the indices by element, rather than dimension, use:

```
transpose(nonzero(a))
```

The result of this is always a 2-D array, with a row for each non-zero element.

## Parameters

a: array_like
Input array.

## Returns

tuple_of_arrays : tuple
Indices of elements that are non-zero.

## See Also:

## flatnonzero

Return indices that are non-zero in the flattened version of the input array.
ndarray.nonzero
Equivalent ndarray method.
count_nonzero
Counts the number of non-zero elements in the input array.

## Examples

```
>>> x = np.eye(3)
>>> x
array([[ 1., 0., 0.],
    [ 0., 1., 0.],
    [ 0., 0., 1.]])
>>> np.nonzero(x)
(array([0, 1, 2]), array([0, 1, 2]))
>>> x[np.nonzero(x)]
array([ 1., 1., 1.])
>>> np.transpose(np.nonzero(x))
array([[0, 0],
    [1, 1],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , np.nonzero( $a>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a = np.array([[1,2,3],[4,5,6],[7,8,9]])
>>> a > 3
array([[False, False, False],
    [ True, True, True],
    [ True, True, True]], dtype=bool)
>>> np.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the boolean array can also be called.

```
>>> (a > 3).nonzero()
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

numpy $\cdot \operatorname{prod}(a$, axis=None, dtype=None, out=None)
Return the product of array elements over a given axis.

## Parameters

a : array_like
Input data.
axis : int, optional
Axis over which the product is taken. By default, the product of all elements is calculated.
dtype : data-type, optional
The data-type of the returned array, as well as of the accumulator in which the elements are multiplied. By default, if $a$ is of integer type, dtype is the default platform integer. (Note: if the type of $a$ is unsigned, then so is dtype.) Otherwise, the dtype is the same as that of $a$.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output, but the type of the output values will be cast if necessary.

## Returns

product_along_axis : ndarray, see dtype parameter above.
An array shaped as $a$ but with the specified axis removed. Returns a reference to out if specified.

## See Also:

ndarray.prod
equivalent method
numpy.doc. ufuncs
Section "Output arguments"

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow. That means that, on a 32-bit platform:

```
>>> x = np.array([536870910, 536870910, 536870910, 536870910])
>>> np.prod(x) #random
16
```


## Examples

By default, calculate the product of all elements:

```
>>> np.prod([1., 2.])
2.0
```

Even when the input array is two-dimensional:

```
>>> np.prod([[1.,2.],[3.,4.]])
24.0
```

But we can also specify the axis over which to multiply:

```
>>> np.prod([[1.,2.],[3.,4.]], axis=1)
array([ 2., 12.])
```

If the type of $x$ is unsigned, then the output type is the unsigned platform integer:

```
>>> x = np.array([1, 2, 3], dtype=np.uint8)
>>> np.prod(x).dtype == np.uint
True
```

If $x$ is of a signed integer type, then the output type is the default platform integer:

```
>>> x = np.array([1, 2, 3], dtype=np.int8)
>>> np.prod(x).dtype == np.int
True
```

numpy.ptp $(a$, axis=None, out $=$ None $)$

Range of values (maximum - minimum) along an axis.
The name of the function comes from the acronym for 'peak to peak'.

## Parameters

a : array_like
Input values.
axis : int, optional
Axis along which to find the peaks. By default, flatten the array.
out : array_like

Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output, but the type of the output values will be cast if necessary.

## Returns

ptp : ndarray
A new array holding the result, unless out was specified, in which case a reference to out is returned.

## Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
            [2, 3]])
>>> np.ptp(x, axis=0)
array([2, 2])
>>> np.ptp(x, axis=1)
array([1, 1])
```

numpy.put ( $a$, ind, $v$, mode='raise')
Replaces specified elements of an array with given values.
The indexing works on the flattened target array. put is roughly equivalent to:

$$
\text { a.flat[ind] }=\text { v }
$$

## Parameters

a : ndarray
Target array.
ind : array_like
Target indices, interpreted as integers.
$\mathbf{v}$ : array_like
Values to place in $a$ at target indices. If $v$ is shorter than ind it will be repeated as necessary.
mode : \{'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## See Also:

putmask, place

## Examples

```
>>> a = np.arange(5)
>>> np.put(a, [0, 2], [-44, -55])
>>> a
array([-44, 1, -55, 3, 4])
>>> a = np.arange(5)
>>> np.put(a, 22, -5, mode='clip')
>>> a
array([ 0, 1, 2, 3, -5])
```

numpy. ravel ( $a$, order= ' $C$ ')
Return a flattened array.
A 1-D array, containing the elements of the input, is returned. A copy is made only if needed.

## Parameters

a : array_like
Input array. The elements in a are read in the order specified by order, and packed as a 1-D array.
order : \{ 'C','F', 'A', 'K' \}, optional
The elements of a are read in this order. ' $C$ ' means to view the elements in $C$ (rowmajor) order. ' F ' means to view the elements in Fortran (column-major) order. 'A' means to view the elements in ' $F$ ' order if a is Fortran contiguous, ' $C$ ' order otherwise. ' K ' means to view the elements in the order they occur in memory, except for reversing the data when strides are negative. By default, ' C ' order is used.

## Returns <br> 1d_array : ndarray

Output of the same dtype as $a$, and of shape (a.size(), ).

## See Also:

ndarray.flat
1-D iterator over an array.
ndarray.flatten
1-D array copy of the elements of an array in row-major order.

## Notes

In row-major order, the row index varies the slowest, and the column index the quickest. This can be generalized to multiple dimensions, where row-major order implies that the index along the first axis varies slowest, and the index along the last quickest. The opposite holds for Fortran-, or column-major, mode.

## Examples

It is equivalent to reshape ( -1 , order=order).

```
>>> x = np.array([[1, 2, 3], [4, 5, 6]])
>>> print np.ravel(x)
[1 2 3 3 4 5 6]
>>> print x.reshape(-1)
[14 2 3 4 5 6]
```

```
>>> print np.ravel(x, order='F')
[1 4 2 5 3 6]
```

When order is ' A ', it will preserve the array's ' $C$ ' or ' $F$ ' ordering:

```
>>> print np.ravel(x.T)
[11 4 2 5 3 3 6]
>>> print np.ravel(x.T, order='A')
[1 2 3 4 5 6]
```

When order is ' $K$ ', it will preserve orderings that are neither ' C ' nor ' F ', but won't reverse axes:

```
>>> a = np.arange(3)[::-1]; a
array([2, 1, 0])
>>> a.ravel(order='C')
array([2, 1, 0])
>>> a.ravel(order=' K')
array([2, 1, 0])
>>> a = np.arange(12).reshape(2,3,2).swapaxes(1,2); a
array([[[ 0, 2, 4],
            [ 1, 3, 5]],
            [[ 6, 8, 10],
            [ 7, 9, 11]]])
>>> a.ravel(order='C')
array([ 0, 2, 4, 1, 3, 5, 6, 8, 10, 7, 9, 11])
>>> a.ravel(order=' K')
array([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11])
```

numpy.repeat (a, repeats, axis=None)
Repeat elements of an array.

## Parameters

a : array_like
Input array.
repeats : \{int, array of ints \}
The number of repetitions for each element. repeats is broadcasted to fit the shape of the given axis.
axis : int, optional
The axis along which to repeat values. By default, use the flattened input array, and return a flat output array.

## Returns

```
        repeated_array : ndarray
```

Output array which has the same shape as $a$, except along the given axis.

## See Also:

tile
Tile an array.

## Examples

```
>>> x = np.array([[1,2],[3,4]])
>>> np.repeat(x, 2)
```

```
array([1, 1, 2, 2, 3, 3, 4, 4])
>>> np.repeat (x, 3, axis=1)
array([[1, 1, 1, 2, 2, 2],
            [3, 3, 3, 4, 4, 4]])
>>> np.repeat(x, [1, 2], axis=0)
array([[1, 2],
    [3, 4],
    [3, 4]])
```

numpy. reshape ( $a$, newshape, order=' $C$ ')

Gives a new shape to an array without changing its data.

## Parameters

a : array_like
Array to be reshaped.
newshape : int or tuple of ints
The new shape should be compatible with the original shape. If an integer, then the result will be a 1-D array of that length. One shape dimension can be -1 . In this case, the value is inferred from the length of the array and remaining dimensions.
order : \{ 'C', 'F', 'A'\}, optional
Determines whether the array data should be viewed as in C (row-major) order, FORTRAN (column-major) order, or the C/FORTRAN order should be preserved.

## Returns

reshaped_array : ndarray
This will be a new view object if possible; otherwise, it will be a copy.

## See Also:

ndarray. reshape
Equivalent method.

## Notes

It is not always possible to change the shape of an array without copying the data. If you want an error to be raise if the data is copied, you should assign the new shape to the shape attribute of the array:

```
>>> a = np.zeros((10, 2))
# A transpose make the array non-contiguous
>>> b = a.T
# Taking a view makes it possible to modify the shape without modiying the
# initial object.
>>> c = b.view()
>>> c.shape = (20)
AttributeError: incompatible shape for a non-contiguous array
```


## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> np.reshape(a, 6)
array([1, 2, 3, 4, 5, 6])
>>> np.reshape(a, 6, order=' F')
array([1, 4, 2, 5, 3, 6])
```

```
>>> np.reshape(a, (3,-1)) # the unspecified value is inferred to be 2
array([[1, 2],
    [3, 4],
    [5, 6]])
```

numpy. resize ( $a$, new_shape)
Return a new array with the specified shape.
If the new array is larger than the original array, then the new array is filled with repeated copies of $a$. Note that this behavior is different from a.resize(new_shape) which fills with zeros instead of repeated copies of $a$.

## Parameters

a : array_like
Array to be resized.
new_shape : int or tuple of int
Shape of resized array.

## Returns

reshaped_array : ndarray
The new array is formed from the data in the old array, repeated if necessary to fill out the required number of elements. The data are repeated in the order that they are stored in memory.

## See Also:

ndarray.resize
resize an array in-place.
Examples

```
>>> a=np.array([[0,1],[2,3]])
>>> np.resize(a,(1,4))
array([[0, 1, 2, 3]])
>>> np.resize(a, (2,4))
array([[0, 1, 2, 3],
            [0, 1, 2, 3]])
```

numpy. searchsorted ( $a, v$, side $=$ 'left')
Find indices where elements should be inserted to maintain order.
Find the indices into a sorted array $a$ such that, if the corresponding elements in $v$ were inserted before the indices, the order of $a$ would be preserved.

## Parameters

a : 1-D array_like
Input array, sorted in ascending order.
$\mathbf{v}$ : array_like
Values to insert into $a$.
side : \{'left', 'right' \}, optional
If 'left', the index of the first suitable location found is given. If 'right', return the last such index. If there is no suitable index, return either 0 or N (where N is the length of $a)$.

## Returns

indices : array of ints
Array of insertion points with the same shape as $v$.

## See Also:

sort
Return a sorted copy of an array.
histogram
Produce histogram from 1-D data.

## Notes

Binary search is used to find the required insertion points.
As of Numpy 1.4.0 searchsorted works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

```
>>> np.searchsorted([1,2,3,4,5], 3)
2
>>> np.searchsorted([1,2,3,4,5], 3, side='right')
3
>>> np.searchsorted([1,2,3,4,5], [-10, 10, 2, 3])
array([0, 5, 1, 2])
```

numpy.sort ( $a$, axis=-1, kind='quicksort', order $=$ None )

Return a sorted copy of an array.

## Parameters

a: array_like
Array to be sorted.
axis : int or None, optional
Axis along which to sort. If None, the array is flattened before sorting. The default is -1 , which sorts along the last axis.
kind : \{'quicksort', 'mergesort', 'heapsort'\}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is a structured array, this argument specifies which fields to compare first, second, and so on. This list does not need to include all of the fields.

## Returns

sorted_array : ndarray
Array of the same type and shape as $a$.

## See Also:

ndarray.sort
Method to sort an array in-place.
argsort
Indirect sort.

## lexsort

Indirect stable sort on multiple keys.

```
searchsorted
```

Find elements in a sorted array.

## Notes

The various sorting algorithms are characterized by their average speed, worst case performance, work space size, and whether they are stable. A stable sort keeps items with the same key in the same relative order. The three available algorithms have the following properties:

| kind | speed | worst case | work space | stable |
| :--- | :--- | :--- | :--- | :--- |
| 'quicksort' | 1 | $\mathrm{O}\left(\mathrm{n}^{\wedge} 2\right)$ | 0 | no |
| 'mergesort' | 2 | $\mathrm{O}\left(\mathrm{n}^{*} \log (\mathrm{n})\right)$ | $\sim \mathrm{n} / 2$ | yes |
| 'heapsort' | 3 | $\mathrm{O}(\mathrm{n} * \log (\mathrm{n}))$ | 0 | no |

All the sort algorithms make temporary copies of the data when sorting along any but the last axis. Consequently, sorting along the last axis is faster and uses less space than sorting along any other axis.
The sort order for complex numbers is lexicographic. If both the real and imaginary parts are non-nan then the order is determined by the real parts except when they are equal, in which case the order is determined by the imaginary parts.

Previous to numpy 1.4.0 sorting real and complex arrays containing nan values led to undefined behaviour. In numpy versions $>=1.4 .0$ nan values are sorted to the end. The extended sort order is:

- Real: [R, nan]
-Complex: [ $\mathrm{R}+\mathrm{Rj}, \mathrm{R}+$ nanj, nan +Rj , nan + nanj $]$
where R is a non-nan real value. Complex values with the same nan placements are sorted according to the non-nan part if it exists. Non-nan values are sorted as before.


## Examples

```
>>> a = np.array([[1,4],[3,1]])
>>> np.sort(a) # sort along the last axis
array([[1, 4],
    [1, 3]])
>>> np.sort(a, axis=None) # sort the flattened array
array([1, 1, 3, 4])
>>> np.sort(a, axis=0) # sort along the first axis
array([[1, 1],
    [3, 4]])
```

Use the order keyword to specify a field to use when sorting a structured array:

```
>>> dtype = [('name', 'S10'), ('height', float), ('age', int)]
>>> values = [('Arthur', 1.8, 41), ('Lancelot', 1.9, 38),
... ('Galahad', 1.7, 38)]
>>> a = np.array(values, dtype=dtype) # create a structured array
>>> np.sort(a, order='height')
array([('Galahad', 1.7, 38), ('Arthur', 1.8, 41),
    ('Lancelot', 1.8999999999999999, 38)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

Sort by age, then height if ages are equal:

```
>>> np.sort(a, order=['age', 'height'])
array([('Galahad', 1.7, 38), ('Lancelot', 1.8999999999999999, 38),
```

    ('Arthur', 1.8, 41)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
numpy.squeeze ( $a$ )
Remove single-dimensional entries from the shape of an array.

## Parameters

a : array_like
Input data.

## Returns

squeezed: ndarray
The input array, but with with all dimensions of length 1 removed. Whenever possible, a view on $a$ is returned.

## Examples

```
>>> x = np.array([[[0], [1], [2]]])
>>> x.shape
(1, 3, 1)
>>> np.squeeze(x).shape
(3,)
```

numpy.std ( $a$, axis=None, dtype $=$ None, out=None, $d d o f=0$ )

Compute the standard deviation along the specified axis.
Returns the standard deviation, a measure of the spread of a distribution, of the array elements. The standard deviation is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Calculate the standard deviation of these values.
axis : int, optional
Axis along which the standard deviation is computed. The default is to compute the standard deviation of the flattened array.
dtype : dtype, optional
Type to use in computing the standard deviation. For arrays of integer type the default is float64, for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type (of the calculated values) will be cast if necessary.
ddof : int, optional
Means Delta Degrees of Freedom. The divisor used in calculations is N - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

standard_deviation : ndarray, see dtype parameter above.
If out is None, return a new array containing the standard deviation, otherwise return a reference to the output array.

## See Also:

```
var, mean
```


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Section "Output arguments"

## Notes

The standard deviation is the square root of the average of the squared deviations from the mean, i.e., std $=\operatorname{sqrt}(m e a n(a b s(x-x . m e a n()) * * 2))$.

The average squared deviation is normally calculated as $x \cdot \operatorname{sum}() / N$, where $N=\operatorname{len}(x)$. If, however, $d d o f$ is specified, the divisor $N$ - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of the infinite population. ddof $=0$ provides a maximum likelihood estimate of the variance for normally distributed variables. The standard deviation computed in this function is the square root of the estimated variance, so even with ddof $=1$, it will not be an unbiased estimate of the standard deviation per se.

Note that, for complex numbers, std takes the absolute value before squaring, so that the result is always real and nonnegative.

For floating-point input, the $s t d$ is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.std(a)
1.1180339887498949
>>> np.std(a, axis=0)
array([ 1., 1.])
>>> np.std(a, axis=1)
array([ 0.5, 0.5])
```

In single precision, $\operatorname{std}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.std(a)
0.45172946707416706
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.std(a, dtype=np.float64)
0.44999999925552653
```

numpy.sum ( $a$, axis=None, dtype=None, out=None)
Sum of array elements over a given axis.

## Parameters

a : array_like
Elements to sum.
axis : integer, optional
Axis over which the sum is taken. By default axis is None, and all elements are summed.
dtype : dtype, optional

The type of the returned array and of the accumulator in which the elements are summed. By default, the dtype of $a$ is used. An exception is when $a$ has an integer type with less precision than the default platform integer. In that case, the default platform integer is used instead.
out : ndarray, optional
Array into which the output is placed. By default, a new array is created. If out is given, it must be of the appropriate shape (the shape of $a$ with axis removed, i.e., numpy.delete (a.shape, axis)). Its type is preserved. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

sum_along_axis : ndarray
An array with the same shape as $a$, with the specified axis removed. If $a$ is a $0-\mathrm{d}$ array, or if axis is None, a scalar is returned. If an output array is specified, a reference to out is returned.

## See Also:

ndarray.sum
Equivalent method.
cumsum
Cumulative sum of array elements.
trapz
Integration of array values using the composite trapezoidal rule.
mean, average

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> np.sum([0.5, 1.5])
2.0
>>> np.sum([0.5, 0.7, 0.2, 1.5], dtype=np.int32)
1
>>> np.sum([[0, 1], [0, 5]])
6
>>> np.sum([[0, 1], [0, 5]], axis=0)
array([0, 6])
>>> np.sum([[0, 1], [0, 5]], axis=1)
array([1, 5])
```

If the accumulator is too small, overflow occurs:

```
>>> np.ones(128, dtype=np.int8).sum(dtype=np.int8)
-128
```

numpy.swapaxes (a, axis1, axis2)
Interchange two axes of an array.

## Parameters

a : array_like
Input array.
axis1 : int
First axis.
axis2 : int
Second axis.

## Returns

a_swapped : ndarray
If $a$ is an ndarray, then a view of $a$ is returned; otherwise a new array is created.

## Examples

```
>>> x = np.array([[1,2,3]])
>>> np.swapaxes(x,0,1)
array([[1],
            [2],
            [3]])
>>> x = np.array([[[0,1],[2,3]],[[4,5],[6,7]]])
>>> x
array([[[0, 1],
    [2, 3]],
    [[4, 5],
    [6, 7]]])
>>> np.swapaxes(x,0,2)
array([[[0, 4],
            [2, 6]],
            [[1, 5],
            [3, 7]]])
```

numpy.take ( $a$, indices, axis=None, out=None, mode='raise')

Take elements from an array along an axis.
This function does the same thing as "fancy" indexing (indexing arrays using arrays); however, it can be easier to use if you need elements along a given axis.

## Parameters

a : array_like
The source array.
indices : array_like
The indices of the values to extract.
axis : int, optional
The axis over which to select values. By default, the flattened input array is used.
out : ndarray, optional
If provided, the result will be placed in this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## Returns

subarray : ndarray
The returned array has the same type as $a$.

## See Also:

ndarray.take
equivalent method

## Examples

```
>>> a = [4, 3, 5, 7, 6, 8]
>>> indices = [0, 1, 4]
>>> np.take(a, indices)
array([4, 3, 6])
```

In this example if $a$ is an ndarray, "fancy" indexing can be used.

```
>>> a = np.array(a)
>>> a[indices]
array([4, 3, 6])
```

numpy.trace $(a$, offset $=0$, axis $1=0$, axis $2=1$, dtype $=$ None, out $=$ None $)$
Return the sum along diagonals of the array.
If $a$ is $2-D$, the sum along its diagonal with the given offset is returned, i.e., the sum of elements a [i,i+offset] for all i.

If $a$ has more than two dimensions, then the axes specified by axis1 and axis 2 are used to determine the 2-D sub-arrays whose traces are returned. The shape of the resulting array is the same as that of $a$ with axis1 and axis2 removed.

## Parameters

a : array_like
Input array, from which the diagonals are taken.
offset : int, optional
Offset of the diagonal from the main diagonal. Can be both positive and negative. Defaults to 0 .
axis1, axis2 : int, optional
Axes to be used as the first and second axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults are the first two axes of $a$.
dtype : dtype, optional
Determines the data-type of the returned array and of the accumulator where the elements are summed. If dtype has the value None and $a$ is of integer type of precision less than the default integer precision, then the default integer precision is used. Otherwise, the precision is the same as that of $a$.
out : ndarray, optional

Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

 sum_along_diagonals : ndarrayIf $a$ is 2-D, the sum along the diagonal is returned. If $a$ has larger dimensions, then an array of sums along diagonals is returned.

## See Also:

diag, diagonal, diagflat

## Examples

```
    >>> np.trace(np.eye(3))
    3.0
>>> a = np.arange(8).reshape((2,2,2))
>>> np.trace(a)
array([6, 8])
>>> a = np.arange(24).reshape((2,2,2,3))
>>> np.trace(a).shape
(2, 3)
numpy.transpose (a, axes=None)
```

Permute the dimensions of an array.

## Parameters

a : array_like
Input array.
axes : list of ints, optional
By default, reverse the dimensions, otherwise permute the axes according to the values given.

## Returns

p: ndarray
$a$ with its axes permuted. A view is returned whenever possible.

## See Also:

rollaxis

## Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
    [2, 3]])
>>> np.transpose(x)
array([[0, 2],
    [1, 3]])
>>> x = np.ones((1, 2, 3))
>>> np.transpose(x, (1, 0, 2)).shape
(2, 1, 3)
```

numpy .var ( $a$, axis=None, dtype=None, out=None, ddof=0)
Compute the variance along the specified axis.
Returns the variance of the array elements, a measure of the spread of a distribution. The variance is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Array containing numbers whose variance is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the variance is computed. The default is to compute the variance of the flattened array.
dtype : data-type, optional
Type to use in computing the variance. For arrays of integer type the default is float32; for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output, but the type is cast if necessary.
ddof : int, optional
"Delta Degrees of Freedom": the divisor used in the calculation is N - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

variance : ndarray, see dtype parameter above
If out=None, returns a new array containing the variance; otherwise, a reference to the output array is returned.

## See Also:

std
Standard deviation
mean
Average
numpy.doc.ufuncs
Section "Output arguments"

## Notes

The variance is the average of the squared deviations from the mean, i.e., var $=$ mean (abs ( $\mathrm{x}-$ $x$.mean()) **2).

The mean is normally calculated as $\mathrm{x} . \operatorname{sum}() / \mathrm{N}$, where $\mathrm{N}=\operatorname{len}(\mathrm{x})$. If, however, $d d o f$ is specified, the divisor N - ddof is used instead. In standard statistical practice, ddof $=1$ provides an unbiased estimator of the variance of a hypothetical infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables.
Note that for complex numbers, the absolute value is taken before squaring, so that the result is always real and nonnegative.

For floating-point input, the variance is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1,2],[3,4]])
>>> np.var(a)
1.25
>>> np.var(a,0)
array([ 1., 1.])
>>> np.var(a,1)
array([ 0.25, 0.25])
```

In single precision, $\operatorname{var}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.var(a)
0.20405951142311096
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.var(a, dtype=np.float64)
0.202499999932997387
>>> ((1-0.55)**2 + (0.1-0.55)**2)/2
0.202500000000000001
```

generic.__array__()
sc.__array__(Itype) return 0-dim array
generic.__array_wrap__()
sc.__array_wrap__(obj) return scalar from array
generic.squeeze()
Not implemented (virtual attribute)

Class generic exists solely to derive numpy scalars from, and possesses, albeit unimplemented, all the attributes of the ndarray class so as to provide a uniform API.

## See Also:

The

```
generic.byteswap()
```

Not implemented (virtual attribute)
Class generic exists solely to derive numpy scalars from, and possesses, albeit unimplemented, all the attributes of the ndarray class so as to provide a uniform API.

See Also:
The
generic.__reduce__()
generic.__setstate__()
generic.setflags()

Not implemented (virtual attribute)

Class generic exists solely to derive numpy scalars from, and possesses, albeit unimplemented, all the attributes of the ndarray class so as to provide a uniform API.

## See Also:

The

### 1.2.5 Defining new types

There are two ways to effectively define a new array scalar type (apart from composing record dtypes from the built-in scalar types): One way is to simply subclass the ndarray and overwrite the methods of interest. This will work to a degree, but internally certain behaviors are fixed by the data type of the array. To fully customize the data type of an array you need to define a new data-type, and register it with NumPy. Such new types can only be defined in C, using the Numpy C-API.

### 1.3 Data type objects (dtype)

A data type object (an instance of numpy. dtype class) describes how the bytes in the fixed-size block of memory corresponding to an array item should be interpreted. It describes the following aspects of the data:

1. Type of the data (integer, float, Python object, etc.)
2. Size of the data (how many bytes is in e.g. the integer)
3. Byte order of the data (little-endian or big-endian)
4. If the data type is a record, an aggregate of other data types, (e.g., describing an array item consisting of an integer and a float),
(a) what are the names of the "fields" of the record, by which they can be accessed,
(b) what is the data-type of each field, and
(c) which part of the memory block each field takes.
5. If the data is a sub-array, what is its shape and data type.

To describe the type of scalar data, there are several built-in scalar types in Numpy for various precision of integers, floating-point numbers, etc. An item extracted from an array, e.g., by indexing, will be a Python object whose type is the scalar type associated with the data type of the array.
Note that the scalar types are not dtype objects, even though they can be used in place of one whenever a data type specification is needed in Numpy. Record data types are formed by creating a data type whose fields contain other data types. Each field has a name by which it can be accessed. The parent data type should be of sufficient size to contain all its fields; the parent can for example be based on the void type which allows an arbitrary item size. Record data types may also contain other record types and fixed-size sub-array data types in their fields. Finally, a data type can describe items that are themselves arrays of items of another data type. These sub-arrays must, however, be of a fixed size. If an array is created using a data-type describing a sub-array, the dimensions of the sub-array are appended to the shape of the array when the array is created. Sub-arrays in a field of a record behave differently, see Record Access.

## Example

A simple data type containing a 32-bit big-endian integer: (see Specifying and constructing data types for details on construction)

```
>>> dt = np.dtype('>i4')
>>> dt.byteorder
'>'
>>> dt.itemsize
4
>>> dt.name
'int32'
>>> dt.type is np.int32
True
```

The corresponding array scalar type is int 32 .

## Example

A record data type containing a 16-character string (in field 'name') and a sub-array of two 64-bit floating-point number (in field 'grades'):

```
>>> dt = np.dtype([('name', np.str_, 16), ('grades', np.float64, (2,))])
>>> dt['name']
dtype('|S16')
>>> dt['grades']
dtype(('float64',(2,)))
```

Items of an array of this data type are wrapped in an array scalar type that also has two fields:

```
>>> x = np.array([('Sarah', (8.0, 7.0)), ('John', (6.0, 7.0))], dtype=dt)
>>> x[1]
('John', [6.0, 7.0])
>>> x[1]['grades']
array([ 6., 7.])
>>> type(x[1])
<type 'numpy.void'>
>>> type(x[1]['grades'])
<type 'numpy.ndarray'>
```


### 1.3.1 Specifying and constructing data types

Whenever a data-type is required in a NumPy function or method, either a dtype object or something that can be converted to one can be supplied. Such conversions are done by the dtype constructor:
dtype Create a data type object.
class numpy.dtype
Create a data type object.
A numpy array is homogeneous, and contains elements described by a dtype object. A dtype object can be constructed from different combinations of fundamental numeric types.

## Parameters

obj :
Object to be converted to a data type object.
align : bool, optional
Add padding to the fields to match what a C compiler would output for a similar C struct. Can be True only if obj is a dictionary or a comma-separated string.
copy : bool, optional

Make a new copy of the data-type object. If False, the result may just be a reference to a built-in data-type object.

## Examples

Using array-scalar type:

```
>>> np.dtype(np.int16)
dtype('int16')
```

Record, one field name 'f1', containing int16:

```
>>> np.dtype([('f1', np.int16)])
dtype([('f1', '<i2')])
```

Record, one field named ' f 1 ', in itself containing a record with one field:

```
>>> np.dtype([('f1', [('f1', np.int16)])])
dtype([('f1', [('f1', '<i2')])])
```

Record, two fields: the first field contains an unsigned int, the second an int32:

```
>>> np.dtype([('f1', np.uint), ('f2', np.int32)])
dtype([('f1', '<u4'), ('f2', '<i4')])
```

Using array-protocol type strings:

```
>>> np.dtype([('a','f8'),('b','S10')])
dtype([('a', '<f8'), ('b', '|S10')])
```

Using comma-separated field formats. The shape is $(2,3)$ :

```
>>> np.dtype("i4, (2,3) f8")
dtype([('f0', '<i4'), ('f1', '<f8', (2, 3))])
```

Using tuples. int is a fixed type, 3 the field's shape. void is a flexible type, here of size 10 :

```
>>> np.dtype([('hello',(np.int,3)),('world',np.void,10)])
dtype([('hello', '<i4', 3), ('world', '|V10')])
```

Subdivide int 16 into 2 int 8 's, called $x$ and $y .0$ and 1 are the offsets in bytes:

```
>>> np.dtype((np.int16, {' x':(np.int8,0), ' Y':(np.int8,1)}))
dtype(('<i2', [('x', '|i1'), ('Y', '|i1')]))
```

Using dictionaries. Two fields named 'gender' and 'age':

```
>>> np.dtype({'names':['gender','age'], 'formats':['S1',np.uint8]})
dtype([('gender', '|S1'), ('age', '|ul')])
```

Offsets in bytes, here 0 and 25:

```
>>> np.dtype({'surname':('S25',0),'age':(np.uint8, 25)})
dtype([('surname', '|S25'), ('age', '|u1')])
```


## Methods

newbyteorder

What can be converted to a data-type object is described below:
dtype object

Used as-is.
None
The default data type: float_.
Array-scalar types
The 24 built-in array scalar type objects all convert to an associated data-type object. This is true for their sub-classes as well.

Note that not all data-type information can be supplied with a type-object: for example, flexible data-types have a default itemsize of 0 , and require an explicitly given size to be useful.

## Example

```
>>> dt = np.dtype(np.int32) # 32-bit integer
>>> dt = np.dtype(np.complex128) # l28-bit complex floating-point number
```

Generic types
The generic hierarchical type objects convert to corresponding type objects according to the associations:

| number, inexact, floating | float |
| :--- | :--- |
| complexfloating | cfloat |
| integer, signedinteger | int_ |
| unsignedinteger | uint |
| character | string |
| generic, flexible | void |

## Built-in Python types

Several python types are equivalent to a corresponding array scalar when used to generate a dtype object:

| int | int__ $^{\text {bool }}$ |
| :--- | :--- |
| bool | bool_- $^{\text {float }}$ |
| float_ |  |
| complex | cfloat |
| str | string |
| unicode | unicode_ |
| buffer | void |
| (all others) | object_- |

## Example

```
>>> dt = np.dtype(float) # Python-compatible floating-point number
>>> dt = np.dtype(int) # Python-compatible integer
>>> dt = np.dtype(object) # Python object
```

Types with . dtype
Any type object with a dtype attribute: The attribute will be accessed and used directly. The attribute must return something that is convertible into a dtype object.

Several kinds of strings can be converted. Recognized strings can be prepended with '>' (big-endian), ' <' (littleendian), or ${ }^{\prime}=$ ' (hardware-native, the default), to specify the byte order.

One-character strings
Each built-in data-type has a character code (the updated Numeric typecodes), that uniquely identifies it.

## Example

```
>>> dt = np.dtype('b') # byte, native byte order
>>> dt = np.dtype('>H') # big-endian unsigned short
>>> dt = np.dtype('<f') # little-endian single-precision float
>>> dt = np.dtype('d') # double-precision floating-point number
```

Array-protocol type strings (see The Array Interface)
The first character specifies the kind of data and the remaining characters specify how many bytes of data. The supported kinds are

| ' ${ }^{\prime}$ ' | Boolean |
| :---: | :---: |
| 'i' | (signed) integer |
| 'u' | unsigned integer |
| 'f' | floating-point |
| ' C' | complex-floating point |
| 'S', 'a' | string |
| 'U' | unicode |
| 'V' | anything (void) |

## Example

```
>>> dt = np.dtype('i4') # 32-bit signed integer
>>> dt = np.dtype('f8') # 64-bit floating-point number
>>> dt = np.dtype('c16') # 128-bit complex floating-point number
>>> dt = np.dtype('a25') # 25-character string
```

String with comma-separated fields
Numarray introduced a short-hand notation for specifying the format of a record as a comma-separated string of basic formats.

A basic format in this context is an optional shape specifier followed by an array-protocol type string. Parenthesis are required on the shape if it is greater than 1-d. NumPy allows a modification on the format in that any string that can uniquely identify the type can be used to specify the data-type in a field. The generated data-type fields are named $\left.{ }^{\prime} £ 0^{\prime},{ }^{\prime} £ 1^{\prime}, \ldots, ' £<\mathrm{N}-1\right\rangle^{\prime}$ where $\mathrm{N}(>1)$ is the number of commaseparated basic formats in the string. If the optional shape specifier is provided, then the data-type for the corresponding field describes a sub-array.

## Example

- field named $f 0$ containing a 32-bit integer
- field named $f 1$ containing a $2 \times 3$ sub-array of 64-bit floating-point numbers
- field named $f 2$ containing a 32-bit floating-point number

```
>>> dt = np.dtype("i4, (2,3) f8, f4")
```

- field named $f 0$ containing a 3-character string
- field named $f 1$ containing a sub-array of shape ( 3 ,) containing 64-bit unsigned integers
- field named $£ 2$ containing a $3 \times 4$ sub-array containing 10-character strings

```
>>> dt = np.dtype("a3, 3u8, (3,4)a10")
```

Type strings
Any string in numpy. sctypeDict.keys():

## Example

$\ggg d t=n p \cdot d t y p e\left({ }^{\prime} u i n t 32^{\prime}\right) \quad$ \# 32-bit unsigned integer
$\ggg d t=n p . d t y p e(' F l o a t 64 ')$ \# 64-bit floating-point number
(flexible_dtype, itemsize)
The first argument must be an object that is converted to a flexible data-type object (one whose element size is 0 ), the second argument is an integer providing the desired itemsize.

## Example

```
>>> dt = np.dtype((void, 10)) # 10-byte wide data block
>>> dt = np.dtype((str, 35)) # 35-character string
>>> dt = np.dtype(('U', 10)) # 10-character unicode string
(fixed_dtype, shape)
```

The first argument is any object that can be converted into a fixed-size data-type object. The second argument is the desired shape of this type. If the shape parameter is 1 , then the data-type object is equivalent to fixed dtype. If shape is a tuple, then the new dtype defines a sub-array of the given shape.

## Example

```
>>> dt = np.dtype((np.int32, (2,2))) # 2 x 2 integer sub-array
>>> dt = np.dtype(('S10', 1)) # 10-character string
>>> dt = np.dtype(('i4, (2,3)f8, f4', (2,3))) # 2 x 3 record sub-array
(base_dtype, new_dtype)
```

Both arguments must be convertible to data-type objects in this case. The base_dtype is the data-type object that the new data-type builds on. This is how you could assign named fields to any built-in datatype object.

## Example

32-bit integer, whose first two bytes are interpreted as an integer via field real, and the following two bytes via field imag.

```
>>> dt = np.dtype((np.int32,{'real':(np.int16, 0),'imag':(np.int16, 2)})
```

32-bit integer, which is interpreted as consisting of a sub-array of shape ( 4, ) containing 8-bit integers:

```
>>> dt = np.dtype((np.int32, (np.int8, 4)))
```

32-bit integer, containing fields $r, g, b$, a that interpret the 4 bytes in the integer as four unsigned integers:

```
>>> dt = np.dtype(('i4', [('r','u1'),('g','u1'),('b','ul'),('a','u1')]))
```

[(field_name, field_dtype, field_shape), ...]
obj should be a list of fields where each field is described by a tuple of length 2 or 3 . (Equivalent to the descr item in the $\qquad$ array_interface_ $\qquad$ attribute.)

The first element, field_name, is the field name (if this is " then a standard field name, ' $£ \#^{\prime}$, is assigned). The field name may also be a 2-tuple of strings where the first string is either a "title" (which may be any string or unicode string) or meta-data for the field which can be any object, and the second string is the "name" which must be a valid Python identifier.

The second element, field_dtype, can be anything that can be interpreted as a data-type.
The optional third element field_shape contains the shape if this field represents an array of the data-type in the second element. Note that a 3 -tuple with a third argument equal to 1 is equivalent to a 2 -tuple.

This style does not accept align in the dtype constructor as it is assumed that all of the memory is accounted for by the array interface description.

## Example

Data-type with fields big (big-endian 32-bit integer) and little (little-endian 32-bit integer):

```
>>> dt = np.dtype([('big', '>i4'), ('little', '<i4')])
```

Data-type with fields R, G, B, A, each being an unsigned 8-bit integer:

```
    >>> dt = np.dtype([('R','u1'), ('G','u1'), ('B','u1'), ('A','u1')])
{'names': ..., 'formats': ..., 'offsets': ..., 'titles': ...}
```

This style has two required and two optional keys. The names and formats keys are required. Their respective values are equal-length lists with the field names and the field formats. The field names must be strings and the field formats can be any object accepted by dtype constructor.

The optional keys in the dictionary are offsets and titles and their values must each be lists of the same length as the names and formats lists. The offsets value is a list of byte offsets (integers) for each field, while the titles value is a list of titles for each field (None can be used if no title is desired for that field). The titles can be any string or unicode object and will add another entry to the fields dictionary keyed by the title and referencing the same field tuple which will contain the title as an additional tuple member.

## Example

Data type with fields $r, g, b, a$, each being a 8 -bit unsigned integer:

```
>>> dt = np.dtype({'names': ['r','g','b','a'],
... 'formats': [uint8, uint8, uint8, uint8]})
```

Data type with fields $r$ and $b$ (with the given titles), both being 8-bit unsigned integers, the first at byte position 0 from the start of the field and the second at position 2 :

```
>>> dt = np.dtype({'names': ['r','b'], 'formats': ['u1', 'u1'],
... 'offsets': [0, 2],
... 'titles': ['Red pixel', 'Blue pixel']})
{'field1': ..., 'field2': ..., ...}
```

This style allows passing in the fields attribute of a data-type object.
obj should contain string or unicode keys that refer to (data-type, offset) or (data-type, offset, title) tuples.

## Example

Data type containing field coll (10-character string at byte position 0 ), col2 (32-bit float at byte position 10), and col 3 (integers at byte position 14):

```
>>> dt = np.dtype({'col1': ('S10', 0), 'col2': (float32, 10),
    'col3': (int, 14)})
```


### 1.3.2 dtype

Numpy data type descriptions are instances of the dtype class.

## Attributes

The type of the data is described by the following dtype attributes:

| dtype.type | The type object used to instantiate a scalar of this data-type. |
| :--- | :--- |
| dtype.kind | A character code (one of 'biufcSUV') identifying the general kind of data. |
| dtype.char | A unique character code for each of the 21 different built-in types. |
| dtype. num | A unique number for each of the 21 different built-in types. |
| dtype.str | The array-protocol typestring of this data-type object. |

## dtype.type

The type object used to instantiate a scalar of this data-type.

```
dtype.kind
```

A character code (one of 'biufcSUV') identifying the general kind of data.

```
dtype.char
```

A unique character code for each of the 21 different built-in types.

```
dtype.num
```

A unique number for each of the 21 different built-in types.
These are roughly ordered from least-to-most precision.

```
dtype.str
```

The array-protocol typestring of this data-type object.
Size of the data is in turn described by:
dtype. name A bit-width name for this data-type.
dtype.itemsize The element size of this data-type object.
dtype. name
A bit-width name for this data-type.
Un-sized flexible data-type objects do not have this attribute.

## dtype.itemsize

The element size of this data-type object.
For 18 of the 21 types this number is fixed by the data-type. For the flexible data-types, this number can be anything.
Endianness of this data:
dtype.byteorder A character indicating the byte-order of this data-type object.
dtype.byteorder
A character indicating the byte-order of this data-type object.
One of:

| $'='$ | native |
| :--- | :--- |
| $'<'$ | little-endian |
| $'>$ | big-endian |
| ' $l '$ | not applicable |

All built-in data-type objects have byteorder either ' $=$ ' or 'l'.

## Examples

```
>>> dt = np.dtype('i2')
>>> dt.byteorder
\prime=
```

```
>>> # endian is not relevant for 8 bit numbers
>>> np.dtype('il').byteorder
'|'
>>> # or ASCII strings
>>> np.dtype('S2').byteorder
'|'
>>> # Even if specific code is given, and it is native
>>> # '=' is the byteorder
>>> import sys
>>> sys_is_le = sys.byteorder == 'little'
>>> native_code = sys_is_le and '<' or '>'
>>> swapped_code = sys_is_le and '>' or '<'
>>> dt = np.dtype(native_code + 'i2')
>>> dt.byteorder
\prime='
>>> # Swapped code shows up as itself
>>> dt = np.dtype(swapped_code + 'i2')
>>> dt.byteorder == swapped_code
True
```

Information about sub-data-types in a record:

> | dtype.fields | Dictionary of named fields defined for this data type, or None. |
| :--- | :--- |
| dtype. names | Ordered list of field names, or None if there are no fields. |

## dtype.fields

Dictionary of named fields defined for this data type, or None.
The dictionary is indexed by keys that are the names of the fields. Each entry in the dictionary is a tuple fully describing the field:

```
(dtype, offset[, title])
```

If present, the optional title can be any object (if it is a string or unicode then it will also be a key in the fields dictionary, otherwise it's meta-data). Notice also that the first two elements of the tuple can be passed directly as arguments to the ndarray.getfield and ndarray.setfield methods.

## See Also:

```
ndarray.getfield, ndarray.setfield
```


## Examples

```
>>> dt = np.dtype([('name', np.str_, 16), ('grades', np.float64, (2,))])
>>> print dt.fields
{'grades': (dtype(('float64',(2,))), 16), 'name': (dtype('|S16'), 0)}
```

dtype.names

Ordered list of field names, or None if there are no fields.
The names are ordered according to increasing byte offset. This can be used, for example, to walk through all of the named fields in offset order.

## Examples

```
>>> dt = np.dtype([('name', np.str_, 16), ('grades', np.float64, (2,))])
>>> dt.names
('name', 'grades')
```

For data types that describe sub-arrays:
dtype.subdtype Tuple (item_dtype, shape) if this dtype describes a sub-array, and
dtype.shape $\quad$ Shape tuple of the sub-array if this data type describes a sub-array,
dtype.subdtype
Tuple (item_dtype, shape) if this dtype describes a sub-array, and None otherwise.
The shape is the fixed shape of the sub-array described by this data type, and item_dtype the data type of the array.

If a field whose dtype object has this attribute is retrieved, then the extra dimensions implied by shape are tacked on to the end of the retrieved array.

## dtype.shape

Shape tuple of the sub-array if this data type describes a sub-array, and () otherwise.
Attributes providing additional information:
dtype. hasobject Boolean indicating whether this dtype contains any reference-counted objects in any fields or sub-dtypes.
dtype.flags Bit-flags describing how this data type is to be interpreted.
dtype.isbuiltinInteger indicating how this dtype relates to the built-in dtypes.
dtype.isnative Boolean indicating whether the byte order of this dtype is native
dtype.descr Array-interface compliant full description of the data-type.
dtype.alignment The required alignment (bytes) of this data-type according to the compiler.
dtype.hasobject
Boolean indicating whether this dtype contains any reference-counted objects in any fields or sub-dtypes.
Recall that what is actually in the ndarray memory representing the Python object is the memory address of that object (a pointer). Special handling may be required, and this attribute is useful for distinguishing data types that may contain arbitrary Python objects and data-types that won't.

```
dtype.flags
```

Bit-flags describing how this data type is to be interpreted.
Bit-masks are in numpy.core.multiarray as the constants ITEM_HASOBJECT, LIST_PICKLE, ITEM_IS_POINTER, NEEDS_INIT, NEEDS_PYAPI, USE_GETITEM, USE_SETITEM. A full explanation of these flags is in C-API documentation; they are largely useful for user-defined data-types.

## dtype.isbuiltin

Integer indicating how this dtype relates to the built-in dtypes.
Read-only.

```
0 if this is a structured array type, with fields
1 if this is a dtype compiled into numpy (such as ints, floats etc)
2 if the dtype is for a user-defined numpy type A user-defined type uses the numpy C-API machinery to
extend numpy to handle a new array type. See user.user-defined-data-types in the Numpy manual.
```


## Examples

```
>>> dt = np.dtype('i2')
>>> dt.isbuiltin
1
>>> dt = np.dtype('f8')
>>> dt.isbuiltin
1
>>> dt = np.dtype([('fieldl', 'f8')])
>>> dt.isbuiltin
0
```


## dtype.isnative

Boolean indicating whether the byte order of this dtype is native to the platform.
dtype.descr
Array-interface compliant full description of the data-type.
The format is that required by the 'descr' key in the __array_interface __ attribute.

## dtype.alignment

The required alignment (bytes) of this data-type according to the compiler.
More information is available in the C-API section of the manual.

## Methods

Data types have the following method for changing the byte order:

$$
\text { dtype. newbyteorder([new_order]) } \quad \text { Return a new dtype with a different byte order. }
$$

dtype.newbyteorder (new_order='S')
Return a new dtype with a different byte order.
Changes are also made in all fields and sub-arrays of the data type.

## Parameters

new_order : string, optional
Byte order to force; a value from the byte order specifications below. The default value (' S ') results in swapping the current byte order. new_order codes can be any of:

```
* 'S' - swap dtype from current to opposite endian
* {'<', 'L'} - little endian
* {'>', 'B'} - big endian
* {'=', 'N'} - native order
* {'|', 'I'} - ignore (no change to byte order)
```

The code does a case-insensitive check on the first letter of new_order for these alternatives. For example, any of ' $>$ ' or ' B ' or ' b ' or 'brian' are valid to specify big-endian.

## Returns

new_dtype : dtype
New dtype object with the given change to the byte order.

## Notes

Changes are also made in all fields and sub-arrays of the data type.

## Examples

```
>>> import sys
>>> sys_is_le = sys.byteorder == 'little'
>>> native_code = sys_is_le and '<' or '>'
>>> swapped_code = sys_is_le and '>' or '<'
>>> native_dt = np.dtype(native_code+'i2')
>>> swapped_dt = np.dtype(swapped_code+'i2')
>>> native_dt.newbyteorder('S') == swapped_dt
True
>>> native_dt.newbyteorder() == swapped_dt
True
>>> native_dt == swapped_dt.newbyteorder('S')
```

```
True
>>> native_dt == swapped_dt.newbyteorder (' =' )
True
>>> native_dt == swapped_dt.newbyteorder('N')
True
>>> native_dt == native_dt.newbyteorder(' |')
True
>>> np.dtype('<i2') == native_dt.newbyteorder('<')
True
>>> np.dtype('<i2') == native_dt.newbyteorder('L')
True
>>> np.dtype('>i2') == native_dt.newbyteorder('>')
True
>>> np.dtype('>i2') == native_dt.newbyteorder('B')
True
```

The following methods implement the pickle protocol:

```
dtype.__reduce___
dtype.__setstate______
dtype.__reduce__()
dtype.__setstate___()
```


### 1.4 Indexing

ndarrays can be indexed using the standard Python $\mathrm{x}[\mathrm{obj}]$ syntax, where $x$ is the array and obj the selection. There are three kinds of indexing available: record access, basic slicing, advanced indexing. Which one occurs depends on obj.

Note: In Python, $x[(\exp 1, \exp 2, \ldots, \operatorname{expN})]$ is equivalent to $x[\exp 1, \exp 2, \ldots, \operatorname{expN}]$; the latter is just syntactic sugar for the former.

### 1.4.1 Basic Slicing

Basic slicing extends Python's basic concept of slicing to N dimensions. Basic slicing occurs when obj is a slice object (constructed by start: stop: step notation inside of brackets), an integer, or a tuple of slice objects and integers. Ellipsis and newaxis objects can be interspersed with these as well. In order to remain backward compatible with a common usage in Numeric, basic slicing is also initiated if the selection object is any sequence (such as a list) containing slice objects, the Ellipsis object, or the newaxis object, but no integer arrays or other embedded sequences. The simplest case of indexing with $N$ integers returns an array scalar representing the corresponding item. As in Python, all indices are zero-based: for the $i$-th index $n_{i}$, the valid range is $0 \leq n_{i}<d_{i}$ where $d_{i}$ is the $i$-th element of the shape of the array. Negative indices are interpreted as counting from the end of the array (i.e., if $i<0$, it means $n_{i}+i$ ).
All arrays generated by basic slicing are always views of the original array.
The standard rules of sequence slicing apply to basic slicing on a per-dimension basis (including using a step index). Some useful concepts to remember include:

- The basic slice syntax is $i: j: k$ where $i$ is the starting index, $j$ is the stopping index, and $k$ is the step $(k \neq 0)$. This selects the $m$ elements (in the corresponding dimension) with index values $i, i+k, \ldots, i+(m-1) k$ where
$m=q+(r \neq 0)$ and $q$ and $r$ are the quotient and remainder obtained by dividing $j-i$ by $k: j-i=q k+r$, so that $i+(m-1) k<j$.


## Example

```
>>> x = np.array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> x[1:7:2]
array([1, 3, 5])
```

- Negative $i$ and $j$ are interpreted as $n+i$ and $n+j$ where $n$ is the number of elements in the corresponding dimension. Negative $k$ makes stepping go towards smaller indices.


## Example

```
>>> x[-2:10]
array([8, 9])
>>> x[-3:3:-1]
array([7, 6, 5, 4])
```

- Assume $n$ is the number of elements in the dimension being sliced. Then, if $i$ is not given it defaults to 0 for $k>$ 0 and $n$ for $k<0$. If $j$ is not given it defaults to $n$ for $k>0$ and -1 for $k<0$. If $k$ is not given it defaults to 1 . Note that : : is the same as : and means select all indices along this axis.


## Example

```
>>> x[5:]
array([5, 6, 7, 8, 9])
```

- If the number of objects in the selection tuple is less than $N$, then : is assumed for any subsequent dimensions.


## Example

```
>>> x = np.array([[[1],[2],[3]], [[4],[5],[6]]])
>>> x.shape
(2, 3, 1)
>>> x[1:2]
array([[[4],
    [5],
    [6]]])
```

- Ellipsis expand to the number of : objects needed to make a selection tuple of the same length as x. ndim. Only the first ellipsis is expanded, any others are interpreted as : .


## Example

```
>>> x[...,0]
array([[1, 2, 3],
    [4, 5, 6]])
```

- Each newaxis object in the selection tuple serves to expand the dimensions of the resulting selection by one unit-length dimension. The added dimension is the position of the newaxis object in the selection tuple.


## Example

```
>>> x[:,np.newaxis,:,:].shape
(2, 1, 3, 1)
```

- An integer, $i$, returns the same values as i:i+1 except the dimensionality of the returned object is reduced by 1 . In particular, a selection tuple with the $p$-th element an integer (and all other entries :) returns the corresponding sub-array with dimension $N-1$. If $N=1$ then the returned object is an array scalar. These objects are explained in Scalars.
- If the selection tuple has all entries : except the $p$-th entry which is a slice object $i: j: k$, then the returned array has dimension $N$ formed by concatenating the sub-arrays returned by integer indexing of elements $i, i+k$, ..., $i+(m-1) k<j$,
- Basic slicing with more than one non-: entry in the slicing tuple, acts like repeated application of slicing using a single non-: entry, where the non-: entries are successively taken (with all other non-: entries replaced by :). Thus, $\mathrm{x}[$ ind1, . . ., ind2, :] acts like $\mathrm{x}[$ ind1] [..., ind2, :] under basic slicing.

Warning: The above is not true for advanced slicing.

- You may use slicing to set values in the array, but (unlike lists) you can never grow the array. The size of the value to be set in $\mathrm{x}[0, \mathrm{bj}]=$ value must be (broadcastable) to the same shape as $\mathrm{x}[\mathrm{obj}]$.

Note: Remember that a slicing tuple can always be constructed as obj and used in the $\mathrm{x}[\mathrm{obj}]$ notation. Slice objects can be used in the construction in place of the [start:stop:step] notation. For example, $x[1: 10: 5,::-1]$ can also be implemented as obj $=$ (slice ( $1,10,5$ ), slice (None, None, -1 )); $\mathrm{x}[\mathrm{obj}]$. This can be useful for constructing generic code that works on arrays of arbitrary dimension.
numpy. newaxis
The newaxis object can be used in the basic slicing syntax discussed above. None can also be used instead of newaxis.

### 1.4.2 Advanced indexing

Advanced indexing is triggered when the selection object, obj, is a non-tuple sequence object, an ndarray (of data type integer or bool), or a tuple with at least one sequence object or ndarray (of data type integer or bool). There are two types of advanced indexing: integer and Boolean.

Advanced indexing always returns a copy of the data (contrast with basic slicing that returns a view).

## Integer

Integer indexing allows selection of arbitrary items in the array based on their $N$-dimensional index. This kind of selection occurs when advanced indexing is triggered and the selection object is not an array of data type bool. For the discussion below, when the selection object is not a tuple, it will be referred to as if it had been promoted to a 1 -tuple, which will be called the selection tuple. The rules of advanced integer-style indexing are:

- If the length of the selection tuple is larger than $N$ an error is raised.
- All sequences and scalars in the selection tuple are converted to intp indexing arrays.
- All selection tuple objects must be convertible to intp arrays, slice objects, or the Ellipsis object.
- The first Ellipsis object will be expanded, and any other Ellipsis objects will be treated as full slice (:) objects. The expanded Ellipsis object is replaced with as many full slice (:) objects as needed to make the length of the selection tuple $N$.
- If the selection tuple is smaller than $N$, then as many : objects as needed are added to the end of the selection tuple so that the modified selection tuple has length $N$.
- All the integer indexing arrays must be broadcastable to the same shape.
- The shape of the output (or the needed shape of the object to be used for setting) is the broadcasted shape.
- After expanding any ellipses and filling out any missing : objects in the selection tuple, then let $N_{t}$ be the number of indexing arrays, and let $N_{s}=N-N_{t}$ be the number of slice objects. Note that $N_{t}>0$ (or we wouldn't be doing advanced integer indexing).
- If $N_{s}=0$ then the $M$-dimensional result is constructed by varying the index tuple (i_1, ..., i_M) over the range of the result shape and for each value of the index tuple (ind_1, ...., ind_M):

```
result [i_1, ..., i_M] == x[ind_1[i_1, ..., i_M], ind_2[i_1, ..., i_M],
    ..., ind_N[i_1, ..., i_M]]
```


## Example

Suppose the shape of the broadcasted indexing arrays is 3 -dimensional and $N$ is 2 . Then the result is found by letting $i, j, k$ run over the shape found by broadcasting ind_1 and ind_2, and each $i, j, k$ yields:

```
result[i,j,k] = x[ind_1[i,j,k], ind_2[i,j,k]]
```

- If $N_{s}>0$, then partial indexing is done. This can be somewhat mind-boggling to understand, but if you think in terms of the shapes of the arrays involved, it can be easier to grasp what happens. In simple cases (i.e. one indexing array and $N-l$ slice objects) it does exactly what you would expect (concatenation of repeated application of basic slicing). The rule for partial indexing is that the shape of the result (or the interpreted shape of the object to be used in setting) is the shape of $x$ with the indexed subspace replaced with the broadcasted indexing subspace. If the index subspaces are right next to each other, then the broadcasted indexing space directly replaces all of the indexed subspaces in $x$. If the indexing subspaces are separated (by slice objects), then the broadcasted indexing space is first, followed by the sliced subspace of $x$.


## Example

Suppose $x$.shape is $(10,20,30)$ and ind is a (2,3,4)-shaped indexing intp array, then result $=$ $x[\ldots$, ind,:] has shape ( $10,2,3,4,30$ ) because the ( 20, )-shaped subspace has been replaced with a (2,3,4)-shaped broadcasted indexing subspace. If we let $i, j, k$ loop over the ( $2,3,4$ )-shaped subspace then result $[\ldots, i, j, k,:]=x[\ldots, i n d[i, j, k],:]$. This example produces the same result as x.take(ind, axis=-2).

## Example

Now let x . shape be $(10,20,30,40,50)$ and suppose ind_1 and ind_2 are broadcastable to the shape ( $2,3,4$ ). Then $x[:$,ind_1,ind_2] has shape ( $10,2,3,4,40,50$ ) because the ( 20,30 )-shaped subspace from X has been replaced with the ( $2,3,4$ ) subspace from the indices. However, $x\left[:, i n d \_1,:, i n d \_2\right]$ has shape $(2,3,4,10,30,50)$ because there is no unambiguous place to drop in the indexing subspace, thus it is tackedon to the beginning. It is always possible to use .transpose () to move the subspace anywhere desired. (Note that this example cannot be replicated using take.)

## Boolean

This advanced indexing occurs when obj is an array object of Boolean type (such as may be returned from comparison operators). It is always equivalent to (but faster than) x[obj.nonzero()] where, as described above, obj.nonzero () returns a tuple (of length obj.ndim) of integer index arrays showing the True elements of obj.

The special case when obj. ndim $==\mathrm{x}$. ndim is worth mentioning. In this case $\mathrm{x}[\mathrm{obj}$ ] returns a 1 -dimensional array filled with the elements of $x$ corresponding to the True values of $o b j$. The search order will be C-style (last index varies the fastest). If obj has True values at entries that are outside of the bounds of $x$, then an index error will be raised.

You can also use Boolean arrays as element of the selection tuple. In such instances, they will always be interpreted as nonzero (obj) and the equivalent integer indexing will be done.

Warning: The definition of advanced indexing means that $\mathrm{x}[(1,2,3)$,$] is fundamentally different than$ $x[(1,2,3)]$. The latter is equivalent to $x[1,2,3]$ which will trigger basic selection while the former will trigger advanced indexing. Be sure to understand why this is occurs.
Also recognize that $\mathrm{x}[[1,2,3]]$ will trigger advanced indexing, whereas $\mathrm{x}[[1,2$, slice (None) ] ] will trigger basic slicing.

### 1.4.3 Record Access

## See Also:

## Data type objects (dtype), Scalars

If the ndarray object is a record array, i.e. its data type is a record data type, the fields of the array can be accessed by indexing the array with strings, dictionary-like.
Indexing $\mathrm{x}[$ 'field-name'] returns a new view to the array, which is of the same shape as $x$ (except when the field is a sub-array) but of data type $x$.dtype ['field-name'] and contains only the part of the data in the specified field. Also record array scalars can be "indexed" this way.

If the accessed field is a sub-array, the dimensions of the sub-array are appended to the shape of the result.

## Example

```
>>> x = np.zeros((2,2), dtype=[('a', np.int32), ('b', np.float64, (3,3))])
>>> x['a'].shape
(2, 2)
>>> x['a'].dtype
dtype('int32')
>>> x['b'].shape
(2, 2, 3, 3)
>>> x['b'].dtype
dtype('float64')
```


### 1.4.4 Flat Iterator indexing

x.flat returns an iterator that will iterate over the entire array (in C-contiguous style with the last index varying the fastest). This iterator object can also be indexed using basic slicing or advanced indexing as long as the selection object is not a tuple. This should be clear from the fact that x . fl at is a 1-dimensional view. It can be used for integer indexing with 1-dimensional C-style-flat indices. The shape of any returned array is therefore the shape of the integer indexing object.

### 1.5 Standard array subclasses

The ndarray in NumPy is a "new-style" Python built-in-type. Therefore, it can be inherited from (in Python or in C) if desired. Therefore, it can form a foundation for many useful classes. Often whether to sub-class the array object or to simply use the core array component as an internal part of a new class is a difficult decision, and can be simply a matter of choice. NumPy has several tools for simplifying how your new object interacts with other array objects, and so the choice may not be significant in the end. One way to simplify the question is by asking yourself if the object you are interested in can be replaced as a single array or does it really require two or more arrays at its core.

Note that asarray always returns the base-class ndarray. If you are confident that your use of the array object can handle any subclass of an ndarray, then asanyarray can be used to allow subclasses to propagate more cleanly through your subroutine. In principal a subclass could redefine any aspect of the array and therefore, under strict guidelines, asanyarray would rarely be useful. However, most subclasses of the arrayobject will not redefine certain aspects of the array object such as the buffer interface, or the attributes of the array. One important example, however, of why your subroutine may not be able to handle an arbitrary subclass of an array is that matrices redefine the "*" operator to be matrix-multiplication, rather than element-by-element multiplication.

### 1.5.1 Special attributes and methods

## See Also:

## Subclassing ndarray

Numpy provides several hooks that subclasses of ndarray can customize:

```
numpy.___array_finalize___(self)
```

This method is called whenever the system internally allocates a new array from obj, where obj is a subclass (subtype) of the ndarray. It can be used to change attributes of self after construction (so as to ensure a 2-d matrix for example), or to update meta-information from the "parent." Subclasses inherit a default implementation of this method that does nothing.

```
numpy.___array_prepare___(array, context=None)
```

At the beginning of every ufunc, this method is called on the input object with the highest array priority, or the output object if one was specified. The output array is passed in and whatever is returned is passed to the ufunc. Subclasses inherit a default implementation of this method which simply returns the output array unmodified. Subclasses may opt to use this method to transform the output array into an instance of the subclass and update metadata before returning the array to the ufunc for computation.

```
numpy.__array_wrap__ (array, context=None)
```

At the end of every ufunc, this method is called on the input object with the highest array priority, or the output object if one was specified. The ufunc-computed array is passed in and whatever is returned is passed to the user. Subclasses inherit a default implementation of this method, which transforms the array into a new instance of the object's class. Subclasses may opt to use this method to transform the output array into an instance of the subclass and update metadata before returning the array to the user.
numpy.__array_priority
The value of this attribute is used to determine what type of object to return in situations where there is more than one possibility for the Python type of the returned object. Subclasses inherit a default value of 1.0 for this attribute.
numpy.__array__ ([dtype])
If a class having the __array__ method is used as the output object of an ufunc, results will be written to the object returned by __array__.

### 1.5.2 Matrix objects

matrix objects inherit from the ndarray and therefore, they have the same attributes and methods of ndarrays. There are six important differences of matrix objects, however, that may lead to unexpected results when you use matrices but expect them to act like arrays:

1. Matrix objects can be created using a string notation to allow Matlab-style syntax where spaces separate columns and semicolons (';') separate rows.
2. Matrix objects are always two-dimensional. This has far-reaching implications, in that m.ravel() is still twodimensional (with a 1 in the first dimension) and item selection returns two-dimensional objects so that sequence behavior is fundamentally different than arrays.
3. Matrix objects over-ride multiplication to be matrix-multiplication. Make sure you understand this for functions that you may want to receive matrices. Especially in light of the fact that asanyarray(m) returns a matrix when $m$ is a matrix.
4. Matrix objects over-ride power to be matrix raised to a power. The same warning about using power inside a function that uses asanyarray(...) to get an array object holds for this fact.
5. The default __array_priority__ of matrix objects is 10.0, and therefore mixed operations with ndarrays always produce matrices.
6. Matrices have special attributes which make calculations easier. These are
```
matrix.T transpose
matrix.H hermitian (conjugate) transpose
matrix.I inverse
matrix.A base array
matrix.T
    transpose
matrix.H
    hermitian (conjugate) transpose
matrix.I
    inverse
matrix.A
    base array
```

Warning: Matrix objects over-ride multiplication, '*', and power, '**', to be matrix-multiplication and matrix power, respectively. If your subroutine can accept sub-classes and you do not convert to base- class arrays, then you must use the ufuncs multiply and power to be sure that you are performing the correct operation for all inputs.

The matrix class is a Python subclass of the ndarray and can be used as a reference for how to construct your own subclass of the ndarray. Matrices can be created from other matrices, strings, and anything else that can be converted to an ndarray. The name "mat "is an alias for "matrix "in NumPy.

| matrix | Returns a matrix from an array-like object, or from a string of data. |
| :--- | :--- |
| asmatrix(data[, dtype]) | Interpret the input as a matrix. |
| bmat(obj[, ldict, gdict]) | Build a matrix object from a string, nested sequence, or array. |

class numpy .matrix
Returns a matrix from an array-like object, or from a string of data. A matrix is a specialized 2-D array that retains its 2-D nature through operations. It has certain special operators, such as * (matrix multiplication) and ** (matrix power).

## Parameters

data : array_like or string
If data is a string, it is interpreted as a matrix with commas or spaces separating columns, and semicolons separating rows.
dtype : data-type
Data-type of the output matrix.
copy : bool
If data is already an ndarray, then this flag determines whether the data is copied (the default), or whether a view is constructed.

## See Also:

```
    array
```


## Examples

```
>>> a = np.matrix('1 2; 3 4')
```

>>> print a
[ $\left.\begin{array}{ll}1 & 2\end{array}\right]$
[3 4] ]

```
>>> np.matrix([[1, 2], [3, 4]])
matrix([[1, 2],
    [3, 4]])
```


## Methods



Table 1.3 - continued from previous page

| squeeze(a) | Remove single-dimensional entries from the shape of an array. |
| :---: | :---: |
| std(a[, axis, dtype, out, ddof]) | Compute the standard deviation along the specified axis. |
| $\operatorname{sum}(\mathrm{a}, \mathrm{axis}$, dtype, out]) | Sum of array elements over a given axis. |
| swapaxes(a, axis1, axis2) | Interchange two axes of an array. |
| take(a, indices[, axis, out, mode]) tofile | Take elements from an array along an axis. |
| tolist |  |
| tostring |  |
| trace(a[, offset, axis1, axis2, dtype, out]) | Return the sum along diagonals of the array. |
| transpose(a[, axes]) | Permute the dimensions of an array. |
| $\operatorname{var}(\mathrm{a}$, axis, dtype, out, ddof]) | Compute the variance along the specified axis. |
| view |  |

numpy.all $(a$, axis=None, out=None $)$
Test whether all array elements along a given axis evaluate to True.

## Parameters

a : array_like
Input array or object that can be converted to an array.
axis : int, optional
Axis along which a logical AND is performed. The default (axis $=$ None $)$ is to perform a logical AND over a flattened input array. axis may be negative, in which case it counts from the last to the first axis.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output and its type is preserved (e.g., if dtype (out) is float, the result will consist of 0.0 's and 1.0 's). See doc.ufuncs (Section "Output arguments") for more details.

## Returns

all : ndarray, bool
A new boolean or array is returned unless out is specified, in which case a reference to out is returned.

## See Also:

ndarray.all
equivalent method
any
Test whether any element along a given axis evaluates to True.

## Notes

Not a Number (NaN), positive infinity and negative infinity evaluate to True because these are not equal to zero.

## Examples

```
>>> np.all([[True,False],[True,True]])
False
```

```
>>> np.all([[True,False],[True,True]], axis=0)
array([ True, False], dtype=bool)
>>> np.all([-1, 4, 5])
True
>>> np.all([1.0, np.nan])
True
>>> o=np.array([False])
>>> z=np.all([-1, 4, 5], out=o)
>>> id(z), id(o), z
(28293632, 28293632, array([ True], dtype=bool))
```

numpy . any ( $a$, axis=None, out=None)
Test whether any array element along a given axis evaluates to True.
Returns single boolean unless axis is not None

## Parameters

a : array_like
Input array or object that can be converted to an array.
axis : int, optional
Axis along which a logical OR is performed. The default (axis = None) is to perform a logical OR over a flattened input array. axis may be negative, in which case it counts from the last to the first axis.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output and its type is preserved (e.g., if it is of type float, then it will remain so, returning 1.0 for True and 0.0 for False, regardless of the type of $a$ ). See doc.ufuncs (Section "Output arguments") for details.

## Returns

any : bool or ndarray
A new boolean or ndarray is returned unless out is specified, in which case a reference to out is returned.

## See Also:

ndarray.any
equivalent method
all
Test whether all elements along a given axis evaluate to True.

## Notes

Not a Number (NaN), positive infinity and negative infinity evaluate to True because these are not equal to zero.

## Examples

```
>>> np.any([[True, False], [True, True]])
True
```

```
>>> np.any([[True, False], [False, False]], axis=0)
array([ True, False], dtype=bool)
>>> np.any([-1, 0, 5])
True
>>> np.any(np.nan)
True
>>> o=np.array([False])
>>> z=np.any([-1, 4, 5], out=0)
>>> z, O
(array([ True], dtype=bool), array([ True], dtype=bool))
>>> # Check now that z is a reference to o
>>> z is o
True
>>> id(z), id(o) # identity of z and o
(191614240, 191614240)
numpy. argmax (a, axis=None)
Indices of the maximum values along an axis.
```


## Parameters

a : array_like
Input array.
axis : int, optional
By default, the index is into the flattened array, otherwise along the specified axis.

## Returns

index_array : ndarray of ints
Array of indices into the array. It has the same shape as a.shape with the dimension along axis removed.

## See Also:

```
ndarray.argmax, argmin
```

amax
The maximum value along a given axis.
unravel_index
Convert a flat index into an index tuple.

## Notes

In case of multiple occurrences of the maximum values, the indices corresponding to the first occurrence are returned.

## Examples

```
>>> a = np.arange(6).reshape(2,3)
>>> a
array([[0, 1, 2],
    [3, 4, 5]])
>>> np.argmax(a)
5
>>> np.argmax(a, axis=0)
array([1, 1, 1])
```

```
>>> np.argmax(a, axis=1)
array([2, 2])
>>> b = np.arange (6)
>>> b[1] = 5
>>> b
array([0, 5, 2, 3, 4, 5])
>>> np.argmax(b) # Only the first occurrence is returned.
1
```

numpy. argmin (a, axis=None)

Return the indices of the minimum values along an axis.
See Also:
argmax
Similar function. Please refer to numpy . argmax for detailed documentation.
numpy. argsort ( $a$, axis=-1, kind='quicksort', order=None)
Returns the indices that would sort an array.
Perform an indirect sort along the given axis using the algorithm specified by the kind keyword. It returns an array of indices of the same shape as $a$ that index data along the given axis in sorted order.

## Parameters

a : array_like
Array to sort.
axis : int or None, optional
Axis along which to sort. The default is -1 (the last axis). If None, the flattened array is used.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## Returns

index_array : ndarray, int
Array of indices that sort $a$ along the specified axis. In other words, a [index_array] yields a sorted $a$.

## See Also:

sort
Describes sorting algorithms used.
lexsort
Indirect stable sort with multiple keys.
ndarray.sort
Inplace sort.

## Notes

See sort for notes on the different sorting algorithms.
As of NumPy 1.4.0 argsort works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

One dimensional array:

```
>>> x = np.array([3, 1, 2])
>>> np.argsort(x)
array([1, 2, 0])
```

Two-dimensional array:

```
>>> x = np.array([[0, 3], [2, 2]])
>>> x
array([[0, 3],
    [2, 2]])
>>> np.argsort(x, axis=0)
array([[0, 1],
    [1, 0]])
>>> np.argsort(x, axis=1)
array([[0, 1],
    [0, 1]])
```

Sorting with keys:

```
>>> x = np.array([(1, 0), (0, 1)], dtype=[('x', '<i4'), ('y', '<i4')])
>>> x
array([(1, 0), (0, 1)],
    dtype=[('x', '<i4'), ('y', '<i4')])
>>> np.argsort(x, order=(' x','y'))
array([1, 0])
>>> np.argsort(x, order=('y',' (x'))
array([0, 1])
```

numpy. choose ( $a$, choices, out=None, mode = 'raise')
Construct an array from an index array and a set of arrays to choose from.
First of all, if confused or uncertain, definitely look at the Examples - in its full generality, this function is less simple than it might seem from the following code description (below ndi $=$ numpy.lib.index_tricks):
np.choose(a,c) == np.array([c[a[I]][I] for I in ndi.ndindex(a.shape)]).
But this omits some subtleties. Here is a fully general summary:
Given an "index" array ( $a$ ) of integers and a sequence of $n$ arrays (choices), $a$ and each choice array are first broadcast, as necessary, to arrays of a common shape; calling these Ba and Bchoices[i],i=0,..,n-1 we have that, necessarily, Ba.shape $==$ Bchoices[i].shape for each $i$. Then, a new array with shape Ba. shape is created as follows:
-if mode=raise (the default), then, first of all, each element of $a$ (and thus $B a$ ) must be in the range $[0, n-1]$; now, suppose that $i$ (in that range) is the value at the $(j 0, j 1, \ldots, j m)$ position in $B a$ - then the value at the same position in the new array is the value in Bchoices $[i]$ at that same position;
-if mode=wrap, values in $a$ (and thus $B a$ ) may be any (signed) integer; modular arithmetic is used to map integers outside the range [ $0, n-1]$ back into that range; and then the new array is constructed as above;
-if mode $=$ clip, values in $a$ (and thus $B a$ ) may be any (signed) integer; negative integers are mapped to 0 ; values greater than $n-1$ are mapped to $n-1$; and then the new array is constructed as above.

## Parameters

a : int array
This array must contain integers in [0, $n-1]$, where $n$ is the number of choices, unless mode=wrap or mode=clip, in which cases any integers are permissible.
choices : sequence of arrays
Choice arrays. $a$ and all of the choices must be broadcastable to the same shape. If choices is itself an array (not recommended), then its outermost dimension (i.e., the one corresponding to choices. shape [0]) is taken as defining the "sequence".
out : array, optional
If provided, the result will be inserted into this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise' (default), 'wrap', 'clip'\}, optional
Specifies how indices outside [ $0, n-1]$ will be treated:

- 'raise' : an exception is raised
- 'wrap' : value becomes value $\bmod n$
- 'clip' : values $<0$ are mapped to 0 , values $>\mathrm{n}-1$ are mapped to $\mathrm{n}-1$


## Returns

 merged_array : arrayThe merged result.

## Raises

ValueError: shape mismatch :
If $a$ and each choice array are not all broadcastable to the same shape.

## See Also:

ndarray. choose
equivalent method

## Notes

To reduce the chance of misinterpretation, even though the following "abuse" is nominally supported, choices should neither be, nor be thought of as, a single array, i.e., the outermost sequence-like container should be either a list or a tuple.

## Examples

```
>>> choices = [[0, 1, 2, 3], [10, 11, 12, 13],
... [20, 21, 22, 23], [30, 31, 32, 33]]
>>> np.choose([2, 3, 1, 0], choices
... # the first element of the result will be the first element of the
... # third (2+1) "array" in choices, namely, 20; the second element
... # will be the second element of the fourth (3+1) choice array, i.e.,
```

```
... # 31, etc.
... )
array([20, 31, 12, 3])
>>> np.choose([2, 4, 1, 0], choices, mode='clip') # 4 goes to 3 (4-1)
array([20, 31, 12, 3])
>>> # because there are 4 choice arrays
>>> np.choose([2, 4, 1, 0], choices, mode='wrap') # 4 goes to (4 mod 4)
array([20, 1, 12, 3])
>>> # i.e., 0
```

A couple examples illustrating how choose broadcasts:

```
>>> a = [[1, 0, 1], [0, 1, 0], [1, 0, 1]]
>>> choices = [-10, 10]
>>> np.choose(a, choices)
array([[ 10, -10, 10],
    [-10, 10, -10],
    [ 10, -10, 10]])
>>> # With thanks to Anne Archibald
>>> a = np.array([0, 1]).reshape((2,1,1))
>>> c1 = np.array([1, 2, 3]).reshape((1,3,1))
>>> c2 = np.array([-1, -2, -3, -4, -5]).reshape((1,1,5))
>>> np.choose(a, (c1, c2)) # result is 2x3x5, res[0,:,:]=c1, res[1,:,:]=c2
array([[[ 1, 1, 1, 1, 1],
    [2, 2, 2, 2, 2],
    [3, 3, 3, 3, 3]],
    [[-1, -2, -3, -4, -5],
    [-1, -2, -3, -4, -5],
    [-1, -2, -3, -4, -5]]])
```

numpy.clip ( $a, a \_$min, $a \_m a x$, out=None)
Clip (limit) the values in an array.
Given an interval, values outside the interval are clipped to the interval edges. For example, if an interval of $[0,1]$ is specified, values smaller than 0 become 0 , and values larger than 1 become 1 .

## Parameters

a : array_like
Array containing elements to clip.
a_min : scalar or array_like
Minimum value.
a_max : scalar or array_like
Maximum value. If $a \_m i n$ or $a \_m a x$ are array_like, then they will be broadcasted to the shape of $a$.
out : ndarray, optional
The results will be placed in this array. It may be the input array for in-place clipping. out must be of the right shape to hold the output. Its type is preserved.

## Returns

 clipped_array : ndarrayAn array with the elements of $a$, but where values $<a \_$min are replaced with $a \_$min, and those > a_max with $a_{-}$max.

## See Also:

numpy.doc.ufuncs
Section "Output arguments"

## Examples

```
>>> a = np.arange(10)
>>> np.clip(a, 1, 8)
array([1, 1, 2, 3, 4, 5, 6, 7, 8, 8])
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, 3, 6, out=a)
array([3, 3, 3, 3, 4, 5, 6, 6, 6, 6])
>>> a = np.arange(10)
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, [3,4,1,1,1,4,4,4,4,4], 8)
array([3, 4, 2, 3, 4, 5, 6, 7, 8, 8])
```

numpy. compress (condition, a, axis=None, out=None)
Return selected slices of an array along given axis.
When working along a given axis, a slice along that axis is returned in output for each index where condition evaluates to True. When working on a 1-D array, compress is equivalent to extract.

## Parameters

condition : 1-D array of bools
Array that selects which entries to return. If len(condition) is less than the size of $a$ along the given axis, then output is truncated to the length of the condition array.
a : array_like
Array from which to extract a part.
axis : int, optional
Axis along which to take slices. If None (default), work on the flattened array.
out : ndarray, optional
Output array. Its type is preserved and it must be of the right shape to hold the output.

## Returns

compressed_array : ndarray
A copy of $a$ without the slices along axis for which condition is false.

## See Also:

take, choose, diag, diagonal, select
ndarray. compress
Equivalent method.
numpy.doc.ufuncs
Section "Output arguments"

## Examples

```
>>> a = np.array([[1, 2], [3, 4], [5, 6]])
>>> a
array([[1, 2],
        [3, 4],
        [5, 6]])
>>> np.compress([0, 1], a, axis=0)
array([[3, 4]])
>>> np.compress([False, True, True], a, axis=0)
array([[3, 4],
    [5, 6]])
>>> np.compress([False, True], a, axis=1)
array([[2],
    [4],
    [6]])
```

Working on the flattened array does not return slices along an axis but selects elements.

```
>>> np.compress([False, True], a)
array([2])
```

numpy.conj ( $x$ [, out $]$ )

Return the complex conjugate, element-wise.
The complex conjugate of a complex number is obtained by changing the sign of its imaginary part.

## Parameters

$\mathbf{x}$ : array_like
Input value.

## Returns

$\mathbf{y}$ : ndarray
The complex conjugate of $x$, with same dtype as $y$.

## Examples

```
>>> np.conjugate(1+2j)
(1-2j)
>>> x = np.eye(2) + 1j * np.eye(2)
>>> np.conjugate(x)
array([[ 1.-1.j, 0.-0.j],
            [ 0.-0.j, 1.-1.j]])
```

numpy. copy (a)
Return an array copy of the given object.

## Parameters

a : array_like
Input data.

## Returns

arr : ndarray
Array interpretation of $a$.

## Notes

This is equivalent to

```
>>> np.array(a, copy=True)
```


## Examples

Create an array $x$, with a reference $y$ and a copy $z$ :

```
>>> x = np.array([1, 2, 3])
>>> y = x
>>> z = np.copy(x)
```

Note that, when we modify x , y changes, but not z :

```
>>> x[0] = 10
>>> x[0] == y[0]
True
>>> x[0] == z[0]
False
```

numpy . cumprod (a, axis=None, dtype=None, out=None)

Return the cumulative product of elements along a given axis.

## Parameters

a: array_like
Input array.
axis : int, optional
Axis along which the cumulative product is computed. By default the input is flattened.
dtype : dtype, optional
Type of the returned array, as well as of the accumulator in which the elements are multiplied. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used instead.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type of the resulting values will be cast if necessary.

## Returns

cumprod : ndarray
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.
See Also:
numpy. doc. ufuncs
Section "Output arguments"

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.
Examples

```
>>> a = np.array([1,2,3])
>>> np.cumprod(a) # intermediate results 1, 1*2
... # total product 1*2*3 = 6
array([1, 2, 6])
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
>>> np.cumprod(a, dtype=float) # specify type of output
array([ 1., 2., 6., 24., 120., 720.])
```

The cumulative product for each column (i.e., over the rows) of $a$ :

```
>>> np.cumprod(a, axis=0)
array([[ 1, 2, 3],
    [ 4, 10, 18]])
```

The cumulative product for each row (i.e. over the columns) of $a$ :

```
>>> np.cumprod(a,axis=1)
array([[[ 1, 2, 6],
    [4, 20, 120]])
```

numpy. cumsum ( $a$, axis=None, dtype $=$ None, out=None )
Return the cumulative sum of the elements along a given axis.

## Parameters

a : array_like
Input array.
axis : int, optional
Axis along which the cumulative sum is computed. The default (None) is to compute the cumsum over the flattened array.
dtype : dtype, optional
Type of the returned array and of the accumulator in which the elements are summed. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

cumsum_along_axis : ndarray.
A new array holding the result is returned unless out is specified, in which case a reference to out is returned. The result has the same size as $a$, and the same shape as $a$ if axis is not None or $a$ is a 1-d array.

## See Also:

sum
Sum array elements.
trapz
Integration of array values using the composite trapezoidal rule.

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> a
array([[1, 2, 3],
    [4, 5, 6]])
>>> np.cumsum(a)
array([ 1, 3, 6, 10, 15, 21])
>>> np.cumsum(a, dtype=float) # specifies type of output value(s)
array([ 1., 3., 6., 10., 15., 21.])
>>> np.cumsum(a,axis=0) # sum over rows for each of the 3 columns
array([[1, 2, 3],
    [5, 7, 9]])
>>> np.cumsum(a,axis=1) # sum over columns for each of the 2 rows
array([[ 1, 3, 6],
    [ 4, 9, 15]])
```

numpy.diagonal ( $a$, offset $=0$, axis $1=0$, axis $2=1$ )
Return specified diagonals.
If $a$ is 2-D, returns the diagonal of $a$ with the given offset, i.e., the collection of elements of the form a [i, i+offset]. If $a$ has more than two dimensions, then the axes specified by axisl and axis 2 are used to determine the 2-D sub-array whose diagonal is returned. The shape of the resulting array can be determined by removing axis 1 and axis 2 and appending an index to the right equal to the size of the resulting diagonals.

## Parameters

a: array_like
Array from which the diagonals are taken.
offset : int, optional
Offset of the diagonal from the main diagonal. Can be positive or negative. Defaults to main diagonal (0).
axis1 : int, optional
Axis to be used as the first axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults to first axis (0).
axis2 : int, optional
Axis to be used as the second axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults to second axis (1).

## Returns

array_of_diagonals : ndarray
If $a$ is 2-D, a $1-\mathrm{D}$ array containing the diagonal is returned. If the dimension of $a$ is larger, then an array of diagonals is returned, "packed" from left-most dimension to right-most (e.g., if $a$ is 3-D, then the diagonals are "packed" along rows).

## Raises

ValueError :
If the dimension of $a$ is less than 2 .

## See Also:

diag
MATLAB work-a-like for 1-D and 2-D arrays.
diagflat
Create diagonal arrays.
trace
Sum along diagonals.

## Examples

```
>>> a = np.arange(4).reshape(2,2)
>>> a
array([[0, 1],
    [2, 3]])
>>> a.diagonal()
array([0, 3])
>>> a.diagonal(1)
array([1])
```

A 3-D example:

```
>>> a = np.arange(8).reshape(2,2,2); a
array([[[0, 1],
        [2, 3]],
    [[4, 5],
        [6, 7]]])
>>> a.diagonal(0, # Main diagonals of two arrays created by skipping
... 0, # across the outer(left)-most axis last and
... 1) # the "middle" (row) axis first.
array([[0, 6],
    [1, 7]])
```

The sub-arrays whose main diagonals we just obtained; note that each corresponds to fixing the right-most (column) axis, and that the diagonals are "packed" in rows.

```
>>> a[:,:,0] # main diagonal is [0 6]
array([[0, 2],
    [4, 6]])
>>> a[:,:,1] # main diagonal is [1 7]
array([[1, 3],
    [5, 7]])
```

numpy.dot ( $a, b$, out=None)
Dot product of two arrays.
For 2-D arrays it is equivalent to matrix multiplication, and for 1-D arrays to inner product of vectors (without complex conjugation). For N dimensions it is a sum product over the last axis of $a$ and the second-to-last of $b$ :

```
dot(a, b)[i,j,k,m] = sum(a[i,j,:] * b[k,:,m])
```


## Parameters

a : array_like
First argument.
b : array_like

Second argument.
out : ndarray, optional
Output argument. This must have the exact kind that would be returned if it was not used. In particular, it must have the right type, must be C-contiguous, and its dtype must be the dtype that would be returned for $\operatorname{dot}(a, b)$. This is a performance feature. Therefore, if these conditions are not met, an exception is raised, instead of attempting to be flexible.

## Returns

output : ndarray
Returns the dot product of $a$ and $b$. If $a$ and $b$ are both scalars or both 1-D arrays then a scalar is returned; otherwise an array is returned. If out is given, then it is returned.

## Raises

## ValueError :

If the last dimension of $a$ is not the same size as the second-to-last dimension of $b$.

```
See Also:
vdot
    Complex-conjugating dot product.
tensordot
```

Sum products over arbitrary axes.
einsum

Einstein summation convention.

## Examples

```
>>> np.dot(3, 4)
12
```

Neither argument is complex-conjugated:

```
>>> np.dot([2j, 3j], [2j, 3j])
(-13+0j)
```

For 2-D arrays it's the matrix product:

```
>>> a = [[1, 0], [0, 1]]
>>> b = [[4, 1], [2, 2]]
>>> np.dot(a, b)
array([[4, 1],
        [2, 2]])
>>> a = np.arange(3*4*5*6).reshape((3,4,5,6))
>>> b = np.arange( }3*4*5*6)[::-1].reshape( (5,4,6,3)
>>> np.dot(a, b)[2,3,2,1,2,2]
499128
>>> sum(a[2,3,2,:] * b[1,2,:,2])
4 9 9 1 2 8
```

numpy . mean ( $a$, axis=None, dtype=None, out=None)
Compute the arithmetic mean along the specified axis.
Returns the average of the array elements. The average is taken over the flattened array by default, otherwise over the specified axis. float64 intermediate and return values are used for integer inputs.

## Parameters

a : array_like
Array containing numbers whose mean is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the means are computed. The default is to compute the mean of the flattened array.
dtype : data-type, optional
Type to use in computing the mean. For integer inputs, the default is float64; for floating point inputs, it is the same as the input dtype.
out : ndarray, optional
Alternate output array in which to place the result. The default is None; if provided, it must have the same shape as the expected output, but the type will be cast if necessary. See doc.ufuncs for details.

## Returns

m : ndarray, see dtype parameter above
If out=None, returns a new array containing the mean values, otherwise a reference to the output array is returned.

## See Also:

average
Weighted average

## Notes

The arithmetic mean is the sum of the elements along the axis divided by the number of elements.
Note that for floating-point input, the mean is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-precision accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.mean(a)
2.5
>>> np.mean(a, axis=0)
array([ 2., 3.])
>>> np.mean(a, axis=1)
array([ 1.5, 3.5])
```

In single precision, mean can be inaccurate:

```
>>> a = np.zeros((2, 512*512), dtype=np.float32)
>>> a[0, :] = 1.0
>>> a[1, :] = 0.1
>>> np.mean(a)
0.546875
```

Computing the mean in float64 is more accurate:

```
>>> np.mean(a, dtype=np.float64)
0.55000000074505806
```

numpy. nonzero (a)
Return the indices of the elements that are non-zero.
Returns a tuple of arrays, one for each dimension of $a$, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

```
a[nonzero(a)]
```

To group the indices by element, rather than dimension, use:

```
transpose(nonzero(a))
```

The result of this is always a 2-D array, with a row for each non-zero element.

## Parameters

a : array_like
Input array.

```
Returns
    tuple_of_arrays : tuple
Indices of elements that are non-zero.
```


## See Also:

flatnonzero
Return indices that are non-zero in the flattened version of the input array.
ndarray.nonzero
Equivalent ndarray method.
count_nonzero
Counts the number of non-zero elements in the input array.

## Examples

```
>>> x = np.eye(3)
>>> x
array([[ 1., 0., 0.],
    [ 0., 1., 0.],
    [ 0., 0., 1.]])
>>> np.nonzero(x)
(array([0, 1, 2]), array([0, 1, 2]))
>>> x[np.nonzero(x)]
array([ 1., 1., 1.])
>>> np.transpose(np.nonzero(x))
array([[0, 0],
    [1, 1],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , np.nonzero( $a>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a = np.array([[1,2,3],[4,5,6],[7,8,9]])
>>> a > 3
array([[False, False, False],
    [ True, True, True],
    [ True, True, True]], dtype=bool)
>>> np.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the boolean array can also be called.

```
>>> (a > 3).nonzero()
```

(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
numpy $\cdot \operatorname{prod}(a$, axis=None, dtype=None, out=None)
Return the product of array elements over a given axis.

## Parameters

a : array_like
Input data.
axis : int, optional
Axis over which the product is taken. By default, the product of all elements is calculated.
dtype : data-type, optional
The data-type of the returned array, as well as of the accumulator in which the elements are multiplied. By default, if $a$ is of integer type, dtype is the default platform integer. (Note: if the type of $a$ is unsigned, then so is dtype.) Otherwise, the dtype is the same as that of $a$.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output, but the type of the output values will be cast if necessary.

## Returns

product_along_axis : ndarray, see dtype parameter above.
An array shaped as $a$ but with the specified axis removed. Returns a reference to out if specified.

## See Also:

ndarray.prod
equivalent method
numpy.doc.ufuncs Section "Output arguments"

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow. That means that, on a 32-bit platform:

```
>>> x = np.array([536870910, 536870910, 536870910, 536870910])
>>> np.prod(x) #random
16
```


## Examples

By default, calculate the product of all elements:

```
>>> np.prod([1.,2.])
2.0
```

Even when the input array is two-dimensional:

```
>>> np.prod([[1.,2.],[3.,4.]])
24.0
```

But we can also specify the axis over which to multiply:

```
>>> np.prod([[1.,2.],[3.,4.]], axis=1)
array([ 2., 12.])
```

If the type of $x$ is unsigned, then the output type is the unsigned platform integer:

```
>>> x = np.array([1, 2, 3], dtype=np.uint8)
>>> np.prod(x).dtype == np.uint
True
```

If $x$ is of a signed integer type, then the output type is the default platform integer:

```
>>> x = np.array([1, 2, 3], dtype=np.int8)
>>> np.prod(x).dtype == np.int
```

True
numpy.ptp ( $a$, axis=None, out=None)

Range of values (maximum - minimum) along an axis.
The name of the function comes from the acronym for 'peak to peak'.

## Parameters

a : array_like
Input values.
axis : int, optional
Axis along which to find the peaks. By default, flatten the array.
out : array_like
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output, but the type of the output values will be cast if necessary.

## Returns

ptp: ndarray
A new array holding the result, unless out was specified, in which case a reference to out is returned.

## Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
    [2, 3]])
>>> np.ptp(x, axis=0)
array([2, 2])
```

```
>>> np.ptp(x, axis=1)
array([1, 1])
```

numpy .put ( $a$, ind, $v$, mode $=$ 'raise')
Replaces specified elements of an array with given values.
The indexing works on the flattened target array. put is roughly equivalent to:

```
a.flat[ind] = v
```


## Parameters

a: ndarray
Target array.
ind : array_like
Target indices, interpreted as integers.
$\mathbf{v}$ : array_like
Values to place in $a$ at target indices. If $v$ is shorter than ind it will be repeated as necessary.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## See Also:

putmask, place

## Examples

```
>>> a = np.arange(5)
>>> np.put(a, [0, 2], [-44, -55])
>>> a
array([-44, 1, -55, 3, 4])
>>> a = np.arange(5)
>>> np.put(a, 22, -5, mode='clip')
>>> a
array([ 0, 1, 2, 3, -5])
```

numpy.ravel ( $a$, order=' $C^{\prime}$ )

Return a flattened array.
A 1-D array, containing the elements of the input, is returned. A copy is made only if needed.

## Parameters

a : array_like

Input array. The elements in a are read in the order specified by order, and packed as a 1-D array.
order : \{ 'C',' F ', ' A ', ' K ' \}, optional
The elements of a are read in this order. ' C ' means to view the elements in C (rowmajor) order. ' $F$ ' means to view the elements in Fortran (column-major) order. ' $A$ ' means to view the elements in ' F ' order if a is Fortran contiguous, ' C ' order otherwise. ' K ' means to view the elements in the order they occur in memory, except for reversing the data when strides are negative. By default, ' C ' order is used.

## Returns

1d_array : ndarray
Output of the same dtype as $a$, and of shape (a.size(), ).

## See Also:

ndarray.flat
1-D iterator over an array.
ndarray.flatten
1-D array copy of the elements of an array in row-major order.

## Notes

In row-major order, the row index varies the slowest, and the column index the quickest. This can be generalized to multiple dimensions, where row-major order implies that the index along the first axis varies slowest, and the index along the last quickest. The opposite holds for Fortran-, or column-major, mode.

## Examples

It is equivalent to reshape ( -1 , order=order).

```
>>> x = np.array([[1, 2, 3], [4, 5, 6]])
>>> print np.ravel(x)
[1 [12 3 4 5 5 6]
>>> print x.reshape(-1)
[1 [14 3 4 5 6]
>>> print np.ravel(x, order=' F')
[1 [4 2 5 5 3 6]
```

When order is ' A ', it will preserve the array's ' C ' or ' F ' ordering:

```
>>> print np.ravel(x.T)
[1 4 4 2 5 5 3 6]
>>> print np.ravel(x.T, order=' A')
[1 [12 3
```

When order is ' $K$ ', it will preserve orderings that are neither ' $C$ ' nor ' $F$ ', but won't reverse axes:

```
>>> a = np.arange(3) [::-1]; a
array([2, 1, 0])
>>> a.ravel(order=' C')
array([2, 1, 0])
>>> a.ravel(order=' K')
array([2, 1, 0])
```

```
>>> a = np.arange(12).reshape(2,3,2).swapaxes(1,2); a
array([[[ 0, 2, 4],
            [ 1, 3, 5]],
            [[ 6, 8, 10],
            [ 7, 9, 11]]])
>>> a.ravel(order='C')
array([ 0, 2, 4, 1, 3, 5, 6, 8, 10, 7, 9, 11])
>>> a.ravel(order=' K')
array([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11])
```

numpy. repeat (a, repeats, axis=None)
Repeat elements of an array.

## Parameters

a : array_like
Input array.
repeats: \{int, array of ints \}
The number of repetitions for each element. repeats is broadcasted to fit the shape of the given axis.
axis : int, optional
The axis along which to repeat values. By default, use the flattened input array, and return a flat output array.

## Returns

repeated_array : ndarray
Output array which has the same shape as $a$, except along the given axis.

## See Also:

tile
Tile an array.
Examples

```
>>> x = np.array([[1,2],[3,4]])
>>> np.repeat(x, 2)
array([1, 1, 2, 2, 3, 3, 4, 4])
>>> np.repeat(x, 3, axis=1)
array([[1, 1, 1, 2, 2, 2],
            [3, 3, 3, 4, 4, 4]])
>>> np.repeat(x, [1, 2], axis=0)
array([[1, 2],
    [3, 4],
            [3, 4]])
```

numpy. reshape ( $a$, newshape, order=' $C$ ')
Gives a new shape to an array without changing its data.

## Parameters

a : array_like
Array to be reshaped.
newshape : int or tuple of ints

The new shape should be compatible with the original shape. If an integer, then the result will be a 1-D array of that length. One shape dimension can be -1 . In this case, the value is inferred from the length of the array and remaining dimensions.
order : \{ ' C ', ' F ', ' $A$ ' \}, optional
Determines whether the array data should be viewed as in C (row-major) order, FORTRAN (column-major) order, or the C/FORTRAN order should be preserved.

## Returns

reshaped_array : ndarray
This will be a new view object if possible; otherwise, it will be a copy.

## See Also:

ndarray.reshape
Equivalent method.

## Notes

It is not always possible to change the shape of an array without copying the data. If you want an error to be raise if the data is copied, you should assign the new shape to the shape attribute of the array:

```
>>> a = np.zeros((10, 2))
# A transpose make the array non-contiguous
>>> b = a.T
# Taking a view makes it possible to modify the shape without modiying the
# initial object.
>>> c = b.view()
>>> c.shape = (20)
AttributeError: incompatible shape for a non-contiguous array
```


## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> np.reshape(a, 6)
array([1, 2, 3, 4, 5, 6])
>>> np.reshape(a, 6, order=' F')
array([1, 4, 2, 5, 3, 6])
>>> np.reshape(a, (3,-1)) # the unspecified value is inferred to be 2
array([[1, 2],
    [3, 4],
    [5, 6]])
```

numpy.resize ( $a$, new_shape)
Return a new array with the specified shape.
If the new array is larger than the original array, then the new array is filled with repeated copies of $a$. Note that this behavior is different from a.resize(new_shape) which fills with zeros instead of repeated copies of $a$.

## Parameters

a : array_like
Array to be resized.
new_shape : int or tuple of int
Shape of resized array.

## Returns

reshaped_array : ndarray
The new array is formed from the data in the old array, repeated if necessary to fill out the required number of elements. The data are repeated in the order that they are stored in memory.

## See Also:

ndarray.resize
resize an array in-place.

## Examples

```
>>> a=np.array([[0,1],[2,3]])
>>> np.resize(a,(1,4))
array([[0, 1, 2, 3]])
>>> np.resize(a, (2,4))
array([[0, 1, 2, 3],
        [0, 1, 2, 3]])
```

numpy. searchsorted ( $a, v$, side $=$ 'left')

Find indices where elements should be inserted to maintain order.
Find the indices into a sorted array $a$ such that, if the corresponding elements in $v$ were inserted before the indices, the order of $a$ would be preserved.

## Parameters

a: 1-D array_like
Input array, sorted in ascending order.

$$
\mathbf{v} \text { : array_like }
$$

Values to insert into $a$.
side : \{'left', 'right' \}, optional
If 'left', the index of the first suitable location found is given. If 'right', return the last such index. If there is no suitable index, return either 0 or N (where N is the length of $a)$.

## Returns

indices : array of ints
Array of insertion points with the same shape as $v$.

## See Also:

sort
Return a sorted copy of an array.
histogram
Produce histogram from 1-D data.

## Notes

Binary search is used to find the required insertion points.
As of Numpy 1.4.0 searchsorted works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

```
>>> np.searchsorted([1,2,3,4,5], 3)
2
>>> np.searchsorted([1,2,3,4,5], 3, side='right')
3
>>> np.searchsorted([1,2,3,4,5], [-10, 10, 2, 3])
array([0, 5, 1, 2])
numpy.sort (a, axis=-1,kind='quicksort', order=None)
```

Return a sorted copy of an array.

## Parameters

a : array_like
Array to be sorted.
axis : int or None, optional
Axis along which to sort. If None, the array is flattened before sorting. The default is -1 , which sorts along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is a structured array, this argument specifies which fields to compare first, second, and so on. This list does not need to include all of the fields.

## Returns

sorted_array : ndarray
Array of the same type and shape as $a$.

## See Also:

ndarray.sort
Method to sort an array in-place.
argsort
Indirect sort.

## lexsort

Indirect stable sort on multiple keys.

## searchsorted

Find elements in a sorted array.

## Notes

The various sorting algorithms are characterized by their average speed, worst case performance, work space size, and whether they are stable. A stable sort keeps items with the same key in the same relative order. The three available algorithms have the following properties:

| kind | speed | worst case | work space | stable |
| :--- | :--- | :--- | :--- | :--- |
| 'quicksort' | 1 | $\mathrm{O}\left(\mathrm{n}^{\wedge} 2\right)$ | 0 | no |
| 'mergesort' | 2 | $\mathrm{O}\left(\mathrm{n}^{*} \log (\mathrm{n})\right)$ | $\sim \mathrm{n} / 2$ | yes |
| 'heapsort' | 3 | $\mathrm{O}(\mathrm{n} * \log (\mathrm{n}))$ | 0 | no |

All the sort algorithms make temporary copies of the data when sorting along any but the last axis. Consequently, sorting along the last axis is faster and uses less space than sorting along any other axis.

The sort order for complex numbers is lexicographic. If both the real and imaginary parts are non-nan then the order is determined by the real parts except when they are equal, in which case the order is determined by the imaginary parts.

Previous to numpy 1.4.0 sorting real and complex arrays containing nan values led to undefined behaviour. In numpy versions $>=1.4 .0$ nan values are sorted to the end. The extended sort order is:
-Real: [R, nan]
-Complex: [ $\mathrm{R}+\mathrm{Rj}, \mathrm{R}+$ nanj, nan +Rj , nan + nanj]
where R is a non-nan real value. Complex values with the same nan placements are sorted according to the non-nan part if it exists. Non-nan values are sorted as before.

## Examples

```
>>> a = np.array([[1,4],[3,1]])
>>> np.sort(a) # sort along the last axis
array([[1, 4],
    [1, 3]])
>>> np.sort(a, axis=None) # sort the flattened array
array([1, 1, 3, 4])
>>> np.sort(a, axis=0) # sort along the first axis
array([[1, 1],
    [3, 4]])
```

Use the order keyword to specify a field to use when sorting a structured array:

```
>>> dtype = [('name', 'S10'), ('height', float), ('age', int)]
>>> values = [('Arthur', 1.8, 41), ('Lancelot', 1.9, 38),
... ('Galahad', 1.7, 38)]
>>> a = np.array(values, dtype=dtype) # create a structured array
>>> np.sort(a, order='height')
array([('Galahad', 1.7, 38), ('Arthur', 1.8, 41),
    ('Lancelot', 1.89999999999999999, 38)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

Sort by age, then height if ages are equal:

```
>>> np.sort(a, order=['age', 'height'])
array([('Galahad', 1.7, 38), ('Lancelot', 1.8999999999999999, 38),
    ('Arthur', 1.8, 41)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

numpy.squeeze (a)
Remove single-dimensional entries from the shape of an array.

## Parameters

a : array_like
Input data.

## Returns

squeezed : ndarray
The input array, but with with all dimensions of length 1 removed. Whenever possible, a view on $a$ is returned.

## Examples

```
>>> x = np.array([[[0], [1], [2]]])
>>> x.shape
(1, 3, 1)
>>> np.squeeze(x).shape
(3,)
numpy.std (a,axis=None,dtype=None,out=None, ddof=0)
```

Compute the standard deviation along the specified axis.
Returns the standard deviation, a measure of the spread of a distribution, of the array elements. The standard deviation is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Calculate the standard deviation of these values.
axis : int, optional
Axis along which the standard deviation is computed. The default is to compute the standard deviation of the flattened array.
dtype : dtype, optional
Type to use in computing the standard deviation. For arrays of integer type the default is float 64 , for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type (of the calculated values) will be cast if necessary.
ddof : int, optional
Means Delta Degrees of Freedom. The divisor used in calculations is N - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

standard_deviation : ndarray, see dtype parameter above.
If out is None, return a new array containing the standard deviation, otherwise return a reference to the output array.

## See Also:

var, mean
numpy.doc.ufuncs
Section "Output arguments"

## Notes

The standard deviation is the square root of the average of the squared deviations from the mean, i.e., std $=\operatorname{sqrt}($ mean (abs ( $\mathrm{x}-\mathrm{x}$.mean()) **2) ).
The average squared deviation is normally calculated as $\mathrm{x} . \operatorname{sum}() / \mathrm{N}$, where $\mathrm{N}=$ len(x). If, however, $d d o f$ is specified, the divisor N - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of the infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables. The standard deviation computed in this function is the square root of the estimated variance, so even with ddof $=1$, it will not be an unbiased estimate of the standard deviation per se.

Note that, for complex numbers, std takes the absolute value before squaring, so that the result is always real and nonnegative.

For floating-point input, the std is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.std(a)
1.1180339887498949
>>> np.std(a, axis=0)
array([ 1., 1.])
>>> np.std(a, axis=1)
array([ 0.5, 0.5])
```

In single precision, $\operatorname{std}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.std(a)
0.45172946707416706
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.std(a, dtype=np.float64)
0.44999999925552653
```

numpy. sum ( $a$, axis=None, dtype=None, out=None)
Sum of array elements over a given axis.

## Parameters

a : array_like
Elements to sum.
axis : integer, optional
Axis over which the sum is taken. By default axis is None, and all elements are summed.
dtype : dtype, optional
The type of the returned array and of the accumulator in which the elements are summed. By default, the dtype of $a$ is used. An exception is when $a$ has an integer type with less precision than the default platform integer. In that case, the default platform integer is used instead.
out : ndarray, optional
Array into which the output is placed. By default, a new array is created. If out is given, it must be of the appropriate shape (the shape of $a$ with axis removed, i.e., numpy.delete (a.shape, axis)). Its type is preserved. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

sum_along_axis : ndarray
An array with the same shape as $a$, with the specified axis removed. If $a$ is a $0-\mathrm{d}$ array, or if axis is None, a scalar is returned. If an output array is specified, a reference to out is returned.

## See Also:

ndarray.sum
Equivalent method.

## cumsum

Cumulative sum of array elements.
trapz
Integration of array values using the composite trapezoidal rule.
mean, average

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> np.sum([0.5, 1.5])
2.0
>>> np.sum([0.5, 0.7, 0.2, 1.5], dtype=np.int32)
1
>>> np.sum([[0, 1], [0, 5]])
6
>>> np.sum([[0, 1], [0, 5]], axis=0)
array([0, 6])
>>> np.sum([[0, 1], [0, 5]], axis=1)
array([1, 5])
```

If the accumulator is too small, overflow occurs:

```
>>> np.ones(128, dtype=np.int8).sum(dtype=np.int8)
-128
```

numpy.swapaxes (a, axis1, axis2)

Interchange two axes of an array.

## Parameters

a : array_like
Input array.
axis1 : int
First axis.
axis2 : int
Second axis.

## Returns

a_swapped : ndarray
If $a$ is an ndarray, then a view of $a$ is returned; otherwise a new array is created.

## Examples

```
>>> x = np.array([[1,2,3]])
>>> np.swapaxes(x,0,1)
array([[1],
    [2],
        [3]])
```

```
>>> x = np.array([[[0,1],[2,3]],[[4,5],[6,7]]])
>>> x
array([[[0, 1],
    [2, 3]],
    [[4, 5],
        [6, 7]]])
>>> np.swapaxes(x,0,2)
array([[[0, 4],
        [2, 6]],
        [[1, 5],
        [3, 7]]])
```

numpy.take ( $a$, indices, axis=None, out=None, mode ='raise')

Take elements from an array along an axis.
This function does the same thing as "fancy" indexing (indexing arrays using arrays); however, it can be easier to use if you need elements along a given axis.

## Parameters

a : array_like
The source array.
indices : array_like
The indices of the values to extract.
axis : int, optional
The axis over which to select values. By default, the flattened input array is used.
out : ndarray, optional
If provided, the result will be placed in this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## Returns

subarray : ndarray
The returned array has the same type as $a$.

## See Also:

ndarray.take
equivalent method

## Examples

```
>>> a = [4, 3, 5, 7, 6, 8]
>>> indices = [0, 1, 4]
>>> np.take(a, indices)
array([4, 3, 6])
```

In this example if $a$ is an ndarray, "fancy" indexing can be used.

```
>>> a = np.array(a)
>>> a[indices]
array([4, 3, 6])
```

numpy.trace ( $a$, offset $=0$, axis $1=0$, axis $2=1$, dtype $=$ None, out $=$ None)
Return the sum along diagonals of the array.
If $a$ is 2 -D, the sum along its diagonal with the given offset is returned, i.e., the sum of elements a[i,i+offset] for all i.

If $a$ has more than two dimensions, then the axes specified by axis 1 and axis 2 are used to determine the 2-D sub-arrays whose traces are returned. The shape of the resulting array is the same as that of $a$ with axis1 and axis2 removed.

## Parameters

a : array_like
Input array, from which the diagonals are taken.
offset : int, optional
Offset of the diagonal from the main diagonal. Can be both positive and negative. Defaults to 0 .
axis1, axis2 : int, optional
Axes to be used as the first and second axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults are the first two axes of $a$.
dtype : dtype, optional
Determines the data-type of the returned array and of the accumulator where the elements are summed. If dtype has the value None and $a$ is of integer type of precision less than the default integer precision, then the default integer precision is used. Otherwise, the precision is the same as that of $a$.
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

sum_along_diagonals : ndarray
If $a$ is 2-D, the sum along the diagonal is returned. If $a$ has larger dimensions, then an array of sums along diagonals is returned.

## See Also:

diag, diagonal, diagflat

## Examples

```
>>> np.trace(np.eye(3))
3.0
>>> a = np.arange(8).reshape((2,2,2))
>>> np.trace(a)
array([6, 8])
>>> a = np.arange(24).reshape((2,2,2,3))
>>> np.trace(a).shape
(2, 3)
```

numpy.transpose (a, axes=None)
Permute the dimensions of an array.

## Parameters

a : array_like
Input array.
axes: list of ints, optional
By default, reverse the dimensions, otherwise permute the axes according to the values given.

## Returns

p: ndarray
$a$ with its axes permuted. A view is returned whenever possible.

## See Also:

```
rollaxis
```


## Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
        [2, 3]])
>>> np.transpose(x)
array([[0, 2],
            [1, 3]])
>>> x = np.ones((1, 2, 3))
>>> np.transpose(x, (1, 0, 2)).shape
(2, 1, 3)
```

numpy $\cdot \operatorname{var}(a$, axis $=$ None, dtype $=$ None, out $=$ None, $d d o f=0$ )

Compute the variance along the specified axis.
Returns the variance of the array elements, a measure of the spread of a distribution. The variance is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Array containing numbers whose variance is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the variance is computed. The default is to compute the variance of the flattened array.
dtype : data-type, optional
Type to use in computing the variance. For arrays of integer type the default is float32; for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output, but the type is cast if necessary.

## ddof : int, optional

"Delta Degrees of Freedom": the divisor used in the calculation is N - ddof, where N represents the number of elements. By default ddof is zero.

## Returns

variance : ndarray, see dtype parameter above
If out=None, returns a new array containing the variance; otherwise, a reference to the output array is returned.

```
See Also:
std
    Standard deviation
mean
    Average
numpy.doc.ufuncs
    Section "Output arguments"
```


## Notes

The variance is the average of the squared deviations from the mean, i.e., var $=$ mean $(a b s(x-$ $x . \operatorname{mean}()) * * 2$ ).

The mean is normally calculated as $x . \operatorname{sum}() / N$, where $N=$ len ( $x$ ). If, however, $d d o f$ is specified, the divisor $N$ - ddof is used instead. In standard statistical practice, ddof $=1$ provides an unbiased estimator of the variance of a hypothetical infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables.

Note that for complex numbers, the absolute value is taken before squaring, so that the result is always real and nonnegative.
For floating-point input, the variance is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1,2],[3,4]])
>>> np.var(a)
1.25
>>> np.var(a,0)
array([ 1., 1.])
>>> np.var(a,1)
array([ 0.25, 0.25])
```

In single precision, $\operatorname{var}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.var(a)
0.20405951142311096
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.var(a, dtype=np.float64)
0.20249999932997387
>>> ((1-0.55)**2 + (0.1-0.55)**2)/2
0.202500000000000001
```

numpy.asmatrix (data, dtype $=$ None $)$
Interpret the input as a matrix.
Unlike matrix, asmatrix does not make a copy if the input is already a matrix or an ndarray. Equivalent to matrix(data, copy=False).

## Parameters

data : array_like
Input data.

## Returns

mat : matrix
data interpreted as a matrix.

## Examples

```
>>> x = np.array([[1, 2], [3, 4]])
>>> m = np.asmatrix(x)
>>> x[0,0] = 5
>>> m
matrix([[5, 2],
    [3, 4]])
```

numpy .bmat (obj, ldict=None, gdict=None)
Build a matrix object from a string, nested sequence, or array.

## Parameters

obj : str or array_like
Input data. Names of variables in the current scope may be referenced, even if obj is a string.

## Returns

out : matrix
Returns a matrix object, which is a specialized 2-D array.
See Also:
matrix

## Examples

```
>>> A = np.mat('1 1; 1 1')
>>> B = np.mat('2 2; 2 2')
>>> C = np.mat('3 4; 5 6')
>>> D = np.mat('7 8; 9 0')
```

All the following expressions construct the same block matrix:

```
>>> np.bmat([[A, B], [C, D]])
matrix([[1, 1, 2, 2],
    [1, 1, 2, 2],
    [3, 4, 7, 8],
    [5, 6, 9, 0]])
>>> np.bmat(np.r_[np.c_[A, B], np.c_[C, D]])
matrix([[1, 1, 2, 2],
    [1, 1, 2, 2],
    [3, 4, 7, 8],
    [5, 6, 9, 0]])
>>> np.bmat('A,B; C, D')
matrix([[1, 1, 2, 2],
    [1, 1, 2, 2],
    [3, 4, 7, 8],
    [5, 6, 9, 0]])
```

Example 1: Matrix creation from a string

```
>>> a=mat('1
>>> print (a*a.T).I
[[ 0.2924 -0.1345]
    [-0.1345 0.0819]]
```

Example 2: Matrix creation from nested sequence

```
>>> mat([[1,5,10],[1.0,3,4j]])
matrix([[ 1.+0.j, 5.+0.j, 10.+0.j],
    [ 1.+0.j, 3.+0.j, 0.+4.j]])
```

Example 3: Matrix creation from an array

```
>>> mat(random.rand(3,3)).T
matrix([[ 0.7699, 0.7922, 0.3294],
    [ 0.2792, 0.0101, 0.9219],
    [0.3398, 0.7571, 0.8197]])
```


### 1.5.3 Memory-mapped file arrays

Memory-mapped files are useful for reading and/or modifying small segments of a large file with regular layout, without reading the entire file into memory. A simple subclass of the ndarray uses a memory-mapped file for the data buffer of the array. For small files, the over-head of reading the entire file into memory is typically not significant, however for large files using memory mapping can save considerable resources.
Memory-mapped-file arrays have one additional method (besides those they inherit from the ndarray): .flush () which must be called manually by the user to ensure that any changes to the array actually get written to disk.
Note: Memory-mapped arrays use the the Python memory-map object which (prior to Python 2.5 ) does not allow files to be larger than a certain size depending on the platform. This size is always $<2 \mathrm{~GB}$ even on 64 -bit systems.

| memmap | Create a memory-map to an array stored in a binary file on disk. |
| :--- | :--- |
| memmap.flush() | Write any changes in the array to the file on disk. |

## class numpy . memmap

Create a memory-map to an array stored in a binary file on disk.
Memory-mapped files are used for accessing small segments of large files on disk, without reading the entire file into memory. Numpy's memmap's are array-like objects. This differs from Python's mmap module, which uses file-like objects.

## Parameters

filename : str or file-like object
The file name or file object to be used as the array data buffer.
dtype : data-type, optional
The data-type used to interpret the file contents. Default is uint8.
mode : \{ 'r+', 'r', 'w+', 'c'\}, optional
The file is opened in this mode:

| 'r' | Open existing file for reading only. |
| :---: | :---: |
| 'r+' | Open existing file for reading and writing. |
| 'w+' | Create or overwrite existing file for reading and writing. |
| 'c' | Copy-on-write: assignments affect data in memory, but changes are not saved to disk. The file on disk is read-only. |

Default is ' $r+$ '.
offset : int, optional
In the file, array data starts at this offset. Since offset is measured in bytes, it should be a multiple of the byte-size of dtype. Requires shape=None. The default is 0 .
shape : tuple, optional
The desired shape of the array. By default, the returned array will be 1-D with the number of elements determined by file size and data-type.
order : \{ 'C', 'F'\}, optional
Specify the order of the ndarray memory layout: C (row-major) or Fortran (columnmajor). This only has an effect if the shape is greater than 1-D. The default order is 'C'.

## Notes

The memmap object can be used anywhere an ndarray is accepted. Given memmap $f p$, isinstance ( $f$ p, numpy. ndarray) returns True.

Memory-mapped arrays use the Python memory-map object which (prior to Python 2.5) does not allow files to be larger than a certain size depending on the platform. This size is always $<2 \mathrm{~GB}$ even on 64 -bit systems.

## Examples

```
>>> data = np.arange(12, dtype='float32')
>>> data.resize((3,4))
```

This example uses a temporary file so that doctest doesn't write files to your directory. You would use a 'normal' filename.

```
>>> from tempfile import mkdtemp
>>> import os.path as path
>>> filename = path.join(mkdtemp(), 'newfile.dat')
```

Create a memmap with dtype and shape that matches our data:

```
>>> fp = np.memmap(filename, dtype='float 32', mode='w+', shape=(3,4))
>>> fp
memmap([[ 0., 0., 0., 0.],
    [ 0., 0., 0., 0.],
    [ 0., 0., 0., 0.]], dtype=float32)
```

Write data to memmap array:

```
>>> fp[:] = data[:]
>>> fp
memmap([[[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.]], dtype=float32)
>>> fp.filename == path.abspath(filename)
True
```

Deletion flushes memory changes to disk before removing the object:

```
>>> del fp
```

Load the memmap and verify data was stored:

```
>>> newfp = np.memmap(filename, dtype='float 32', mode='r', shape=(3,4))
>>> newfp
memmap([[[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.]], dtype=float32)
```

Read-only memmap:

```
>>> fpr = np.memmap(filename, dtype='float 32', mode='r', shape=(3,4))
>>> fpr.flags.writeable
False
```

Copy-on-write memmap:

```
>>> fpc = np.memmap(filename, dtype='float 32', mode='c', shape=(3,4))
>>> fpc.flags.writeable
True
```

It's possible to assign to copy-on-write array, but values are only written into the memory copy of the array, and not written to disk:

```
>>> fpc
memmap([[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.]], dtype=float32)
>>> fpc[0,:] = 0
>>> fpc
memmap([[ 0., 0., 0., 0.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.]], dtype=float32)
```

File on disk is unchanged:

```
>>> fpr
memmap([[ 0., 1., 2., 3.],
```

```
[ 4., 5., 6., 7.],
[ 8., 9., 10., 11.]], dtype=float 32)
```

Offset into a memmap:

```
>>> fpo = np.memmap(filename, dtype='float32', mode='r', offset=16)
>>> fpo
memmap([ 4., 5., 6., 7., 8., 9., 10., 11.], dtype=float 32)
```


## Attributes

| filename <br> offset <br> mode | str <br> int | Path to the mapped file. <br> str |
| :--- | :--- | :--- |
| Offset position in the file. <br> File mode. |  |  |

## Methods

memmap.flush ()
Write any changes in the array to the file on disk.
For further information, see memmap.

## Parameters

None :

## See Also:

memmap
Example:

```
>>> a = memmap('newfile.dat', dtype=float, mode='w+', shape=1000)
>>> a[10] = 10.0
>>> a[30] = 30.0
>>> del a
>>> b = fromfile('newfile.dat', dtype=float)
>>> print b[10], b[30]
10.0 30.0
>>> a = memmap('newfile.dat', dtype=float)
>>> print a[10], a[30]
10.0 30.0
```


### 1.5.4 Character arrays (numpy . char)

## See Also:

## Creating character arrays (numpy.char)

Note: The chararray class exists for backwards compatibility with Numarray, it is not recommended for new development. Starting from numpy 1.4, if one needs arrays of strings, it is recommended to use arrays of dtype object_, string_ or unicode_, and use the free functions in the numpy. char module for fast vectorized string operations.

These are enhanced arrays of either string_ type or unicode_ type. These arrays inherit from the ndarray, but specially-define the operations,$+ *$, and $\%$ on a (broadcasting) element-by-element basis. These operations are not available on the standard ndarray of character type. In addition, the chararray has all of the standard string (and unicode) methods, executing them on an element-by-element basis. Perhaps the easiest way to create a chararray is to use self.view (chararray) where self is an ndarray of str or unicode data-type. However, a chararray can also be created using the numpy. chararray constructor, or via the numpy. char. array function:

```
chararray Provides a convenient view on arrays of string and unicode
                                    values.
core.defchararray.array(obj[, itemsize, Create a chararray.
...])
```

class numpy . chararray
Provides a convenient view on arrays of string and unicode values.
Note: The chararray class exists for backwards compatibility with Numarray, it is not recommended for new development. Starting from numpy 1.4, if one needs arrays of strings, it is recommended to use arrays of dtype object_, string_ or unicode_, and use the free functions in the numpy. char module for fast vectorized string operations.

Versus a regular Numpy array of type str or unicode, this class adds the following functionality:
1.values automatically have whitespace removed from the end when indexed
2.comparison operators automatically remove whitespace from the end when comparing values
3.vectorized string operations are provided as methods (e.g. endswith) and infix operators (e.g. "+", "*", " \% ")
chararrays should be created using numpy.char. array or numpy. char. asarray, rather than this constructor directly.

This constructor creates the array, using buffer (with offset and strides) if it is not None. If buffer is None, then constructs a new array with strides in "C order", unless both len (shape) >= 2 and order='Fortran', in which case strides is in "Fortran order".

## Parameters shape : tuple

Shape of the array.
itemsize : int, optional
Length of each array element, in number of characters. Default is 1.
unicode : bool, optional
Are the array elements of type unicode (True) or string (False). Default is False.
buffer : int, optional
Memory address of the start of the array data. Default is None, in which case a new array is created.
offset : int, optional
Fixed stride displacement from the beginning of an axis? Default is 0 . Needs to be $>=0$.
strides : array_like of ints, optional
Strides for the array (see ndarray.strides for full description). Default is None.
order : \{ 'C', 'F'\}, optional
The order in which the array data is stored in memory: 'C' -> "row major" order (the default), 'F' -> "column major" (Fortran) order.

## Examples

```
>>> charar = np.chararray((3, 3))
>>> charar[:] = 'a'
>>> charar
chararray([['a', 'a', 'a'],
```

```
        ['a', 'a', 'a'],
        ['a', 'a', 'a']],
        dtype='|S1')
>>> charar = np.chararray(charar.shape, itemsize=5)
>>> charar[:] = 'abc'
>>> charar
chararray([['abc', 'abc', 'abc'],
            ['abc', 'abc', 'abc'],
            ['abc', 'abc', 'abc']],
        dtype='|S5')
```


## Methods

## astype

argsort(a[, axis, kind, order $]$ Returns the indices that would sort an array.
copy(a)
Return an array copy of the given object.
count
decode
dump
dumps
encode
endswith
expandtabs
fill
find
flatten
getfield
index
isalnum
isalpha
isdecimal
isdigit
islower
isnumeric
isspace
istitle
isupper
item
join
ljust
lower
lstrip
nonzero(a)
put(a, ind, $\quad \mathrm{v}[$, mode]) Replaces specified elements of an array with given values.
ravel(a[, order])
repeat(a, repeats[, axis])
Return a flattened array.
replace
reshape(a, newshape[, order])
resize(a, new_shape)
rfind
rindex
rjust
$\square$ Continued on next page

Table 1.4 - continued from previous page

```
rsplit
rstrip
searchsorted(a, v[, side]) Find indices where elements should be inserted to maintain order.
setfield
setflags
sort(a[, axis, kind, order]) Return a sorted copy of an array.
split(ary, indices_or_sections[, axis]) Split an array into multiple sub-arrays of equal size.
splitlines
squeeze(a)
startswith
strip
swapaxes(a, axis1, axis2) Interchange two axes of an array.
swapcase
take(a, indices[, axis, out, mode]) Take elements from an array along an axis.
title
tofile
tolist
tostring
translate
transpose(a[, axes]) Permute the dimensions of an array.
upper
view
zfill
```

numpy.argsort ( $a$, axis=-1, kind='quicksort', order=None)

Returns the indices that would sort an array.
Perform an indirect sort along the given axis using the algorithm specified by the kind keyword. It returns an array of indices of the same shape as $a$ that index data along the given axis in sorted order.

## Parameters

a : array_like
Array to sort.
axis : int or None, optional
Axis along which to sort. The default is -1 (the last axis). If None, the flattened array is used.
kind : \{'quicksort', 'mergesort', 'heapsort'\}, optional
Sorting algorithm.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## Returns

index_array : ndarray, int
Array of indices that sort $a$ along the specified axis. In other words, a [index_array] yields a sorted $a$.

See Also:
sort
Describes sorting algorithms used.
lexsort
Indirect stable sort with multiple keys.
ndarray.sort
Inplace sort.

## Notes

See sort for notes on the different sorting algorithms.
As of NumPy 1.4.0 argsort works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

One dimensional array:

```
>>> x = np.array([3, 1, 2])
>>> np.argsort(x)
array([1, 2, 0])
```

Two-dimensional array:

```
>>> x = np.array([[0, 3], [2, 2]])
>>> x
array([[0, 3],
    [2, 2]])
>>> np.argsort(x, axis=0)
array([[0, 1],
    [1, 0]])
>>> np.argsort(x, axis=1)
array([[0, 1],
    [0, 1]])
```

Sorting with keys:

```
>>> x = np.array([(1, 0), (0, 1)], dtype=[('x', '<i4'), ('y', '<i4')])
>>> x
array([(1, 0), (0, 1)],
    dtype=[('x', '<i4'), ('y', '<i4')])
>>> np.argsort(x, order=('x','y'))
array([1, 0])
>>> np.argsort(x, order=('y',' ('))
array([0, 1])
Return an array copy of the given object.
```

numpy. copy (a)

## Parameters

a : array_like
Input data.

## Returns

arr : ndarray

Array interpretation of $a$.

## Notes

This is equivalent to

```
>>> np.array(a, copy=True)
```


## Examples

Create an array x , with a reference y and a copy z :

```
>>> x = np.array([1, 2, 3])
>>> y = x
>>> z = np.copy(x)
```

Note that, when we modify $x, y$ changes, but not $z$ :

```
>> x[0] = 10
>>> x[0] == y[0]
True
>>> x[0] == z[0]
False
```

numpy.nonzero (a)
Return the indices of the elements that are non-zero.
Returns a tuple of arrays, one for each dimension of $a$, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

```
a [nonzero(a)]
```

To group the indices by element, rather than dimension, use:
transpose(nonzero(a))
The result of this is always a 2-D array, with a row for each non-zero element.

## Parameters

a : array_like
Input array.

## Returns

tuple_of_arrays : tuple
Indices of elements that are non-zero.

## See Also:

flatnonzero
Return indices that are non-zero in the flattened version of the input array.
ndarray.nonzero
Equivalent ndarray method.
count_nonzero
Counts the number of non-zero elements in the input array.
Examples

```
>>> x = np.eye(3)
>>> x
array([[ 1., 0., 0.],
    [ 0., 1., 0.],
    [ 0., 0., 1.]])
>>> np.nonzero(x)
(array([0, 1, 2]), array([0, 1, 2]))
>>> x[np.nonzero(x)]
array([ 1., 1., 1.])
>>> np.transpose(np.nonzero(x))
array([[0, 0],
    [1, 1],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , np.nonzero( $a>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a = np.array([[1,2,3],[4,5,6],[7, 8,9]])
>>> a > 3
array([[False, False, False],
    [ True, True, True],
    [ True, True, True]], dtype=bool)
>>> np.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the boolean array can also be called.

```
>>> (a > 3).nonzero()
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

numpy .put ( $a$, ind, $v$, mode $=$ 'raise')
Replaces specified elements of an array with given values.
The indexing works on the flattened target array. put is roughly equivalent to:
a.flat [ind] = v

## Parameters

a : ndarray
Target array.
ind : array_like
Target indices, interpreted as integers.
$\mathbf{v}$ : array_like
Values to place in $a$ at target indices. If $v$ is shorter than ind it will be repeated as necessary.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## See Also:

putmask, place

## Examples

```
>>> a = np.arange(5)
>>> np.put(a, [0, 2], [-44, -55])
>>> a
array([-44, 1, -55, 3, 4])
>>> a = np.arange(5)
>>> np.put(a, 22, -5, mode='clip')
>>> a
array([ 0, 1, 2, 3, -5])
```

numpy. ravel ( $a$, order= ' $C$ ')

Return a flattened array.
A 1-D array, containing the elements of the input, is returned. A copy is made only if needed.

## Parameters

a: array_like
Input array. The elements in a are read in the order specified by order, and packed as a
1-D array.
order : \{ 'C',' F ', 'A', 'K' , optional
The elements of a are read in this order. ' C ' means to view the elements in C (rowmajor) order. ' F ' means to view the elements in Fortran (column-major) order. ' A ' means to view the elements in ' F ' order if a is Fortran contiguous, ' C ' order otherwise. ' K ' means to view the elements in the order they occur in memory, except for reversing the data when strides are negative. By default, ' C ' order is used.

## Returns

1d_array : ndarray
Output of the same dtype as $a$, and of shape (a.size(), ).

## See Also:

ndarray.flat
1-D iterator over an array.
ndarray.flatten
1-D array copy of the elements of an array in row-major order.

## Notes

In row-major order, the row index varies the slowest, and the column index the quickest. This can be generalized to multiple dimensions, where row-major order implies that the index along the first axis varies slowest, and the index along the last quickest. The opposite holds for Fortran-, or column-major, mode.

## Examples

It is equivalent to reshape ( -1 , order=order).

```
>>> x = np.array([[1, 2, 3], [4, 5, 6]])
>>> print np.ravel(x)
[1 2 3 4 5 6]
>>> print x.reshape(-1)
[1 2 3 4 5 6]
>>> print np.ravel(x, order='F')
[1 4 2 5 3 6]
```

When order is ' $A$ ', it will preserve the array's ' $C$ ' or ' $F$ ' ordering:

```
>>> print np.ravel(x.T)
[1 4 2 5 3 6]
>>> print np.ravel(x.T, order='A')
[1 2 3 4 5 6]
```

When order is ' $K$ ', it will preserve orderings that are neither ' $C$ ' nor ' $F$ ', but won't reverse axes:

```
>>> a = np.arange(3)[::-1]; a
array([2, 1, 0])
>>> a.ravel(order='C')
array([2, 1, 0])
>>> a.ravel(order='K')
array([2, 1, 0])
>>> a = np.arange(12).reshape(2,3,2).swapaxes(1,2); a
array([[[ 0, 2, 4],
            [ 1, 3, 5]],
            [[ 6, 8, 10],
            [ 7, 9, 11]]])
>>> a.ravel(order='C')
array([ 0, 2, 4, 1, 3, 5, 6, 8, 10, 7, 9, 11])
>>> a.ravel(order='K')
array([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11])
```

numpy.repeat (a, repeats, axis=None)
Repeat elements of an array.

## Parameters

a : array_like
Input array.
repeats: \{int, array of ints \}
The number of repetitions for each element. repeats is broadcasted to fit the shape of the given axis.
axis : int, optional
The axis along which to repeat values. By default, use the flattened input array, and return a flat output array.

## Returns

repeated_array : ndarray
Output array which has the same shape as $a$, except along the given axis.

## See Also:

tile
Tile an array.

## Examples

```
>>> x = np.array([[1,2],[3,4]])
>>> np.repeat(x, 2)
array([1, 1, 2, 2, 3, 3, 4, 4])
>>> np.repeat(x, 3, axis=1)
array([[1, 1, 1, 2, 2, 2],
            [3, 3, 3, 4, 4, 4]])
>>> np.repeat(x, [1, 2], axis=0)
array([[1, 2],
    [3, 4],
    [3, 4]])
```

numpy. reshape ( $a$, newshape, order $=$ ' $C$ ')
Gives a new shape to an array without changing its data.

## Parameters

a : array_like
Array to be reshaped.
newshape : int or tuple of ints
The new shape should be compatible with the original shape. If an integer, then the result will be a 1-D array of that length. One shape dimension can be -1 . In this case, the value is inferred from the length of the array and remaining dimensions.
order : \{ ' C ', ' F ', ' A '\}, optional
Determines whether the array data should be viewed as in C (row-major) order, FORTRAN (column-major) order, or the C/FORTRAN order should be preserved.

## Returns

reshaped_array : ndarray
This will be a new view object if possible; otherwise, it will be a copy.

## See Also:

ndarray.reshape
Equivalent method.

## Notes

It is not always possible to change the shape of an array without copying the data. If you want an error to be raise if the data is copied, you should assign the new shape to the shape attribute of the array:

```
>>> a = np.zeros((10, 2))
# A transpose make the array non-contiguous
>>> b = a.T
# Taking a view makes it possible to modify the shape without modiying the
# initial object.
>>> c = b.view()
>>> c.shape = (20)
AttributeError: incompatible shape for a non-contiguous array
```


## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> np.reshape(a, 6)
array([1, 2, 3, 4, 5, 6])
>>> np.reshape(a, 6, order=' F')
array([1, 4, 2, 5, 3, 6])
>>> np.reshape(a, (3,-1)) # the unspecified value is inferred to be 2
array([[1, 2],
    [3, 4],
    [5, 6]])
```

numpy.resize (a, new_shape)
Return a new array with the specified shape.
If the new array is larger than the original array, then the new array is filled with repeated copies of $a$. Note that this behavior is different from a.resize(new_shape) which fills with zeros instead of repeated copies of $a$.

## Parameters

a : array_like
Array to be resized.
new_shape : int or tuple of int
Shape of resized array.

## Returns

reshaped_array : ndarray
The new array is formed from the data in the old array, repeated if necessary to fill out the required number of elements. The data are repeated in the order that they are stored in memory.

## See Also:

ndarray.resize
resize an array in-place.

## Examples

```
>>> a=np.array([[0,1],[2,3]])
>>> np.resize(a, (1,4))
array([[0, 1, 2, 3]])
>>> np.resize(a, (2,4))
array([[0, 1, 2, 3],
            [0, 1, 2, 3]])
```

numpy. searchsorted ( $a, v$, side $=$ 'left')
Find indices where elements should be inserted to maintain order.
Find the indices into a sorted array $a$ such that, if the corresponding elements in $v$ were inserted before the indices, the order of $a$ would be preserved.

## Parameters

a : 1-D array_like
Input array, sorted in ascending order.
$\mathbf{v}$ : array_like

Values to insert into $a$.
side : \{ 'left', 'right' \}, optional
If 'left', the index of the first suitable location found is given. If 'right', return the last such index. If there is no suitable index, return either 0 or N (where N is the length of $a)$.

## Returns

indices : array of ints
Array of insertion points with the same shape as $v$.

## See Also:

sort
Return a sorted copy of an array.
histogram
Produce histogram from 1-D data.

## Notes

Binary search is used to find the required insertion points.
As of Numpy 1.4.0 searchsorted works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

```
>>> np.searchsorted([1,2,3,4,5], 3)
2
>>> np.searchsorted([1,2,3,4,5], 3, side='right')
3
>>> np.searchsorted([1,2,3,4,5], [-10, 10, 2, 3])
array([0, 5, 1, 2])
numpy.sort (a, axis=-1, kind='quicksort', order=None)
```

Return a sorted copy of an array.

## Parameters

a : array_like
Array to be sorted.
axis : int or None, optional
Axis along which to sort. If None, the array is flattened before sorting. The default is -1 , which sorts along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort'\}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is a structured array, this argument specifies which fields to compare first, second, and so on. This list does not need to include all of the fields.

## Returns

sorted_array : ndarray
Array of the same type and shape as $a$.

## See Also:

ndarray.sort
Method to sort an array in-place.
argsort
Indirect sort.
lexsort
Indirect stable sort on multiple keys.
searchsorted
Find elements in a sorted array.

## Notes

The various sorting algorithms are characterized by their average speed, worst case performance, work space size, and whether they are stable. A stable sort keeps items with the same key in the same relative order. The three available algorithms have the following properties:

| kind | speed | worst case | work space | stable |
| :--- | :--- | :--- | :--- | :--- |
| 'quicksort' | 1 | $\mathrm{O}\left(\mathrm{n}^{\wedge} 2\right)$ | 0 | no |
| 'mergesort' | 2 | $\mathrm{O}(\mathrm{n} * \log (\mathrm{n}))$ | $\sim \mathrm{n} / 2$ | yes |
| 'heapsort' | 3 | $\mathrm{O}(\mathrm{n} * \log (\mathrm{n}))$ | 0 | no |

All the sort algorithms make temporary copies of the data when sorting along any but the last axis. Consequently, sorting along the last axis is faster and uses less space than sorting along any other axis.

The sort order for complex numbers is lexicographic. If both the real and imaginary parts are non-nan then the order is determined by the real parts except when they are equal, in which case the order is determined by the imaginary parts.

Previous to numpy 1.4.0 sorting real and complex arrays containing nan values led to undefined behaviour. In numpy versions $>=1.4 .0$ nan values are sorted to the end. The extended sort order is:
-Real: [R, nan]
-Complex: [ $\mathrm{R}+\mathrm{Rj}, \mathrm{R}+$ nanj, nan +Rj , nan + nanj]
where R is a non-nan real value. Complex values with the same nan placements are sorted according to the non-nan part if it exists. Non-nan values are sorted as before.

## Examples

```
>>> a = np.array([[1,4],[3,1]])
>>> np.sort(a) # sort along the last axis
array([[1, 4],
    [1, 3]])
>>> np.sort(a, axis=None) # sort the flattened array
array([1, 1, 3, 4])
>>> np.sort(a, axis=0) # sort along the first axis
array([[1, 1],
    [3, 4]])
```

Use the order keyword to specify a field to use when sorting a structured array:

```
>>> dtype = [('name', 'S10'), ('height', float), ('age', int)]
>>> values = [('Arthur', 1.8, 41), ('Lancelot', 1.9, 38),
... ('Galahad', 1.7, 38)]
>>> a = np.array(values, dtype=dtype) # create a structured array
>>> np.sort(a, order='height')
array([('Galahad', 1.7, 38), ('Arthur', 1.8, 41),
    ('Lancelot', 1.8999999999999999, 38)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

Sort by age, then height if ages are equal:

```
>>> np.sort(a, order=['age', 'height'])
array([('Galahad', 1.7, 38), ('Lancelot', 1.8999999999999999, 38),
    ('Arthur', 1.8, 41)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

numpy.split (ary, indices_or_sections, axis=0)

Split an array into multiple sub-arrays of equal size.

## Parameters

ary : ndarray
Array to be divided into sub-arrays.
indices_or_sections : int or 1-D array
If indices_or_sections is an integer, N , the array will be divided into N equal arrays along axis. If such a split is not possible, an error is raised.

If indices_or_sections is a 1-D array of sorted integers, the entries indicate where along axis the array is split. For example, $[2,3]$ would, for axis=0, result in

- ary[:2]
- ary[2:3]
- ary[3:]

If an index exceeds the dimension of the array along axis, an empty sub-array is returned correspondingly.
axis : int, optional
The axis along which to split, default is 0 .

## Returns

sub-arrays : list of ndarrays
A list of sub-arrays.

## Raises

ValueError :
If indices_or_sections is given as an integer, but a split does not result in equal division.

## See Also:

array_split
Split an array into multiple sub-arrays of equal or near-equal size. Does not raise an exception if an equal division cannot be made.
hsplit
Split array into multiple sub-arrays horizontally (column-wise).
vsplit
Split array into multiple sub-arrays vertically (row wise).
dsplit
Split array into multiple sub-arrays along the 3rd axis (depth).
concatenate
Join arrays together.
hstack
Stack arrays in sequence horizontally (column wise).
vstack
Stack arrays in sequence vertically (row wise).
dstack
Stack arrays in sequence depth wise (along third dimension).

## Examples

```
>>> x = np.arange(9.0)
>>> np.split(x, 3)
[array([ 0., 1., 2.]), array([ 3., 4., 5.]), array([ 6., 7., 8.])]
>>> x = np.arange(8.0)
>>> np.split(x, [3, 5, 6, 10])
[array([ 0., 1., 2.]),
    array([ 3., 4.]),
    array([ 5.]),
    array([ 6., 7.]),
    array([], dtype=float64)]
```

numpy.squeeze (a)
Remove single-dimensional entries from the shape of an array.

## Parameters

a : array_like
Input data.

## Returns

squeezed : ndarray
The input array, but with with all dimensions of length 1 removed. Whenever possible, a view on $a$ is returned.

## Examples

```
>>> x = np.array([[[0], [1], [2]]])
>>> x.shape
(1, 3, 1)
>>> np.squeeze(x).shape
(3,)
```

numpy.swapaxes (a, axis1, axis2)
Interchange two axes of an array.

## Parameters

a : array_like
Input array.
axis1: int
First axis.
axis2 : int
Second axis.

## Returns

a_swapped : ndarray

If $a$ is an ndarray, then a view of $a$ is returned; otherwise a new array is created.

## Examples

```
>>> x = np.array([[1,2,3]])
>>> np.swapaxes(x,0,1)
array([[1],
    [2],
    [3]])
>>> x = np.array([[[0,1],[2,3]],[[4,5],[6,7]]])
>>> x
array([[[0, 1],
        [2, 3]],
    [[4, 5],
        [6, 7]]])
>>> np.swapaxes(x,0,2)
array([[[0, 4],
        [2, 6]],
        [[1, 5],
        [3, 7]]])
```

numpy.take ( $a$, indices, axis=None, out=None, mode='raise')

Take elements from an array along an axis.
This function does the same thing as "fancy" indexing (indexing arrays using arrays); however, it can be easier to use if you need elements along a given axis.

## Parameters

a: array_like
The source array.
indices : array_like
The indices of the values to extract.
axis : int, optional
The axis over which to select values. By default, the flattened input array is used.
out : ndarray, optional
If provided, the result will be placed in this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## Returns

```
        subarray : ndarray
```

The returned array has the same type as $a$.

## See Also:

ndarray.take
equivalent method

## Examples

```
>>> a = [4, 3, 5, 7, 6, 8]
>>> indices = [0, 1, 4]
>>> np.take(a, indices)
array([4, 3, 6])
```

In this example if $a$ is an ndarray, "fancy" indexing can be used.

```
>>> a = np.array(a)
>>> a[indices]
array([4, 3, 6])
```

numpy.transpose ( $a$, axes $=$ None )
Permute the dimensions of an array.

## Parameters

a : array_like
Input array.
axes: list of ints, optional
By default, reverse the dimensions, otherwise permute the axes according to the values given.

## Returns

$\mathbf{p}$ : ndarray
$a$ with its axes permuted. A view is returned whenever possible.

## See Also:

rollaxis

## Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
            [2, 3]])
>>> np.transpose(x)
array([[0, 2],
            [1, 3]])
>>> x = np.ones((1, 2, 3))
>>> np.transpose(x, (1, 0, 2)).shape
(2, 1, 3)
```

numpy. core.defchararray.array (obj, itemsize $=$ None, copy=True, unicode=None, order=None)
Create a chararray.
Note: This class is provided for numarray backward-compatibility. New code (not concerned with numarray compatibility) should use arrays of type string_ or unicode_ and use the free functions in numpy. char for fast vectorized string operations instead.

Versus a regular Numpy array of type str or unicode, this class adds the following functionality:
1.values automatically have whitespace removed from the end when indexed
2.comparison operators automatically remove whitespace from the end when comparing values
3.vectorized string operations are provided as methods (e.g. str.endswith) and infix operators (e.g. +, *, \%)

## Parameters

obj : array of str or unicode-like
itemsize : int, optional
itemsize is the number of characters per scalar in the resulting array. If itemsize is None, and obj is an object array or a Python list, the itemsize will be automatically determined. If itemsize is provided and obj is of type str or unicode, then the obj string will be chunked into itemsize pieces.
copy : bool, optional
If true (default), then the object is copied. Otherwise, a copy will only be made if __array__ returns a copy, if obj is a nested sequence, or if a copy is needed to satisfy any of the other requirements (itemsize, unicode, order, etc.).
unicode : bool, optional
When true, the resulting chararray can contain Unicode characters, when false only 8 -bit characters. If unicode is None and obj is one of the following:

- a chararray,
- an ndarray of type str or unicode
- a Python str or unicode object,
then the unicode setting of the output array will be automatically determined.
order : \{ 'C', 'F', 'A'\}, optional
Specify the order of the array. If order is ' C ' (default), then the array will be in C contiguous order (last-index varies the fastest). If order is ' $F$ ', then the returned array will be in Fortran-contiguous order (first-index varies the fastest). If order is ' $A$ ', then the returned array may be in any order (either C-, Fortran-contiguous, or even discontiguous).

Another difference with the standard ndarray of str data-type is that the chararray inherits the feature introduced by Numarray that white-space at the end of any element in the array will be ignored on item retrieval and comparison operations.

### 1.5.5 Record arrays (numpy.rec)

## See Also:

Creating record arrays (numpy.rec), Data type routines, Data type objects (dtype).
Numpy provides the recarray class which allows accessing the fields of a record/structured array as attributes, and a corresponding scalar data type object record.

| recarray | Construct an ndarray that allows field access using attributes. |
| :--- | :--- |
| record | A data-type scalar that allows field access as attribute lookup. |

class numpy.recarray
Construct an ndarray that allows field access using attributes.
Arrays may have a data-types containing fields, analogous to columns in a spread sheet. An example is [ ( $x$, int), (y, float)], where each entry in the array is a pair of (int, float). Normally, these attributes are accessed using dictionary lookups such as arr [' $\left.x^{\prime}\right]$ and $\operatorname{arr}\left[' y^{\prime}\right]$. Record arrays allow the fields to be accessed as members of the array, using arr. x and arr. y .

## Parameters

shape : tuple
Shape of output array.
dtype : data-type, optional
The desired data-type. By default, the data-type is determined from formats, names, titles, aligned and byteorder.
formats : list of data-types, optional
A list containing the data-types for the different columns, e.g. ['i4', $\quad \mathrm{f} 8^{\prime}$, 'i4']. formats does not support the new convention of using types directly, i.e. (int, float, int). Note that formats must be a list, not a tuple. Given that formats is somewhat limited, we recommend specifying dtype instead.
names : tuple of str, optional
The name of each column, e.g. (' $\mathrm{x}^{\prime}, ~ ' \mathrm{y}$ ', ' $\mathrm{z}^{\prime}$ ).
buf : buffer, optional
By default, a new array is created of the given shape and data-type. If buf is specified and is an object exposing the buffer interface, the array will use the memory from the existing buffer. In this case, the offset and strides keywords are available.

## Returns

rec : recarray
Empty array of the given shape and type.

## Other Parameters

titles : tuple of str, optional
Aliases for column names. For example, if names were ( ${ }^{\prime} x^{\prime}, y^{\prime} y^{\prime} \mathrm{I}^{\prime}$ ) and titles is ('x_coordinate', 'y_coordinate', 'z_coordinate'), then $\operatorname{arr}\left[{ }^{\prime} x^{\prime}\right]$ is equivalent to both arr. $x$ and arr. x _coordinate.
byteorder : \{ ‘<', '>’, ‘=’\}, optional
Byte-order for all fields.
aligned : bool, optional
Align the fields in memory as the C -compiler would.
strides : tuple of ints, optional
Buffer (buf) is interpreted according to these strides (strides define how many bytes each array element, row, column, etc. occupy in memory).
offset : int, optional
Start reading buffer (buf) from this offset onwards.
order : \{ ' $C$ ', ' $F$ ' $\}$, optional

Row-major or column-major order.

## See Also:

## rec.fromrecords

Construct a record array from data.
record
fundamental data-type for recarray.
format_parser
determine a data-type from formats, names, titles.

## Notes

This constructor can be compared to empt $y$ : it creates a new record array but does not fill it with data. To create a record array from data, use one of the following methods:
1.Create a standard ndarray and convert it to a record array, using arr.view (np.recarray)
2.Use the buf keyword.
3.Use np.rec.fromrecords.

## Examples

Create an array with two fields, $x$ and $y$ :

```
>>> x = np.array([(1.0, 2), (3.0, 4)], dtype=[('x', float), ('y', int)])
>>> x
array([(1.0, 2), (3.0, 4)],
    dtype=[('x', '<f8'), ('y', '<i4')])
>>> x['x']
array([ 1., 3.])
```

View the array as a record array:

```
>>> x = x.view(np.recarray)
>>> x.x
array([ 1., 3.])
>>> x.y
array([2, 4])
```

Create a new, empty record array:

```
>>> np.recarray((2,),
... dtype=[('x', int), ('y', float), ('z', int)])
rec.array([(-1073741821, 1.2249118382103472e-301, 24547520),
    (3471280, 1.2134086255804012e-316, 0)],
    dtype=[('x', '<i4'), ('y', '<f8'), ('z', '<i4')])
```


## Methods

| $\operatorname{all}(\mathrm{a}[$, | axis, | out $])$ | Test whether all array elements along a given axis evaluate to True. |
| :--- | :--- | :--- | :--- |
| $\operatorname{any}(\mathrm{a}[$, | axis, | out $])$ | Test whether any array element along a given axis evaluates to True. |
| $\operatorname{argmax}(\mathrm{a}[$, |  | axis $])$ | Indices of the maximum values along an axis. |
| $\operatorname{argmin}(\mathrm{a}[$, |  | axis $])$ | Return the indices of the minimum values along an axis. |

Table 1.5 - continued from previous page

numpy.all (a, axis=None, out=None)
Test whether all array elements along a given axis evaluate to True.

## Parameters

a : array_like
Input array or object that can be converted to an array.
axis : int, optional
Axis along which a logical AND is performed. The default (axis = None) is to perform a logical AND over a flattened input array. axis may be negative, in which case it counts from the last to the first axis.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output and its type is preserved (e.g., if dtype (out) is float, the result will consist of 0.0 's and 1.0 's). See doc.ufuncs (Section "Output arguments") for more details.

## Returns

all : ndarray, bool
A new boolean or array is returned unless out is specified, in which case a reference to out is returned.

## See Also:

ndarray.all
equivalent method
any
Test whether any element along a given axis evaluates to True.

## Notes

Not a Number (NaN), positive infinity and negative infinity evaluate to True because these are not equal to zero.

## Examples

```
>>> np.all([[True,False],[True,True]])
False
>>> np.all([[True,False],[True,True]], axis=0)
array([ True, False], dtype=bool)
>>> np.all([-1, 4, 5])
True
>>> np.all([1.0, np.nan])
True
>>> o=np.array([False])
>>> z=np.all([-1, 4, 5], out=0)
>>> id(z), id(0), z
(28293632, 28293632, array([ True], dtype=bool))
```

numpy . any ( $a$, axis=None, out=None)
Test whether any array element along a given axis evaluates to True.

Returns single boolean unless axis is not None

## Parameters

a : array_like
Input array or object that can be converted to an array.
axis : int, optional
Axis along which a logical OR is performed. The default (axis =None) is to perform a logical OR over a flattened input array. axis may be negative, in which case it counts from the last to the first axis.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output and its type is preserved (e.g., if it is of type float, then it will remain so, returning 1.0 for True and 0.0 for False, regardless of the type of $a$ ). See doc.ufuncs (Section "Output arguments") for details.

## Returns

any : bool or ndarray
A new boolean or ndarray is returned unless out is specified, in which case a reference to out is returned.

## See Also:

ndarray.any
equivalent method
all
Test whether all elements along a given axis evaluate to True.

## Notes

Not a Number (NaN), positive infinity and negative infinity evaluate to True because these are not equal to zero.

## Examples

```
>>> np.any([[True, False], [True, True]])
True
>>> np.any([[True, False], [False, False]], axis=0)
array([ True, False], dtype=bool)
>>> np.any([-1, 0, 5])
True
>>> np.any(np.nan)
True
>>> o=np.array([False])
>>> z=np.any([-1, 4, 5], out=0)
>>> z, O
(array([ True], dtype=bool), array([ True], dtype=bool))
>>> # Check now that z is a reference to o
>>> z is o
True
>>> id(z), id(o) # identity of z and o
(191614240, 191614240)
```

numpy .argmax (a, axis=None)
Indices of the maximum values along an axis.

## Parameters

a : array_like
Input array.
axis : int, optional
By default, the index is into the flattened array, otherwise along the specified axis.

## Returns

index_array : ndarray of ints
Array of indices into the array. It has the same shape as a.shape with the dimension along axis removed.

## See Also:

```
ndarray.argmax, argmin
```

amax
The maximum value along a given axis.
unravel_index
Convert a flat index into an index tuple.

## Notes

In case of multiple occurrences of the maximum values, the indices corresponding to the first occurrence are returned.

Examples

```
>>> a = np.arange(6).reshape(2,3)
>>> a
array([[0, 1, 2],
        [3, 4, 5]])
>>> np.argmax(a)
5
>>> np.argmax(a, axis=0)
array([1, 1, 1])
>>> np.argmax(a, axis=1)
array([2, 2])
>>> b = np.arange(6)
>>> b[1] = 5
>>> b
array([0, 5, 2, 3, 4, 5])
>>> np.argmax(b) # Only the first occurrence is returned.
1
numpy.argmin (a, axis=None)
```

Return the indices of the minimum values along an axis.

## See Also:

argmax
Similar function. Please refer to numpy. argmax for detailed documentation.
numpy.argsort (a, axis=-1, kind='quicksort', order=None)
Returns the indices that would sort an array.
Perform an indirect sort along the given axis using the algorithm specified by the kind keyword. It returns an array of indices of the same shape as $a$ that index data along the given axis in sorted order.

## Parameters

a : array_like
Array to sort.
axis : int or None, optional
Axis along which to sort. The default is -1 (the last axis). If None, the flattened array is used.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## Returns

index_array : ndarray, int
Array of indices that sort $a$ along the specified axis. In other words, a [index_array] yields a sorted $a$.

See Also:
sort
Describes sorting algorithms used.
lexsort
Indirect stable sort with multiple keys.
ndarray.sort
Inplace sort.

## Notes

See sort for notes on the different sorting algorithms.
As of NumPy 1.4.0 argsort works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

One dimensional array:

```
>>> x = np.array([3, 1, 2])
>>> np.argsort(x)
array([1, 2, 0])
```

Two-dimensional array:

```
>>> x = np.array([[0, 3], [2, 2]])
>>> x
array([[0, 3],
    [2, 2]])
```

```
>>> np.argsort(x, axis=0)
array([[0, 1],
    [1, 0]])
>>> np.argsort(x, axis=1)
array([[0, 1],
    [0, 1]])
```

Sorting with keys:

```
>>> x = np.array([(1, 0), (0, 1)], dtype=[('x', '<i4'), ('y', '<i4')])
>>> x
array([(1, 0), (0, 1)],
    dtype=[('x', '<i4'), ('y', '<i4')])
>>> np.argsort(x, order=(' x',' y'))
array([1, 0])
>>> np.argsort(x, order=(' y',' x'))
array([0, 1])
```

numpy. choose ( $a$, choices, out=None, mode='raise')
Construct an array from an index array and a set of arrays to choose from.
First of all, if confused or uncertain, definitely look at the Examples - in its full generality, this function is less simple than it might seem from the following code description (below ndi $=$ numpy.lib.index_tricks):
np.choose(a,c) == np.array([c[a[I]][I] for I in ndi.ndindex(a.shape)]).
But this omits some subtleties. Here is a fully general summary:
Given an "index" array (a) of integers and a sequence of $n$ arrays (choices), $a$ and each choice array are first broadcast, as necessary, to arrays of a common shape; calling these Ba and Bchoices $[i], i=0, \ldots, n-1$ we have that, necessarily, Ba.shape == Bchoices[i].shape for each $i$. Then, a new array with shape Ba . shape is created as follows:
-if mode=raise (the default), then, first of all, each element of $a$ (and thus $B a$ ) must be in the range $[0, n-1]$; now, suppose that $i$ (in that range) is the value at the ( $j 0, j 1, \ldots, j m$ ) position in $B a$ - then the value at the same position in the new array is the value in Bchoices[i] at that same position;
-if mode=wrap, values in $a$ (and thus $B a$ ) may be any (signed) integer; modular arithmetic is used to map integers outside the range [ $0, n-1$ ] back into that range; and then the new array is constructed as above;
-if mode=clip, values in $a$ (and thus $B a$ ) may be any (signed) integer; negative integers are mapped to 0 ; values greater than $n-1$ are mapped to $n-1$; and then the new array is constructed as above.

## Parameters

a : int array
This array must contain integers in $[0, n-1]$, where $n$ is the number of choices, unless mode=wrap or mode=clip, in which cases any integers are permissible.
choices : sequence of arrays
Choice arrays. $a$ and all of the choices must be broadcastable to the same shape. If choices is itself an array (not recommended), then its outermost dimension (i.e., the one corresponding to choices.shape [ 0 ]) is taken as defining the "sequence".
out : array, optional

If provided, the result will be inserted into this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise' (default), 'wrap', 'clip' \}, optional
Specifies how indices outside [ $0, n-1]$ will be treated:

- 'raise' : an exception is raised
- 'wrap' : value becomes value $\bmod n$
- 'clip' : values $<0$ are mapped to 0 , values $>\mathrm{n}-1$ are mapped to $\mathrm{n}-1$


## Returns

merged_array : array
The merged result.

## Raises

## ValueError: shape mismatch :

If $a$ and each choice array are not all broadcastable to the same shape.

## See Also:

ndarray. choose
equivalent method

## Notes

To reduce the chance of misinterpretation, even though the following "abuse" is nominally supported, choices should neither be, nor be thought of as, a single array, i.e., the outermost sequence-like container should be either a list or a tuple.

## Examples

```
>>> choices = [[0, 1, 2, 3], [10, 11, 12, 13],
... [20, 21, 22, 23], [30, 31, 32, 33]]
>>> np.choose([2, 3, 1, 0], choices
... # the first element of the result will be the first element of the
... # third (2+1) "array" in choices, namely, 20; the second element
... # will be the second element of the fourth (3+1) choice array, i.e.,
... # 31, etc.
... )
array([20, 31, 12, 3])
>>> np.choose([2, 4, 1, 0], choices, mode='clip') # 4 goes to 3 (4-1)
array([20, 31, 12, 3])
>>> # because there are 4 choice arrays
>> np.choose([2, 4, 1, 0], choices, mode='wrap') # 4 goes to (4 mod 4)
array([20, 1, 12, 3])
>>> # i.e., 0
```

A couple examples illustrating how choose broadcasts:

```
>>> a = [[1, 0, 1], [0, 1, 0], [1, 0, 1]]
>>> choices = [-10, 10]
>>> np.choose(a, choices)
array([[ 10, -10, 10],
    [-10, 10, -10],
    [ 10, -10, 10]])
```

```
>>> # With thanks to Anne Archibald
>>> a = np.array([0, 1]).reshape((2,1,1))
>>> c1 = np.array([1, 2, 3]).reshape((1,3,1))
>>> c2 = np.array([-1, -2, -3, -4, -5]).reshape((1,1,5))
>> np.choose(a, (c1, c2)) # result is 2x3x5, res[0,:,:]=c1, res[1,:,:]=c2
array([[[ 1, 1, 1, 1, 1],
    [2, 2, 2, 2, 2],
    [3, 3, 3, 3, 3]],
        [[-1, -2, -3, -4, -5],
        [-1, -2, -3, -4, -5],
        [-1, -2, -3, -4, -5]]])
```

numpy.clip ( $a, a \_m i n, a \_m a x$, out=None)

Clip (limit) the values in an array.
Given an interval, values outside the interval are clipped to the interval edges. For example, if an interval of $[0,1]$ is specified, values smaller than 0 become 0 , and values larger than 1 become 1 .

## Parameters

a : array_like
Array containing elements to clip.
a_min : scalar or array_like
Minimum value.
a_max : scalar or array_like
Maximum value. If $a \_m i n$ or $a \_m a x$ are array_like, then they will be broadcasted to the shape of $a$. out : ndarray, optional

The results will be placed in this array. It may be the input array for in-place clipping. out must be of the right shape to hold the output. Its type is preserved.

## Returns

clipped_array : ndarray
An array with the elements of $a$, but where values $<a \_$min are replaced with $a \_$min, and those > a_max with $a_{-}$max.

## See Also:

numpy.doc.ufuncs
Section "Output arguments"

## Examples

```
>>> a = np.arange(10)
>>> np.clip(a, 1, 8)
array([1, 1, 2, 3, 4, 5, 6, 7, 8, 8])
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, 3, 6, out=a)
array([3, 3, 3, 3, 4, 5, 6, 6, 6, 6])
>>> a = np.arange(10)
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, [3,4,1,1,1,4,4,4,4,4], 8)
array([3, 4, 2, 3, 4, 5, 6, 7, 8, 8])
```

numpy. compress (condition, a, axis=None, out=None)
Return selected slices of an array along given axis.
When working along a given axis, a slice along that axis is returned in output for each index where condition evaluates to True. When working on a 1-D array, compress is equivalent to extract.

## Parameters

condition : 1-D array of bools
Array that selects which entries to return. If len(condition) is less than the size of $a$ along the given axis, then output is truncated to the length of the condition array.
a : array_like
Array from which to extract a part.
axis : int, optional
Axis along which to take slices. If None (default), work on the flattened array.
out : ndarray, optional
Output array. Its type is preserved and it must be of the right shape to hold the output.

## Returns

compressed_array : ndarray
A copy of $a$ without the slices along axis for which condition is false.

## See Also:

```
take, choose, diag, diagonal, select
ndarray.compress
    Equivalent method.
numpy.doc.ufuncs
    Section "Output arguments"
Examples
```

```
>>> a = np.array([[1, 2], [3, 4], [5, 6]])
```

>>> a = np.array([[1, 2], [3, 4], [5, 6]])
>>> a
>>> a
array([[1, 2],
array([[1, 2],
[3, 4],
[3, 4],
[5, 6]])
[5, 6]])
>>> np.compress([0, 1], a, axis=0)
>>> np.compress([0, 1], a, axis=0)
array([[3, 4]])
array([[3, 4]])
>>> np.compress([False, True, True], a, axis=0)
>>> np.compress([False, True, True], a, axis=0)
array([[3, 4],
array([[3, 4],
[5, 6]])
[5, 6]])
>>> np.compress([False, True], a, axis=1)
>>> np.compress([False, True], a, axis=1)
array([[2],
array([[2],
[4],
[4],
[6]])

```
        [6]])
```

Working on the flattened array does not return slices along an axis but selects elements.

```
>>> np.compress([False, True], a)
array([2])
```

numpy.conj ( $x$ [, out $]$ )
Return the complex conjugate, element-wise.
The complex conjugate of a complex number is obtained by changing the sign of its imaginary part.

## Parameters

$\mathbf{x}$ : array_like
Input value.

## Returns

$\mathbf{y}$ : ndarray
The complex conjugate of $x$, with same dtype as $y$.

## Examples

```
>>> np.conjugate(1+2j)
(1-2j)
>>> x = np.eye(2) + 1j * np.eye(2)
>>> np.conjugate(x)
array([[ 1.-1.j, 0.-0.j],
            [ 0.-0.j, 1.-1.j]])
```

numpy. copy (a)
Return an array copy of the given object.

## Parameters

a : array_like
Input data.

## Returns

arr : ndarray
Array interpretation of $a$.

## Notes

This is equivalent to

```
>>> np.array(a, copy=True)
```


## Examples

Create an array $x$, with a reference $y$ and a copy $z$ :

```
>>> x = np.array([1, 2, 3])
>>> y = x
>>> z = np.copy(x)
```

Note that, when we modify $\mathrm{x}, \mathrm{y}$ changes, but not z :

```
>>> x[0] = 10
>>> x[0] == y[0]
True
>>> x[0] == z[0]
False
```

numpy. cumprod (a, axis=None, dtype=None, out=None)
Return the cumulative product of elements along a given axis.

## Parameters

$\mathbf{a}$ : array_like
Input array.
axis : int, optional
Axis along which the cumulative product is computed. By default the input is flattened.

```
dtype : dtype, optional
```

Type of the returned array, as well as of the accumulator in which the elements are multiplied. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used instead.

```
out : ndarray, optional
```

Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type of the resulting values will be cast if necessary.

## Returns

cumprod : ndarray
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## See Also:

## numpy.doc.ufuncs

Section "Output arguments"

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> a = np.array([1,2,3])
>>> np.cumprod(a) # intermediate results 1, 1*2
... # total product 1*2*3 = 6
array([1, 2, 6])
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
>>> np.cumprod(a, dtype=float) # specify type of output
array([ 1., 2., 6., 24., 120., 720.])
```

The cumulative product for each column (i.e., over the rows) of $a$ :

```
>>> np.cumprod(a, axis=0)
array([[ 1, 2, 3],
    [ 4, 10, 18]])
```

The cumulative product for each row (i.e. over the columns) of $a$ :

```
>>> np.cumprod(a,axis=1)
array([[ 1, 2, 6],
    [ 4, 20, 120]])
```

numpy. cumsum ( $a$, axis=None, dtype $=$ None, out=None )
Return the cumulative sum of the elements along a given axis.

## Parameters

a : array_like
Input array.
axis : int, optional

Axis along which the cumulative sum is computed. The default (None) is to compute the cumsum over the flattened array.

```
dtype : dtype, optional
```

Type of the returned array and of the accumulator in which the elements are summed. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used.

```
out : ndarray, optional
```

Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

```
        cumsum_along_axis : ndarray.
```

A new array holding the result is returned unless out is specified, in which case a reference to out is returned. The result has the same size as $a$, and the same shape as $a$ if axis is not None or $a$ is a 1-d array.

## See Also:

sum
Sum array elements.
trapz
Integration of array values using the composite trapezoidal rule.

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> a
array([[1, 2, 3],
    [4, 5, 6]])
>>> np.cumsum(a)
array([ 1, 3, 6, 10, 15, 21])
>>> np.cumsum(a, dtype=float) # specifies type of output value(s)
array([ 1., 3., 6., 10., 15., 21.])
>>> np.cumsum(a,axis=0) # sum over rows for each of the 3 columns
array([[1, 2, 3],
            [5, 7, 9]])
>>> np.cumsum(a,axis=1) # sum over columns for each of the 2 rows
array([[ 1, 3, 6],
            [ 4, 9, 15]])
```

numpy.diagonal (a, offset=0, axis $1=0$, axis $2=1$ )
Return specified diagonals.
If $a$ is 2-D, returns the diagonal of $a$ with the given offset, i.e., the collection of elements of the form a [i, i+offset]. If $a$ has more than two dimensions, then the axes specified by axisl and axis 2 are used to determine the 2-D sub-array whose diagonal is returned. The shape of the resulting array can be determined by removing axisl and axis 2 and appending an index to the right equal to the size of the resulting diagonals.

## Parameters

a : array_like
Array from which the diagonals are taken.
offset : int, optional
Offset of the diagonal from the main diagonal. Can be positive or negative. Defaults to main diagonal (0).
axis1 : int, optional
Axis to be used as the first axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults to first axis (0).
axis2 : int, optional
Axis to be used as the second axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults to second axis (1).

## Returns

array_of_diagonals : ndarray
If $a$ is $2-\mathrm{D}$, a $1-\mathrm{D}$ array containing the diagonal is returned. If the dimension of $a$ is larger, then an array of diagonals is returned, "packed" from left-most dimension to right-most (e.g., if $a$ is 3-D, then the diagonals are "packed" along rows).

## Raises

ValueError :
If the dimension of $a$ is less than 2 .

## See Also:

diag
MATLAB work-a-like for 1-D and 2-D arrays.
diagflat
Create diagonal arrays.
trace
Sum along diagonals.

## Examples

```
>>> a = np.arange(4).reshape(2,2)
>>> a
array([[0, 1],
            [2, 3]])
>>> a.diagonal()
array([0, 3])
>>> a.diagonal(1)
array([1])
```

A 3-D example:

```
>>> a = np.arange(8).reshape(2,2,2); a
array([[[0, 1],
            [2, 3]],
            [[4, 5],
            [6, 7]]])
>>> a.diagonal(0, # Main diagonals of two arrays created by skipping
... 0, # across the outer(left)-most axis last and
```

```
1) # the "middle" (row) axis first.
array([[0, 6],
    [1, 7]])
```

The sub-arrays whose main diagonals we just obtained; note that each corresponds to fixing the right-most (column) axis, and that the diagonals are "packed" in rows.

```
>>> a[:,:,0] # main diagonal is [0 6]
array([[0, 2],
    [4, 6]])
>>> a[:,:,1] # main diagonal is [1 7]
array([[1, 3],
    [5, 7]])
```

numpy.dot ( $a, b$, out=None)

Dot product of two arrays.
For 2-D arrays it is equivalent to matrix multiplication, and for 1-D arrays to inner product of vectors (without complex conjugation). For N dimensions it is a sum product over the last axis of $a$ and the second-to-last of $b$ :

$$
\operatorname{dot}(a, b)[i, j, k, m]=\operatorname{sum}(a[i, j,:] * b[k,: m])
$$

## Parameters

a : array_like
First argument.
b: array_like
Second argument.
out : ndarray, optional
Output argument. This must have the exact kind that would be returned if it was not used. In particular, it must have the right type, must be C-contiguous, and its dtype must be the dtype that would be returned for $\operatorname{dot}(a, b)$. This is a performance feature. Therefore, if these conditions are not met, an exception is raised, instead of attempting to be flexible.

## Returns

output : ndarray
Returns the dot product of $a$ and $b$. If $a$ and $b$ are both scalars or both 1-D arrays then a scalar is returned; otherwise an array is returned. If out is given, then it is returned.

## Raises

ValueError :
If the last dimension of $a$ is not the same size as the second-to-last dimension of $b$.

## See Also:

vdot
Complex-conjugating dot product.
tensordot
Sum products over arbitrary axes.
einsum
Einstein summation convention.

## Examples

```
>>> np.dot(3, 4)
12
```

Neither argument is complex-conjugated:

```
>>> np.dot([2j, 3j], [2j, 3j])
(-13+0j)
```

For 2-D arrays it's the matrix product:

```
>>> a = [[1, 0], [0, 1]]
>>> b = [[4, 1], [2, 2]]
>>> np.dot(a, b)
array([[4, 1],
    [2, 2]])
>>> a = np.arange( }3*4*5*6).reshape( (3,4,5,6)
>>> b = np.arange(3*4*5*6) [::-1].reshape((5,4,6,3))
>>> np.dot(a, b)[2,3,2,1,2,2]
499128
>>> sum(a[2,3,2,:] * b[1,2,:,2])
499128
```

numpy .mean ( $a$, axis=None, dtype=None, out=None)
Compute the arithmetic mean along the specified axis.
Returns the average of the array elements. The average is taken over the flattened array by default, otherwise over the specified axis. float64 intermediate and return values are used for integer inputs.

## Parameters

a : array_like
Array containing numbers whose mean is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the means are computed. The default is to compute the mean of the flattened array.
dtype : data-type, optional
Type to use in computing the mean. For integer inputs, the default is float64; for floating point inputs, it is the same as the input dtype.
out : ndarray, optional
Alternate output array in which to place the result. The default is None; if provided, it must have the same shape as the expected output, but the type will be cast if necessary. See doc.ufuncs for details.

## Returns

m : ndarray, see dtype parameter above
If out=None, returns a new array containing the mean values, otherwise a reference to the output array is returned.

## See Also:

average
Weighted average

## Notes

The arithmetic mean is the sum of the elements along the axis divided by the number of elements.
Note that for floating-point input, the mean is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-precision accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.mean(a)
2.5
>>> np.mean(a, axis=0)
array([ 2., 3.])
>>> np.mean(a, axis=1)
array([ 1.5, 3.5])
```

In single precision, mean can be inaccurate:

```
>>> a = np.zeros((2, 512*512), dtype=np.float 32)
>>> a[0, :] = 1.0
>>> a[1,:] = 0.1
>>> np.mean(a)
0.546875
```

Computing the mean in float64 is more accurate:

```
>>> np.mean(a, dtype=np.float64)
0.550000000074505806
```

numpy. nonzero (a)
Return the indices of the elements that are non-zero.
Returns a tuple of arrays, one for each dimension of $a$, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

$$
a[\text { nonzero (a) }]
$$

To group the indices by element, rather than dimension, use:

```
transpose(nonzero(a))
```

The result of this is always a 2-D array, with a row for each non-zero element.

## Parameters

a: array_like
Input array.

## Returns

tuple_of_arrays : tuple
Indices of elements that are non-zero.

## See Also:

flatnonzero
Return indices that are non-zero in the flattened version of the input array.
ndarray. nonzero
Equivalent ndarray method.
count_nonzero
Counts the number of non-zero elements in the input array.

## Examples

```
>>> x = np.eye(3)
>>> x
array([[ 1., 0., 0.],
    [ 0., 1., 0.],
    [ 0., 0., 1.]])
>>> np.nonzero(x)
(array([0, 1, 2]), array([0, 1, 2]))
>>> x[np.nonzero(x)]
array([ 1., 1., 1.])
>>> np.transpose(np.nonzero(x))
array([[0, 0],
    [1, 1],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , np.nonzero( $a>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a = np.array([[1,2,3],[4,5,6],[7, 8,9]])
>>> a > 3
array([[False, False, False],
    [ True, True, True],
    [ True, True, True]], dtype=bool)
>>> np.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the boolean array can also be called.

```
>>> (a > 3).nonzero()
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

numpy $\cdot \operatorname{prod}(a$, axis=None, dtype=None, out=None)
Return the product of array elements over a given axis.

## Parameters

a : array_like
Input data.
axis : int, optional
Axis over which the product is taken. By default, the product of all elements is calculated.
dtype : data-type, optional
The data-type of the returned array, as well as of the accumulator in which the elements are multiplied. By default, if $a$ is of integer type, dtype is the default platform integer. (Note: if the type of $a$ is unsigned, then so is dtype.) Otherwise, the dtype is the same as that of $a$.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output, but the type of the output values will be cast if necessary.

## Returns

product_along_axis : ndarray, see dtype parameter above.
An array shaped as $a$ but with the specified axis removed. Returns a reference to out if specified.

## See Also:

ndarray.prod
equivalent method
numpy.doc.ufuncs
Section "Output arguments"

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow. That means that, on a 32-bit platform:

```
>>> x = np.array([536870910, 536870910, 536870910, 536870910])
>>> np.prod(x) #random
16
```


## Examples

By default, calculate the product of all elements:

```
>>> np.prod([1.,2.])
2.0
```

Even when the input array is two-dimensional:

```
>>> np.prod([[1.,2.],[3.,4.]])
24.0
```

But we can also specify the axis over which to multiply:

```
>>> np.prod([[1.,2.],[3.,4.]], axis=1)
array([ 2., 12.])
```

If the type of $x$ is unsigned, then the output type is the unsigned platform integer:

```
>>> x = np.array([1, 2, 3], dtype=np.uint8)
>>> np.prod(x).dtype == np.uint
True
```

If $x$ is of a signed integer type, then the output type is the default platform integer:
$\ggg x=n p . \operatorname{array}([1,2,3]$, dtype=np.int8)
>>> np.prod(x).dtype == np.int
True
numpy $\cdot$ ptp ( $a$, axis=None, out=None)
Range of values (maximum - minimum) along an axis.
The name of the function comes from the acronym for 'peak to peak'.

## Parameters

a : array_like
Input values.
axis : int, optional

Axis along which to find the peaks. By default, flatten the array.
out : array_like
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output, but the type of the output values will be cast if necessary.

## Returns

ptp : ndarray
A new array holding the result, unless out was specified, in which case a reference to out is returned.

## Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
            [2, 3]])
>>> np.ptp(x, axis=0)
array([2, 2])
>>> np.ptp(x, axis=1)
array([1, 1])
```

numpy .put ( $a$, ind, $v$, mode $=$ 'raise')
Replaces specified elements of an array with given values.
The indexing works on the flattened target array. put is roughly equivalent to:

$$
\text { a.flat }[\text { ind }]=\text { v }
$$

## Parameters

a: ndarray
Target array.
ind : array_like
Target indices, interpreted as integers.
$\mathbf{v}$ : array_like
Values to place in $a$ at target indices. If $v$ is shorter than ind it will be repeated as necessary.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## See Also:

putmask, place

## Examples

```
>>> a = np.arange(5)
>>> np.put(a, [0, 2], [-44, -55])
>>> a
array([-44, 1, -55, 3, 4])
>>> a = np.arange(5)
>>> np.put(a, 22, -5, mode='clip')
>>> a
array([ 0, 1, 2, 3, -5])
```

numpy.ravel ( $a$, order=' $C^{\prime}$ )

Return a flattened array.
A 1-D array, containing the elements of the input, is returned. A copy is made only if needed.

## Parameters

a : array_like
Input array. The elements in a are read in the order specified by order, and packed as a 1-D array.
order : \{ 'C',' $\mathrm{F}^{\prime}$, 'A', 'K'\}, optional
The elements of a are read in this order. ' C ' means to view the elements in C (rowmajor) order. ' F ' means to view the elements in Fortran (column-major) order. ' A ' means to view the elements in ' $F$ ' order if a is Fortran contiguous, ' $C$ ' order otherwise. ' K ' means to view the elements in the order they occur in memory, except for reversing the data when strides are negative. By default, ' C ' order is used.

## Returns

1d_array : ndarray
Output of the same dtype as $a$, and of shape (a.size(), ).

## See Also:

ndarray.flat
1-D iterator over an array.
ndarray.flatten
1-D array copy of the elements of an array in row-major order.

## Notes

In row-major order, the row index varies the slowest, and the column index the quickest. This can be generalized to multiple dimensions, where row-major order implies that the index along the first axis varies slowest, and the index along the last quickest. The opposite holds for Fortran-, or column-major, mode.

## Examples

It is equivalent to reshape ( -1 , order=order).

```
>>> x = np.array([[1, 2, 3], [4, 5, 6]])
>>> print np.ravel(x)
[1
```

```
>>> print x.reshape(-1)
[1 2 3 4 5 6]
>>> print np.ravel(x, order='F')
[1 4 2 5 3 6]
```

When order is ' $A$ ', it will preserve the array's ' $C$ ' or ' $F$ ' ordering:

```
>>> print np.ravel(x.T)
[1 4 2 2 5 3 6]
>>> print np.ravel(x.T, order='A')
[14 2 3 4 5 6]
```

When order is ' $K$ ', it will preserve orderings that are neither ' $C$ ' nor ' $F$ ', but won't reverse axes:

```
>>> a = np.arange(3)[::-1]; a
array([2, 1, 0])
>>> a.ravel(order=' C')
array([2, 1, 0])
>>> a.ravel(order=' K')
array([2, 1, 0])
>>> a = np.arange(12).reshape(2,3,2).swapaxes(1,2); a
array([[[ 0, 2, 4],
            [ 1, 3, 5]],
            [[ 6, 8, 10],
            [ 7, 9, 11]]])
>>> a.ravel(order='C')
array([ 0, 2, 4, 1, 3, 5, 6, 8, 10, 7, 9, 11])
>>> a.ravel(order=' K')
array([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11])
```

numpy.repeat ( $a$, repeats, axis=None)
Repeat elements of an array.

## Parameters

a : array_like
Input array.
repeats: \{int, array of ints \}
The number of repetitions for each element. repeats is broadcasted to fit the shape of the given axis.
axis : int, optional
The axis along which to repeat values. By default, use the flattened input array, and return a flat output array.

## Returns

repeated_array : ndarray
Output array which has the same shape as $a$, except along the given axis.

## See Also:

tile
Tile an array.

## Examples

```
>>> x = np.array([[1,2],[3,4]])
>>> np.repeat(x, 2)
array([1, 1, 2, 2, 3, 3, 4, 4])
>>> np.repeat(x, 3, axis=1)
array([[1, 1, 1, 2, 2, 2],
            [3, 3, 3, 4, 4, 4]])
>>> np.repeat (x, [1, 2], axis=0)
array([[1, 2],
            [3, 4],
            [3, 4]])
```

numpy. reshape ( $a$, newshape, order=' $C$ ')

Gives a new shape to an array without changing its data.

## Parameters

a : array_like
Array to be reshaped.
newshape : int or tuple of ints
The new shape should be compatible with the original shape. If an integer, then the result will be a 1-D array of that length. One shape dimension can be -1 . In this case, the value is inferred from the length of the array and remaining dimensions.
order : \{ 'C', 'F', 'A'\}, optional
Determines whether the array data should be viewed as in C (row-major) order, FORTRAN (column-major) order, or the C/FORTRAN order should be preserved.

## Returns

reshaped_array : ndarray
This will be a new view object if possible; otherwise, it will be a copy.

## See Also:

ndarray.reshape
Equivalent method.

## Notes

It is not always possible to change the shape of an array without copying the data. If you want an error to be raise if the data is copied, you should assign the new shape to the shape attribute of the array:

```
>>> a = np.zeros((10, 2))
# A transpose make the array non-contiguous
>>> b = a.T
# Taking a view makes it possible to modify the shape without modiying the
# initial object.
>>> c = b.view()
>>> c.shape = (20)
AttributeError: incompatible shape for a non-contiguous array
```


## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> np.reshape(a, 6)
array([1, 2, 3, 4, 5, 6])
```

```
>>> np.reshape(a, 6, order=' F')
array([1, 4, 2, 5, 3, 6])
>>> np.reshape(a, (3,-1)) # the unspecified value is inferred to be 2
array([[1, 2],
    [3, 4],
    [5, 6]])
```

numpy.resize (a, new_shape)
Return a new array with the specified shape.
If the new array is larger than the original array, then the new array is filled with repeated copies of $a$. Note that this behavior is different from a.resize(new_shape) which fills with zeros instead of repeated copies of $a$.

## Parameters

a : array_like
Array to be resized.
new_shape : int or tuple of int
Shape of resized array.

## Returns

reshaped_array : ndarray
The new array is formed from the data in the old array, repeated if necessary to fill out the required number of elements. The data are repeated in the order that they are stored in memory.

See Also:
ndarray.resize
resize an array in-place.

## Examples

```
>>> a=np.array([[0,1],[2,3]])
>>> np.resize(a, (1,4))
array([[0, 1, 2, 3]])
>>> np.resize(a, (2,4))
array([[0, 1, 2, 3],
            [0, 1, 2, 3]])
```

numpy. searchsorted ( $a, v$, side='left')

Find indices where elements should be inserted to maintain order.
Find the indices into a sorted array $a$ such that, if the corresponding elements in $v$ were inserted before the indices, the order of $a$ would be preserved.

## Parameters

a: 1-D array_like
Input array, sorted in ascending order.
$\mathbf{v}$ : array_like
Values to insert into $a$.
side : \{ 'left', 'right' \}, optional

If 'left', the index of the first suitable location found is given. If 'right', return the last such index. If there is no suitable index, return either 0 or $N$ (where $N$ is the length of a).

## Returns

indices : array of ints
Array of insertion points with the same shape as $v$.

## See Also:

sort
Return a sorted copy of an array.
histogram
Produce histogram from 1-D data.

## Notes

Binary search is used to find the required insertion points.
As of Numpy 1.4.0 searchsorted works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

```
>>> np.searchsorted([1,2,3,4,5], 3)
2
>>> np.searchsorted([1,2,3,4,5], 3, side='right')
3
>>> np.searchsorted([1,2,3,4,5], [-10, 10, 2, 3])
array([0, 5, 1, 2])
numpy.sort (a, axis=-1,kind='quicksort', order=None)
```

Return a sorted copy of an array.

## Parameters

a: array_like
Array to be sorted.
axis : int or None, optional
Axis along which to sort. If None, the array is flattened before sorting. The default is -1 , which sorts along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is a structured array, this argument specifies which fields to compare first, second, and so on. This list does not need to include all of the fields.

## Returns

sorted_array : ndarray
Array of the same type and shape as $a$.
See Also:
ndarray.sort
Method to sort an array in-place.
argsort
Indirect sort.
lexsort
Indirect stable sort on multiple keys.
searchsorted
Find elements in a sorted array.

## Notes

The various sorting algorithms are characterized by their average speed, worst case performance, work space size, and whether they are stable. A stable sort keeps items with the same key in the same relative order. The three available algorithms have the following properties:

| kind | speed | worst case | work space | stable |
| :--- | :--- | :--- | :--- | :--- |
| 'quicksort' | 1 | $\mathrm{O}\left(\mathrm{n}^{\wedge} 2\right)$ | 0 | no |
| 'mergesort' | 2 | $\mathrm{O}(\mathrm{n} * \log (\mathrm{n}))$ | $\sim \mathrm{n} / 2$ | yes |
| 'heapsort' | 3 | $\mathrm{O}(\mathrm{n} * \log (\mathrm{n}))$ | 0 | no |

All the sort algorithms make temporary copies of the data when sorting along any but the last axis. Consequently, sorting along the last axis is faster and uses less space than sorting along any other axis.

The sort order for complex numbers is lexicographic. If both the real and imaginary parts are non-nan then the order is determined by the real parts except when they are equal, in which case the order is determined by the imaginary parts.

Previous to numpy 1.4.0 sorting real and complex arrays containing nan values led to undefined behaviour. In numpy versions $>=1.4 .0$ nan values are sorted to the end. The extended sort order is:

- Real: [R, nan]
-Complex: [ $\mathrm{R}+\mathrm{Rj}, \mathrm{R}+$ nanj, nan +Rj , nan + nanj]
where R is a non-nan real value. Complex values with the same nan placements are sorted according to the non-nan part if it exists. Non-nan values are sorted as before.


## Examples

```
>>> a = np.array([[1,4],[3,1]])
>> np.sort(a) # sort along the last axis
array([[1, 4],
        [1, 3]])
>> np.sort(a, axis=None) # sort the flattened array
array([1, 1, 3, 4])
np.sort(a, axis=0) # sort along the first axis
array([[1, 1],
        [3, 4]])
```

Use the order keyword to specify a field to use when sorting a structured array:

```
>>> dtype = [('name', 'S10'), ('height', float), ('age', int)]
>>> values = [('Arthur', 1.8, 41), ('Lancelot', 1.9, 38),
... ('Galahad', 1.7, 38)]
>>> a = np.array(values, dtype=dtype) # create a structured array
>>> np.sort(a, order='height')
array([('Galahad', 1.7, 38), ('Arthur', 1.8, 41),
    ('Lancelot', 1.8999999999999999, 38)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

Sort by age, then height if ages are equal:

```
>>> np.sort(a, order=['age', 'height'])
array([('Galahad', 1.7, 38), ('Lancelot', 1.8999999999999999, 38),
        ('Arthur', 1.8, 41)],
        dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

numpy.squeeze (a)
Remove single-dimensional entries from the shape of an array.

## Parameters

a : array_like
Input data.

## Returns

squeezed : ndarray
The input array, but with with all dimensions of length 1 removed. Whenever possible, a view on $a$ is returned.

## Examples

```
>>> x = np.array([[[0], [1], [2]]])
>>> x.shape
(1, 3, 1)
>>> np.squeeze(x).shape
(3,)
```

numpy. std ( $a$, axis=None, dtype=None, out=None, ddof=0)

Compute the standard deviation along the specified axis.
Returns the standard deviation, a measure of the spread of a distribution, of the array elements. The standard deviation is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Calculate the standard deviation of these values.
axis : int, optional
Axis along which the standard deviation is computed. The default is to compute the standard deviation of the flattened array.
dtype : dtype, optional
Type to use in computing the standard deviation. For arrays of integer type the default is float 64 , for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type (of the calculated values) will be cast if necessary.
ddof : int, optional
Means Delta Degrees of Freedom. The divisor used in calculations is N - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

standard_deviation : ndarray, see dtype parameter above.
If out is None, return a new array containing the standard deviation, otherwise return a reference to the output array.

## See Also:

```
var, mean
```


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## Notes

The standard deviation is the square root of the average of the squared deviations from the mean, i.e., std $=\operatorname{sqrt}(m e a n(a b s(x-x . m e a n()) * * 2))$.

The average squared deviation is normally calculated as $x \cdot \operatorname{sum}() / N$, where $N=\operatorname{len}(x)$. If, however, $d d o f$ is specified, the divisor $N$ - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of the infinite population. ddof $=0$ provides a maximum likelihood estimate of the variance for normally distributed variables. The standard deviation computed in this function is the square root of the estimated variance, so even with ddof $=1$, it will not be an unbiased estimate of the standard deviation per se.

Note that, for complex numbers, std takes the absolute value before squaring, so that the result is always real and nonnegative.

For floating-point input, the std is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.std(a)
1.1180339887498949
>>> np.std(a, axis=0)
array([ 1., 1.])
>>> np.std(a, axis=1)
array([ 0.5, 0.5])
```

In single precision, $\operatorname{std}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.std(a)
0.45172946707416706
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.std(a, dtype=np.float64)
0.44999999925552653
```

numpy.sum ( $a$, axis=None, dtype=None, out=None)
Sum of array elements over a given axis.

## Parameters

a : array_like
Elements to sum.
axis : integer, optional
Axis over which the sum is taken. By default axis is None, and all elements are summed.
dtype : dtype, optional

The type of the returned array and of the accumulator in which the elements are summed. By default, the dtype of $a$ is used. An exception is when $a$ has an integer type with less precision than the default platform integer. In that case, the default platform integer is used instead.
out : ndarray, optional
Array into which the output is placed. By default, a new array is created. If out is given, it must be of the appropriate shape (the shape of $a$ with axis removed, i.e., numpy.delete (a.shape, axis)). Its type is preserved. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

sum_along_axis : ndarray
An array with the same shape as $a$, with the specified axis removed. If $a$ is a $0-\mathrm{d}$ array, or if axis is None, a scalar is returned. If an output array is specified, a reference to out is returned.

## See Also:

ndarray.sum
Equivalent method.
cumsum
Cumulative sum of array elements.
trapz
Integration of array values using the composite trapezoidal rule.
mean, average

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> np.sum([0.5, 1.5])
2.0
>>> np.sum([0.5, 0.7, 0.2, 1.5], dtype=np.int32)
1
>>> np.sum([[0, 1], [0, 5]])
6
>>> np.sum([[0, 1], [0, 5]], axis=0)
array([0, 6])
>>> np.sum([[0, 1], [0, 5]], axis=1)
array([1, 5])
```

If the accumulator is too small, overflow occurs:

```
>>> np.ones(128, dtype=np.int8).sum(dtype=np.int8)
-128
```

numpy.swapaxes (a, axis1, axis 2 )
Interchange two axes of an array.

## Parameters

a : array_like
Input array.
axis1 : int
First axis.
axis2 : int
Second axis.

## Returns

a_swapped : ndarray
If $a$ is an ndarray, then a view of $a$ is returned; otherwise a new array is created.

## Examples

```
>>> x = np.array([[1,2,3]])
>>> np.swapaxes(x,0,1)
array([[1],
            [2],
            [3]])
>>> x = np.array([[[0,1],[2,3]],[[4,5],[6,7]]])
>>> x
array([[[0, 1],
    [2, 3]],
    [[4, 5],
    [6, 7]]])
>>> np.swapaxes(x,0,2)
array([[[0, 4],
            [2, 6]],
            [[1, 5],
            [3, 7]]])
```

numpy.take ( $a$, indices, axis=None, out=None, mode='raise')

Take elements from an array along an axis.
This function does the same thing as "fancy" indexing (indexing arrays using arrays); however, it can be easier to use if you need elements along a given axis.

## Parameters

a : array_like
The source array.
indices : array_like
The indices of the values to extract.
axis : int, optional
The axis over which to select values. By default, the flattened input array is used.
out : ndarray, optional
If provided, the result will be placed in this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## Returns

subarray : ndarray
The returned array has the same type as $a$.

## See Also:

ndarray.take
equivalent method

## Examples

```
>>> a = [4, 3, 5, 7, 6, 8]
>>> indices = [0, 1, 4]
>>> np.take(a, indices)
array([4, 3, 6])
```

In this example if $a$ is an ndarray, "fancy" indexing can be used.

```
>>> a = np.array(a)
>>> a[indices]
array([4, 3, 6])
```

numpy.trace $(a$, offset $=0$, axis $1=0$, axis $2=1$, dtype $=$ None, out $=$ None $)$
Return the sum along diagonals of the array.
If $a$ is $2-D$, the sum along its diagonal with the given offset is returned, i.e., the sum of elements a [i,i+offset] for all i.

If $a$ has more than two dimensions, then the axes specified by axis1 and axis 2 are used to determine the 2-D sub-arrays whose traces are returned. The shape of the resulting array is the same as that of $a$ with axis1 and axis2 removed.

## Parameters

a : array_like
Input array, from which the diagonals are taken.
offset : int, optional
Offset of the diagonal from the main diagonal. Can be both positive and negative. Defaults to 0 .
axis1, axis2 : int, optional
Axes to be used as the first and second axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults are the first two axes of $a$.
dtype : dtype, optional
Determines the data-type of the returned array and of the accumulator where the elements are summed. If dtype has the value None and $a$ is of integer type of precision less than the default integer precision, then the default integer precision is used. Otherwise, the precision is the same as that of $a$.
out : ndarray, optional

Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

 sum_along_diagonals : ndarrayIf $a$ is 2-D, the sum along the diagonal is returned. If $a$ has larger dimensions, then an array of sums along diagonals is returned.

## See Also:

diag, diagonal, diagflat

## Examples

```
    >>> np.trace(np.eye(3))
    3.0
>>> a = np.arange(8).reshape((2,2,2))
>>> np.trace(a)
array([6, 8])
>>> a = np.arange(24).reshape((2,2,2,3))
>>> np.trace(a).shape
(2, 3)
numpy.transpose (a, axes=None)
Permute the dimensions of an array.
```


## Parameters

a : array_like
Input array.
axes : list of ints, optional
By default, reverse the dimensions, otherwise permute the axes according to the values given.

## Returns

p: ndarray
$a$ with its axes permuted. A view is returned whenever possible.

## See Also:

rollaxis

## Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
    [2, 3]])
>>> np.transpose(x)
array([[0, 2],
    [1, 3]])
>>> x = np.ones((1, 2, 3))
>>> np.transpose(x, (1, 0, 2)).shape
(2, 1, 3)
```

numpy .var ( $a$, axis=None, dtype=None, out=None, ddof=0)
Compute the variance along the specified axis.
Returns the variance of the array elements, a measure of the spread of a distribution. The variance is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Array containing numbers whose variance is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the variance is computed. The default is to compute the variance of the flattened array.
dtype : data-type, optional
Type to use in computing the variance. For arrays of integer type the default is float32; for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output, but the type is cast if necessary.
ddof : int, optional
"Delta Degrees of Freedom": the divisor used in the calculation is N - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

variance : ndarray, see dtype parameter above
If out=None, returns a new array containing the variance; otherwise, a reference to the output array is returned.

## See Also:

std
Standard deviation
mean
Average
numpy.doc.ufuncs
Section "Output arguments"

## Notes

The variance is the average of the squared deviations from the mean, i.e., var $=$ mean (abs ( $x-$ $x$.mean()) **2).

The mean is normally calculated as $\mathrm{x} . \operatorname{sum}() / \mathrm{N}$, where $\mathrm{N}=\operatorname{len}(\mathrm{x})$. If, however, $d d o f$ is specified, the divisor N - ddof is used instead. In standard statistical practice, ddof $=1$ provides an unbiased estimator of the variance of a hypothetical infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables.
Note that for complex numbers, the absolute value is taken before squaring, so that the result is always real and nonnegative.

For floating-point input, the variance is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1,2],[3,4]])
>>> np.var(a)
1.25
>>> np.var(a,0)
array([ 1., 1.])
>>> np.var(a,1)
array([ 0.25, 0.25])
```

In single precision, $\operatorname{var}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.var(a)
0.20405951142311096
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.var(a, dtype=np.float64)
0.202499999932997387
>>> ((1-0.55)**2 + (0.1-0.55)**2)/2
0.202500000000000001
```


## class numpy. record

A data-type scalar that allows field access as attribute lookup.

## Methods

|  | Test whether all array elements along a given axis evaluate to True. Test whether any array element along a given axis evaluates to True. Indices of the maximum values along an axis. <br> Return the indices of the minimum values along an axis. Returns the indices that would sort an array. <br> Construct an array from an index array and a set of arrays to choose from. <br> Clip (limit) the values in an array. <br> Return selected slices of an array along given axis. <br> Return the complex conjugate, element-wise. <br> Return the complex conjugate, element-wise. <br> Return an array copy of the given object. <br> Return the cumulative product of elements along a given axis. <br> Return the cumulative sum of the elements along a given axis. <br> Return specified diagonals. |
| :---: | :---: |
|  | Continued on next page |

Table 1.6 - continued from previous page

```
itemset
max(a[, axis, out]) Return the maximum of an array or maximum along an axis.
mean(a[, axis, dtype, out]) Compute the arithmetic mean along the specified axis.
min(a[, axis, out]) Return the minimum of an array or minimum along an axis.
newbyteorder
nonzero(a)
pprint
prod(a[, axis, dtype, out])
ptp(a[, axis, out])
put(a, ind, v[, mode])
ravel(a[, order])
repeat(a, repeats[, axis])
reshape(a, newshape[, order])
resize(a, new_shape)
round(a[, decimals, out])
searchsorted(a, v[, side])
setfield
setflags
sort(a[, axis, kind, order]) Return a sorted copy of an array.
squeeze(a)
std(a[, axis, dtype, out, ddof])
sum(a[, axis, dtype, out])
swapaxes(a, axis1, axis2)
take(a, indices[, axis, out, mode]) Take elements from an array along an axis.
tofile
tolist
tostring
trace(a[,offset, axis1, axis2, dtype, out]) Return the sum along diagonals of the array.
transpose(a[, axes]) Permute the dimensions of an array.
var(a[, axis, dtype, out, ddof]) Compute the variance along the specified axis.
view
```

numpy.all (a, axis=None, out=None)
Test whether all array elements along a given axis evaluate to True.

## Parameters

a : array_like
Input array or object that can be converted to an array.
axis : int, optional
Axis along which a logical AND is performed. The default (axis = None) is to perform a logical AND over a flattened input array. axis may be negative, in which case it counts from the last to the first axis.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output and its type is preserved (e.g., if dtype (out) is float, the result will consist of 0.0 's and 1.0 's). See doc.ufuncs (Section "Output arguments") for more details.

## Returns

all : ndarray, bool

A new boolean or array is returned unless out is specified, in which case a reference to out is returned.

## See Also:

ndarray.all
equivalent method
any
Test whether any element along a given axis evaluates to True.

## Notes

Not a Number (NaN), positive infinity and negative infinity evaluate to True because these are not equal to zero.

## Examples

```
>>> np.all([[True,False],[True,True]])
False
>>> np.all([[True,False],[True,True]], axis=0)
array([ True, False], dtype=bool)
>>> np.all([-1, 4, 5])
True
>>> np.all([1.0, np.nan])
True
>>> o=np.array([False])
>>> z=np.all([-1, 4, 5], out=o)
>>> id(z), id(o), z
(28293632, 28293632, array([ True], dtype=bool))
```

numpy . any ( $a$, axis=None, out=None)
Test whether any array element along a given axis evaluates to True.
Returns single boolean unless axis is not None

## Parameters

a : array_like
Input array or object that can be converted to an array.
axis : int, optional
Axis along which a logical OR is performed. The default (axis = None) is to perform a logical OR over a flattened input array. axis may be negative, in which case it counts from the last to the first axis.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output and its type is preserved (e.g., if it is of type float, then it will remain so, returning 1.0 for True and 0.0 for False, regardless of the type of $a$ ). See doc.ufuncs (Section "Output arguments") for details.

## Returns

any : bool or ndarray

A new boolean or ndarray is returned unless out is specified, in which case a reference to out is returned.

## See Also:

ndarray.any
equivalent method
all
Test whether all elements along a given axis evaluate to True.
Notes
Not a Number (NaN), positive infinity and negative infinity evaluate to True because these are not equal to zero.

Examples

```
>>> np.any([[True, False], [True, True]])
True
>>> np.any([[True, False], [False, False]], axis=0)
array([ True, False], dtype=bool)
>>> np.any([-1, 0, 5])
True
>>> np.any(np.nan)
True
>>> o=np.array([False])
>>> z=np.any([-1, 4, 5], out=0)
>>> z, o
(array([ True], dtype=bool), array([ True], dtype=bool))
>>> # Check now that z is a reference to o
>>> z is o
True
>>> id(z), id(o) # identity of z and o
(191614240, 191614240)
```

numpy.argmax (a, axis=None)

Indices of the maximum values along an axis.

## Parameters

a : array_like
Input array.
axis : int, optional
By default, the index is into the flattened array, otherwise along the specified axis.

## Returns

index_array : ndarray of ints
Array of indices into the array. It has the same shape as a.shape with the dimension along axis removed.

## See Also:

```
ndarray.argmax, argmin
```


## amax

The maximum value along a given axis.
unravel_index
Convert a flat index into an index tuple.

## Notes

In case of multiple occurrences of the maximum values, the indices corresponding to the first occurrence are returned.

## Examples

```
>>> a = np.arange(6).reshape (2,3)
>>> a
array([[0, 1, 2],
    [3, 4, 5]])
>>> np.argmax(a)
5
>>> np.argmax(a, axis=0)
array([1, 1, 1])
>>> np.argmax(a, axis=1)
array([2, 2])
>>> b = np.arange(6)
>>> b[1] = 5
>>> b
array([0, 5, 2, 3, 4, 5])
>>> np.argmax(b) # Only the first occurrence is returned.
1
```

numpy.argmin (a, axis=None)

Return the indices of the minimum values along an axis.
See Also:
argmax
Similar function. Please refer to numpy. argmax for detailed documentation.
numpy. argsort ( a, axis=-1, kind='quicksort', order=None)
Returns the indices that would sort an array.
Perform an indirect sort along the given axis using the algorithm specified by the kind keyword. It returns an array of indices of the same shape as $a$ that index data along the given axis in sorted order.

## Parameters

a : array_like
Array to sort.
axis : int or None, optional
Axis along which to sort. The default is -1 (the last axis). If None, the flattened array is used.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm.
order : list, optional

When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## Returns

index_array : ndarray, int
Array of indices that sort $a$ along the specified axis. In other words, a [index_array] yields a sorted $a$.

## See Also:

sort
Describes sorting algorithms used.

## lexsort

Indirect stable sort with multiple keys.

```
ndarray.sort
```

Inplace sort.

## Notes

See sort for notes on the different sorting algorithms.
As of NumPy 1.4.0 argsort works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

One dimensional array:

```
>>> x = np.array([3, 1, 2])
>>> np.argsort(x)
array([1, 2, 0])
```

Two-dimensional array:

```
>>> x = np.array([[0, 3], [2, 2]])
>>> x
array([[0, 3],
    [2, 2]])
>>> np.argsort(x, axis=0)
array([[0, 1],
    [1, 0]])
>>> np.argsort(x, axis=1)
array([[0, 1],
    [0, 1]])
```

Sorting with keys:

```
>>> x = np.array([(1, 0), (0, 1)], dtype=[('x', '<i4'), ('y', '<i4')])
>>> x
array([(1, 0), (0, 1)],
    dtype=[('x', '<i4'), ('y', '<i4')])
>>> np.argsort(x, order=(' x','y'))
array([1, 0])
```

```
>>> np.argsort(x, order=('y',' x'))
array([0, 1])
```

numpy. choose ( $a$, choices, out=None, mode='raise')
Construct an array from an index array and a set of arrays to choose from.
First of all, if confused or uncertain, definitely look at the Examples - in its full generality, this function is less simple than it might seem from the following code description (below ndi $=$ numpy.lib.index_tricks):
np.choose(a,c) == np.array([c[a[I]][I] for I in ndi.ndindex(a.shape)]).
But this omits some subtleties. Here is a fully general summary:
Given an "index" array ( $a$ ) of integers and a sequence of $n$ arrays (choices), $a$ and each choice array are first broadcast, as necessary, to arrays of a common shape; calling these Ba and Bchoices $[i], i=0, \ldots, n-1$ we have that, necessarily, Ba.shape == Bchoices[i].shape for each $i$. Then, a new array with shape Ba . shape is created as follows:
-if mode=raise (the default), then, first of all, each element of $a$ (and thus $B a$ ) must be in the range $[0, n-1]$; now, suppose that $i$ (in that range) is the value at the ( $j 0, j 1, \ldots, j m$ ) position in $B a$ - then the value at the same position in the new array is the value in Bchoices $[i]$ at that same position;
-if mode=wrap, values in $a$ (and thus $B a$ ) may be any (signed) integer; modular arithmetic is used to map integers outside the range [ $0, n-1$ ] back into that range; and then the new array is constructed as above;
-if mode=clip, values in $a$ (and thus $B a$ ) may be any (signed) integer; negative integers are mapped to 0 ; values greater than $n-1$ are mapped to $n-1$; and then the new array is constructed as above.

## Parameters

a : int array
This array must contain integers in [0, n-1], where $n$ is the number of choices, unless mode=wrap or mode=clip, in which cases any integers are permissible.
choices : sequence of arrays
Choice arrays. $a$ and all of the choices must be broadcastable to the same shape. If choices is itself an array (not recommended), then its outermost dimension (i.e., the one corresponding to choices.shape [0]) is taken as defining the "sequence".
out : array, optional
If provided, the result will be inserted into this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise' (default), 'wrap', 'clip'\}, optional
Specifies how indices outside [ $0, n-1]$ will be treated:

- 'raise' : an exception is raised
- 'wrap' : value becomes value $\bmod n$
- 'clip' : values $<0$ are mapped to 0 , values $>\mathrm{n}-1$ are mapped to $\mathrm{n}-1$


## Returns

merged_array : array
The merged result.

## Raises

ValueError: shape mismatch :

If $a$ and each choice array are not all broadcastable to the same shape.

## See Also:

ndarray. choose
equivalent method

## Notes

To reduce the chance of misinterpretation, even though the following "abuse" is nominally supported, choices should neither be, nor be thought of as, a single array, i.e., the outermost sequence-like container should be either a list or a tuple.

## Examples

```
>>> choices = [[0, 1, 2, 3], [10, 11, 12, 13],
... [20, 21, 22, 23], [30, 31, 32, 33]]
>>> np.choose([2, 3, 1, 0], choices
... # the first element of the result will be the first element of the
... # third (2+1) "array" in choices, namely, 20; the second element
... # will be the second element of the fourth (3+1) choice array, i.e.,
... # 31, etc.
... )
array([20, 31, 12, 3])
>>> np.choose([2, 4, 1, 0], choices, mode='clip') # 4 goes to 3 (4-1)
array([20, 31, 12, 3])
>>> # because there are 4 choice arrays
>>> np.choose([2, 4, 1, 0], choices, mode='wrap') # 4 goes to (4 mod 4)
array([20, 1, 12, 3])
>>> # i.e., 0
```

A couple examples illustrating how choose broadcasts:

```
>>> a = [[1, 0, 1], [0, 1, 0], [1, 0, 1]]
>>> choices = [-10, 10]
>>> np.choose(a, choices)
array([[ 10, -10, 10],
    [-10, 10, -10],
    [ 10, -10, 10]])
>>> # With thanks to Anne Archibald
>>> a = np.array([0, 1]).reshape((2,1,1))
>>> c1 = np.array([1, 2, 3]).reshape((1,3,1))
>>> c2 = np.array([-1, -2, -3, -4, -5]).reshape((1, 1,5))
>>> np.choose(a, (c1, c2)) # result is 2x3x5, res[0,:,:]=c1, res[1,:,:]=c2
array([[[ 1, 1, 1, 1, 1],
    [ 2, 2, 2, 2, 2],
    [ 3, 3, 3, 3, 3]],
    [[l-1, -2, -3, -4, -5],
        [-1, -2, -3, -4, -5],
        [-1, -2, -3, -4, -5]]])
```

numpy.clip (a, a_min, a_max, out=None)
Clip (limit) the values in an array.
Given an interval, values outside the interval are clipped to the interval edges. For example, if an interval of $[0,1]$ is specified, values smaller than 0 become 0 , and values larger than 1 become 1 .

## Parameters

a : array_like

Array containing elements to clip.
a_min : scalar or array_like
Minimum value.
a_max : scalar or array_like
Maximum value. If $a \_$min or $a \_m a x$ are array_like, then they will be broadcasted to the shape of $a$.
out : ndarray, optional
The results will be placed in this array. It may be the input array for in-place clipping. out must be of the right shape to hold the output. Its type is preserved.

## Returns <br> clipped_array : ndarray

An array with the elements of $a$, but where values $<a_{-} \min$ are replaced with $a \_$min, and those $>a \_m a x$ with $a \_m a x$.

## See Also:

numpy.doc.ufuncs
Section "Output arguments"

## Examples

```
>>> a = np.arange(10)
>>> np.clip(a, 1, 8)
array([1, 1, 2, 3, 4, 5, 6, 7, 8, 8])
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, 3, 6, out=a)
array([3, 3, 3, 3, 4, 5, 6, 6, 6, 6])
>>> a = np.arange(10)
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, [3,4,1,1,1,4,4,4,4,4], 8)
array([3, 4, 2, 3, 4, 5, 6, 7, 8, 8])
```

numpy. compress (condition, a, axis=None, out=None)
Return selected slices of an array along given axis.
When working along a given axis, a slice along that axis is returned in output for each index where condition evaluates to True. When working on a 1-D array, compress is equivalent to extract.

## Parameters

condition : 1-D array of bools
Array that selects which entries to return. If len(condition) is less than the size of $a$ along the given axis, then output is truncated to the length of the condition array.
a : array_like
Array from which to extract a part.
axis : int, optional
Axis along which to take slices. If None (default), work on the flattened array.
out : ndarray, optional

Output array. Its type is preserved and it must be of the right shape to hold the output.

## Returns

compressed_array : ndarray
A copy of $a$ without the slices along axis for which condition is false.

## See Also:

take, choose, diag, diagonal, select
ndarray. compress
Equivalent method.
numpy.doc.ufuncs
Section "Output arguments"

## Examples

```
>>> a = np.array([[1, 2], [3, 4], [5, 6]])
>>> a
array([[1, 2],
    [3, 4],
    [5, 6]])
>>> np.compress([0, 1], a, axis=0)
array([[3, 4]])
>>> np.compress([False, True, True], a, axis=0)
array([[3, 4],
    [5, 6]])
>>> np.compress([False, True], a, axis=1)
array([[2],
    [4],
    [6]])
```

Working on the flattened array does not return slices along an axis but selects elements.

```
>>> np.compress([False, True], a)
array([2])
```

numpy. conj ( $x[$, out $]$ )
Return the complex conjugate, element-wise.
The complex conjugate of a complex number is obtained by changing the sign of its imaginary part.

## Parameters

$\mathbf{x}$ : array_like
Input value.

## Returns

$\mathbf{y}$ : ndarray
The complex conjugate of $x$, with same dtype as $y$.

## Examples

```
>>> np.conjugate(1+2j)
(1-2j)
>>> x = np.eye(2) + 1j * np.eye(2)
>>> np.conjugate(x)
array([[ 1.-1.j, 0.-0.j],
    [0.-0.j, 1.-1.j]])
```

numpy. copy (a)
Return an array copy of the given object.

## Parameters

a : array_like
Input data.

## Returns

arr : ndarray
Array interpretation of $a$.

## Notes

This is equivalent to

```
>>> np.array(a, copy=True)
```


## Examples

Create an array $x$, with a reference $y$ and a copy $z$ :

```
>>> x = np.array([1, 2, 3])
>>> y = x
>>> z = np.copy(x)
```

Note that, when we modify $x$, $y$ changes, but not $z$ :

```
>>> x[0] = 10
>>> x[0] == y[0]
True
>>> x[0] == z[0]
False
```

numpy. cumprod ( $a$, axis=None, dtype=None, out=None)
Return the cumulative product of elements along a given axis.

## Parameters

a: array_like
Input array.
axis : int, optional
Axis along which the cumulative product is computed. By default the input is flattened.
dtype : dtype, optional
Type of the returned array, as well as of the accumulator in which the elements are multiplied. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used instead.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type of the resulting values will be cast if necessary.

## Returns

cumprod : ndarray

A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## See Also:

numpy.doc.ufuncs
Section "Output arguments"

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> a = np.array([1,2,3])
>>> np.cumprod(a) # intermediate results 1, 1*2
... # total product 1*2*3 = 6
array([1, 2, 6])
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
>>> np.cumprod(a, dtype=float) # specify type of output
array([ 1., 2., 6., 24., 120., 720.])
```

The cumulative product for each column (i.e., over the rows) of $a$ :

```
>>> np.cumprod(a, axis=0)
array([[ 1, 2, 3],
    [ 4, 10, 18]])
```

The cumulative product for each row (i.e. over the columns) of $a$ :

```
>>> np.cumprod(a,axis=1)
array([[ 1, 2, 6],
    [ 4, 20, 120]])
```

numpy. cumsum ( $a$, axis=None, dtype $=$ None, out=None )
Return the cumulative sum of the elements along a given axis.

## Parameters

a : array_like
Input array.
axis : int, optional
Axis along which the cumulative sum is computed. The default (None) is to compute the cumsum over the flattened array.
dtype : dtype, optional
Type of the returned array and of the accumulator in which the elements are summed. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

cumsum_along_axis : ndarray.

A new array holding the result is returned unless out is specified, in which case a reference to out is returned. The result has the same size as $a$, and the same shape as $a$ if axis is not None or $a$ is a 1-d array.

## See Also:

sum
Sum array elements.
trapz
Integration of array values using the composite trapezoidal rule.

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> a
array([[1, 2, 3],
    [4, 5, 6]])
>>> np.cumsum(a)
array([ 1, 3, 6, 10, 15, 21])
>>> np.cumsum(a, dtype=float) # specifies type of output value(s)
array([ 1., 3., 6., 10., 15., 21.])
>>> np.cumsum(a,axis=0) # sum over rows for each of the 3 columns
array([[1, 2, 3],
    [5, 7, 9]])
>>> np.cumsum(a,axis=1) # sum over columns for each of the 2 rows
array([[ 1, 3, 6],
    [ 4, 9, 15]])
```

numpy.diagonal ( $a$, offset $=0$, axis $1=0$, axis $2=1$ )
Return specified diagonals.
If $a$ is 2-D, returns the diagonal of $a$ with the given offset, i.e., the collection of elements of the form a [i, i+offset]. If $a$ has more than two dimensions, then the axes specified by axisl and axis 2 are used to determine the 2-D sub-array whose diagonal is returned. The shape of the resulting array can be determined by removing axisl and axis 2 and appending an index to the right equal to the size of the resulting diagonals.

## Parameters

a : array_like
Array from which the diagonals are taken.
offset : int, optional
Offset of the diagonal from the main diagonal. Can be positive or negative. Defaults to main diagonal (0).
axis1 : int, optional
Axis to be used as the first axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults to first axis (0).
axis2 : int, optional
Axis to be used as the second axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults to second axis (1).

## Returns

array_of_diagonals : ndarray
If $a$ is 2-D, a 1-D array containing the diagonal is returned. If the dimension of $a$ is larger, then an array of diagonals is returned, "packed" from left-most dimension to right-most (e.g., if $a$ is 3-D, then the diagonals are "packed" along rows).

## Raises

## ValueError :

If the dimension of $a$ is less than 2 .

## See Also:

diag
MATLAB work-a-like for 1-D and 2-D arrays.
diagflat
Create diagonal arrays.

## trace

Sum along diagonals.

## Examples

```
>>> a = np.arange(4).reshape (2,2)
>>> a
array([[0, 1],
    [2, 3]])
>>> a.diagonal()
array([0, 3])
>>> a.diagonal(1)
array([1])
```

A 3-D example:

```
>>> a = np.arange(8).reshape (2,2,2); a
array([[[0, 1],
            [2, 3]],
    [[4, 5],
        [6, 7]]])
>>> a.diagonal(0, # Main diagonals of two arrays created by skipping
... 0, # across the outer(left)-most axis last and
... 1) # the "middle" (row) axis first.
array([[0, 6],
    [1, 7]])
```

The sub-arrays whose main diagonals we just obtained; note that each corresponds to fixing the right-most (column) axis, and that the diagonals are "packed" in rows.

```
>>> a[:,:,0] # main diagonal is [0 6]
array([[0, 2],
    [4, 6]])
>>> a[:,:,1] # main diagonal is [1 7]
array([[1, 3],
    [5, 7]])
```

numpy .mean ( $a$, axis=None, dtype=None, out=None)
Compute the arithmetic mean along the specified axis.

Returns the average of the array elements. The average is taken over the flattened array by default, otherwise over the specified axis. float64 intermediate and return values are used for integer inputs.

## Parameters

a : array_like
Array containing numbers whose mean is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the means are computed. The default is to compute the mean of the flattened array.
dtype : data-type, optional
Type to use in computing the mean. For integer inputs, the default is float64; for floating point inputs, it is the same as the input dtype.
out : ndarray, optional
Alternate output array in which to place the result. The default is None; if provided, it must have the same shape as the expected output, but the type will be cast if necessary. See doc.ufuncs for details.

## Returns

$\mathbf{m}$ : ndarray, see dtype parameter above
If out=None, returns a new array containing the mean values, otherwise a reference to the output array is returned.

## See Also:

average
Weighted average

## Notes

The arithmetic mean is the sum of the elements along the axis divided by the number of elements.
Note that for floating-point input, the mean is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-precision accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.mean(a)
2.5
>>> np.mean(a, axis=0)
array([ 2., 3.])
>>> np.mean(a, axis=1)
array([ 1.5, 3.5])
```

In single precision, mean can be inaccurate:

```
>>> a = np.zeros((2, 512*512), dtype=np.float 32)
>>> a[0, :] = 1.0
>>> a[1, :] = 0.1
>>> np.mean(a)
0.546875
```

Computing the mean in float64 is more accurate:

```
>>> np.mean(a, dtype=np.float 64)
0.55000000074505806
```

numpy. nonzero (a)

Return the indices of the elements that are non-zero.
Returns a tuple of arrays, one for each dimension of $a$, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

```
a[nonzero(a)]
```

To group the indices by element, rather than dimension, use:

```
transpose(nonzero(a))
```

The result of this is always a 2-D array, with a row for each non-zero element.

## Parameters

a : array_like
Input array.

## Returns

tuple_of_arrays : tuple
Indices of elements that are non-zero.

## See Also:

flatnonzero
Return indices that are non-zero in the flattened version of the input array.
ndarray.nonzero
Equivalent ndarray method.
count_nonzero
Counts the number of non-zero elements in the input array.

## Examples

```
>>> x = np.eye(3)
>>> x
array([[ 1., 0., 0.],
    [ 0., 1., 0.],
    [ 0., 0., 1.]])
>>> np.nonzero(x)
(array([0, 1, 2]), array([0, 1, 2]))
>>> x[np.nonzero(x)]
array([ 1., 1., 1.])
>>> np.transpose(np.nonzero(x))
array([[0, 0],
    [1, 1],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , np.nonzero( $a>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a = np.array([[1,2,3],[4,5,6],[7,8,9]])
>>> a > 3
array([[False, False, False],
    [ True, True, True],
    [ True, True, True]], dtype=bool)
>>> np.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the boolean array can also be called.

```
>>> (a > 3).nonzero()
```

(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
numpy $\cdot \operatorname{prod}(a$, axis=None, dtype=None, out=None)
Return the product of array elements over a given axis.

## Parameters

a : array_like
Input data.
axis : int, optional
Axis over which the product is taken. By default, the product of all elements is calculated.
dtype : data-type, optional
The data-type of the returned array, as well as of the accumulator in which the elements are multiplied. By default, if $a$ is of integer type, dtype is the default platform integer. (Note: if the type of $a$ is unsigned, then so is dtype.) Otherwise, the dtype is the same as that of $a$.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output, but the type of the output values will be cast if necessary.

## Returns

product_along_axis : ndarray, see dtype parameter above.
An array shaped as $a$ but with the specified axis removed. Returns a reference to out if specified.

## See Also:

ndarray.prod
equivalent method
numpy.doc.ufuncs Section "Output arguments"

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow. That means that, on a 32-bit platform:

```
>>> x = np.array([536870910, 536870910, 536870910, 536870910])
>>> np.prod(x) #random
16
```


## Examples

By default, calculate the product of all elements:

```
>>> np.prod([1.,2.])
2.0
```

Even when the input array is two-dimensional:

```
>>> np.prod([[1.,2.],[3.,4.]])
24.0
```

But we can also specify the axis over which to multiply:

```
>>> np.prod([[1.,2.],[3.,4.]], axis=1)
array([ 2., 12.])
```

If the type of $x$ is unsigned, then the output type is the unsigned platform integer:

```
>>> x = np.array([1, 2, 3], dtype=np.uint8)
>>> np.prod(x).dtype == np.uint
True
```

If $x$ is of a signed integer type, then the output type is the default platform integer:

```
>>> x = np.array([1, 2, 3], dtype=np.int8)
>>> np.prod(x).dtype == np.int
```

True
numpy.ptp ( $a$, axis=None, out=None)

Range of values (maximum - minimum) along an axis.
The name of the function comes from the acronym for 'peak to peak'.

## Parameters

a : array_like
Input values.
axis : int, optional
Axis along which to find the peaks. By default, flatten the array.
out : array_like
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output, but the type of the output values will be cast if necessary.

## Returns

ptp: ndarray
A new array holding the result, unless out was specified, in which case a reference to out is returned.

## Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
    [2, 3]])
>>> np.ptp(x, axis=0)
array([2, 2])
```

```
>>> np.ptp(x, axis=1)
array([1, 1])
```

numpy .put ( $a$, ind, $v$, mode $=$ 'raise')
Replaces specified elements of an array with given values.
The indexing works on the flattened target array. put is roughly equivalent to:

```
a.flat[ind] = v
```


## Parameters

a: ndarray
Target array.
ind : array_like
Target indices, interpreted as integers.
$\mathbf{v}$ : array_like
Values to place in $a$ at target indices. If $v$ is shorter than ind it will be repeated as necessary.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## See Also:

putmask, place

## Examples

```
>>> a = np.arange(5)
>>> np.put(a, [0, 2], [-44, -55])
>>> a
array([-44, 1, -55, 3, 4])
>>> a = np.arange(5)
>>> np.put(a, 22, -5, mode='clip')
>>> a
array([ 0, 1, 2, 3, -5])
```

numpy.ravel ( $a$, order=' $C^{\prime}$ )

Return a flattened array.
A 1-D array, containing the elements of the input, is returned. A copy is made only if needed.

## Parameters

a : array_like

Input array. The elements in a are read in the order specified by order, and packed as a 1-D array.
order : \{ 'C',' F ', ' A ', ' K ' \}, optional
The elements of a are read in this order. ' C ' means to view the elements in C (rowmajor) order. ' $F$ ' means to view the elements in Fortran (column-major) order. ' $A$ ' means to view the elements in ' F ' order if a is Fortran contiguous, ' C ' order otherwise. ' K ' means to view the elements in the order they occur in memory, except for reversing the data when strides are negative. By default, ' C ' order is used.

## Returns

1d_array : ndarray
Output of the same dtype as $a$, and of shape (a.size(), ).

## See Also:

ndarray.flat
1-D iterator over an array.
ndarray.flatten
1-D array copy of the elements of an array in row-major order.

## Notes

In row-major order, the row index varies the slowest, and the column index the quickest. This can be generalized to multiple dimensions, where row-major order implies that the index along the first axis varies slowest, and the index along the last quickest. The opposite holds for Fortran-, or column-major, mode.

## Examples

It is equivalent to reshape ( -1 , order=order).

```
>>> x = np.array([[1, 2, 3], [4, 5, 6]])
>>> print np.ravel(x)
[1 [12 3 4 5 5 6]
>>> print x.reshape(-1)
[1 [14 3 4 5 6]
>>> print np.ravel(x, order=' F')
[1 [4 2 5 5 3 6]
```

When order is ' A ', it will preserve the array's ' C ' or ' F ' ordering:

```
>>> print np.ravel(x.T)
[1 4 4 2 5 5 3 6]
>>> print np.ravel(x.T, order=' A')
[1 [12 3
```

When order is ' $K$ ', it will preserve orderings that are neither ' $C$ ' nor ' $F$ ', but won't reverse axes:

```
>>> a = np.arange(3) [::-1]; a
array([2, 1, 0])
>>> a.ravel(order=' C')
array([2, 1, 0])
>>> a.ravel(order=' K')
array([2, 1, 0])
```

```
>>> a = np.arange(12).reshape(2,3,2).swapaxes(1,2); a
array([[[ 0, 2, 4],
            [ 1, 3, 5]],
            [[ 6, 8, 10],
            [ 7, 9, 11]]])
>>> a.ravel(order='C')
array([ 0, 2, 4, 1, 3, 5, 6, 8, 10, 7, 9, 11])
>>> a.ravel(order=' K')
array([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11])
```

numpy. repeat (a, repeats, axis=None)
Repeat elements of an array.

## Parameters

a : array_like
Input array.
repeats: \{int, array of ints \}
The number of repetitions for each element. repeats is broadcasted to fit the shape of the given axis.
axis : int, optional
The axis along which to repeat values. By default, use the flattened input array, and return a flat output array.

## Returns

repeated_array : ndarray
Output array which has the same shape as $a$, except along the given axis.

## See Also:

tile
Tile an array.
Examples

```
>>> x = np.array([[1,2],[3,4]])
>>> np.repeat(x, 2)
array([1, 1, 2, 2, 3, 3, 4, 4])
>>> np.repeat(x, 3, axis=1)
array([[1, 1, 1, 2, 2, 2],
            [3, 3, 3, 4, 4, 4]])
>>> np.repeat(x, [1, 2], axis=0)
array([[1, 2],
    [3, 4],
            [3, 4]])
```

numpy. reshape ( $a$, newshape, order=' $C$ ')
Gives a new shape to an array without changing its data.

## Parameters

a : array_like
Array to be reshaped.
newshape : int or tuple of ints

The new shape should be compatible with the original shape. If an integer, then the result will be a 1-D array of that length. One shape dimension can be -1 . In this case, the value is inferred from the length of the array and remaining dimensions.
order : \{ ' C ', ' F ', ' $A$ ' \}, optional
Determines whether the array data should be viewed as in C (row-major) order, FORTRAN (column-major) order, or the C/FORTRAN order should be preserved.

## Returns

reshaped_array : ndarray
This will be a new view object if possible; otherwise, it will be a copy.

## See Also:

ndarray.reshape
Equivalent method.

## Notes

It is not always possible to change the shape of an array without copying the data. If you want an error to be raise if the data is copied, you should assign the new shape to the shape attribute of the array:

```
>>> a = np.zeros((10, 2))
# A transpose make the array non-contiguous
>>> b = a.T
# Taking a view makes it possible to modify the shape without modiying the
# initial object.
>>> c = b.view()
>>> c.shape = (20)
AttributeError: incompatible shape for a non-contiguous array
```


## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> np.reshape(a, 6)
array([1, 2, 3, 4, 5, 6])
>>> np.reshape(a, 6, order=' F')
array([1, 4, 2, 5, 3, 6])
>>> np.reshape(a, (3,-1)) # the unspecified value is inferred to be 2
array([[1, 2],
    [3, 4],
    [5, 6]])
```

numpy.resize (a, new_shape)
Return a new array with the specified shape.
If the new array is larger than the original array, then the new array is filled with repeated copies of $a$. Note that this behavior is different from a.resize(new_shape) which fills with zeros instead of repeated copies of $a$.

## Parameters

a : array_like
Array to be resized.
new_shape : int or tuple of int
Shape of resized array.

## Returns

reshaped_array : ndarray
The new array is formed from the data in the old array, repeated if necessary to fill out the required number of elements. The data are repeated in the order that they are stored in memory.

## See Also:

ndarray.resize
resize an array in-place.

## Examples

```
>>> a=np.array([[0,1],[2,3]])
>>> np.resize(a,(1,4))
array([[0, 1, 2, 3]])
>>> np.resize(a, (2,4))
array([[0, 1, 2, 3],
        [0, 1, 2, 3]])
```

numpy. searchsorted ( $a, v$, side $=$ 'left')

Find indices where elements should be inserted to maintain order.
Find the indices into a sorted array $a$ such that, if the corresponding elements in $v$ were inserted before the indices, the order of $a$ would be preserved.

## Parameters

a: 1-D array_like
Input array, sorted in ascending order.

$$
\mathbf{v} \text { : array_like }
$$

Values to insert into $a$.
side : \{'left', 'right' \}, optional
If 'left', the index of the first suitable location found is given. If 'right', return the last such index. If there is no suitable index, return either 0 or N (where N is the length of $a)$.

## Returns

indices : array of ints
Array of insertion points with the same shape as $v$.

## See Also:

sort
Return a sorted copy of an array.
histogram
Produce histogram from 1-D data.

## Notes

Binary search is used to find the required insertion points.
As of Numpy 1.4.0 searchsorted works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

```
>>> np.searchsorted([1,2,3,4,5], 3)
2
>>> np.searchsorted([1,2,3,4,5], 3, side='right')
3
>>> np.searchsorted([1,2,3,4,5], [-10, 10, 2, 3])
array([0, 5, 1, 2])
numpy.sort (a, axis=-1,kind='quicksort', order=None)
```

Return a sorted copy of an array.

## Parameters

a : array_like
Array to be sorted.
axis : int or None, optional
Axis along which to sort. If None, the array is flattened before sorting. The default is -1 , which sorts along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is a structured array, this argument specifies which fields to compare first, second, and so on. This list does not need to include all of the fields.

## Returns

sorted_array : ndarray
Array of the same type and shape as $a$.

## See Also:

ndarray.sort
Method to sort an array in-place.
argsort
Indirect sort.

## lexsort

Indirect stable sort on multiple keys.

## searchsorted

Find elements in a sorted array.

## Notes

The various sorting algorithms are characterized by their average speed, worst case performance, work space size, and whether they are stable. A stable sort keeps items with the same key in the same relative order. The three available algorithms have the following properties:

| kind | speed | worst case | work space | stable |
| :--- | :--- | :--- | :--- | :--- |
| 'quicksort' | 1 | $\mathrm{O}\left(\mathrm{n}^{\wedge} 2\right)$ | 0 | no |
| 'mergesort' | 2 | $\mathrm{O}\left(\mathrm{n}^{*} \log (\mathrm{n})\right)$ | $\sim \mathrm{n} / 2$ | yes |
| 'heapsort' | 3 | $\mathrm{O}(\mathrm{n} * \log (\mathrm{n}))$ | 0 | no |

All the sort algorithms make temporary copies of the data when sorting along any but the last axis. Consequently, sorting along the last axis is faster and uses less space than sorting along any other axis.

The sort order for complex numbers is lexicographic. If both the real and imaginary parts are non-nan then the order is determined by the real parts except when they are equal, in which case the order is determined by the imaginary parts.

Previous to numpy 1.4.0 sorting real and complex arrays containing nan values led to undefined behaviour. In numpy versions $>=1.4 .0$ nan values are sorted to the end. The extended sort order is:
-Real: [R, nan]
-Complex: [ $\mathrm{R}+\mathrm{Rj}, \mathrm{R}+$ nanj, nan +Rj , nan + nanj]
where R is a non-nan real value. Complex values with the same nan placements are sorted according to the non-nan part if it exists. Non-nan values are sorted as before.

## Examples

```
>>> a = np.array([[1,4],[3,1]])
>>> np.sort(a) # sort along the last axis
array([[1, 4],
    [1, 3]])
>>> np.sort(a, axis=None) # sort the flattened array
array([1, 1, 3, 4])
>>> np.sort(a, axis=0) # sort along the first axis
array([[1, 1],
    [3, 4]])
```

Use the order keyword to specify a field to use when sorting a structured array:

```
>>> dtype = [('name', 'S10'), ('height', float), ('age', int)]
>>> values = [('Arthur', 1.8, 41), ('Lancelot', 1.9, 38),
... ('Galahad', 1.7, 38)]
>>> a = np.array(values, dtype=dtype) # create a structured array
>>> np.sort(a, order='height')
array([('Galahad', 1.7, 38), ('Arthur', 1.8, 41),
    ('Lancelot', 1.89999999999999999, 38)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

Sort by age, then height if ages are equal:

```
>>> np.sort(a, order=['age', 'height'])
array([('Galahad', 1.7, 38), ('Lancelot', 1.8999999999999999, 38),
    ('Arthur', 1.8, 41)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

numpy.squeeze (a)
Remove single-dimensional entries from the shape of an array.

## Parameters

a : array_like
Input data.

## Returns

squeezed : ndarray
The input array, but with with all dimensions of length 1 removed. Whenever possible, a view on $a$ is returned.

## Examples

```
>>> x = np.array([[[0], [1], [2]]])
>>> x.shape
(1, 3, 1)
>>> np.squeeze(x).shape
(3,)
```

numpy.std $(a$, axis $=$ None, dtype $=$ None, out $=$ None,,$d d o f=0)$

Compute the standard deviation along the specified axis.
Returns the standard deviation, a measure of the spread of a distribution, of the array elements. The standard deviation is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Calculate the standard deviation of these values.
axis : int, optional
Axis along which the standard deviation is computed. The default is to compute the standard deviation of the flattened array.
dtype : dtype, optional
Type to use in computing the standard deviation. For arrays of integer type the default is float 64 , for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type (of the calculated values) will be cast if necessary.
ddof: int, optional
Means Delta Degrees of Freedom. The divisor used in calculations is N - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

standard_deviation : ndarray, see dtype parameter above.
If out is None, return a new array containing the standard deviation, otherwise return a reference to the output array.

## See Also:

var, mean
numpy.doc.ufuncs
Section "Output arguments"

## Notes

The standard deviation is the square root of the average of the squared deviations from the mean, i.e., std $=\operatorname{sqrt}($ mean (abs ( $\mathrm{x}-\mathrm{x}$.mean()) **2) ).
The average squared deviation is normally calculated as $\mathrm{x} . \operatorname{sum}() / \mathrm{N}$, where $\mathrm{N}=$ len(x). If, however, $d d o f$ is specified, the divisor N - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of the infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables. The standard deviation computed in this function is the square root of the estimated variance, so even with ddof $=1$, it will not be an unbiased estimate of the standard deviation per se.

Note that, for complex numbers, std takes the absolute value before squaring, so that the result is always real and nonnegative.

For floating-point input, the std is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.std(a)
1.1180339887498949
>>> np.std(a, axis=0)
array([ 1., 1.])
>>> np.std(a, axis=1)
array([ 0.5, 0.5])
```

In single precision, $\operatorname{std}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.std(a)
0.45172946707416706
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.std(a, dtype=np.float64)
0.44999999925552653
```

numpy. sum ( $a$, axis=None, dtype=None, out=None)
Sum of array elements over a given axis.

## Parameters

a : array_like
Elements to sum.
axis : integer, optional
Axis over which the sum is taken. By default axis is None, and all elements are summed.
dtype : dtype, optional
The type of the returned array and of the accumulator in which the elements are summed. By default, the dtype of $a$ is used. An exception is when $a$ has an integer type with less precision than the default platform integer. In that case, the default platform integer is used instead.
out : ndarray, optional
Array into which the output is placed. By default, a new array is created. If out is given, it must be of the appropriate shape (the shape of $a$ with axis removed, i.e., numpy.delete (a.shape, axis)). Its type is preserved. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

sum_along_axis : ndarray
An array with the same shape as $a$, with the specified axis removed. If $a$ is a $0-\mathrm{d}$ array, or if axis is None, a scalar is returned. If an output array is specified, a reference to out is returned.

## See Also:

ndarray.sum
Equivalent method.
cumsum
Cumulative sum of array elements.
trapz
Integration of array values using the composite trapezoidal rule.
mean, average

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> np.sum([0.5, 1.5])
2.0
>>> np.sum([0.5, 0.7, 0.2, 1.5], dtype=np.int32)
1
>>> np.sum([[0, 1], [0, 5]])
6
>>> np.sum([[0, 1], [0, 5]], axis=0)
array([0, 6])
>>> np.sum([[0, 1], [0, 5]], axis=1)
array([1, 5])
```

If the accumulator is too small, overflow occurs:

```
>>> np.ones(128, dtype=np.int8).sum(dtype=np.int8)
-128
```

numpy.swapaxes (a, axis1, axis2)

Interchange two axes of an array.

## Parameters

a : array_like
Input array.
axis1 : int
First axis.
axis2 : int
Second axis.

## Returns

a_swapped : ndarray
If $a$ is an ndarray, then a view of $a$ is returned; otherwise a new array is created.

## Examples

```
>>> x = np.array([[1,2,3]])
>>> np.swapaxes(x,0,1)
array([[1],
    [2],
        [3]])
```

```
>>> x = np.array([[[0,1],[2,3]],[[4,5],[6,7]]])
>>> x
array([[[0, 1],
    [2, 3]],
    [[4, 5],
        [6, 7]]])
>>> np.swapaxes(x,0,2)
array([[[0, 4],
        [2, 6]],
        [[1, 5],
        [3, 7]]])
```

numpy.take ( $a$, indices, axis=None, out=None, mode ='raise')

Take elements from an array along an axis.
This function does the same thing as "fancy" indexing (indexing arrays using arrays); however, it can be easier to use if you need elements along a given axis.

## Parameters

a : array_like
The source array.
indices : array_like
The indices of the values to extract.
axis : int, optional
The axis over which to select values. By default, the flattened input array is used.
out : ndarray, optional
If provided, the result will be placed in this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## Returns

subarray : ndarray
The returned array has the same type as $a$.

## See Also:

ndarray.take
equivalent method

## Examples

```
>>> a = [4, 3, 5, 7, 6, 8]
>>> indices = [0, 1, 4]
>>> np.take(a, indices)
array([4, 3, 6])
```

In this example if $a$ is an ndarray, "fancy" indexing can be used.

```
>>> a = np.array(a)
>>> a[indices]
array([4, 3, 6])
```

numpy.trace ( $a$, offset $=0$, axis $1=0$, axis $2=1$, dtype $=$ None, out $=$ None )
Return the sum along diagonals of the array.
If $a$ is 2 -D, the sum along its diagonal with the given offset is returned, i.e., the sum of elements a[i,i+offset] for all i.

If $a$ has more than two dimensions, then the axes specified by axis 1 and axis 2 are used to determine the 2-D sub-arrays whose traces are returned. The shape of the resulting array is the same as that of $a$ with axis1 and axis2 removed.

## Parameters

a : array_like
Input array, from which the diagonals are taken.
offset : int, optional
Offset of the diagonal from the main diagonal. Can be both positive and negative. Defaults to 0 .
axis1, axis2 : int, optional
Axes to be used as the first and second axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults are the first two axes of $a$.
dtype : dtype, optional
Determines the data-type of the returned array and of the accumulator where the elements are summed. If dtype has the value None and $a$ is of integer type of precision less than the default integer precision, then the default integer precision is used. Otherwise, the precision is the same as that of $a$.
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

sum_along_diagonals : ndarray
If $a$ is 2-D, the sum along the diagonal is returned. If $a$ has larger dimensions, then an array of sums along diagonals is returned.

## See Also:

diag, diagonal, diagflat

## Examples

```
>>> np.trace(np.eye(3))
3.0
>>> a = np.arange(8).reshape((2,2,2))
>>> np.trace(a)
array([6, 8])
>>> a = np.arange(24).reshape((2,2,2,3))
>>> np.trace(a).shape
(2, 3)
```

numpy.transpose (a, axes=None)
Permute the dimensions of an array.

## Parameters

a : array_like
Input array.
axes : list of ints, optional
By default, reverse the dimensions, otherwise permute the axes according to the values given.

## Returns

p: ndarray
$a$ with its axes permuted. A view is returned whenever possible.

## See Also:

```
rollaxis
```


## Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
        [2, 3]])
>>> np.transpose(x)
array([[0, 2],
            [1, 3]])
>>> x = np.ones((1, 2, 3))
>>> np.transpose(x, (1, 0, 2)).shape
(2, 1, 3)
```

numpy $\cdot \operatorname{var}(a$, axis $=$ None, dtype $=$ None, out $=$ None, $d d o f=0$ )

Compute the variance along the specified axis.
Returns the variance of the array elements, a measure of the spread of a distribution. The variance is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Array containing numbers whose variance is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the variance is computed. The default is to compute the variance of the flattened array.
dtype : data-type, optional
Type to use in computing the variance. For arrays of integer type the default is float32; for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output, but the type is cast if necessary.

## ddof : int, optional

"Delta Degrees of Freedom": the divisor used in the calculation is N - ddof, where N represents the number of elements. By default ddof is zero.

## Returns

variance : ndarray, see dtype parameter above
If out=None, returns a new array containing the variance; otherwise, a reference to the output array is returned.

```
See Also:
std
    Standard deviation
mean
    Average
numpy.doc.ufuncs
    Section "Output arguments"
```


## Notes

The variance is the average of the squared deviations from the mean, i.e., var $=$ mean $(a b s(x-$ $x . \operatorname{mean}()) * * 2$ ).

The mean is normally calculated as $x . \operatorname{sum}() / N$, where $N=$ len ( $x$ ). If, however, $d d o f$ is specified, the divisor $N$ - ddof is used instead. In standard statistical practice, ddof $=1$ provides an unbiased estimator of the variance of a hypothetical infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables.

Note that for complex numbers, the absolute value is taken before squaring, so that the result is always real and nonnegative.
For floating-point input, the variance is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1,2],[3,4]])
>>> np.var(a)
1.25
>>> np.var(a,0)
array([ 1., 1.])
>>> np.var(a,1)
array([ 0.25, 0.25])
```

In single precision, $\operatorname{var}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.var(a)
0.20405951142311096
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.var(a, dtype=np.float64)
0.20249999932997387
>>>((1-0.55)**2+(0.1-0.55)**2)/2
0.202500000000000001
```


### 1.5.6 Masked arrays (numpy .ma)

## See Also:

## Masked arrays

### 1.5.7 Standard container class

For backward compatibility and as a standard "container "class, the UserArray from Numeric has been brought over to NumPy and named numpy.lib.user_array.container The container class is a Python class whose self.array attribute is an ndarray. Multiple inheritance is probably easier with numpy.lib.user_array.container than with the ndarray itself and so it is included by default. It is not documented here beyond mentioning its existence because you are encouraged to use the ndarray class directly if you can.

```
numpy.lib.user_array.container(data[, ..])
```

class numpy.lib.user_array. container (data, dtype=None, copy=True)

### 1.5.8 Array Iterators

Iterators are a powerful concept for array processing. Essentially, iterators implement a generalized for-loop. If myiter is an iterator object, then the Python code:

```
for val in myiter:
    some code involving val
```

calls val = myiter. next () repeatedly until StopIteration is raised by the iterator. There are several ways to iterate over an array that may be useful: default iteration, flat iteration, and $N$-dimensional enumeration.

## Default iteration

The default iterator of an ndarray object is the default Python iterator of a sequence type. Thus, when the array object itself is used as an iterator. The default behavior is equivalent to:

```
for i in xrange(arr.shape[0]):
    val = arr[i]
```

This default iterator selects a sub-array of dimension $N-1$ from the array. This can be a useful construct for defining recursive algorithms. To loop over the entire array requires $N$ for-loops.

```
>>> a = arange(24).reshape (3,2,4)+10
>>> for val in a:
... print 'item:', val
item: [[10 11 12 13]
    [14 15 16 17]]
item: [[18 19 20 21]
    [22 23 24 25]]
item: [[\begin{array}{lll}{26}&{27}&{28}\\{29}\end{array}]
    [30 31 32 33]]
```


## Flat iteration

```
ndarray.flat A 1-D iterator over the array.
ndarray.flat
```

A 1-D iterator over the array.
This is a numpy.flatiter instance, which acts similarly to, but is not a subclass of, Python's built-in iterator object.

## See Also:

## flatten

Return a copy of the array collapsed into one dimension.
flatiter

## Examples

```
>>> x = np.arange(1, 7).reshape(2, 3)
>>> x
array([[1, 2, 3],
                    [4, 5, 6]])
>>> x.flat[3]
4
>>> x.T
array([[1, 4],
                    [2, 5],
                    [3, 6]])
>>> x.T.flat[3]
5
>>> type(x.flat)
<type 'numpy.flatiter'>
```

An assignment example:

```
>>> x.flat = 3; x
array([[3, 3, 3],
    [3, 3, 3]])
>>> x.flat[[1,4]] = 1; x
array([[3, 1, 3],
    [3, 1, 3]])
```

As mentioned previously, the flat attribute of ndarray objects returns an iterator that will cycle over the entire array in C-style contiguous order.

```
>>> for i, val in enumerate(a.flat):
... if i%5 == 0: print i, val
0 10
5 15
10 20
15 25
20 30
```

Here, I've used the built-in enumerate iterator to return the iterator index as well as the value.

## N -dimensional enumeration

```
ndenumerate(arr) Multidimensional index iterator.
```

class numpy . ndenumerate (arr)
Multidimensional index iterator.
Return an iterator yielding pairs of array coordinates and values.

## Parameters

a : ndarray
Input array.
See Also:

```
ndindex, flatiter
```


## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> for index, x in np.ndenumerate(a):
... print index, x
(0, 0) 1
(0, 1) 2
(1, 0) 3
(1, 1) 4
```


## Methods

next

Sometimes it may be useful to get the N -dimensional index while iterating. The ndenumerate iterator can achieve this.

```
>>> for i, val in ndenumerate(a):
... if sum(i)%5 == 0: print i, val
(0, 0, 0) 10
(1, 1, 3) 25
(2, 0, 3) 29
(2, 1, 2) 32
```


## Iterator for broadcasting

broadcast Produce an object that mimics broadcasting.
class numpy.broadcast
Produce an object that mimics broadcasting.

## Parameters

in1, in2, ... : array_like
Input parameters.

## Returns

b : broadcast object
Broadcast the input parameters against one another, and return an object that encapsulates the result. Amongst others, it has shape and nd properties, and may be used as an iterator.

## Examples

Manually adding two vectors, using broadcasting:

```
>>> x = np.array([[1], [2], [3]])
>>> y = np.array([4, 5, 6])
>>> b = np.broadcast(x, y)
>>> out = np.empty(b.shape)
>>> out.flat = [u+v for (u,v) in b]
>>> out
array([[ 5., 6., 7.],
    [ 6., 7., 8.],
    [ 7., 8., 9.]])
```

Compare against built-in broadcasting:

```
>>> x + y
array([[5, 6, 7],
    [6, 7, 8],
    [7, 8, 9]])
```


## Methods

next
reset

The general concept of broadcasting is also available from Python using the broadcast iterator. This object takes $N$ objects as inputs and returns an iterator that returns tuples providing each of the input sequence elements in the broadcasted result.

```
>>> for val in broadcast([[1,0],[2,3]],[0,1]):
    print val
(1, 0)
(0, 1)
(2, 0)
(3, 1)
```


### 1.6 Masked arrays

Masked arrays are arrays that may have missing or invalid entries. The numpy . ma module provides a nearly workalike replacement for numpy that supports data arrays with masks.

### 1.6.1 The numpy .ma module

## Rationale

Masked arrays are arrays that may have missing or invalid entries. The numpy . ma module provides a nearly workalike replacement for numpy that supports data arrays with masks.

## What is a masked array?

In many circumstances, datasets can be incomplete or tainted by the presence of invalid data. For example, a sensor may have failed to record a data, or recorded an invalid value. The numpy . ma module provides a convenient way to address this issue, by introducing masked arrays.

A masked array is the combination of a standard numpy. ndarray and a mask. A mask is either nomask, indicating that no value of the associated array is invalid, or an array of booleans that determines for each element of the associated array whether the value is valid or not. When an element of the mask is False, the corresponding element of the associated array is valid and is said to be unmasked. When an element of the mask is True, the corresponding element of the associated array is said to be masked (invalid).

The package ensures that masked entries are not used in computations.
As an illustration, let's consider the following dataset:

```
>>> import numpy as np
>>> import numpy.ma as ma
>>> x = np.array ([1, 2, 3, -1, 5])
```

We wish to mark the fourth entry as invalid. The easiest is to create a masked array:

```
>>> mx = ma.masked_array(x, mask=[0, 0, 0, 1, 0])
```

We can now compute the mean of the dataset, without taking the invalid data into account:

```
>>> mx.mean()
2.75
```


## The numpy .ma module

The main feature of the numpy.ma module is the MaskedArray class, which is a subclass of numpy.ndarray. The class, its attributes and methods are described in more details in the MaskedArray class section.

The numpy . ma module can be used as an addition to numpy:

```
>>> import numpy as np
>>> import numpy.ma as ma
```

To create an array with the second element invalid, we would do:

```
>>> y = ma.array([1, 2, 3], mask = [0, 1, 0])
```

To create a masked array where all values close to $1 . \mathrm{e} 20$ are invalid, we would do:

```
>>> z = masked_values([1.0, 1.e20, 3.0, 4.0], 1.e20)
```

For a complete discussion of creation methods for masked arrays please see section Constructing masked arrays.

### 1.6.2 Using numpy.ma

## Constructing masked arrays

There are several ways to construct a masked array.

- A first possibility is to directly invoke the MaskedArray class.
- A second possibility is to use the two masked array constructors, array and masked_array.
array(data[, dtype, copy, order, mask, ...]) An array class with possibly masked values. masked_array An array class with possibly masked values.
numpy.ma.array (data, dtype=None, copy=False, order=False, mask=False, fill_value=None, keep_mask=True, hard_mask=False, shrink=True, subok=True, ndmin=0)
An array class with possibly masked values.
Masked values of True exclude the corresponding element from any computation.
Construction:

```
x = MaskedArray(data, mask=nomask, dtype=None,
    copy=False, subok=True, ndmin=0, fill_value=None,
    keep_mask=True, hard_mask=None, shrink=True)
```


## Parameters

data : array_like
Input data.
mask : sequence, optional
Mask. Must be convertible to an array of booleans with the same shape as data. True indicates a masked (i.e. invalid) data.
dtype : dtype, optional
Data type of the output. If dtype is None, the type of the data argument (data.dt ype) is used. If dtype is not None and different from data.dt ype, a copy is performed.
copy : bool, optional
Whether to copy the input data (True), or to use a reference instead. Default is False.
subok : bool, optional
Whether to return a subclass of MaskedArray if possible (True) or a plain MaskedArray. Default is True.
ndmin : int, optional
Minimum number of dimensions. Default is 0 .
fill_value : scalar, optional
Value used to fill in the masked values when necessary. If None, a default based on the data-type is used.
keep_mask : bool, optional
Whether to combine mask with the mask of the input data, if any (True), or to use only mask for the output (False). Default is True.
hard_mask : bool, optional

Whether to use a hard mask or not. With a hard mask, masked values cannot be unmasked. Default is False.
shrink : bool, optional
Whether to force compression of an empty mask. Default is True.
numpy.ma.masked_array
alias of MaskedArray

- A third option is to take the view of an existing array. In that case, the mask of the view is set to nomask if the array has no named fields, or an array of boolean with the same structure as the array otherwise.

```
>>> x = np.array([1, 2, 3])
>>> x.view(ma.MaskedArray)
masked_array(data = [1 2 3],
            mask = False,
    fill_value = 999999)
>>> x = np.array([(1, 1.), (2, 2.)], dtype=[('a',int), ('b', float)])
>>> x.view(ma.MaskedArray)
masked_array(data = [(1, 1.0) (2, 2.0)],
            mask = [(False, False) (False, False)],
    fill_value = (999999, 1e+20),
        dtype = [('a', '<i4'), ('b', '<f8')])
```

- Yet another possibility is to use any of the following functions:

```
asarray(a[, dtype, order]) Convert the input to a masked array of the given data-type.
asanyarray(a[, dtype]) Convert the input to a masked array, conserving subclasses
fix_invalid(a[, mask, copy, fill_value]) Return input with invalid data masked and replaced by a fill
    value.
masked_equal(x, value[, copy]) Mask an array where equal to a given value.
masked_greater(x, value[, copy]) Mask an array where greater than a given value.
masked_greater_equal(x, value[, Mask an array where greater than or equal to a given value.
copy])
masked_inside(x, v1, v2[, copy]) Mask an array inside a given interval.
masked_invalid(a[, copy]) Mask an array where invalid values occur (NaNs or infs).
masked_less(x, value[, copy]) Mask an array where less than a given value.
masked_less_equal(x, value[, copy]) Mask an array where less than or equal to a given value.
masked_not_equal(x, value[, copy]) Mask an array where not equal to a given value.
masked_object(x, value[, copy, shrink]) Mask the array }x\mathrm{ where the data are exactly equal to value.
masked_outside(x, v1, v2[, copy]) Mask an array outside a given interval.
masked_values(x, value[, rtol, atol, Mask using floating point equality.
copy, ...])
masked_where(condition, a[, copy]) Mask an array where a condition is met.
```

numpy.ma. asarray ( $a$, dtype $=$ None, order=None)

Convert the input to a masked array of the given data-type.
No copy is performed if the input is already an ndarray. If $a$ is a subclass of MaskedArray, a base class MaskedArray is returned.

## Parameters

a : array_like
Input data, in any form that can be converted to a masked array. This includes lists, lists of tuples, tuples, tuples of tuples, tuples of lists, ndarrays and masked arrays.
dtype : dtype, optional

By default, the data-type is inferred from the input data.
order : \{ 'C', 'F' \}, optional
Whether to use row-major ('C') or column-major ('FORTRAN') memory representation. Default is ' C '.

## Returns

out : MaskedArray
Masked array interpretation of $a$.

## See Also:

asanyarray
Similar to asarray, but conserves subclasses.

## Examples

```
>>> x = np.arange(10.).reshape(2, 5)
>>> x
array([[ 0., 1., 2., 3., 4.],
            [ 5., 6., 7., 8., 9.]])
>>> np.ma.asarray(x)
masked_array(data =
    [[ 0. 1. 2. 3. 4.]
    [ 5. 6. 7. 8. 9.]],
                            mask =
    False,
            fill_value = 1e+20)
>>> type(np.ma.asarray(x))
<class 'numpy.ma.core.MaskedArray'>
```

numpy.ma.asanyarray (a,dtype=None)
Convert the input to a masked array, conserving subclasses.
If $a$ is a subclass of MaskedArray, its class is conserved. No copy is performed if the input is already an ndarray.

## Parameters

a : array_like
Input data, in any form that can be converted to an array.
dtype : dtype, optional
By default, the data-type is inferred from the input data.
order : \{ 'C', 'F'\}, optional
Whether to use row-major ('C') or column-major ('FORTRAN') memory representation. Default is ' C '.

## Returns

out : MaskedArray
MaskedArray interpretation of $a$.

## See Also:

asarray
Similar to asanyarray, but does not conserve subclass.

## Examples

```
>>> x = np.arange(10.).reshape(2, 5)
>>> x
array([[ 0., 1., 2., 3., 4.],
    [ 5., 6., 7., 8., 9.]])
>>> np.ma.asanyarray(x)
masked_array(data =
    [[ 0. 1. 2. 3. 4.]
    [ 5. 6. 7. 8. 9.]],
                mask =
    False,
            fill_value = 1e+20)
>>> type(np.ma.asanyarray(x))
<class 'numpy.ma.core.MaskedArray'>
```

numpy.ma.fix_invalid(a, mask=False, copy=True, fill_value=None)
Return input with invalid data masked and replaced by a fill value.
Invalid data means values of nan, inf, etc.

## Parameters

a : array_like
Input array, a (subclass of) ndarray.
copy : bool, optional
Whether to use a copy of $a$ (True) or to fix $a$ in place (False). Default is True.
fill_value : scalar, optional
Value used for fixing invalid data. Default is None, in which case the a.fill_value is used.

## Returns

b : MaskedArray
The input array with invalid entries fixed.

## Notes

A copy is performed by default.

## Examples

```
>>> x = np.ma.array([1., -1, np.nan, np.inf], mask=[1] + [0]*3)
>>> x
masked_array(data = [-- -1.0 nan inf],
            mask = [ True False False False],
    fill_value = 1e+20)
>>> np.ma.fix_invalid(x)
masked_array(data = [-- -1.0 -- --],
            mask = [ True False True True],
    fill_value = 1e+20)
>>> fixed = np.ma.fix_invalid(x)
>>> fixed.data
array([ 1.00000000e+00, -1.00000000e+00, 1.00000000ee+20,
        1.00000000e+20])
>>> x.data
array([ 1., -1., NaN, Inf])
```

numpy.ma.masked_equal ( $x$, value, copy=True)
Mask an array where equal to a given value.
This function is a shortcut to masked_where, with condition $=(x==$ value $)$. For floating point arrays, consider using masked_values (x, value).

## See Also:

masked_where Mask where a condition is met.
masked_values
Mask using floating point equality.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_equal(a, 2)
masked_array(data = [0 1 -- 3],
            mask = [False False True False],
            fill_value=999999)
```

numpy.ma.masked_greater ( $x$, value, copy=True)
Mask an array where greater than a given value.
This function is a shortcut to masked_where, with condition $=(x>$ value $)$.
See Also:
masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_greater(a, 2)
masked_array(data = [0 1 2 --],
            mask = [False False False True],
            fill_value=999999)
```

numpy.ma.masked_greater_equal ( $x$, value, copy=True)
Mask an array where greater than or equal to a given value.
This function is a shortcut to masked_where, with condition $=(x>=$ value $)$.
See Also:
masked_where
Mask where a condition is met.
Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_greater_equal(a, 2)
masked_array(data = [0 1 -- -- ],
    mask = [False False True True],
        fill_value=999999)
```

numpy.ma.masked_inside ( $x, v 1, v 2$, copy=True)

Mask an array inside a given interval.
Shortcut to masked_where, where condition is True for $x$ inside the interval [v1,v2] (v1 <= $\mathrm{x}<=\mathrm{v} 2$ ). The boundaries $v 1$ and $v 2$ can be given in either order.

## See Also:

## masked_where

Mask where a condition is met.

## Notes

The array $x$ is prefilled with its filling value.

## Examples

```
>>> import numpy.ma as ma
>> x = [0.31, 1.2, 0.01, 0.2, -0.4, -1.1]
>>> ma.masked_inside(x, -0.3, 0.3)
masked_array(data = [0.31 1.2 -- -- -0.4 -1.1],
    mask = [False False True True False False],
        fill_value=1e+20)
```

The order of $v 1$ and $v 2$ doesn't matter.

```
>>> ma.masked_inside(x, 0.3, -0.3)
masked_array(data = [0.31 1.2 -- -- -0.4 -1.1],
    mask = [False False True True False False],
    fill_value=1e+20)
```

numpy.ma.masked_invalid (a, copy=True)
Mask an array where invalid values occur (NaNs or infs).
This function is a shortcut to masked_where, with condition $=\sim($ np.isfinite(a)). Any pre-existing mask is conserved. Only applies to arrays with a dtype where NaNs or infs make sense (i.e. floating point types), but accepts any array_like object.

## See Also:

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(5, dtype=np.float)
>>> a[2] = np.NaN
>>> a[3] = np.PINF
>>> a
```

```
array([ 0., 1., NaN, Inf, 4.])
>>> ma.masked_invalid(a)
masked_array(data = [0.0 1.0 -- -- 4.0],
    mask = [False False True True False],
    fill_value=1e+20)
```

numpy.ma.masked_less ( $x$, value, copy=True)
Mask an array where less than a given value.
This function is a shortcut to masked_where, with condition $=(\mathrm{x}<$ value $)$.

## See Also:

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_less(a, 2)
masked_array(data = [-- -- 2 3],
    mask = [ True True False False],
        fill_value=999999)
```

numpy.ma.masked_less_equal ( $x$, value, copy=True)
Mask an array where less than or equal to a given value.
This function is a shortcut to masked_where, with condition $=(\mathrm{x}<=$ value $)$.
See Also:
masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_less_equal(a, 2)
masked_array(data = [-- -- -- 3],
    mask = [ True True True False],
    fill_value=999999)
```

numpy.ma.masked_not_equal ( $x$, value, copy=True)

Mask an array where not equal to a given value.
This function is a shortcut to masked_where, with condition $=(x!=$ value $)$.

## See Also:

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_not_equal(a, 2)
masked_array(data = [-- -- 2 --],
    mask = [ True True False True],
    fill_value=999999)
```

numpy.ma.masked_object ( $x$, value, copy=True, shrink=True)
Mask the array $x$ where the data are exactly equal to value.
This function is similar to masked_values, but only suitable for object arrays: for floating point, use masked_values instead.

## Parameters

$\mathbf{x}$ : array_like
Array to mask
value : object
Comparison value
copy : \{True, False \}, optional
Whether to return a copy of $x$.
shrink: \{True, False \}, optional
Whether to collapse a mask full of False to nomask

## Returns

result : MaskedArray
The result of masking $x$ where equal to value.

## See Also:

masked_where
Mask where a condition is met.
masked_equal
Mask where equal to a given value (integers).
masked_values
Mask using floating point equality.

## Examples

```
>>> import numpy.ma as ma
>>> food = np.array(['green_eggs', 'ham'], dtype=object)
>>> # don't eat spoiled food
>>> eat = ma.masked_object(food, 'green_eggs')
>>> print eat
[-- ham]
>>> # plain ol' ham is boring
>>> fresh_food = np.array(['cheese', 'ham', 'pineapple'], dtype=object)
>>> eat = ma.masked_object(fresh_food, 'green_eggs')
>>> print eat
[cheese ham pineapple]
```

Note that mask is set to nomask if possible.

```
>>> eat
masked_array(data = [cheese ham pineapple],
    mask = False,
    fill_value=?)
```

numpy.ma.masked_outside ( $x, v 1, v 2$, copy $=$ True)
Mask an array outside a given interval.
Shortcut to masked_where, where condition is True for $x$ outside the interval $[\mathrm{v} 1, \mathrm{v} 2](\mathrm{x}<\mathrm{v} 1) \mid(\mathrm{x}>\mathrm{v} 2)$. The boundaries $v 1$ and $v 2$ can be given in either order.
See Also:
masked_where
Mask where a condition is met.

## Notes

The array $x$ is prefilled with its filling value.

## Examples

```
>>> import numpy.ma as ma
>>> x = [0.31, 1.2, 0.01, 0.2, -0.4, -1.1]
>>> ma.masked_outside(x, -0.3, 0.3)
masked_array(data = [-- -- 0.01 0.2 -- --],
        mask = [ True True False False True True],
        fill_value=1e+20)
```

The order of $v 1$ and $v 2$ doesn't matter.

```
>>> ma.masked_outside(x, 0.3, -0.3)
masked_array(data = [-- -- 0.01 0.2 -- --],
    mask = [ True True False False True True],
    fill_value=1e+20)
```

numpy.ma.masked_values $(x$, value, rtol=1.00000000000000001e-05, atol=1e-08, copy=True,
shrink=True)

Mask using floating point equality.
Return a MaskedArray, masked where the data in array $x$ are approximately equal to value, i.e. where the following condition is True
(abs(x - value) <= atol+rtol*abs(value))
The fill_value is set to value and the mask is set to nomask if possible. For integers, consider using masked_equal.

## Parameters

$\mathbf{x}$ : array_like
Array to mask.
value : float
Masking value.
rtol : float, optional
Tolerance parameter.
atol : float, optional

Tolerance parameter (1e-8).
copy : bool, optional
Whether to return a copy of $x$.
shrink : bool, optional
Whether to collapse a mask full of False to nomask.

## Returns

 result : MaskedArrayThe result of masking $x$ where approximately equal to value.

## See Also:

masked_where
Mask where a condition is met.
masked_equal
Mask where equal to a given value (integers).

## Examples

```
>>> import numpy.ma as ma
>>> x = np.array([1, 1.1, 2, 1.1, 3])
>>> ma.masked_values(x, 1.1)
masked_array(data = [1.0 -- 2.0 -- 3.0],
    mask = [False True False True False],
    fill_value=1.1)
```

Note that mask is set to nomask if possible.

```
>>> ma.masked_values(x, 1.5)
masked_array(data = [ 1. 1.1 2. 1.1 3. ],
    mask = False,
    fill_value=1.5)
```

For integers, the fill value will be different in general to the result of masked_equal.

```
>>> x = np.arange(5)
>>> x
array([0, 1, 2, 3, 4])
>>> ma.masked_values(x, 2)
masked_array(data = [0 1 -- 3 4],
        mask = [False False True False False],
        fill_value=2)
>>> ma.masked_equal(x, 2)
masked_array(data = [0 1 -- 3 4],
        mask = [False False True False False],
        fill_value=999999)
```

numpy.ma.masked_where (condition, $a$, copy=True)
Mask an array where a condition is met.
Return $a$ as an array masked where condition is True. Any masked values of $a$ or condition are also masked in the output.

```
Parameters
    condition : array_like
```

Masking condition. When condition tests floating point values for equality, consider using masked_values instead.
a : array_like
Array to mask.
copy : bool
If True (default) make a copy of $a$ in the result. If False modify $a$ in place and return a view.

## Returns

result : MaskedArray
The result of masking $a$ where condition is True.

## See Also:

```
masked_values
```

Mask using floating point equality.
masked_equal
Mask where equal to a given value.
masked_not_equal
Mask where not equal to a given value.
masked_less_equal
Mask where less than or equal to a given value.
masked_greater_equal
Mask where greater than or equal to a given value.
masked_less
Mask where less than a given value.
masked_greater
Mask where greater than a given value.
masked_inside
Mask inside a given interval.
masked_outside
Mask outside a given interval.
masked_invalid
Mask invalid values ( NaNs or infs).

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_where(a <= 2, a)
masked_array(data = [-- -- -- 3],
    mask = [ True True True False],
    fill_value=999999)
```

Mask array $b$ conditional on $a$.

```
>>> b = ['a', 'b', 'c', 'd']
>>> ma.masked_where(a == 2, b)
masked_array(data = [a b -- d],
    mask = [False False True False],
    fill_value=N/A)
```

Effect of the copy argument.

```
>>> c = ma.masked_where(a <= 2, a)
>>> c
masked_array(data = [-- -- -- 3],
    mask = [ True True True False],
    fill_value=999999)
>>> c[0] = 99
>>> c
masked_array(data = [99 -- -- 3],
    mask = [False True True False],
    fill_value=999999)
>>> a
array([0, 1, 2, 3])
>>> c = ma.masked_where(a <= 2, a, copy=False)
>>> c[0] = 99
>>> c
masked_array(data = [99 -- -- 3],
    mask = [False True True False],
    fill_value=999999)
>>> a
array([99, 1, 2, 3])
```

When condition or $a$ contain masked values.

```
>>> a = np.arange(4)
>>> a = ma.masked_where(a == 2, a)
>>> a
masked_array(data = [0 1 -- 3],
    mask = [False False True False],
    fill_value=999999)
>>> b = np.arange(4)
>>> b = ma.masked_where(b == 0, b)
>>> b
masked_array(data = [-- 1 2 3],
    mask = [ True False False False],
    fill_value=999999)
>>> ma.masked_where(a == 3, b)
masked_array(data = [-- 1 -- --],
    mask = [ True False True True],
    fill_value=999999)
```


## Accessing the data

The underlying data of a masked array can be accessed in several ways:

- through the data attribute. The output is a view of the array as a numpy. ndarray or one of its subclasses, depending on the type of the underlying data at the masked array creation.
- through the __array __ method. The output is then a numpy . ndarray.
- by directly taking a view of the masked array as a numpy . ndarray or one of its subclass (which is actually what using the data attribute does).
- by using the getdat a function.

None of these methods is completely satisfactory if some entries have been marked as invalid. As a general rule, where a representation of the array is required without any masked entries, it is recommended to fill the array with the filled method.

## Accessing the mask

The mask of a masked array is accessible through its mask attribute. We must keep in mind that a True entry in the mask indicates an invalid data.

Another possibility is to use the getmask and getmaskarray functions. getmask (x) outputs the mask of $x$ if $x$ is a masked array, and the special value nomask otherwise. getmaskarray ( $x$ ) outputs the mask of $x$ if $x$ is a masked array. If $x$ has no invalid entry or is not a masked array, the function outputs a boolean array of False with as many elements as x .

## Accessing only the valid entries

To retrieve only the valid entries, we can use the inverse of the mask as an index. The inverse of the mask can be calculated with the numpy.logical_not function or simply with the $\sim$ operator:

```
>>> x = ma.array([[1, 2], [3, 4]], mask=[[0, 1], [1, 0]])
>>> x[~x.mask]
masked_array(data = [1 4],
    mask = [False False],
    fill_value = 999999)
```

Another way to retrieve the valid data is to use the compressed method, which returns a one-dimensional ndarray (or one of its subclasses, depending on the value of the baseclass attribute):

```
>>> x.compressed()
array([1, 4])
```

Note that the output of compressed is always 1D.

## Modifying the mask

## Masking an entry

The recommended way to mark one or several specific entries of a masked array as invalid is to assign the special value masked to them:

```
>>> x = ma.array([1, 2, 3])
>>> x[0] = ma.masked
>>> x
masked_array(data = [-- 2 3],
            mask = [ True False False],
            fill_value = 999999)
>>> y = ma.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
>>> y[(0, 1, 2), (1, 2, 0)] = ma.masked
>>> y
masked_array(data =
    [[1 -- 3]
    [4 5 -- ]
    [-- 8 9]],
                                    mask =
```

```
[[False True False]
    [False False True]
    [ True False False]],
            fill_value = 999999)
>>> z = ma.array([1, 2, 3, 4])
>>> z[:-2] = ma.masked
>>> z
masked_array(data = [-- -- 3 4],
    mask = [ True True False False],
    fill_value = 999999)
```

A second possibility is to modify the mask directly, but this usage is discouraged.
Note: When creating a new masked array with a simple, non-structured datatype, the mask is initially set to the special value nomask, that corresponds roughly to the boolean False. Trying to set an element of nomask will fail with a TypeError exception, as a boolean does not support item assignment.

All the entries of an array can be masked at once by assigning True to the mask:

```
>>> x = ma.array([1, 2, 3], mask=[0, 0, 1])
>>> x.mask = True
>>> x
masked_array(data = [-- -- --],
    mask = [ True True True],
    fill_value = 999999)
```

Finally, specific entries can be masked and/or unmasked by assigning to the mask a sequence of booleans:

```
>>> x = ma.array([1, 2, 3])
>>> x.mask = [0, 1, 0]
>>> x
masked_array(data = [1 -- 3],
    mask = [False True False],
    fill_value = 999999)
```


## Unmasking an entry

To unmask one or several specific entries, we can just assign one or several new valid values to them:

```
>>> x = ma.array([1, 2, 3], mask=[0, 0, 1])
>>> x
masked_array(data = [1 2 -- ],
    mask = [False False True],
    fill_value = 999999)
>>> x[-1] = 5
>>> x
masked_array(data = [ll 2 5}]\mathrm{ [,
    mask = [False False False],
    fill_value = 999999)
```

Note: Unmasking an entry by direct assignment will silently fail if the masked array has a hard mask, as shown by the hardmask attribute. This feature was introduced to prevent overwriting the mask. To force the unmasking of an entry where the array has a hard mask, the mask must first to be softened using the soften_mask method before the allocation. It can be re-hardened with harden_mask:

```
>>> x = ma.array([1, 2, 3], mask=[0, 0, 1], hard_mask=True)
>>> x
masked_array(data = [1 2 -- ] ],
    mask = [False False True],
    fill_value = 999999)
```

```
>>>x[-1]=5
>>> x
masked_array(data = [1 2 -- ] ],
    mask = [False False True],
    fill_value = 999999)
>>> x.soften_mask()
>>> x[-1] = 5
>>> x
masked_array(data = [ll 2 5}]|
    mask = [False False False],
    fill_value = 999999)
>>> x.harden_mask()
```

To unmask all masked entries of a masked array (provided the mask isn't a hard mask), the simplest solution is to assign the constant nomask to the mask:

```
>>> x = ma.array([1, 2, 3], mask=[0, 0, 1])
>>> x
masked_array(data = [1 2 -- ] ],
    mask = [False False True],
    fill_value = 999999)
>>> x.mask = ma.nomask
>>> x
masked_array(data = [llll}12\mp@code{3}]
    mask = [False False False],
    fill_value = 999999)
```


## Indexing and slicing

As a MaskedArray is a subclass of numpy. ndarray, it inherits its mechanisms for indexing and slicing.
When accessing a single entry of a masked array with no named fields, the output is either a scalar (if the corresponding entry of the mask is False) or the special value masked (if the corresponding entry of the mask is True):

```
>>> x = ma.array([1, 2, 3], mask=[0, 0, 1])
>>> x[0]
1
>>> x[-1]
masked_array(data = --,
    mask = True,
    fill_value = 1e+20)
>>> x[-1] is ma.masked
True
```

If the masked array has named fields, accessing a single entry returns a numpy. void object if none of the fields are masked, or a 0d masked array with the same dtype as the initial array if at least one of the fields is masked.

```
>>> y = ma.masked_array([(1,2), (3, 4)],
... mask=[(0, 0), (0, 1)],
... dtype=[('a', int), ('b', int)])
>>> y[0]
(1, 2)
>>> y[-1]
masked_array(data = (3, --),
    mask = (False, True),
    fill_value = (999999, 999999),
    dtype = [('a', '<i4'), ('b', '<i4')])
```

When accessing a slice, the output is a masked array whose dat a attribute is a view of the original data, and whose mask is either nomask (if there was no invalid entries in the original array) or a copy of the corresponding slice of the original mask. The copy is required to avoid propagation of any modification of the mask to the original.

```
>>> x = ma.array([1, 2, 3, 4, 5], mask=[0, 1, 0, 0, 1])
>>> mx = x[:3]
>>> mx
masked_array(data = [1 -- 3],
    mask = [False True False],
    fill_value = 999999)
>>> mx[1] = -1
>>> mx
masked_array(data = [1 -1 3],
            mask = [False True False],
    fill_value = 999999)
>>> x.mask
array([False, True, False, False, True], dtype=bool)
>>> x.data
array([ 1, -1, 3, 4, 5])
```

Accessing a field of a masked array with structured datatype returns a MaskedArray.

## Operations on masked arrays

Arithmetic and comparison operations are supported by masked arrays. As much as possible, invalid entries of a masked array are not processed, meaning that the corresponding dat a entries should be the same before and after the operation.

Warning: We need to stress that this behavior may not be systematic, that masked data may be affected by the operation in some cases and therefore users should not rely on this data remaining unchanged.

The numpy . ma module comes with a specific implementation of most ufuncs. Unary and binary functions that have a validity domain (such as log or divide) return the masked constant whenever the input is masked or falls outside the validity domain:

```
>>> ma.log([-1, 0, 1, 2])
masked_array(data = [-- -- 0.0 0.69314718056],
    mask = [ True True False False],
    fill_value = 1e+20)
```

Masked arrays also support standard numpy ufuncs. The output is then a masked array. The result of a unary ufunc is masked wherever the input is masked. The result of a binary ufunc is masked wherever any of the input is masked. If the ufunc also returns the optional context output (a 3-element tuple containing the name of the ufunc, its arguments and its domain), the context is processed and entries of the output masked array are masked wherever the corresponding input fall outside the validity domain:

```
>> x = ma.array([-1, 1, 0, 2, 3], mask=[0, 0, 0, 0, 1])
>>> np.log(x)
masked_array(data = [-- -- 0.0 0.69314718056 --],
    mask = [ True True False False True],
    fill_value = 1e+20)
```


### 1.6.3 Examples

## Data with a given value representing missing data

Let's consider a list of elements, $x$, where values of -9999. represent missing data. We wish to compute the average value of the data and the vector of anomalies (deviations from the average):

```
>>> import numpy.ma as ma
>>> x = [0.,1.,-9999.,3.,4.]
>>> mx = ma.masked_values (x, -9999.)
>>> print mx.mean()
2.0
>>> print mx - mx.mean()
[-2.0 -1.0 -- 1.0 2.0]
>>> print mx.anom()
[-2.0 -1.0 -- 1.0 2.0]
```


## Filling in the missing data

Suppose now that we wish to print that same data, but with the missing values replaced by the average value.

```
>>> print mx.filled(mx.mean())
[ 0. 1. 2. 3. 4.]
```


## Numerical operations

Numerical operations can be easily performed without worrying about missing values, dividing by zero, square roots of negative numbers, etc.:

```
>>> import numpy as np, numpy.ma as ma
>>> x = ma.array([1., -1., 3., 4., 5., 6.], mask=[0,0,0,0,1,0])
>>> y = ma.array([1., 2., 0., 4., 5., 6.], mask=[0,0,0,0,0,1])
>>> print np.sqrt(x/y)
[1.0 -- -- 1.0 -- --]
```

Four values of the output are invalid: the first one comes from taking the square root of a negative number, the second from the division by zero, and the last two where the inputs were masked.

## Ignoring extreme values

Let's consider an array $d$ of random floats between 0 and 1 . We wish to compute the average of the values of $d$ while ignoring any data outside the range $[0.1,0.9]$ :

```
>>> print ma.masked_outside(d, 0.1, 0.9).mean()
```


### 1.6.4 Constants of the numpy .ma module

In addition to the MaskedArray class, the numpy .ma module defines several constants.

## numpy.ma.masked

The masked constant is a special case of MaskedArray, with a float datatype and a null shape. It is used to test whether a specific entry of a masked array is masked, or to mask one or several entries of a masked array:

```
>>> x = ma.array([1, 2, 3], mask=[0, 1, 0])
>>> x[1] is ma.masked
True
>>> x[-1] = ma.masked
>>> x
masked_array(data = [1 -- --],
            mask = [False True True],
    fill_value = 999999)
```

numpy.ma.nomask

Value indicating that a masked array has no invalid entry. nomask is used internally to speed up computations when the mask is not needed.

```
numpy.ma.masked_print_options
```

String used in lieu of missing data when a masked array is printed. By default, this string is ${ }^{\prime}-{ }^{\prime}$.

### 1.6.5 The MaskedArray class

class numpy.ma.MaskedArray

A subclass of ndarray designed to manipulate numerical arrays with missing data.
An instance of MaskedArray can be thought as the combination of several elements:

- The data, as a regular numpy. ndarray of any shape or datatype (the data).
- A boolean mask with the same shape as the data, where a True value indicates that the corresponding element of the data is invalid. The special value nomask is also acceptable for arrays without named fields, and indicates that no data is invalid.
- A fill_value, a value that may be used to replace the invalid entries in order to return a standard numpy. ndarray.


## Attributes and properties of masked arrays

## See Also:

## Array Attributes

MaskedArray.data
Returns the underlying data, as a view of the masked array. If the underlying data is a subclass of numpy. ndarray, it is returned as such.

```
>>> x = ma.array(np.matrix([[1, 2], [3, 4]]), mask=[[0, 1], [1, 0]])
>>> x.data
matrix([[1, 2],
            [3, 4]])
```

The type of the data can be accessed through the baseclass attribute.

```
MaskedArray.mask
```

Returns the underlying mask, as an array with the same shape and structure as the data, but where all fields are atomically booleans. A value of True indicates an invalid entry.

## MaskedArray.recordmask

Returns the mask of the array if it has no named fields. For structured arrays, returns a ndarray of booleans where entries are True if all the fields are masked, False otherwise:

```
>>> x = ma.array([(1, 1), (2, 2), (3, 3), (4, 4), (5, 5)],
mask=[(0, 0), (1, 0), (1, 1), (0, 1), (0, 0)],
... dtype=[('a', int), ('b', int)])
>>> x.recordmask
array([False, False, True, False, False], dtype=bool)
```

MaskedArray.fill_value

Returns the value used to fill the invalid entries of a masked array. The value is either a scalar (if the masked array has no named fields), or a 0-D ndarray with the same dtype as the masked array if it has named fields.

The default filling value depends on the datatype of the array:

| datatype | default |
| :--- | :--- |
| bool | True |
| int | 999999 |
| float | $1 . \mathrm{e} 20$ |
| complex | $1 . \mathrm{e} 20+0 \mathrm{j}$ |
| object | $? ?$ |
| string | 'N/A' |

MaskedArray.baseclass
Returns the class of the underlying data.

```
>>> x = ma.array(np.matrix([[1, 2], [3, 4]]), mask=[[0, 0], [1, 0]])
>>> x.baseclass
<class 'numpy.matrixlib.defmatrix.matrix'>
```

MaskedArray.sharedmask
Returns whether the mask of the array is shared between several masked arrays. If this is the case, any modification to the mask of one array will be propagated to the others.

MaskedArray. hardmask
Returns whether the mask is hard (True) or soft (False). When the mask is hard, masked entries cannot be unmasked.

As MaskedArray is a subclass of ndarray, a masked array also inherits all the attributes and properties of a ndarray instance.

| MaskedArray.base | Base object if memory is from some other object. <br> An object to simplify the interaction of the array with the ctypes <br> MaskedArray.ctypes |
| :--- | :--- |
|  | module. |
| MaskedArray.dtype | Data-type of the array's elements. |
| MaskedArray.flags | Information about the memory layout of the array. |
| MaskedArray.itemsize | Length of one array element in bytes. |
| MaskedArray.nbytes | Total bytes consumed by the elements of the array. |
| MaskedArray.ndim | Number of array dimensions. |
| MaskedArray.shape | Tuple of array dimensions. |
| MaskedArray.size | Number of elements in the array. |
| MaskedArray.strides | Tuple of bytes to step in each dimension when traversing an array. |
| MaskedArray.imag | Imaginary part. |
| MaskedArray.real | Real part |
| MaskedArray.flat | Flat version of the array. |
| MaskedArray.__array_priority |  |
| MaskedArray.base |  |
| Base object if memory is from some other object. |  |

## Examples

The base of an array that owns its memory is None:

```
>>> x = np.array([1,2,3,4])
>>> x.base is None
True
```

Slicing creates a view, whose memory is shared with x :

```
>>> y = x[2:]
>>> y.base is x
True
```

MaskedArray.ctypes
An object to simplify the interaction of the array with the ctypes module.
This attribute creates an object that makes it easier to use arrays when calling shared libraries with the ctypes module. The returned object has, among others, data, shape, and strides attributes (see Notes below) which themselves return ctypes objects that can be used as arguments to a shared library.

## Parameters

None :

## Returns

c : Python object
Possessing attributes data, shape, strides, etc.

## See Also:

numpy.ctypeslib

## Notes

Below are the public attributes of this object which were documented in "Guide to NumPy" (we have omitted undocumented public attributes, as well as documented private attributes):
-data: A pointer to the memory area of the array as a Python integer. This memory area may contain data that is not aligned, or not in correct byte-order. The memory area may not even be writeable. The array flags and data-type of this array should be respected when passing this attribute to arbitrary C-code to avoid trouble that can include Python crashing. User Beware! The value of this attribute is exactly the same as self._array_interface_['data'][0].
-shape (c_intp*self.ndim): A ctypes array of length self.ndim where the basetype is the C-integer corresponding to dtype( ' p ') on this platform. This base-type could be c_int, c_long, or c_longlong depending on the platform. The c_intp type is defined accordingly in numpy.ctypeslib. The ctypes array contains the shape of the underlying array.
-strides (c_intp*self.ndim): A ctypes array of length self.ndim where the basetype is the same as for the shape attribute. This ctypes array contains the strides information from the underlying array. This strides information is important for showing how many bytes must be jumped to get to the next element in the array.
-data_as(obj): Return the data pointer cast to a particular c-types object. For example, calling self._as_parameter_ is equivalent to self.data_as(ctypes.c_void_p). Perhaps you want to use the data as a pointer to a ctypes array of floating-point data: self.data_as(ctypes.POINTER(ctypes.c_double)).
-shape_as(obj): Return the shape tuple as an array of some other c-types type. For example: self.shape_as(ctypes.c_short).
-strides_as(obj): Return the strides tuple as an array of some other c-types type. For example: self.strides_as(ctypes.c_longlong).

Be careful using the ctypes attribute - especially on temporary arrays or arrays constructed on the fly. For example, calling ( $a+b$ ).ctypes.data_as (ctypes.c_void_p) returns a pointer to memory that is invalid because the array created as $(a+b)$ is deallocated before the next Python statement. You can avoid this problem using either $c=a+b$ or $c t=(a+b) . c t y p e s$. In the latter case, ct will hold a reference to the array until ct is deleted or re-assigned.

If the ctypes module is not available, then the ctypes attribute of array objects still returns something useful, but ctypes objects are not returned and errors may be raised instead. In particular, the object will still have the as parameter attribute which will return an integer equal to the data attribute.

## Examples

```
>>> import ctypes
>>> x
array([[0, 1],
    [2, 3]])
>>> x.ctypes.data
30439712
>>> x.ctypes.data_as(ctypes.POINTER(ctypes.c_long))
<ctypes.LP_c_long object at 0x01F01300>
>>> x.ctypes.data_as(ctypes.POINTER(ctypes.c_long)).contents
c_long(0)
>>> x.ctypes.data_as(ctypes.POINTER(ctypes.c_longlong)).contents
c_longlong(4294967296L)
>>> x.ctypes.shape
<numpy.core._internal.c_long_Array_2 object at 0x01FFD580>
>>> x.ctypes.shape_as(ctypes.c_long)
<numpy.core._internal.c_long_Array_2 object at 0x01FCE620>
>>> x.ctypes.strides
<numpy.core._internal.c_long_Array_2 object at 0x01FCE620>
>>> x.ctypes.strides_as(ctypes.c_longlong)
<numpy.core._internal.c_longlong_Array_2 object at 0x01F01300>
```


## MaskedArray.dtype

Data-type of the array's elements.

## Parameters

## None :

## Returns

d : numpy dtype object

## See Also:

numpy.dtype

## Examples

>>> $x$
array([[0, 1],
$[2,3]])$
>>> x.dtype
dtype('int32')
>>> type(x.dtype)
<type 'numpy.dtype'>
MaskedArray.flags
Information about the memory layout of the array.

## Notes

The flags object can be accessed dictionary-like (as in a.flags ['WRITEABLE' ]), or by using lowercased attribute names (as in a.flags.writeable). Short flag names are only supported in dictionary access.

Only the UPDATEIFCOPY, WRITEABLE, and ALIGNED flags can be changed by the user, via direct assignment to the attribute or dictionary entry, or by calling ndarray.setflags.

The array flags cannot be set arbitrarily:

- UPDATEIFCOPY can only be set False.
-ALIGNED can only be set True if the data is truly aligned.
-WRITEABLE can only be set True if the array owns its own memory or the ultimate owner of the memory exposes a writeable buffer interface or is a string.


## Attributes

## MaskedArray.itemsize

Length of one array element in bytes.

## Examples

```
>>> x = np.array([1,2,3], dtype=np.float64)
>>> x.itemsize
8
>>> x = np.array([1,2,3], dtype=np.complex128)
>>> x.itemsize
16
```

MaskedArray.nbytes

Total bytes consumed by the elements of the array.

## Notes

Does not include memory consumed by non-element attributes of the array object.

## Examples

```
>>> x = np.zeros((3,5,2), dtype=np.complex128)
>>> x.nbytes
480
>>> np.prod(x.shape) * x.itemsize
480
```

MaskedArray.ndim

Number of array dimensions.

## Examples

```
>>> x = np.array([1, 2, 3])
>>> x.ndim
1
>>> y = np.zeros((2, 3, 4))
>>> y.ndim
3
MaskedArray.shape
Tuple of array dimensions.
```


## Notes

May be used to "reshape" the array, as long as this would not require a change in the total number of elements

## Examples

```
>>> x = np.array([1, 2, 3, 4])
>>> x.shape
(4,)
>>> y = np.zeros((2, 3, 4))
>>> y.shape
(2, 3, 4)
>>> y.shape = (3, 8)
>>> y
array([[ 0., 0., 0., 0., 0., 0., 0., 0.],
    [ 0., 0., 0., 0., 0., 0., 0., 0.],
    [0., 0., 0., 0., 0., 0., 0., 0.]])
>>> y.shape = (3, 6)
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
ValueError: total size of new array must be unchanged
MaskedArray.size
```

Number of elements in the array.
Equivalent to np.prod (a.shape), i.e., the product of the array's dimensions.

## Examples

```
>>> x = np.zeros((3, 5, 2), dtype=np.complex128)
>>> x.size
30
>>> np.prod(x.shape)
30
MaskedArray.strides
```

Tuple of bytes to step in each dimension when traversing an array.
The byte offset of element (i[0], i[1], ..., $i[n]$ ) in an array $a$ is:

```
offset = sum(np.array(i) * a.strides)
```

A more detailed explanation of strides can be found in the "ndarray.rst" file in the NumPy reference guide.

## See Also:

```
numpy.lib.stride_tricks.as_strided
```


## Notes

Imagine an array of 32-bit integers (each 4 bytes):

```
x = np.array([[0, 1, 2, 3, 4],
    [5, 6, 7, 8, 9]], dtype=np.int32)
```

This array is stored in memory as 40 bytes, one after the other (known as a contiguous block of memory). The strides of an array tell us how many bytes we have to skip in memory to move to the next position along a certain axis. For example, we have to skip 4 bytes ( 1 value) to move to the next column, but 20 bytes ( 5 values) to get to the same position in the next row. As such, the strides for the array $x$ will be $(20,4)$.

## Examples

```
>>> y = np.reshape(np.arange(2*3*4), (2, 3,4))
>>> y
array([[[ 0, 1, 2, 3],
    [4, 5, 6, 7],
    [ 8, 9, 10, 11]],
    [[12, 13, 14, 15],
        [16, 17, 18, 19],
        [20, 21, 22, 23]]])
>>> y.strides
(48, 16, 4)
>>> y[1,1,1]
17
>>> offset=sum(y.strides * np.array((1,1,1)))
>>> offset/y.itemsize
17
```

$\ggg x=n p . r e s h a p e(n p . a r a n g e(5 * 6 * 7 * 8),(5,6,7,8))$.transpose $(2,3,1,0)$
>>> x.strides
(32, 4, 224, 1344)
$\ggg$ i $=$ np.array $([3,5,2,2])$
$\ggg$ offset $=$ sum(i * x.strides)
>>> $x[3,5,2,2]$
813
>>> offset / x.itemsize
813
MaskedArray.imag
Imaginary part.
MaskedArray.real
Real part
MaskedArray.flat

Flat version of the array.

### 1.6.6 MaskedArray methods

## See Also:

Array methods

## Conversion



New view of array with the same data.

## Parameters <br> dtype : data-type, optional

Data-type descriptor of the returned view, e.g., float32 or int16. The default, None, results in the view having the same data-type as $a$.
type : Python type, optional
Type of the returned view, e.g., ndarray or matrix. Again, the default None results in type preservation.

## Notes

a.view () is used two different ways:
a.view (some_dtype) or a.view (dtype=some_dtype) constructs a view of the array's memory with a different data-type. This can cause a reinterpretation of the bytes of memory.
a.view (ndarray_subclass) or a.view(type=ndarray_subclass) just returns an instance of ndarray_subclass that looks at the same array (same shape, dtype, etc.) This does not cause a reinterpretation
of the memory.

## Examples

```
>>> x = np.array([(1, 2)], dtype=[('a', np.int8), ('b', np.int8)])
```

Viewing array data using a different type and dtype:

```
>>> y = x.view(dtype=np.int16, type=np.matrix)
>>> y
matrix([[513]], dtype=int16)
>>> print type(y)
<class 'numpy.matrixlib.defmatrix.matrix'>
```

Creating a view on a structured array so it can be used in calculations

```
>>> x = np.array([(1, 2), (3,4)], dtype=[('a', np.int8), ('b', np.int8)])
>>> xv = x.view(dtype=np.int8).reshape (-1,2)
>>> xv
array([[1, 2],
    [3, 4]], dtype=int8)
>>> xv.mean(0)
array([ 2., 3.])
```

Making changes to the view changes the underlying array

```
>>> xv[0,1]=20
>>> print x
[(1, 20) (3, 4)]
```

Using a view to convert an array to a record array:

```
>>> z = x.view(np.recarray)
>>> z.a
array([1], dtype=int8)
```

Views share data:

```
>>> x[0] = (9, 10)
>>> z[0]
(9, 10)
```

MaskedArray.astype (newtype)
Returns a copy of the MaskedArray cast to given newtype.

## Returns

output : MaskedArray
A copy of self cast to input newtype. The returned record shape matches self.shape.

## Examples

```
>>> x = np.ma.array([[1,2,3.1],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1.0 -- 3.1]
    [-- 5.0 --]
    [7.0 -- 9.0]]
>>> print x.astype(int32)
[[1 -- 3]
            [-- 5 --]
            [7 -- 9]]
```

MaskedArray.byteswap (inplace)
Swap the bytes of the array elements
Toggle between low-endian and big-endian data representation by returning a byteswapped array, optionally swapped in-place.

## Parameters

inplace: bool, optional :
If True, swap bytes in-place, default is False.

## Returns

out: ndarray :
The byteswapped array. If inplace is True, this is a view to self.

## Examples

```
>>> A = np.array([1, 256, 8755], dtype=np.int16)
>>> map(hex, A)
['0x1', '0x100', '0x2233']
>>> A.byteswap(True)
array([ 256, 1, 13090], dtype=int16)
>>> map (hex, A)
['0x100', '0x1', '0x3322']
```

Arrays of strings are not swapped

```
>>> A = np.array(['ceg', 'fac'])
>>> A.byteswap()
array(['ceg', 'fac'],
    dtype='|S3')
```

MaskedArray. compressed ()

Return all the non-masked data as a 1-D array.

## Returns

data : ndarray
A new ndarray holding the non-masked data is returned.

## Notes

The result is not a MaskedArray!

## Examples

```
>>> x = np.ma.array(np.arange(5), mask=[0]*2 + [1]*3)
>>> x.compressed()
array([0, 1])
>>> type(x.compressed())
<type 'numpy.ndarray'>
MaskedArray.filled (fill_value=None)
Return a copy of self, with masked values filled with a given value.
```


## Parameters

fill_value : scalar, optional
The value to use for invalid entries (None by default). If None, the fill_value attribute of the array is used instead.

## Returns

filled_array : ndarray
A copy of self with invalid entries replaced by fill_value (be it the function argument or the attribute of self.

## Notes

The result is not a MaskedArray!

## Examples

```
>>> x = np.ma.array([1,2,3,4,5], mask=[0,0,1,0,1], fill_value=-999)
>>> x.filled()
array([1, 2, -999, 4, -999])
>>> type(x.filled())
<type 'numpy.ndarray'>
```

Subclassing is preserved. This means that if the data part of the masked array is a matrix, filled returns a matrix:

```
>>> x = np.ma.array(np.matrix([[1, 2], [3, 4]]), mask=[[0, 1], [1, 0]])
>>> x.filled()
matrix([[ 1, 999999],
    [999999, 4]])
MaskedArray.tofile (fid, sep='',format='%s')
```

Save a masked array to a file in binary format.
Warning: This function is not implemented yet.

## Raises

## NotImplementedError :

When tofile is called.
MaskedArray.toflex()
Transforms a masked array into a flexible-type array.
The flexible type array that is returned will have two fields:
-the _dat a field stores the _dat a part of the array.
-the _mask field stores the _mask part of the array.

## Parameters

None :

## Returns

record: ndarray
A new flexible-type ndarray with two fields: the first element containing a value, the second element containing the corresponding mask boolean. The returned record shape matches self.shape.

## Notes

A side-effect of transforming a masked array into a flexible ndarray is that meta information (fill_value, ...) will be lost.

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 --]
    [7 -- 9]]
>>> print x.toflex()
[[(1, False) (2, True) (3, False)]
    [(4, True) (5, False) (6, True)]
    [(7, False) (8, True) (9, False)]]
```

MaskedArray.tolist (fill_value=None)
Return the data portion of the masked array as a hierarchical Python list.
Data items are converted to the nearest compatible Python type. Masked values are converted to fill_value. If fill_value is None, the corresponding entries in the output list will be None.

## Parameters

fill_value : scalar, optional
The value to use for invalid entries. Default is None.

## Returns

result : list
The Python list representation of the masked array.

## Examples

```
>>> x = np.ma.array([[1,2,3], [4,5,6], [7,8,9]], mask=[0] + [1,0]*4)
>>> x.tolist()
[[1, None, 3], [None, 5, None], [7, None, 9]]
>>> x.tolist(-999)
[[1, -999, 3], [-999, 5, -999], [7, -999, 9]]
```

MaskedArray.torecords()
Transforms a masked array into a flexible-type array.
The flexible type array that is returned will have two fields:
-the _data field stores the _data part of the array.
-the _mask field stores the _mask part of the array.

## Parameters

None :

## Returns

record: ndarray
A new flexible-type ndarray with two fields: the first element containing a value, the second element containing the corresponding mask boolean. The returned record shape matches self.shape.

## Notes

A side-effect of transforming a masked array into a flexible ndarray is that meta information (fill_value, ...) will be lost.

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 --]
    [7 -- 9]]
>>> print x.toflex()
[[(1, False) (2, True) (3, False)]
    [(4, True) (5, False) (6, True)]
    [(7, False) (8, True) (9, False)]]
```

MaskedArray.tostring (fill_value=None, order=' ${ }^{\prime}$ ')

Return the array data as a string containing the raw bytes in the array.
The array is filled with a fill value before the string conversion.

## Parameters

fill_value : scalar, optional
Value used to fill in the masked values. Deafult is None, in which case MaskedArray.fill_value is used.
order : \{ ' C ', ' F ', ' A ' $\}$, optional
Order of the data item in the copy. Default is ' C '.

- 'C' - C order (row major).
- 'F' - Fortran order (column major).
- 'A' - Any, current order of array.
- None - Same as 'A'.


## See Also:

```
ndarray.tostring,tolist,tofile
```


## Notes

As for ndarray.tostring, information about the shape, dtype, etc., but also about fill_value, will be lost.

## Examples

```
>>> x = np.ma.array(np.array([[1, 2], [3, 4]]), mask=[[0, 1], [1, 0]])
>>> x.tostring()
'\x01\x00\x00\x00?B\x0f\x00?B\x0f\x00\x04\x00\x00\x00'
```


## Shape manipulation

For reshape, resize, and transpose, the single tuple argument may be replaced with $n$ integers which will be interpreted as an n-tuple.

```
MaskedArray.flatten([order])
MaskedArray.ravel()
MaskedArray.reshape(*s,**kwargs)
MaskedArray.resize(newshape[, refcheck,
order])
MaskedArray.squeeze()
MaskedArray.swapaxes(axis1, axis2)
MaskedArray.transpose(*axes)
MaskedArray.T
MaskedArray.flatten (order='C')
Return a copy of the array collapsed into one dimension.
```


## Parameters

order : $\left\{{ }^{\prime} C\right.$ ', ' $F$ ', ' $A$ ' $\}$, optional
Whether to flatten in C (row-major), Fortran (column-major) order, or preserve the $\mathrm{C} /$ Fortran ordering from $a$. The default is ' C '.

## Returns

 y : ndarrayA copy of the input array, flattened to one dimension.

## See Also:

ravel
Return a flattened array.
flat
A 1-D flat iterator over the array.

## Examples

```
>>> a = np.array([[1,2], [3,4]])
>>> a.flatten()
array([1, 2, 3, 4])
>>> a.flatten('F')
array([1, 3, 2, 4])
```

MaskedArray.ravel()
Returns a 1D version of self, as a view.

## Returns

MaskedArray :
Output view is of shape (self.size,) (or
(np.ma.product (self.shape), )).

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
            [-- 5 --]
            [7 -- 9]]
>>> print x.ravel()
[1 -- 3 -- 5 -- 7 -- 9]
```

MaskedArray.reshape (*s, **kwargs)
Give a new shape to the array without changing its data.
Returns a masked array containing the same data, but with a new shape. The result is a view on the original array; if this is not possible, a ValueError is raised.

## Parameters

shape : int or tuple of ints
The new shape should be compatible with the original shape. If an integer is supplied, then the result will be a 1-D array of that length.
order : \{ 'C', 'F'\}, optional
Determines whether the array data should be viewed as in C (row-major) or FORTRAN (column-major) order.

## Returns

reshaped_array : array
A new view on the array.

## See Also:

```
reshape
```

Equivalent function in the masked array module.
numpy.ndarray.reshape
Equivalent method on ndarray object.
numpy. reshape
Equivalent function in the NumPy module.

## Notes

The reshaping operation cannot guarantee that a copy will not be made, to modify the shape in place, use a.shape $=\mathrm{s}$

## Examples

```
>>> x = np.ma.array([[1,2],[3,4]], mask=[1,0,0,1])
>>> print x
[[-- 2]
    [3 --]]
>>> x = x.reshape((4,1))
>>> print x
[[--]
    [2]
    [3]
    [--]]
MaskedArray.resize (newshape, refcheck=True, order=False)
```

Warning: This method does nothing, except raise a ValueError exception. A masked array does not own its data and therefore cannot safely be resized in place. Use the numpy.ma. resize function instead.

This method is difficult to implement safely and may be deprecated in future releases of NumPy.

```
MaskedArray.squeeze()
```

Remove single-dimensional entries from the shape of $a$.
Refer to numpy. squeeze for full documentation.

## See Also:

numpy.squeeze equivalent function

MaskedArray.swapaxes (axis1, axis2)
Return a view of the array with axis 1 and axis 2 interchanged.
Refer to numpy. swapaxes for full documentation.

## See Also:

numpy.swapaxes
equivalent function
MaskedArray.transpose (*axes)
Returns a view of the array with axes transposed.
For a 1-D array, this has no effect. (To change between column and row vectors, first cast the 1-D array into a matrix object.) For a 2-D array, this is the usual matrix transpose. For an n-D array, if axes are given, their order indicates how the axes are permuted (see Examples). If axes are not provided and a.shape $=(i[0], i[1]$, ... i[n-2], $i[n-1])$, then a.transpose().shape $=(i[n-1], i[n-2], \ldots i[1]$, i[0]).

## Parameters

axes : None, tuple of ints, or $n$ ints

- None or no argument: reverses the order of the axes.
- tuple of ints: $i$ in the $j$-th place in the tuple means $a$ 's $i$-th axis becomes a.transpose()'s $j$-th axis.
- $n$ ints: same as an n-tuple of the same ints (this form is intended simply as a "convenience" alternative to the tuple form)


## Returns

out : ndarray
View of $a$, with axes suitably permuted.

## See Also:

ndarray.T
Array property returning the array transposed.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> a
array([[1, 2],
    [3, 4]])
>>> a.transpose()
array([[1, 3],
            [2, 4]])
>>> a.transpose((1, 0))
array([[1, 3],
    [2, 4]])
>>> a.transpose(1, 0)
array([[1, 3],
    [2, 4]])
```

```
MaskedArray.T
```


## Item selection and manipulation

For array methods that take an axis keyword, it defaults to None. If axis is None, then the array is treated as a 1-D array. Any other value for axis represents the dimension along which the operation should proceed.

```
MaskedArray.argmax([axis, fill_value, Returns array of indices of the maximum values along the given
out])
MaskedArray.argmin([axis, fill_value,
out])
MaskedArray.argsort([axis, kind,
order, ...])
MaskedArray.choose(choices[, out,
mode])
MaskedArray.compress(condition[,
axis,out])
MaskedArray.diagonal([offset, axis1,
axis2])
MaskedArray.fill(value)
MaskedArray.item(*args)
MaskedArray.nonzero()
MaskedArray.put(indices, values[,
mode])
MaskedArray.repeat(repeats[, axis])
MaskedArray.searchsorted(v[, side])
MaskedArray.sort([axis, kind, order,
...])
MaskedArray.take(indices[, axis, out,
mode])
```

MaskedArray.argmax (axis=None, fill_value=None, out=None)
Returns array of indices of the maximum values along the given axis. Masked values are treated as if they had the value fill_value.

## Parameters

axis: $\{$ None, integer $\}$
If None, the index is into the flattened array, otherwise along the specified axis
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, the output of maximum_fill_value(self._data) is used instead.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

```
Returns
    index_array : {integer_array}
```


## Examples

```
>>> a = np.arange(6).reshape (2,3)
>>> a.argmax()
5
>>> a.argmax(0)
array([1, 1, 1])
>>> a.argmax(1)
array([2, 2])
```

MaskedArray.argmin (axis=None, fill_value=None, out=None)

Return array of indices to the minimum values along the given axis.

## Parameters

axis : \{None, integer\}
If None, the index is into the flattened array, otherwise along the specified axis
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, the output of minimum_fill_value(self._data) is used instead.
out : \{None, array\}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

\{ndarray, scalar\} :
If multi-dimension input, returns a new ndarray of indices to the minimum values along the given axis. Otherwise, returns a scalar of index to the minimum values along the given axis.

## Examples

```
>>> x = np.ma.array(arange(4), mask=[1,1,0,0])
>>> x.shape = (2,2)
>>> print x
[[-- --]
    [2 3]]
>>> print x.argmin(axis=0, fill_value=-1)
[0 0]
>>> print x.argmin(axis=0, fill_value=9)
[1 1]
```

MaskedArray.argsort (axis=None, kind='quicksort', order=None, fill_value=None)
Return an ndarray of indices that sort the array along the specified axis. Masked values are filled beforehand to fill_value.

## Parameters

axis : int, optional
Axis along which to sort. The default is -1 (last axis). If None, the flattened array is used.
fill_value : var, optional
Value used to fill the array before sorting. The default is the fill_value attribute of the input array.
kind : \{'quicksort', 'mergesort', 'heapsort'\}, optional

Sorting algorithm.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## Returns

index_array : ndarray, int
Array of indices that sort $a$ along the specified axis. In other words, a [index_array] yields a sorted $a$.

## See Also:

```
sort
```

Describes sorting algorithms used.

## lexsort

Indirect stable sort with multiple keys.
ndarray.sort
Inplace sort.

## Notes

See sort for notes on the different sorting algorithms.

## Examples

```
>>> a = np.ma.array([3,2,1], mask=[False, False, True])
>>> a
masked_array(data = [3 2 -- ] ],
    mask = [False False True],
    fill_value = 999999)
>>> a.argsort()
array([1, 0, 2])
```

MaskedArray.choose (choices, out=None, mode='raise')
Use an index array to construct a new array from a set of choices.
Refer to numpy. choose for full documentation.
See Also:
numpy. choose
equivalent function

MaskedArray.compress (condition, axis=None, out=None)
Return $a$ where condition is True.
If condition is a MaskedArray, missing values are considered as False.

## Parameters

condition : var
Boolean 1-d array selecting which entries to return. If len(condition) is less than the size of a along the axis, then output is truncated to length of condition array.
axis: \{None, int \}, optional
Axis along which the operation must be performed.
out : \{None, ndarray \}, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type will be cast if necessary.

## Returns

result : MaskedArray
A MaskedArray object.

## Notes

Please note the difference with compressed! The output of compress has a mask, the output of compressed does not.

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 --]
    [7 -- 9]]
>>> x.compress([1, 0, 1])
masked_array(data = [1 3],
            mask = [False False],
            fill_value=999999)
>>> x.compress([1, 0, 1], axis=1)
masked_array(data =
    [[ll 3]
    [-- --]
    [7 9]],
                mask =
    [[False False]
    [ True True]
    [False False]],
            fill_value=999999)
```

MaskedArray.diagonal (offset=0, axis $1=0$, axis $2=1$ )

Return specified diagonals.
Refer to numpy. diagonal for full documentation.
See Also:
numpy.diagonal
equivalent function
MaskedArray.fill (value)
Fill the array with a scalar value.

## Parameters

value: scalar
All elements of $a$ will be assigned this value.

## Examples

```
>>> a = np.array([1, 2])
>>> a.fill(0)
>>> a
```

```
array([0, 0])
>>> a = np.empty(2)
>>> a.fill(1)
>>> a
array([ 1., 1.])
MaskedArray.item(*args)
```

Copy an element of an array to a standard Python scalar and return it.

## Parameters

*args : Arguments (variable number and type)

- none: in this case, the method only works for arrays with one element (a.size $==1$ ), which element is copied into a standard Python scalar object and returned.
- int_type: this argument is interpreted as a flat index into the array, specifying which element to copy and return.
- tuple of int_types: functions as does a single int_type argument, except that the argument is interpreted as an nd-index into the array.


## Returns

## z : Standard Python scalar object

A copy of the specified element of the array as a suitable Python scalar

## Notes

When the data type of $a$ is longdouble or clongdouble, item() returns a scalar array object because there is no available Python scalar that would not lose information. Void arrays return a buffer object for item(), unless fields are defined, in which case a tuple is returned.
item is very similar to a[args], except, instead of an array scalar, a standard Python scalar is returned. This can be useful for speeding up access to elements of the array and doing arithmetic on elements of the array using Python's optimized math.

## Examples

```
>>> x = np.random.randint(9, size=(3, 3))
>>> x
array([[3, 1, 7],
    [2, 8, 3],
    [8, 5, 3]])
>>> x.item(3)
2
>>> x.item(7)
5
>>> x.item((0, 1))
1
>>> x.item((2, 2))
3
MaskedArray.nonzero()
```

Return the indices of unmasked elements that are not zero.
Returns a tuple of arrays, one for each dimension, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

```
a[a.nonzero()]
```

To group the indices by element, rather than dimension, use instead:

```
np.transpose(a.nonzero())
```

The result of this is always a 2d array, with a row for each non-zero element.

## Parameters

None :

## Returns

tuple_of_arrays : tuple
Indices of elements that are non-zero.

## See Also:

numpy.nonzero
Function operating on ndarrays.

## flatnonzero

Return indices that are non-zero in the flattened version of the input array.

```
ndarray.nonzero
```

Equivalent ndarray method.

```
count_nonzero
```

Counts the number of non-zero elements in the input array.

## Examples

```
>>> import numpy.ma as ma
>>> x = ma.array(np.eye(3))
>>> x
masked_array(data =
    [[ 1. 0. 0.]
    [ 0. 1. 0.]
    [ 0. 0. 1.]],
        mask =
    False,
        fill_value=1e+20)
>>> x.nonzero()
(array([0, 1, 2]), array([0, 1, 2]))
```

Masked elements are ignored.

```
>>> x[1, 1] = ma.masked
>>> x
masked_array(data =
    [[1.0 0.0 0.0]
    [0.0 -- 0.0]
    [0.0 0.0 1.0]],
            mask =
    [[False False False]
    [False True False]
    [False False False]],
            fill_value=1e+20)
>>> x.nonzero()
(array([0, 2]), array([0, 2]))
```

Indices can also be grouped by element.

```
>>> np.transpose(x.nonzero())
array([[0, 0],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , ma.nonzero( $a>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a ma.array([[1,2,3],[4,5,6],[7, 8,9]])
>>> a > 3
masked_array(data =
    [[False False False]
    [ True True True]
    [ True True True]],
            mask =
    False,
            fill_value=999999)
>>> ma.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the condition array can also be called.

```
>>> (a > 3).nonzero()
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

MaskedArray.put (indices, values, mode='raise')
Set storage-indexed locations to corresponding values.
Sets self._data.flat $[\mathrm{n}]=$ values $[\mathrm{n}]$ for each n in indices. If values is shorter than indices then it will repeat. If values has some masked values, the initial mask is updated in consequence, else the corresponding values are unmasked.

## Parameters

indices : 1-D array_like
Target indices, interpreted as integers.
values : array_like
Values to place in self._data copy at target indices.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave. 'raise' : raise an error. 'wrap' : wrap around. 'clip' : clip to the range.

## Notes

values can be a scalar or length 1 array.

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 --]
    [7 -- 9]]
>>> x.put([0,4,8],[10,20,30])
>>> print x
[[10 -- 3]
```

```
    [-- 20 --]
    [7 -- 30]]
>>> x.put(4,999)
>>> print x
[[10 -- 3]
    [-- 999 --]
    [7 -- 30]]
```

MaskedArray. repeat (repeats, axis=None)

Repeat elements of an array.
Refer to numpy . repeat for full documentation.

## See Also:

numpy.repeat
equivalent function
MaskedArray. searchsorted ( $v$, side='left')
Find indices where elements of v should be inserted in a to maintain order.
For full documentation, see numpy. searchsorted
See Also:
numpy.searchsorted
equivalent function
MaskedArray.sort ( axis=-1, kind='quicksort', order=None, endwith=True, fill_value=None)
Sort the array, in-place

## Parameters

a: array_like
Array to be sorted.
axis : int, optional
Axis along which to sort. If None, the array is flattened before sorting. The default is -1 , which sorts along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is a structured array, this argument specifies which fields to compare first, second, and so on. This list does not need to include all of the fields.
endwith : \{True, False \}, optional
Whether missing values (if any) should be forced in the upper indices (at the end of the array) (True) or lower indices (at the beginning).
fill_value : \{var\}, optional
 endwith.

## Returns

sorted_array : ndarray

Array of the same type and shape as $a$.

## See Also:

## ndarray.sort

Method to sort an array in-place.
argsort
Indirect sort.

## lexsort

Indirect stable sort on multiple keys.

```
searchsorted
```

Find elements in a sorted array.

## Notes

See sort for notes on the different sorting algorithms.

## Examples

```
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # Default
>>> a.sort()
>>> print a
[1 [ 3 5 -- --]
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # Put missing values in the front
>>> a.sort(endwith=False)
>>> print a
[-- -- 1 3 5]
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # fill_value takes over endwith
>>> a.sort(endwith=False, fill_value=3)
>>> print a
[1 -- -- 3 5]
```

MaskedArray.take (indices, axis=None, out=None, mode='raise')

## Pickling and copy

| MaskedArray.copy([order]) | Return a copy of the array. |
| :--- | :--- |
| MaskedArray.dump(file) | Dump a pickle of the array to the specified file. |
| MaskedArray.dumps() | Returns the pickle of the array as a string. |
| MaskedArray.copy (order $=$ 'C') |  |

Return a copy of the array.

## Parameters

order : \{ 'C', 'F', 'A' \}, optional
By default, the result is stored in C-contiguous (row-major) order in memory. If order is $F$, the result has 'Fortran' (column-major) order. If order is ' $A$ ' ('Any'), then the result has the same order as the input.

## Examples

```
>>> x = np.array([[1,2,3],[4,5,6]], order='F')
    >>> y = x.copy()
    >>> x.fill(0)
    >>> x
    array([[0, 0, 0],
            [0, 0, 0]])
>>> y
array([[1, 2, 3],
            [4, 5, 6]])
>>> y.flags['C_CONTIGUOUS']
True
```

MaskedArray. dump (file)
Dump a pickle of the array to the specified file. The array can be read back with pickle.load or numpy.load.

## Parameters

file : str
A string naming the dump file.
MaskedArray.dumps()
Returns the pickle of the array as a string. pickle.loads or numpy.loads will convert the string back to an array.

## Parameters

None :

## Calculations

| MaskedArray.all([axis, out]) | Check if all of the elements of $a$ are true. |
| :---: | :---: |
| MaskedArray . anom([axis, dtype]) | Compute the anomalies (deviations from the arithmetic mean) along the given axis. |
| MaskedArray.any([axis, out]) | Check if any of the elements of $a$ are true. |
| MaskedArray.clip(a_min, a_max[, out]) | Return an array whose values are limited to [a_min, a_max]. |
| MaskedArray.conj() | Complex-conjugate all elements. |
| MaskedArray.conjugate() | Return the complex conjugate, element-wise. |
| MaskedArray. cumprod([axis, dtype, out]) | Return the cumulative product of the elements along the given axis. |
| MaskedArray.cumsum([axis, dtype, out]) | Return the cumulative sum of the elements along the given axis. |
| MaskedArray.max([axis, out, fill_value]) | Return the maximum along a given axis. |
| MaskedArray.mean([axis, dtype, out]) | Returns the average of the array elements. |
| MaskedArray.min([axis, out, fill_value]) | Return the minimum along a given axis. |
| MaskedArray.prod([axis, dtype, out]) | Return the product of the array elements over the given axis. |
| MaskedArray.product([axis, dtype, out]) | Return the product of the array elements over the given axis. |
| MaskedArray.ptp([axis, out, fill_value]) | Return (maximum - minimum) along the the given dimension (i.e. |
| MaskedArray.round([decimals, out]) | Return $a$ with each element rounded to the given number of decimals. |
| MaskedArray.std([axis, dtype, out, ddof]) | Compute the standard deviation along the specified axis. |
| MaskedArray.sum([axis, dtype, out]) | Return the sum of the array elements over the given axis. |
| MaskedArray.trace([offset, axis1, axis2, ...]) | Return the sum along diagonals of the array. |
| MaskedArray.var([axis, dtype, out, ddof]) | Compute the variance along the specified axis. |

MaskedArray.all (axis=None, out=None)
Check if all of the elements of $a$ are true.
Performs a logical_and over the given axis and returns the result. Masked values are considered as True during computation. For convenience, the output array is masked where ALL the values along the current axis are masked: if the output would have been a scalar and that all the values are masked, then the output is masked.

## Parameters

axis: \{None, integer \}
Axis to perform the operation over. If None, perform over flattened array.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## See Also:

all
equivalent function

## Examples

```
>>> np.ma.array([1,2,3]).all()
True
>>> a = np.ma.array([1,2,3], mask=True)
>>> (a.all() is np.ma.masked)
True
```

MaskedArray. anom (axis=None, dtype=None)
Compute the anomalies (deviations from the arithmetic mean) along the given axis.
Returns an array of anomalies, with the same shape as the input and where the arithmetic mean is computed along the given axis.

## Parameters

axis : int, optional
Axis over which the anomalies are taken. The default is to use the mean of the flattened array as reference.
dtype : dtype, optional
Type to use in computing the variance. For arrays of integer type
the default is float 32 ; for arrays of float types it is the same as the array type.

## See Also:

mean
Compute the mean of the array.

## Examples

```
>>> a = np.ma.array([1,2,3])
>>> a.anom()
masked_array(data = [-1. 0. 1.],
                    mask = False,
            fill_value = 1e+20)
```

MaskedArray .any (axis=None, out=None)
Check if any of the elements of $a$ are true.
Performs a logical_or over the given axis and returns the result. Masked values are considered as False during computation.

## Parameters

axis : \{None, integer\}
Axis to perform the operation over. If None, perform over flattened array and return a scalar.
out : \{None, array\}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## See Also:

any
equivalent function

MaskedArray.clip (a_min, a_max, out=None)
Return an array whose values are limited to [a_min, a_max].
Refer to numpy.clip for full documentation.

## See Also:

numpy.clip
equivalent function

MaskedArray.conj()
Complex-conjugate all elements.
Refer to numpy. con jugate for full documentation.
See Also:
numpy. conjugate
equivalent function
MaskedArray. conjugate ()
Return the complex conjugate, element-wise.
Refer to numpy. conjugate for full documentation.

## See Also:

numpy.conjugate
equivalent function
MaskedArray. cumprod (axis=None, dtype=None, out=None)
Return the cumulative product of the elements along the given axis. The cumulative product is taken over the flattened array by default, otherwise over the specified axis.

Masked values are set to 1 internally during the computation. However, their position is saved, and the result will be masked at the same locations.

## Parameters

axis: $\{$ None, -1 , int $\}$, optional
Axis along which the product is computed. The default (axis $=$ None) is to compute over the flattened array.
dtype : \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are multiplied. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

cumprod : ndarray
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## Notes

The mask is lost if out is not a valid MaskedArray!
Arithmetic is modular when using integer types, and no error is raised on overflow.
MaskedArray. cumsum (axis=None, dtype=None, out=None)
Return the cumulative sum of the elements along the given axis. The cumulative sum is calculated over the flattened array by default, otherwise over the specified axis.

Masked values are set to 0 internally during the computation. However, their position is saved, and the result will be masked at the same locations.

## Parameters

axis : $\{$ None, -1 , int \}, optional
Axis along which the sum is computed. The default (axis = None) is to compute over the flattened array. axis may be negative, in which case it counts from the last to the first axis.
dtype : \{None, dtype\}, optional
Type of the returned array and of the accumulator in which the elements are summed. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

cumsum : ndarray.
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## Notes

The mask is lost if out is not a valid MaskedArray!
Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> marr = np.ma.array(np.arange(10), mask=[0,0,0,1,1,1,0,0,0,0])
>>> print marr.cumsum()
[0 1 3 -- -- -- 9 16 24 33]
```

MaskedArray.max (axis=None, out=None, fill_value=None)
Return the maximum along a given axis.

## Parameters

axis: \{None, int \}, optional
Axis along which to operate. By default, axis is None and the flattened input is used.
out : array_like, optional
Alternative output array in which to place the result. Must be of the same shape and buffer length as the expected output.
fill_value : \{var\}, optional

Value used to fill in the masked values. If None, use the output of maximum_fill_value().

## Returns

 amax : array_likeNew array holding the result. If out was specified, out is returned.

## See Also:

maximum_fill_value
Returns the maximum filling value for a given datatype.

```
MaskedArray.mean (axis=None,dtype=None,out=None)
```

Returns the average of the array elements.
Masked entries are ignored. The average is taken over the flattened array by default, otherwise over the specified axis. Refer to numpy.mean for the full documentation.

## Parameters

a : array_like
Array containing numbers whose mean is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the means are computed. The default is to compute the mean of the flattened array.
dtype : dtype, optional
Type to use in computing the mean. For integer inputs, the default is float64; for floating point, inputs it is the same as the input dtype.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type will be cast if necessary.

## Returns

mean : ndarray, see dtype parameter above
If out=None, returns a new array containing the mean values, otherwise a reference to the output array is returned.

## See Also:

numpy.ma.mean
Equivalent function.
numpy.mean
Equivalent function on non-masked arrays.
numpy.ma.average
Weighted average.

## Examples

```
>>> a = np.ma.array([1,2,3], mask=[False, False, True])
>>> a
masked_array(data = [1 2 --],
                    mask = [False False True],
```

```
        fill_value = 999999)
>>> a.mean()
1.5
MaskedArray.min (axis=None,out=None,fill_value=None)
```

Return the minimum along a given axis.

## Parameters

axis : $\{$ None, int $\}$, optional
Axis along which to operate. By default, axis is None and the flattened input is used.
out : array_like, optional
Alternative output array in which to place the result. Must be of the same shape and buffer length as the expected output.
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, use the output of minimum_fill_value.

## Returns

amin : array_like

New array holding the result. If out was specified, out is returned.
See Also:
minimum_fill_value
Returns the minimum filling value for a given datatype.
MaskedArray.prod (axis=None, dtype=None, out=None)
Return the product of the array elements over the given axis. Masked elements are set to 1 internally for computation.

## Parameters

axis: \{None, int \}, optional
Axis over which the product is taken. If None is used, then the product is over all the array elements.
dtype : \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are multiplied. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : \{None, array \}, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type will be cast if necessary.

## Returns

product_along_axis : \{array, scalar\}, see dtype parameter above.
Returns an array whose shape is the same as a with the specified axis removed. Returns a 0 d array when a is 1 d or axis=None. Returns a reference to the specified output array if specified.

## See Also:

```
prod
    equivalent function
```


## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> np.prod([1.,2.])
2.0
>>> np.prod([1.,2.], dtype=np.int32)
2
>>> np.prod([[1.,2.],[3.,4.]])
24.0
>>> np.prod([[1.,2.],[3.,4.]], axis=1)
array([ 2., 12.])
```

MaskedArray.product (axis=None, dtype=None, out=None)

Return the product of the array elements over the given axis. Masked elements are set to 1 internally for computation.

## Parameters

axis: \{None, int \}, optional
Axis over which the product is taken. If None is used, then the product is over all the array elements.
dtype : \{None, dtype \}, optional
Determines the type of the returned array and of the accumulator where the elements are multiplied. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : \{None, array \}, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type will be cast if necessary.

## Returns

product_along_axis : \{array, scalar\}, see dtype parameter above.
Returns an array whose shape is the same as a with the specified axis removed. Returns a 0 d array when a is 1 d or axis=None. Returns a reference to the specified output array if specified.

## See Also:

prod
equivalent function

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> np.prod([1.,2.])
2.0
>>> np.prod([1.,2.], dtype=np.int 32)
```

```
2
>>> np.prod([[1.,2.],[3.,4.]])
24.0
>>> np.prod([[1.,2.],[3.,4.]], axis=1)
array([[ 2., 12.])
MaskedArray.ptp (axis=None,out=None, fill_value=None)
```

Return (maximum - minimum) along the the given dimension (i.e. peak-to-peak value).

## Parameters

axis : $\{$ None, int $\}$, optional
Axis along which to find the peaks. If None (default) the flattened array is used.
out : \{None, array_like\}, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.
fill_value : \{var\}, optional
Value used to fill in the masked values.

## Returns

ptp : ndarray.
A new array holding the result, unless out was specified, in which case a reference to out is returned.

MaskedArray. round (decimals=0, out=None)
Return $a$ with each element rounded to the given number of decimals.
Refer to numpy . around for full documentation.

## See Also:

numpy.around
equivalent function
MaskedArray.std (axis=None, dtype=None, out=None, $d$ dof=0)
Compute the standard deviation along the specified axis.
Returns the standard deviation, a measure of the spread of a distribution, of the array elements. The standard deviation is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Calculate the standard deviation of these values.
axis : int, optional
Axis along which the standard deviation is computed. The default is to compute the standard deviation of the flattened array.
dtype : dtype, optional
Type to use in computing the standard deviation. For arrays of integer type the default is float 64 , for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type (of the calculated values) will be cast if necessary.
ddof : int, optional
Means Delta Degrees of Freedom. The divisor used in calculations is $N$ - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

standard_deviation : ndarray, see dtype parameter above.
If out is None, return a new array containing the standard deviation, otherwise return a reference to the output array.

## See Also:

```
var, mean
```


## numpy.doc. ufuncs

Section "Output arguments"

## Notes

The standard deviation is the square root of the average of the squared deviations from the mean, i.e., std $=$ sqrt (mean (abs (x - x.mean()) $* * 2$ )).

The average squared deviation is normally calculated as $\mathrm{x} . \operatorname{sum}() / \mathrm{N}$, where $\mathrm{N}=$ len(x). If, however, $d d o f$ is specified, the divisor $N-d d o f$ is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of the infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables. The standard deviation computed in this function is the square root of the estimated variance, so even with $\operatorname{ddof}=1$, it will not be an unbiased estimate of the standard deviation per se.
Note that, for complex numbers, std takes the absolute value before squaring, so that the result is always real and nonnegative.

For floating-point input, the std is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higheraccuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.std(a)
1.1180339887498949
>>> np.std(a, axis=0)
array([ 1., 1.])
>> np.std(a, axis=1)
array([ 0.5, 0.5])
```

In single precision, $\operatorname{std}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.std(a)
0.45172946707416706
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.std(a, dtype=np.float64)
0.449999999925552653
MaskedArray.sum(axis=None, dtype=None,out=None)
```

Return the sum of the array elements over the given axis. Masked elements are set to 0 internally.

## Parameters

axis : $\{$ None, -1 , int $\}$, optional
Axis along which the sum is computed. The default (axis = None) is to compute over the flattened array.
dtype : \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are summed. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : \{None, ndarray \}, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

sum_along_axis : MaskedArray or scalar
An array with the same shape as self, with the specified axis removed. If self is a $0-\mathrm{d}$ array, or if axis is None, a scalar is returned. If an output array is specified, a reference to out is returned.

```
    Examples
        >>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
        >>> print x
        [[1 -- 3]
        [-- 5 --]
        [7 -- 9]]
        >>> print x.sum()
        25
        >>> print x.sum(axis=1)
    [4 5 16]
    >>> print x.sum(axis=0)
    [8 5 12]
    >>> print type(x.sum(axis=0, dtype=np.int64)[0])
    <type 'numpy.int64'>
MaskedArray.trace (offset=0, axisl=0, axis 2=1,dtype=None, out=None)
```

Return the sum along diagonals of the array.
Refer to numpy . trace for full documentation.

## See Also:

numpy.trace
equivalent function
MaskedArray.var (axis=None, dtype=None, out=None, ddof=0)
Compute the variance along the specified axis.
Returns the variance of the array elements, a measure of the spread of a distribution. The variance is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

## a : array_like

Array containing numbers whose variance is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the variance is computed. The default is to compute the variance of the flattened array.
dtype : data-type, optional
Type to use in computing the variance. For arrays of integer type the default is float32; for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output, but the type is cast if necessary.
ddof : int, optional
"Delta Degrees of Freedom": the divisor used in the calculation is N - ddof, where N represents the number of elements. By default ddof is zero.

## Returns

variance : ndarray, see dtype parameter above
If out=None, returns a new array containing the variance; otherwise, a reference to the output array is returned.

## See Also:

std
Standard deviation
mean
Average
numpy. doc.ufuncs
Section "Output arguments"

## Notes

The variance is the average of the squared deviations from the mean, i.e., var $=$ mean (abs ( $x-$ $x$.mean () ) $\star * 2$ ).

The mean is normally calculated as $x . \operatorname{sum}() / N$, where $N=$ len ( $x$ ). If, however, $d d o f$ is specified, the divisor N - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of a hypothetical infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables.

Note that for complex numbers, the absolute value is taken before squaring, so that the result is always real and nonnegative.

For floating-point input, the variance is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float 32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1,2],[3,4]])
>>> np.var(a)
1.25
>>> np.var(a,0)
array([ 1., 1.])
>>> np.var(a,1)
array([ 0.25, 0.25])
```

In single precision, var() can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.var(a)
0.20405951142311096
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.var(a, dtype=np.float64)
0.202499999932997387
>>> ((1-0.55)**2 + (0.1-0.55)**2)/2
0.202500000000000001
```


## Arithmetic and comparison operations

## Comparison operators:

```
MaskedArray.__lt__ x.__lt__(y) \(<==>x<y\)
MaskedArray.__le__ x.__le__(y) \(<==>x<=y\)
MaskedArray.__gt__ x.__gt__(y) <==>x>y
MaskedArray.__ge__ \(\quad\).__ge__(y) \(<==>x>=y\)
MaskedArray.__eq__(other) Check whether other equals self elementwise
MaskedArray.__ne__(other) Check whether other doesn't equal self elementwise
MaskedArray.__lt__()
    x.__lt__(y) \(<==>x<y\)
MaskedArray.__le__()
    x.__le__(y) <==> x \(<=y\)
MaskedArray.__gt_()
    x.__gt__(y) <==> x>y
MaskedArray.__ge__()
    x.__ge__(y) <==> x>=y
MaskedArray.__eq_(other)
Check whether other equals self elementwise
MaskedArray.__ne__(other)
Check whether other doesn't equal self elementwise
Truth value of an array (bool):
\begin{tabular}{|c|c|}
\hline MaskedArray.__nonzero__ & x.__nonzero__() <==> x !=0 \\
\hline \begin{tabular}{l}
MaskedArray.__nonzero__() \\
x.__nonzero__() <==> x != 0
\end{tabular} & \\
\hline
\end{tabular}
```


## Arithmetic:

| MaskedArray.__abs__(x) |  |
| :---: | :---: |
| MaskedArray.___add__(other) | Add other to self, and return a new masked array. |
| MaskedArray.__radd__(other) | Add other to self, and return a new masked array. |
| MaskedArray.__sub__(other) | Subtract other to self, and return a new masked array. |
| MaskedArray.__rsub__(other) | Subtract other to self, and return a new masked array. |
| MaskedArray.__mul__(other) | Multiply other by self, and return a new masked array. |
| MaskedArray.__rmul__(other) | Multiply other by self, and return a new masked array. |
| MaskedArray.__div__(other) | Divide other into self, and return a new masked array. |
| MaskedArray.__rdiv__ | x.__rdiv__(y) <==> y/x |
| MaskedArray.__truediv__(other) | Divide other into self, and return a new masked array. |
| MaskedArray.__rtruediv__(other) | Divide other into self, and return a new masked array. |
| MaskedArray.__floordiv__(other) | Divide other into self, and return a new masked array. |
| MaskedArray.__rfloordiv__(other) | Divide other into self, and return a new masked array. |
| MaskedArray.__mod | $x . \ldots \_m o d \_$( $y$ ) <==> $x \% y$ |
| MaskedArray.__rmod | x.__rmod__(y) <==> y\%x |
| MaskedArray.__divmod__(x, y) |  |
| MaskedArray.__rdivmod__(y, x) |  |
| MaskedArray.__pow__(other) | Raise self to the power other, masking the potential $\mathrm{NaNs} / \mathrm{Infs}$ |
| MaskedArray.__rpow__(other) | Raise self to the power other, masking the potential $\mathrm{NaNs} / \mathrm{Infs}$ |
| MaskedArray.__lshift_ | x.__lshift__(y) <==> $\mathrm{x} \ll \mathrm{y}$ |
| MaskedArray.__rlshift | x.__rlshift__(y) <==> y<<x |
| MaskedArray.__rshift | x.__rshift__(y) <==> $x \gg y$ |
| MaskedArray.__rrshift | x.__rrshift__(y) <==> y>>x |
| MaskedArray.__and_ | x.__and__(y) <==> x\&y |
| MaskedArray.__rand_ | x.__rand__(y) <==> y\&x |
| MaskedArray.__or__ | x.__or__(y) <==> x\|y |
| MaskedArray.__ror_ | x.__ror__(y) $<==>$ ylx |
| MaskedArray.__xor_ | x.__xor__(y) <==> $\mathrm{x}^{\wedge}$ y |
| MaskedArray.__rxor__ | x.__rxor__(y) <==> $y^{\wedge} x$ |

MaskedArray.__abs__()<==> $a b s(x)$

MaskedArray.__add__(other)
Add other to self, and return a new masked array.
MaskedArray•__radd__(other)
Add other to self, and return a new masked array.
MaskedArray.__sub__(other)
Subtract other to self, and return a new masked array.

```
MaskedArray.__rsub__(other)
```

Subtract other to self, and return a new masked array.

```
MaskedArray.__mul___(other)
```

Multiply other by self, and return a new masked array.
MaskedArray •__rmul__(other)
Multiply other by self, and return a new masked array.
MaskedArray.__div__(other)
Divide other into self, and return a new masked array.

```
MaskedArray.__rdiv__()
    \(x\).__rdiv__(y) <==> y/x
```

MaskedArray.__truediv__(other)
Divide other into self, and return a new masked array.
MaskedArray.__rtruediv__(other)
Divide other into self, and return a new masked array.
MaskedArray.__floordiv__(other)
Divide other into self, and return a new masked array.
MaskedArray.__rfloordiv__(other)
Divide other into self, and return a new masked array.

```
MaskedArray.__mod__()
```

x.__mod__(y) <==> x\%y

MaskedArray.__rmod__()
x.__rmod__(y) <==> y\%x

MaskedArray.__divmod__(y)<==>divmod(x,y)

MaskedArray.__rdivmod__(y)<==> $\operatorname{divmod}(y, x)$

MaskedArray.__pow__(other)
Raise self to the power other, masking the potential $\mathrm{NaNs} / \mathrm{Infs}$
MaskedArray.__rpow__(other)
Raise self to the power other, masking the potential $\mathrm{NaNs} /$ Infs
MaskedArray $\cdot \frac{\text { lshift__() }}{(\mathrm{y})<=\Rightarrow \mathrm{x} \ll \mathrm{y}}$
x.__lshift__(y) <==> x<<y

MaskedArray.__rlshift__()
x.__rlshift__(y) <==> $y \ll x$

MaskedArray.__rshift__()
x.__rshift__(y) <==> x>>y

MaskedArray.__rrshift__()
x.__rrshift__(y) <==> y>>x

MaskedArray.__and__()
x.__and__(y) <==> x\&y

MaskedArray.__rand__()
x.__rand__(y) <==> y\&x

MaskedArray.__or_()
x.__or__(y) <==> xly

MaskedArray.__ror__()
x.__ror__(y) <==> ylx

MaskedArray.__xor_()
x.__xor__(y) <==> $x^{\wedge} y$

MaskedArray.__rxor_()
$x$.__rxor__(y) <==> $y^{\wedge} x$

Arithmetic, in-place:

| MaskedArray.__iadd__(other) | Add other to self in-place. |
| :---: | :---: |
| MaskedArray.__isub__(other) | Subtract other from self in-place. |
| MaskedArray.__imul__(other) | Multiply self by other in-place. |
| MaskedArray.__idiv__(other) | Divide self by other in-place. |
| MaskedArray.__itruediv__(other) | True divide self by other in-place. |
| MaskedArray.__ifloordiv__(other) | Floor divide self by other in-place. |
| MaskedArray.__imod | x.__imod__(y) <==> x\%y |
| MaskedArray.__ipow__(other) | Raise self to the power other, in place. |
| MaskedArray.__ilshift__ | x.__ilshift__(y) <==> $\mathrm{x} \ll \mathrm{y}$ |
| MaskedArray.__irshift__ | x.__irshift__(y) <==> $x \gg y$ |
| MaskedArray.__iand__ | x.__iand__(y) <==> x\&y |
| MaskedArray.__ior_ | x.__ior__(y) <==> xly |
| MaskedArray.__ixor_ | x.__ixor__(y) <==> $x^{\wedge} \mathrm{y}$ |

MaskedArray.__iadd__(other)
Add other to self in-place.
MaskedArray.__isub__(other)
Subtract other from self in-place.
MaskedArray.__imul__(other)
Multiply self by other in-place.
MaskedArray.__idiv__(other)
Divide self by other in-place.
MaskedArray.__itruediv__(other)
True divide self by other in-place.
MaskedArray.__ifloordiv__(other)
Floor divide self by other in-place.
MaskedArray $\cdot$ _imod__()
x.__imod_(y) <==>x\%y

MaskedArray.__ipow__(other)
Raise self to the power other, in place.

```
MaskedArray.__ilshift__()
    x.__ilshift__(y)<==> x<<y
MaskedArray.__irshift__()
    x.__irshift__(y)<==> x>>y
MaskedArray.__iand__()
    x.__iand__(y) <==> x&y
MaskedArray.__ior__()
    x.__ior__(y)<==> xly
MaskedArray.__ixor__()
    x.__ixor__(y)<==> x^y
```


## Representation

| MaskedArray.__repr__() | Literal string representation. <br> MaskedArray._str__() |
| :--- | :--- |
| MaskedArray.ids () | Return the addresses of the data and mask areas. <br> MaskedArray.iscontiguous () <br> Return a boolean indicating whether the data is contiguous. |
| MaskedArray.__repr__() |  |
| Literal string representation. |  |
| MaskedArray.__str__() |  |
| String representation. |  |
| MaskedArray.ids () |  |
| Return the addresses of the data and mask areas. |  |

## Parameters

None :

## Examples

```
>>> x = np.ma.array([1, 2, 3], mask=[0, 1, 1])
>>> x.ids()
(166670640, 166659832)
```

If the array has no mask, the address of nomask is returned. This address is typically not close to the data in memory:

```
>>> x = np.ma.array([1, 2, 3])
>>> x.ids()
(166691080, 3083169284L)
```

MaskedArray.iscontiguous()

Return a boolean indicating whether the data is contiguous.

## Parameters

## None :

## Examples

```
>>> x = np.ma.array([1, 2, 3])
>>> x.iscontiguous()
True
```

iscontiguous returns one of the flags of the masked array:

```
>>> x.flags
    C_CONTIGUOUS : True
    F_CONTIGUOUS : True
    OWNDATA : False
    WRITEABLE : True
    ALIGNED : True
    UPDATEIFCOPY : False
```


## Special methods

For standard library functions:

```
MaskedArray.__copy__() Return a copy of the array.
MaskedArray.___deepcopy__([memo])
MaskedArray.__getstate__() Return the internal state of the masked array, for pickling
MaskedArray.__reduce__() Return a 3-tuple for pickling a MaskedArray.
MaskedArray.__setstate__(state) Restore the internal state of the masked array, for pickling purposes.
MaskedArray.__copy__([order])
    Return a copy of the array.
```


## Parameters

```
order : \{ 'C', 'F', 'A' \}, optional
If order is ' C ' (False) then the result is contiguous (default). If order is 'Fortran' (True) then the result has fortran order. If order is 'Any' (None) then the result has fortran order only if the array already is in fortran order.
MaskedArray.__deepcopy__(memo=None)
MaskedArray.__getstate__()
Return the internal state of the masked array, for pickling purposes.
MaskedArray.__reduce__()
Return a 3-tuple for pickling a MaskedArray.
MaskedArray.__setstate__(state)
Restore the internal state of the masked array, for pickling purposes. state is typically the output of the
```

$\qquad$
$\qquad$

``` output, and is a 5 -tuple:
-class name
-a tuple giving the shape of the data
-a typecode for the data
-a binary string for the data
-a binary string for the mask.
```

Basic customization:

```
MaskedArray.__new__
MaskedArray.__array__ a.__array__(ldtype) -> reference if type unchanged, copy
    MaskedArray.__array_wrap__(obj[, Special hook for ufuncs.
context])
MaskedArray.__array__()
    a.__array__(Idtype) -> reference if type unchanged, copy otherwise.
```

Returns either a new reference to self if dtype is not given or a new array of provided data type if dtype is different from the current dtype of the array.

MaskedArray.__array_wrap__(obj, context=None)
Special hook for ufuncs. Wraps the numpy array and sets the mask according to context.
Container customization: (see Indexing)

```
MaskedArray.__len__(x)
MaskedArray.__getitem__(indx) x.__getitem__(y)<==> x[y]
MaskedArray.__setitem__(indx, value) x.__setitem__(i, y)<==> x[i]=y
MaskedArray.__delitem___ x.__delitem__(y)<==> del x[y]
MaskedArray.__getslice__(i,j) x.__getslice__(i, j)<==> x[i:j]
MaskedArray.__setslice__(i, j, value) x.__setslice__(i, j, value)<==> x[i:j]=value
MaskedArray.__contains___ x.__contains__(y)<==> y in x
MaskedArray.__len__() <==> len(x)
MaskedArray.__getitem__(indx)
    x.__getitem__(y) <==> x[y]
```

Return the item described by $i$, as a masked array.

```
MaskedArray.__setitem__(indx,value)
```

    \(x\).__setitem__(i, y) \(<==>x[i]=y\)
    Set item described by index. If value is masked, masks those locations.

```
MaskedArray.__delitem__()
    x.__delitem__(y)<==> del x[y]
MaskedArray.__getslice__(i,j)
    x.__getslice__(i,j) <==> x[i:j]
```

Return the slice described by ( $\mathrm{i}, \mathrm{j}$ ). The use of negative indices is not supported.

```
MaskedArray.__setslice__(i,j,value)
```

    \(x\).__setslice__(i, j, value) \(<==>x[i ; j]=\) value
    Set the slice $(i, j)$ of a to value. If value is masked, mask those locations.
MaskedArray.__contains__()
x.__contains__(y) <==> y in $x$

## Specific methods

## Handling the mask

The following methods can be used to access information about the mask or to manipulate the mask.

```
MaskedArray.__setmask__(mask[, copy]) Set the mask.
MaskedArray.harden_mask() Force the mask to hard.
MaskedArray.soften_mask() Force the mask to soft.
MaskedArray.unshare_mask() Copy the mask and set the sharedmask flag to False.
MaskedArray.shrink_mask() Reduce a mask to nomask when possible.
MaskedArray.__setmask__(mask, copy=False)
    Set the mask.
MaskedArray.harden_mask()
```

Force the mask to hard.
Whether the mask of a masked array is hard or soft is determined by its hardmask property. harden_mask sets hardmask to True.

See Also:
hardmask

```
MaskedArray.soften_mask()
```

Force the mask to soft.
Whether the mask of a masked array is hard or soft is determined by its hardmask property. soften_mask sets hardmask to False.

## See Also:

hardmask
MaskedArray.unshare_mask ()
Copy the mask and set the sharedmask flag to False.
Whether the mask is shared between masked arrays can be seen from the sharedmask property. unshare_mask ensures the mask is not shared. A copy of the mask is only made if it was shared.

## See Also:

sharedmask
MaskedArray.shrink_mask()
Reduce a mask to nomask when possible.

## Parameters

None :

## Returns

None :

## Examples

```
>>> x = np.ma.array([[1,2 ], [3, 4]], mask=[0]*4)
>>> x.mask
array([[False, False],
                    [False, False]], dtype=bool)
>>> x.shrink_mask()
>>> x.mask
False
```

Handling the fill_value

| MaskedArray.get_fill_value() | Return the filling value of the masked array. |
| :--- | :--- |
| MaskedArray.set_fill_value([value]) | Set the filling value of the masked array. |

MaskedArray.get_fill_value()

Return the filling value of the masked array.

## Returns

fill_value : scalar
The filling value.

## Examples

```
>>> for dt in [np.int32, np.int64, np.float64, np.complex128]:
... np.ma.array([0, 1], dtype=dt).get_fill_value()
..
999999
999999
1e+20
(1e+20+0j)
```

```
>>> x = np.ma.array([0, 1.], fill_value=-np.inf)
>>> x.get_fill_value()
-inf
MaskedArray.set_fill_value (value=None)
```

    Set the filling value of the masked array.
    
## Parameters

 value : scalar, optionalThe new filling value. Default is None, in which case a default based on the data type is used.

## See Also:

ma.set_fill_value
Equivalent function.

## Examples

```
>>> x = np.ma.array([0, 1.], fill_value=-np.inf)
>>> x.fill_value
-inf
>>> x.set_fill_value(np.pi)
>>> x.fill_value
3.1415926535897931
```

Reset to default:

```
>>> x.set_fill_value()
>>> x.fill_value
1e+20
```


## Counting the missing elements

MaskedArray. count ([axis]) Count the non-masked elements of the array along the given axis.
MaskedArray.count (axis=None)
Count the non-masked elements of the array along the given axis.

## Parameters

 axis : int, optionalAxis along which to count the non-masked elements. If axis is None, all non-masked elements are counted.

## Returns

result : int or ndarray
If axis is None, an integer count is returned. When axis is not None, an array with shape determined by the lengths of the remaining axes, is returned.

## See Also:

count_masked
Count masked elements in array or along a given axis.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.arange(6).reshape((2, 3))
>>> a[1, :] = ma.masked
>>> a
masked_array(data =
    [[\begin{array}{lll}{0}&{1}&{2]}\end{array}]
    [-- -- --]],
    mask =
    [[False False False]
    [ True True True]],
        fill_value = 999999)
>>> a.count()
3
```

When the axis keyword is specified an array of appropriate size is returned.

```
>>> a.count(axis=0)
array([1, 1, 1])
>>> a.count(axis=1)
array([3, 0])
```


### 1.6.7 Masked array operations

## Constants

ma. MaskType Numpy's Boolean type. Character code: ?. Alias: bool8
numpy.ma.MaskType
alias of bool_

## Creation

## From existing data

```
ma.masked_array
ma.array(data[, dtype, copy, order, mask, ...])
ma.copy
An array class with possibly masked values.
An array class with possibly masked values.
copy
ma.frombuffer(buffer[, dtype, count, offset])
ma.fromfunction(function, shape, **kwargs)
Interpret a buffer as a 1-dimensional array.
Construct an array by executing a function over each coordinate.
Return a copy of the array.
```

numpy.ma.masked_array
alias of MaskedArray
numpy.ma.array (data, dtype=None, copy=False, order=False, mask=False, fill_value=None,
keep_mask=True, hard_mask=False, shrink=True, subok=True, $n d$ min=0)

An array class with possibly masked values.
Masked values of True exclude the corresponding element from any computation.
Construction:
$\mathrm{x}=$ MaskedArray(data, mask=nomask, dtype=None,
copy=False, subok=True, ndmin=0, fill_value=None, keep_mask=True, hard_mask=None, shrink=True)

## Parameters

data : array_like
Input data.
mask : sequence, optional
Mask. Must be convertible to an array of booleans with the same shape as data. True indicates a masked (i.e. invalid) data.
dtype : dtype, optional
Data type of the output. If dtype is None, the type of the data argument (data.dt ype) is used. If dtype is not None and different from data. dt ype, a copy is performed.
copy : bool, optional
Whether to copy the input data (True), or to use a reference instead. Default is False.
subok : bool, optional
Whether to return a subclass of MaskedArray if possible (True) or a plain MaskedArray. Default is True.
ndmin : int, optional
Minimum number of dimensions. Default is 0 .
fill_value : scalar, optional
Value used to fill in the masked values when necessary. If None, a default based on the data-type is used.
keep_mask : bool, optional
Whether to combine mask with the mask of the input data, if any (True), or to use only mask for the output (False). Default is True.
hard_mask : bool, optional
Whether to use a hard mask or not. With a hard mask, masked values cannot be unmasked. Default is False.
shrink : bool, optional
Whether to force compression of an empty mask. Default is True.

```
numpy.ma.copy
    copy a.copy(order='C')
        Return a copy of the array.
```


## Parameters

```
order : \{ 'C', 'F', 'A'\}, optional has the same order as the input.
```


## Examples

```
>>> x = np.array([[1,2,3],[4,5,6]], order='F')
```

>>> x = np.array([[1,2,3],[4,5,6]], order='F')
>>> y = x.copy()

```
    >>> y = x.copy()
```

By default, the result is stored in C-contiguous (row-major) order in memory. If order is $F$, the result has 'Fortran' (column-major) order. If order is 'A' ('Any'), then the result

```
>>> x.fill(0)
>>> x
array([[0, 0, 0],
    [0, 0, 0]])
>>> y
array([[1, 2, 3],
    [4, 5, 6]])
>>> y.flags['C_CONTIGUOUS' ]
True
```

numpy.ma.frombuffer (buffer, dtype=float, count=-1, offset=0)

Interpret a buffer as a 1-dimensional array.

```
Parameters
        buffer : buffer_like
```

An object that exposes the buffer interface.
dtype : data-type, optional
Data-type of the returned array; default: float.
count : int, optional
Number of items to read. -1 means all data in the buffer.
offset : int, optional
Start reading the buffer from this offset; default: 0 .

## Notes

If the buffer has data that is not in machine byte-order, this should be specified as part of the data-type, e.g.:

```
>>> dt = np.dtype(int)
>>> dt = dt.newbyteorder('>')
>>> np.frombuffer(buf, dtype=dt)
```

The data of the resulting array will not be byteswapped, but will be interpreted correctly.

## Examples

```
>>> s = 'hello world'
>>> np.frombuffer(s, dtype='S1', count=5, offset=6)
array(['w', 'o', 'r', 'l', 'd'],
    dtype='|S1')
```

numpy.ma.fromfunction (function, shape, **kwargs)
Construct an array by executing a function over each coordinate.
The resulting array therefore has a value $f(\mathrm{n}, \mathrm{y}, \mathrm{z})$ at coordinate $(\mathrm{x}, \mathrm{y}, \mathrm{z})$.

## Parameters

function : callable
The function is called with N parameters, each of which represents the coordinates of the array varying along a specific axis. For example, if shape were $(2,2)$, then the parameters would be two arrays, [ [0, 0], [1, 1] ] and [ [0, 1], [0, 1] ]. function must be capable of operating on arrays, and should return a scalar value.
shape : ( N, ) tuple of ints
Shape of the output array, which also determines the shape of the coordinate arrays passed to function.
dtype : data-type, optional
Data-type of the coordinate arrays passed to function. By default, dtype is float.

## Returns

out : any
The result of the call to function is passed back directly. Therefore the type and shape of out is completely determined by function.

## See Also:

```
indices,meshgrid
```


## Notes

Keywords other than shape and dtype are passed to function.

## Examples

```
>>> np.fromfunction(lambda i, j: i == j, (3, 3), dtype=int)
array([[ True, False, False],
            [False, True, False],
            [False, False, True]], dtype=bool)
>>> np.fromfunction(lambda i, j: i + j, (3, 3), dtype=int)
array([[0, 1, 2],
            [1, 2, 3],
            [2, 3, 4]])
```

MaskedArray. copy (order='C')

Return a copy of the array.

## Parameters

order : \{ 'C', 'F', 'A'\}, optional
By default, the result is stored in C-contiguous (row-major) order in memory. If order is $F$, the result has 'Fortran' (column-major) order. If order is 'A' ('Any'), then the result has the same order as the input.

## Examples

```
>>> x = np.array([[1,2,3],[4,5,6]], order='F')
>>> y = x.copy()
>>> x.fill(0)
>>> x
array([[0, 0, 0],
                            [0, 0, 0]])
>>> y
array([[1, 2, 3],
            [4, 5, 6]])
```

```
>>> y.flags['C_CONTIGUOUS']
True
```


## Ones and zeros

ma. empty(shape[, dtype, order])
ma.empty_like(a[, dtype, order, subok])
ma.masked_all(shape[, dtype])
ma.masked_all_like(arr)
ma. ones(shape[, dtype, order])
ma.zeros(shape[, dtype, order])

Return a new array of given shape and type, without initializing entries.
Return a new array with the same shape and type as a given array.
Empty masked array with all elements masked.
Empty masked array with the properties of an existing array.
Return a new array of given shape and type, filled with ones.
Return a new array of given shape and type, filled with zeros.
numpy . ma . empty (shape, dtype =float, order= 'C')
Return a new array of given shape and type, without initializing entries.

## Parameters

shape : int or tuple of int
Shape of the empty array
dtype : data-type, optional
Desired output data-type.
order : \{ 'C', 'F' \}, optional
Whether to store multi-dimensional data in C (row-major) or Fortran (column-major) order in memory.

## See Also:

empty_like, zeros, ones

## Notes

empty, unlike zeros, does not set the array values to zero, and may therefore be marginally faster. On the other hand, it requires the user to manually set all the values in the array, and should be used with caution.

## Examples

```
>>> np.empty([2, 2])
array([[ -9.74499359e+001, 6.69583040e-309],
    [ 2.13182611e-314, 3.06959433e-309]]) #random
>>> np.empty([2, 2], dtype=int)
array([[-1073741821, -1067949133],
    [ 496041986, 19249760]]) #random
```

numpy.ma.empty_like ( $a$, dtype=None, order='K', subok=True)
Return a new array with the same shape and type as a given array.

## Parameters

a : array_like
The shape and data-type of $a$ define these same attributes of the returned array
dtype : data-type, optional
Overrides the data type of the result.
order : \{ 'C', 'F', 'A', or 'K'\}, optional

Overrides the memory layout of the result. 'C' means C-order, ' F ' means F-order, 'A' means ' F ' if a is Fortran contiguous, ' C ' otherwise. ' K ' means match the layout of a as closely as possible.
subok: bool, optional.
If True, then the newly created array will use the sub-class type of ' $a$ ', otherwise it will be a base-class array. Defaults to True.

Returns
out : ndarray
Array of uninitialized (arbitrary) data with the same shape and type as $a$.

## See Also:

## ones_like

Return an array of ones with shape and type of input.

```
zeros_like
```

Return an array of zeros with shape and type of input.

```
empty
```

Return a new uninitialized array.
ones
Return a new array setting values to one.

```
zeros
```

Return a new array setting values to zero.

## Notes

This function does not initialize the returned array; to do that use zeros_like or ones_like instead. It may be marginally faster than the functions that do set the array values.

## Examples

```
>>> a = ([1,2,3], [4,5,6]) # a is array-like
>>> np.empty_like(a)
array([[-1073741821, -1073741821, 3], #random
[ 0, 0, -1073741821]])
>>> a = np.array([[1., 2., 3.],[4.,5.,6.]])
>>> np.empty_like(a)
array([[ -2.00000715e+000, 1.48219694e-323, -2.00000572e+000],#random
    [4.38791518e-305, -2.00000715e+000, 4.17269252e-309]])
```

numpy.ma.masked_all (shape, dtype=<type 'float'>)
Empty masked array with all elements masked.
Return an empty masked array of the given shape and dtype, where all the data are masked.

## Parameters

shape : tuple
Shape of the required MaskedArray.
dtype : dtype, optional
Data type of the output.

## Returns

a : MaskedArray

A masked array with all data masked.
See Also:

```
masked_all_like
```

Empty masked array modelled on an existing array.

## Examples

```
>>> import numpy.ma as ma
>>> ma.masked_all((3, 3))
masked_array(data =
    [[-- -- --]
    [-- -- --]
    [-- -- --]],
            mask =
    [[ True True True]
    [ True True True]
    [ True True True]],
            fill_value=1e+20)
```

The dtype parameter defines the underlying data type.

```
>>> a = ma.masked_all((3, 3))
>>> a.dtype
dtype('float64')
>>> a = ma.masked_all((3, 3), dtype=np.int32)
>>> a.dtype
dtype('int32')
numpy.ma.masked_all_like (arr)
```

Empty masked array with the properties of an existing array.
Return an empty masked array of the same shape and dtype as the array arr, where all the data are masked.

## Parameters

arr : ndarray
An array describing the shape and dtype of the required MaskedArray.

## Returns

a : MaskedArray
A masked array with all data masked.

## Raises

## AttributeError :

If $\operatorname{arr}$ doesn't have a shape attribute (i.e. not an ndarray)

## See Also:

masked_all
Empty masked array with all elements masked.

## Examples

```
>>> import numpy.ma as ma
>>> arr = np.zeros((2, 3), dtype=np.float32)
>>> arr
array([[ 0., 0., 0.],
```

```
            [ 0., 0., 0.]], dtype=float32)
>>> ma.masked_all_like(arr)
masked_array(data =
    [[-- -- --]
    [-- -- --]],
            mask =
    [[ True True True]
    [ True True True]],
            fill_value=1e+20)
```

The dtype of the masked array matches the dtype of arr.

```
>>> arr.dtype
dtype('float32')
>>> ma.masked_all_like(arr).dtype
dtype('float32')
numpy.ma. ones (shape, dtype \(=\) None, order \(=\) ' \(C\) ')
```

Return a new array of given shape and type, filled with ones.
Please refer to the documentation for zeros for further details.

## See Also:

zeros, ones_like

## Examples

```
>>> np.ones(5)
array([ 1., 1., 1., 1., 1.])
>>> np.ones((5,), dtype=np.int)
array([1, 1, 1, 1, 1])
>>> np.ones((2, 1))
array([[ 1.],
            [ 1.]])
>>> s = (2,2)
>>> np.ones(s)
array([[ 1., 1.],
    [ 1., 1.]])
```

numpy .ma. zeros (shape, dtype $=$ float, order $=$ ' $C$ ')
Return a new array of given shape and type, filled with zeros.

## Parameters

shape : int or sequence of ints
Shape of the new array, e.g., $(2,3)$ or 2.
dtype : data-type, optional
The desired data-type for the array, e.g., numpy.int8. Default is numpy.float 64.
order : \{ 'C', 'F' $\}$, optional
Whether to store multidimensional data in C- or Fortran-contiguous (row- or columnwise) order in memory.

## Returns

out : ndarray

Array of zeros with the given shape, dtype, and order.

## See Also:

## zeros_like

Return an array of zeros with shape and type of input.

## ones_like

Return an array of ones with shape and type of input.

```
empty_like
```

Return an empty array with shape and type of input.
ones
Return a new array setting values to one.

```
empty
```

Return a new uninitialized array.

## Examples

```
>>> np.zeros(5)
array([ 0., 0., 0., 0., 0.])
>>> np.zeros((5,), dtype=numpy.int)
array([0, 0, 0, 0, 0])
>>> np.zeros((2, 1))
array([[ 0.],
            [ 0.]])
>>> s = (2,2)
>>> np.zeros(s)
array([[ 0., 0.],
            [ 0., 0.]])
>>> np.zeros((2,), dtype=[('x', 'i4'), ('y', 'i4')]) # custom dtype
array([(0, 0), (0, 0)],
            dtype=[('x', '<i4'), ('y', '<i4')])
```


## Inspecting the array

```
ma.all(self[, axis,out]) Check if all of the elements of a are true.
ma.any(self[, axis, out]) Check if any of the elements of }a\mathrm{ are true.
ma.count(a[, axis])
ma.count_masked(arr[, axis])
ma.getmask(a)
ma.getmaskarray(arr)
ma.getdata(a[, subok])
ma.nonzero(self)
ma.shape(obj)
ma.size(obj[, axis])
ma.MaskedArray.data
ma.MaskedArray.mask
ma.MaskedArray.recordmask Return the mask of the records.
ma.MaskedArray.all([axis,out]) Check if all of the elements of a are true.
ma.MaskedArray.any([axis,out]) Check if any of the elements of a are true.
ma.MaskedArray.count([axis]) Count the non-masked elements of the array along the given axis.
ma.MaskedArray.nonzero() Return the indices of unmasked elements that are not zero.
ma.shape(obj) Return the shape of an array.
ma.size(obj[,axis]) Return the number of elements along a given axis.
```

numpy.ma.all (self, axis=None, out=None)
Check if all of the elements of $a$ are true.
Performs a logical_and over the given axis and returns the result. Masked values are considered as True during computation. For convenience, the output array is masked where ALL the values along the current axis are masked: if the output would have been a scalar and that all the values are masked, then the output is masked.

## Parameters

axis : $\{$ None, integer $\}$
Axis to perform the operation over. If None, perform over flattened array.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## See Also:

all
equivalent function

## Examples

```
>>> np.ma.array([1,2,3]).all()
True
>>> a = np.ma.array([1,2,3], mask=True)
>>> (a.all() is np.ma.masked)
True
```

numpy .ma. any (self, axis=None, out=None)
Check if any of the elements of $a$ are true.
Performs a logical_or over the given axis and returns the result. Masked values are considered as False during computation.

## Parameters

axis : \{None, integer\}
Axis to perform the operation over. If None, perform over flattened array and return a scalar.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

```
    See Also:
    any
        equivalent function
numpy.ma.count (a, axis=None)
    Count the non-masked elements of the array along the given axis.
```


## Parameters

axis : int, optional
Axis along which to count the non-masked elements. If axis is None, all non-masked elements are counted.

## Returns

result : int or ndarray
If axis is None, an integer count is returned. When axis is not None, an array with shape determined by the lengths of the remaining axes, is returned.

## See Also:

count_masked
Count masked elements in array or along a given axis.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.arange(6).reshape((2, 3))
>>> a[1, :] = ma.masked
>>> a
masked_array(data =
    [[00 1 2]
    [-- -- --]],
        mask =
    [[False False False]
    [ True True True]],
                    fill_value = 999999)
>>> a.count()
3
```

When the axis keyword is specified an array of appropriate size is returned.

```
>>> a.count(axis=0)
array([1, 1, 1])
>>> a.count(axis=1)
array([3, 0])
```

numpy.ma.count_masked (arr, axis=None)
Count the number of masked elements along the given axis.

## Parameters

arr : array_like
An array with (possibly) masked elements.
axis : int, optional
Axis along which to count. If None (default), a flattened version of the array is used.

## Returns

count : int, ndarray
The total number of masked elements (axis=None) or the number of masked elements along each slice of the given axis.

## See Also:

MaskedArray. count
Count non-masked elements.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(9).reshape((3,3))
>>> a = ma.array(a)
>>> a[1, 0] = ma.masked
>>> a[1, 2] = ma.masked
>>> a[2, 1] = ma.masked
>>> a
masked_array(data =
    [[l0
    [-- 4 -- ]
    [6 -- 8]],
            mask =
    [[False False False]
    [ True False True]
    [False True False]],
            fill_value=999999)
>>> ma.count_masked(a)
3
```

When the axis keyword is used an array is returned.

```
>>> ma.count_masked(a, axis=0)
array([1, 1, 1])
>>> ma.count_masked(a, axis=1)
array([0, 2, 1])
```

numpy.ma.getmask (a)
Return the mask of a masked array, or nomask.
Return the mask of $a$ as an ndarray if $a$ is a MaskedArray and the mask is not nomask, else return nomask. To guarantee a full array of booleans of the same shape as a, use getmaskarray.

## Parameters

a: array_like
Input MaskedArray for which the mask is required.

## See Also:

```
getdata
```

Return the data of a masked array as an ndarray.

```
getmaskarray
```

Return the mask of a masked array, or full array of False.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.masked_equal([[1,2],[3,4]], 2)
>>> a
masked_array(data =
        [[1 -- ]
        [3 4]],
            mask =
        [[False True]
        [False False]],
            fill_value=999999)
>>> ma.getmask(a)
array([[False, True],
            [False, False]], dtype=bool)
```

Equivalently use the MaskedArray mask attribute.

```
>>> a.mask
array([[False, True],
    [False, False]], dtype=bool)
```

Result when mask $==$ nomask

```
>>> b = ma.masked_array([[1,2],[3,4]])
>>> b
masked_array(data =
    [[1 2]
    [3 4]],
                mask =
    False,
            fill_value=999999)
>>> ma.nomask
False
>>> ma.getmask(b) == ma.nomask
True
>>> b.mask == ma.nomask
True
```

numpy.ma.getmaskarray (arr)
Return the mask of a masked array, or full boolean array of False.
Return the mask of arr as an ndarray if arr is a MaskedArray and the mask is not nomask, else return a full boolean array of False of the same shape as arr.

## Parameters

arr : array_like
Input MaskedArray for which the mask is required.

## See Also:

getmask
Return the mask of a masked array, or nomask.
getdata
Return the data of a masked array as an ndarray.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.masked_equal([[1,2],[3,4]], 2)
>>> a
masked_array(data =
    [[ll --]
    [3 4]],
                mask =
    [[False True]
    [False False]],
                fill_value=999999)
>>> ma.getmaskarray(a)
array([[False, True],
                    [False, False]], dtype=bool)
```

Result when mask $==$ nomask

```
>>> b = ma.masked_array([[1,2], [3,4]])
```

$\ggg b$
masked_array(data =
[ $\left[\begin{array}{ll}1 & 2\end{array}\right]$
$\left[\begin{array}{ll}3 & 4\end{array}\right]$,
mask =
False,
fill_value=999999)
>>\ggma.getmaskarray (b)
array([[False, False],
[False, False]], dtype=bool)
numpy.ma.getdata ( $a$, subok=True)
Return the data of a masked array as an ndarray.
Return the data of $a$ (if any) as an ndarray if $a$ is a MaskedArray, else return $a$ as a ndarray or subclass (depending on subok) if not.

## Parameters

a: array_like
Input MaskedArray, alternatively a ndarray or a subclass thereof.
subok: bool
Whether to force the output to be a pure ndarray (False) or to return a subclass of ndarray if appropriate (True, default).

## See Also:

getmask
Return the mask of a masked array, or nomask.
getmaskarray
Return the mask of a masked array, or full array of False.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.masked_equal([[1,2],[3,4]], 2)
>>> a
masked_array(data =
    [[\begin{array}{ll}{1}&{--}\end{array}]
    [3 4]],
        mask =
    [[False True]
    [False False]],
            fill_value=999999)
>>> ma.getdata(a)
array([[1, 2],
            [3, 4]])
```

Equivalently use the MaskedArray data attribute.

```
>>> a.data
array([[1, 2],
    [3, 4]])
```

numpy.ma.nonzero (self)
Return the indices of unmasked elements that are not zero.
Returns a tuple of arrays, one for each dimension, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

```
a[a.nonzero()]
```

To group the indices by element, rather than dimension, use instead:

```
np.transpose(a.nonzero())
```

The result of this is always a 2d array, with a row for each non-zero element.

## Parameters

## None :

## Returns

tuple_of_arrays : tuple
Indices of elements that are non-zero.

## See Also:

numpy.nonzero
Function operating on ndarrays.

## flatnonzero

Return indices that are non-zero in the flattened version of the input array.
ndarray. nonzero
Equivalent ndarray method.
count_nonzero
Counts the number of non-zero elements in the input array.

## Examples

```
>>> import numpy.ma as ma
>>> x = ma.array(np.eye(3))
>>> x
masked_array(data =
    [[ 1. 0. 0.]
    [ 0. 1. 0.]
    [ 0. 0. 1.]],
        mask =
    False,
        fill_value=1e+20)
>>> x.nonzero()
(array([0, 1, 2]), array([0, 1, 2]))
```

Masked elements are ignored.

```
>>> x[1, 1] = ma.masked
>>> x
masked_array(data =
    [[ll.0 0.0 0.0]
    [0.0 -- 0.0]
    [0.0 0.0 1.0]],
            mask =
    [[False False False]
    [False True False]
    [False False False]],
        fill_value=1e+20)
>>> x.nonzero()
(array([0, 2]), array([0, 2]))
```

Indices can also be grouped by element.

```
>>> np.transpose(x.nonzero())
array([[0, 0],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , ma.nonzero( $a>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a = ma.array([[1,2,3],[4,5,6],[7, 8,9]])
>>> a > 3
masked_array(data =
    [[False False False]
    [ True True True]
    [ True True True]],
        mask =
    False,
        fill_value=999999)
>>> ma.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the condition array can also be called.

```
>>> (a > 3).nonzero()
```

(array ([1, 1, 1, 2, 2, 2]), array ([0, 1, 2, 0, 1, 2]))
numpy.ma.shape (obj)
Return the shape of an array.

## Parameters

a: array_like
Input array.

## Returns

shape : tuple of ints
The elements of the shape tuple give the lengths of the corresponding array dimensions.

```
    See Also:
    alen
ndarray.shape
        Equivalent array method.
    Examples
    >>> np.shape(np.eye(3))
    (3, 3)
    >>> np.shape([[1, 2]])
    (1, 2)
    >>> np.shape([0])
    (1,)
    >>> np.shape(0)
    ()
    >>> a = np.array([(1, 2), (3, 4)], dtype=[('x', 'i4'), ('y', 'i4')])
    >>> np.shape(a)
    (2,)
    >>> a.shape
    (2,)
numpy.ma.size(obj, axis=None)
Return the number of elements along a given axis.
```


## Parameters

``` a: array_like
Input data.
axis : int, optional
```

Axis along which the elements are counted. By default, give the total number of elements.

## Returns

element_count : int
Number of elements along the specified axis.

## See Also:

shape
dimensions of array
ndarray.shape
dimensions of array
ndarray.size
number of elements in array

## Examples

```
>>> a = np.array([[1,2,3],[4,5,6]])
>>> np.size(a)
6
>>> np.size(a,1)
3
>>> np.size(a,0)
2
```

MaskedArray.data
Return the current data, as a view of the original underlying data.

```
MaskedArray.mask
```

Mask
MaskedArray. recordmask
Return the mask of the records. A record is masked when all the fields are masked.
MaskedArray.all (axis=None, out=None)
Check if all of the elements of $a$ are true.
Performs a logical_and over the given axis and returns the result. Masked values are considered as True during computation. For convenience, the output array is masked where ALL the values along the current axis are masked: if the output would have been a scalar and that all the values are masked, then the output is masked.

## Parameters

 axis: \{None, integer \}Axis to perform the operation over. If None, perform over flattened array.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## See Also:

all
equivalent function

## Examples

```
>>> np.ma.array([1,2,3]).all()
True
>>> a = np.ma.array([1,2,3], mask=True)
>>> (a.all() is np.ma.masked)
True
```

MaskedArray any (axis=None, out=None)
Check if any of the elements of $a$ are true.
Performs a logical_or over the given axis and returns the result. Masked values are considered as False during computation.

## Parameters

axis: \{None, integer \}
Axis to perform the operation over. If None, perform over flattened array and return a scalar.
out : \{None, array \}, optional

Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## See Also:

any
equivalent function

MaskedArray. count (axis=None)
Count the non-masked elements of the array along the given axis.

## Parameters

axis : int, optional
Axis along which to count the non-masked elements. If axis is None, all non-masked elements are counted.

## Returns

result : int or ndarray
If axis is None, an integer count is returned. When axis is not None, an array with shape determined by the lengths of the remaining axes, is returned.

## See Also:

```
    count_masked
```

Count masked elements in array or along a given axis.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.arange(6).reshape((2, 3))
>>> a[1, :] = ma.masked
>>> a
masked_array(data =
            [[0 1 2]
            [-- -- --]],
                        mask =
            [[False False False]
            [ True True True]],
                    fill_value = 999999)
>>> a.count()
3
```

When the axis keyword is specified an array of appropriate size is returned.

```
>>> a.count (axis=0)
array([1, 1, 1])
>>> a.count(axis=1)
array([3, 0])
```


## MaskedArray.nonzero()

Return the indices of unmasked elements that are not zero.
Returns a tuple of arrays, one for each dimension, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

```
a[a.nonzero()]
```

To group the indices by element, rather than dimension, use instead:

```
np.transpose(a.nonzero())
```

The result of this is always a 2d array, with a row for each non-zero element.

## Parameters

None :

## Returns

tuple_of_arrays : tuple
Indices of elements that are non-zero.

## See Also:

numpy.nonzero
Function operating on ndarrays.

## flatnonzero

Return indices that are non-zero in the flattened version of the input array.

```
ndarray.nonzero
```

Equivalent ndarray method.

```
count_nonzero
```

Counts the number of non-zero elements in the input array.

## Examples

```
>>> import numpy.ma as ma
>>> x = ma.array(np.eye(3))
>>> x
masked_array(data =
    [[ 1. 0. 0.]
    [ 0. 1. 0.]
    [ 0. 0. 1.]],
        mask =
    False,
        fill_value=1e+20)
>>> x.nonzero()
(array([0, 1, 2]), array([0, 1, 2]))
```

Masked elements are ignored.

```
>>> x[1, 1] = ma.masked
>>> x
masked_array(data =
    [[1.0 0.0 0.0]
    [0.0 -- 0.0]
    [0.0 0.0 1.0]],
            mask =
    [[False False False]
    [False True False]
    [False False False]],
            fill_value=1e+20)
>>> x.nonzero()
(array([0, 2]), array([0, 2]))
```

Indices can also be grouped by element.

```
>>> np.transpose(x.nonzero())
array([[0, 0],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , ma.nonzero( $a>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a ma.array([[1,2,3],[4,5,6],[7, 8,9]])
>>> a > 3
masked_array(data =
    [[False False False]
    [ True True True]
    [ True True True]],
            mask =
    False,
        fill_value=999999)
>>> ma.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the condition array can also be called.

```
>>> (a > 3).nonzero()
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

numpy.ma.shape (obj)
Return the shape of an array.

## Parameters

a: array_like
Input array.

## Returns

shape : tuple of ints
The elements of the shape tuple give the lengths of the corresponding array dimensions.
See Also:
alen
ndarray.shape
Equivalent array method.

## Examples

```
>>> np.shape(np.eye(3))
(3, 3)
>>> np.shape([[1, 2]])
(1, 2)
>>> np.shape([0])
(1,)
>>> np.shape(0)
()
>>> a = np.array([(1, 2), (3, 4)], dtype=[('x', 'i4'), ('y', 'i4')])
>>> np.shape(a)
(2,)
>>> a.shape
(2,)
```

numpy.ma.size (obj, axis=None)
Return the number of elements along a given axis.

## Parameters

a : array_like
Input data.
axis : int, optional
Axis along which the elements are counted. By default, give the total number of elements.

## Returns

element_count : int
Number of elements along the specified axis.

## See Also:

shape
dimensions of array
ndarray.shape
dimensions of array
ndarray.size
number of elements in array
Examples
>>> a = np.array ([[1, 2, 3], [4, 5, 6] ])
>>> np.size(a)
6
>>> np.size(a,1)
3
>>> np.size(a,0)
2

## Manipulating a MaskedArray

Changing the shape

```
ma.ravel(self)
ma.reshape(a, new_shape[, order])
ma.resize(x, new_shape)
ma.MaskedArray.flatten([order])
ma.MaskedArray.ravel()
ma.MaskedArray.reshape(*s, **kwargs)
ma.MaskedArray.resize(newshape[, refcheck,
...])
```

```
numpy.ma.ravel (self)
```

Returns a 1D version of self, as a view.

## Returns

## MaskedArray :

Output view is of shape (self.size,) (or
(np.ma.product (self.shape), ).

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 -- ]
    [7 -- 9]]
>>> print x.ravel()
[1 -- 3 -- 5 -- 7 -- 9]
```

numpy.ma.reshape (a, new_shape, order='C')
Returns an array containing the same data with a new shape.
Refer to MaskedArray.reshape for full documentation.
See Also:

MaskedArray.reshape
equivalent function
numpy.ma.resize ( $x$, new_shape)
Return a new masked array with the specified size and shape.
This is the masked equivalent of the numpy. resize function. The new array is filled with repeated copies of $x$ (in the order that the data are stored in memory). If $x$ is masked, the new array will be masked, and the new mask will be a repetition of the old one.

## See Also:

```
numpy.resize
```

Equivalent function in the top level NumPy module.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.array([[1, 2] ,[3, 4]])
>>> a[0, 1] = ma.masked
>>> a
masked_array(data =
    [[\begin{array}{ll}{1}&{--}\end{array}]
    [3 4]],
                                    mask =
    [[False True]
    [False False]],
                    fill_value = 999999)
>>> np.resize(a, (3, 3))
array([[1, 2, 3],
                    [4, 1, 2],
                    [3, 4, 1]])
>>> ma.resize(a, (3, 3))
masked_array(data =
    [[1 -- 3]
    [4 1 ---]
```

```
[3
            mask =
[[False True False]
[False False True]
[False False False]],
    fill_value = 999999)
```

A MaskedArray is always returned, regardless of the input type.

```
>>> a = np.array([[1, 2] ,[3, 4]])
>>> ma.resize(a, (3, 3))
masked_array(data =
    [[\begin{array}{lll}{1}&{2}&{3}\end{array}]
    [4 1 1 2]
    [3
            mask =
    False,
            fill_value = 999999)
```

MaskedArray. flatten (order $=$ ' $C^{\prime}$ )

Return a copy of the array collapsed into one dimension.

## Parameters

order : \{ 'C', 'F', 'A'\}, optional
Whether to flatten in C (row-major), Fortran (column-major) order, or preserve the $\mathrm{C} /$ Fortran ordering from $a$. The default is ' C '.

## Returns

$\mathbf{y}$ : ndarray
A copy of the input array, flattened to one dimension.

## See Also:

ravel
Return a flattened array.
flat
A 1-D flat iterator over the array.

## Examples

```
>>> a = np.array([[1,2], [3,4]])
>>> a.flatten()
array([1, 2, 3, 4])
>>> a.flatten('F')
array([1, 3, 2, 4])
```

MaskedArray.ravel()
Returns a 1D version of self, as a view.

## Returns

MaskedArray :
Output view $\quad$ is $\begin{gathered}\text { of }\end{gathered}$ shape $\quad$ (self.size,) (or
(np.ma.product (self.shape), ).

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 --]
    [7 -- 9]]
>>> print x.ravel()
[1 -- 3 -- 5 -- 7 -- 9]
```

MaskedArray.reshape (*s, **kwargs)
Give a new shape to the array without changing its data.
Returns a masked array containing the same data, but with a new shape. The result is a view on the original array; if this is not possible, a ValueError is raised.

## Parameters

shape : int or tuple of ints
The new shape should be compatible with the original shape. If an integer is supplied, then the result will be a 1-D array of that length.
order : \{ 'C', 'F'\}, optional
Determines whether the array data should be viewed as in C (row-major) or FORTRAN (column-major) order.

## Returns

reshaped_array : array
A new view on the array.

## See Also:

reshape
Equivalent function in the masked array module.
numpy.ndarray.reshape
Equivalent method on ndarray object.
numpy. reshape
Equivalent function in the NumPy module.

## Notes

The reshaping operation cannot guarantee that a copy will not be made, to modify the shape in place, use a.shape $=\mathrm{s}$

## Examples

```
>>> x = np.ma.array([[1,2],[3,4]], mask=[1,0,0,1])
>>> print x
[[-- 2]
    [3 --]]
>>> x = x.reshape((4,1))
>>> print x
[[--]
    [2]
    [3]
    [--]]
```

MaskedArray.resize (newshape, refcheck=True,order=False)
Warning: This method does nothing, except raise a ValueError exception. A masked array does not own its data and therefore cannot safely be resized in place. Use the numpy.ma. resize function instead.

This method is difficult to implement safely and may be deprecated in future releases of NumPy.

## Modifying axes

```
ma.swapaxes swapaxes
ma.transpose(a[, axes]) Permute the dimensions of an array.
ma.MaskedArray.swapaxes(axis1, axis2) Return a view of the array with axisl and axis2 interchanged.
ma.MaskedArray.transpose(*axes) Returns a view of the array with axes transposed.
numpy.ma.swapaxes
    swapaxes a.swapaxes(axis1, axis2)
        Return a view of the array with axis1 and axis2 interchanged.
        Refer to numpy. swapaxes for full documentation.
    See Also:
    numpy.swapaxes
        equivalent function
numpy.ma.transpose (a, axes=None)
    Permute the dimensions of an array.
    This function is exactly equivalent to numpy.transpose.
    See Also:
    numpy.transpose
        Equivalent function in top-level NumPy module.
    Examples
        >>> import numpy.ma as ma
        >>> x = ma.arange(4).reshape((2,2))
        >>> x[1, 1] = ma.masked
        >>>> x
        masked_array(data =
            [[\begin{array}{ll}{0}&{1}\end{array}]
            [2 -- ]],
                mask =
            [[False False]
            [False True]],
            fill_value = 999999)
        >>> ma.transpose(x)
        masked_array(data =
            [[[0 2]
            [1 --]],
            mask =
            [[False False]
            [False True]],
            fill_value = 999999)
MaskedArray.swapaxes (axis1,axis2)
    Return a view of the array with axis1 and axis2 interchanged.
```

Refer to numpy. swapaxes for full documentation.
See Also:
numpy.swapaxes
equivalent function

MaskedArray.transpose (*axes)
Returns a view of the array with axes transposed.
For a 1-D array, this has no effect. (To change between column and row vectors, first cast the 1-D array into a matrix object.) For a 2-D array, this is the usual matrix transpose. For an n-D array, if axes are given, their order indicates how the axes are permuted (see Examples). If axes are not provided and a.shape $=(i[0], i[1]$, ... i[n-2], i[n-1]), then a.transpose().shape $=(i[n-1], i[n-2], \ldots i[1]$, i[0]).

## Parameters

axes: None, tuple of ints, or $n$ ints

- None or no argument: reverses the order of the axes.
- tuple of ints: $i$ in the $j$-th place in the tuple means $a$ 's $i$-th axis becomes a.transpose()'s $j$-th axis.
- $n$ ints: same as an n-tuple of the same ints (this form is intended simply as a "convenience" alternative to the tuple form)


## Returns

out : ndarray
View of $a$, with axes suitably permuted.

## See Also:

ndarray. T
Array property returning the array transposed.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> a
array([[1, 2],
            [3, 4]])
>>> a.transpose()
array([[1, 3],
            [2, 4]])
>>> a.transpose((1, 0))
array([[1, 3],
            [2, 4]])
>>> a.transpose(1, 0)
array([[1, 3],
    [2, 4]])
```


## Changing the number of dimensions

| ma.atleast_1d(*arys) | Convert inputs to arrays with at least one dimension. |
| :--- | :--- |
| ma.atleast_2d(*arys) | View inputs as arrays with at least two dimensions. |
| ma.atleast_3d(*arys) | View inputs as arrays with at least three dimensions. |
| ma.expand_dims(x, axis) | Expand the shape of an array. |
| ma.squeeze(a) | Remove single-dimensional entries from the shape of an array. |
| ma.MaskedArray.squeeze() | Remove single-dimensional entries from the shape of $a$. |
| ma.column_stack(tup) | Stack 1-D arrays as columns into a 2-D array. |
| ma.concatenate(arrays[, axis]) | Concatenate a sequence of arrays along the given axis. |
| ma.dstack(tup) | Stack arrays in sequence depth wise (along third axis). |
| ma.hstack(tup) | Stack arrays in sequence horizontally (column wise). |
| ma.hsplit(ary, indices_or_sections) | Split an array into multiple sub-arrays horizontally (column-wise). |
| ma.mr_- | Translate slice objects to concatenation along the first axis. |
| ma.row_stack(tup) | Stack arrays in sequence vertically (row wise). |
| ma.vstack(tup) | Stack arrays in sequence vertically (row wise). |
| numpy.ma.atleast_1d(*arys) |  |

Convert inputs to arrays with at least one dimension.
Scalar inputs are converted to 1-dimensional arrays, whilst higher-dimensional inputs are preserved.

## Parameters

```
    array1, array2, ... : array_like
```

One or more input arrays.

## Returns

ret : ndarray
An array, or sequence of arrays, each with a.ndim $>=1$. Copies are made only if necessary.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> np.atleast_1d(1.0)
array([ 1.])
>>> x = np.arange (9.0).reshape (3,3)
>>> np.atleast_1d(x)
array([[ 0., 1., 2.],
    [ 3., 4., 5.],
    [ 6., 7., 8.]])
>>> np.atleast_1d(x) is x
True
>>> np.atleast_1d(1, [3, 4])
[array([1]), array([3, 4])]
numpy.ma.atleast_2d(*arys)
```

View inputs as arrays with at least two dimensions.

## Parameters

array1, array2, ... : array_like
One or more array-like sequences. Non-array inputs are converted to arrays. Arrays that already have two or more dimensions are preserved.

## Returns

res, res $2, \ldots$ : ndarray
An array, or tuple of arrays, each with a.ndim $>=2$. Copies are avoided where possible, and views with two or more dimensions are returned.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> np.atleast_2d(3.0)
array([[ 3.]])
>>> x = np.arange(3.0)
>>> np.atleast_2d(x)
array([[ 0., 1., 2.]])
>>> np.atleast_2d(x).base is x
True
>>> np.atleast_2d(1, [1, 2], [[1, 2]])
[array([[1]]), array([[1, 2]]), array([[1, 2]])]
numpy.ma.atleast_3d(*arys)
```

View inputs as arrays with at least three dimensions.

## Parameters

array1, array2, ... : array_like
One or more array-like sequences. Non-array inputs are converted to arrays. Arrays that already have three or more dimensions are preserved.

## Returns

res1, res2, ... : ndarray
An array, or tuple of arrays, each with a.ndim $>=3$. Copies are avoided where possible, and views with three or more dimensions are returned. For example, a 1-D array of shape $(\mathrm{N}$, ) becomes a view of shape ( $1, ~ \mathrm{~N}, 1$ ), and a 2-D array of shape $(M, N)$ becomes a view of shape ( $M, N, 1$ ).

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> np.atleast_3d(3.0)
array([[[ 3.]]])
>>> x = np.arange(3.0)
>>> np.atleast_3d(x).shape
(1, 3, 1)
```

```
>>> x = np.arange(12,0).reshape (4,3)
>>> np.atleast_3d(x).shape
(4, 3, 1)
>>> np.atleast_3d(x).base is x
True
>>> for arr in np.atleast_3d([1, 2], [[1, 2]], [[[1, 2]]]):
... print arr, arr.shape
* ..
[[ [1]
    [2]]] (1, 2, 1)
[[[1]
    [2]]] (1, 2, 1)
[[[[1 2]]] (1, 1, 2)
numpy.ma.expand_dims ( \(x\), axis)
Expand the shape of an array.
```

Expands the shape of the array by including a new axis before the one specified by the axis parameter. This function behaves the same as numpy. expand_dims but preserves masked elements.

## See Also:

numpy.expand_dims
Equivalent function in top-level NumPy module.

## Examples

```
>>> import numpy.ma as ma
>>> x = ma.array([1, 2, 4])
>>> x[1] = ma.masked
>>> x
masked_array(data = [1 -- 4],
                    mask = [False True False],
            fill_value = 999999)
>>> np.expand_dims(x, axis=0)
array([[1, 2, 4]])
>>> ma.expand_dims(x, axis=0)
masked_array(data =
            [[1 -- 4]],
                        mask =
    [[False True False]],
            fill_value = 9999999)
```

The same result can be achieved using slicing syntax with np.newaxis.

```
>>> x[np.newaxis, :]
masked_array(data =
    [[1 -- 4]],
                    mask =
    [[False True False]],
            fill_value = 999999)
```

numpy.ma.squeeze (a)

Remove single-dimensional entries from the shape of an array.

## Parameters

a : array_like
Input data.

## Returns

squeezed : ndarray
The input array, but with with all dimensions of length 1 removed. Whenever possible, a view on $a$ is returned.

## Examples

```
>>> x = np.array([[[0], [1], [2]]])
```

>>> x.shape
(1, 3, 1)
>>> np.squeeze(x).shape
(3, )

MaskedArray.squeeze()
Remove single-dimensional entries from the shape of $a$.
Refer to numpy. squeeze for full documentation.
See Also:
numpy.squeeze equivalent function

```
numpy.ma.column_stack(tup)
```

Stack 1-D arrays as columns into a 2-D array.
Take a sequence of 1-D arrays and stack them as columns to make a single 2-D array. 2-D arrays are stacked as-is, just like with hstack. 1-D arrays are turned into 2-D columns first.

## Parameters

tup : sequence of 1-D or 2-D arrays.
Arrays to stack. All of them must have the same first dimension.

## Returns

stacked : 2-D array
The array formed by stacking the given arrays.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.column_stack((a,b))
array([[1, 2],
                    [2, 3],
[3, 4]])
```

numpy.ma. concatenate (arrays, axis=0)
Concatenate a sequence of arrays along the given axis.

## Parameters

arrays : sequence of array_like

The arrays must have the same shape, except in the dimension corresponding to axis (the first, by default).
axis : int, optional
The axis along which the arrays will be joined. Default is 0 .

## Returns

result : MaskedArray
The concatenated array with any masked entries preserved.

## See Also:

```
numpy.concatenate
```

Equivalent function in the top-level NumPy module.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.arange(3)
>>> a[1] = ma.masked
>>> b = ma.arange(2, 5)
>>> a
masked_array(data = [0 -- 2],
                                    mask = [False True False],
    fill_value = 999999)
>>> b
masked_array(data = [l2 3 4}]|
    mask = False,
    fill_value = 999999)
>>> ma.concatenate([a, b])
masked_array(data = [0 -- 2 2 3 4],
            mask = [False True False False False False],
            fill_value = 999999)
```

numpy.ma.dstack (tup)

Stack arrays in sequence depth wise (along third axis).
Takes a sequence of arrays and stack them along the third axis to make a single array. Rebuilds arrays divided by dsplit. This is a simple way to stack 2D arrays (images) into a single 3D array for processing.

## Parameters

tup : sequence of arrays
Arrays to stack. All of them must have the same shape along all but the third axis.

## Returns

 stacked : ndarrayThe array formed by stacking the given arrays.

## See Also:

vstack
Stack along first axis.

## hstack

Stack along second axis.
concatenate
Join arrays.

## dsplit

Split array along third axis.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.dstack((a,b))
array([[[1, 2],
    [2, 3],
    [3, 4]]])
>>> a = np.array([[1],[2],[3]])
>>> b = np.array([[2],[3],[4]])
>>> np.dstack((a,b))
array([[[1, 2]],
    [[2, 3]],
    [[3, 4]]])
numpy.ma.hstack(tup)
```

Stack arrays in sequence horizontally (column wise).
Take a sequence of arrays and stack them horizontally to make a single array. Rebuild arrays divided by hsplit.

## Parameters

tup : sequence of ndarrays
All arrays must have the same shape along all but the second axis.

## Returns

stacked : ndarray
The array formed by stacking the given arrays.

## See Also:

vstack
Stack arrays in sequence vertically (row wise).
dstack
Stack arrays in sequence depth wise (along third axis).
concatenate
Join a sequence of arrays together.
hsplit
Split array along second axis.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.hstack((a,b))
array([1, 2, 3, 2, 3, 4])
>>> a = np.array([[1],[2],[3]])
>>> b = np.array([[2],[3],[4]])
>>> np.hstack((a,b))
array([[1, 2],
    [2, 3],
    [3, 4]])
```

numpy.ma.hsplit (ary, indices_or_sections)

Split an array into multiple sub-arrays horizontally (column-wise).
Please refer to the split documentation. hsplit is equivalent to split with axis=1, the array is always split along the second axis regardless of the array dimension.

## See Also:

split
Split an array into multiple sub-arrays of equal size.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> x = np.arange(16.0).reshape(4, 4)
>>> x
array([[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.],
    [ 12., 13., 14., 15.]])
>>> np.hsplit(x, 2)
[array([[ 0., 1.],
    [ 4., 5.],
    [ 8., 9.],
    [ 12., 13.]]),
    array([[ 2., 3.],
    [ 6., 7.],
    [ 10., 11.],
    [ 14., 15.]])]
>>> np.hsplit(x, np.array([3, 6]))
[array([[ 0., 1., 2.],
    [ 4., 5., 6.],
    [ 8., 9., 10.],
    [ 12., 13., 14.]]),
    array([[ 3.],
    [ 7.],
    [ 11.],
```

```
    [ 15.]]),
array([], dtype=float64)]
```

With a higher dimensional array the split is still along the second axis.

```
>>> x = np.arange(8.0).reshape(2, 2, 2)
>>> x
array([[[ 0., 1.],
    [ 2., 3.]],
    [[ 4., 5.],
    [ 6., 7.]]])
>>> np.hsplit(x, 2)
[array([[[ 0., 1.]],
    [[ 4., 5.]]]),
    array([[[ 2., 3.]],
    [[ 6., 7.]]])]
```

numpy.ma.mr_

Translate slice objects to concatenation along the first axis.
This is the masked array version of lib.index_tricks.RClass.

## See Also:

```
lib.index_tricks.RClass
```


## Examples

```
>>> np.ma.mr_[np.ma.array([1,2,3]), 0, 0, np.ma.array([4,5,6])]
array([1, 2, 3, 0, 0, 4, 5, 6])
numpy.ma.row_stack (tup)
```

Stack arrays in sequence vertically (row wise).
Take a sequence of arrays and stack them vertically to make a single array. Rebuild arrays divided by vsplit.

## Parameters

tup : sequence of ndarrays
Tuple containing arrays to be stacked. The arrays must have the same shape along all but the first axis.

## Returns

 stacked : ndarrayThe array formed by stacking the given arrays.

## See Also:

## hstack

Stack arrays in sequence horizontally (column wise).
dstack
Stack arrays in sequence depth wise (along third dimension).
concatenate
Join a sequence of arrays together.

## vsplit

Split array into a list of multiple sub-arrays vertically.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array([1, 2, 3])
>>> b = np.array([2, 3, 4])
>>> np.vstack((a,b))
array([[1, 2, 3],
    [2, 3, 4]])
>>> a = np.array([[1], [2], [3]])
>>> b = np.array([[2], [3], [4]])
>>> np.vstack((a,b))
array([[1],
    [2],
    [3],
    [2],
    [3],
    [4]])
numpy.ma.vstack(tup)
```

Stack arrays in sequence vertically (row wise).
Take a sequence of arrays and stack them vertically to make a single array. Rebuild arrays divided by vsplit.

## Parameters

tup : sequence of ndarrays
Tuple containing arrays to be stacked. The arrays must have the same shape along all but the first axis.

## Returns

stacked : ndarray
The array formed by stacking the given arrays.

## See Also:

hstack
Stack arrays in sequence horizontally (column wise).
dstack
Stack arrays in sequence depth wise (along third dimension).
concatenate
Join a sequence of arrays together.
vsplit
Split array into a list of multiple sub-arrays vertically.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array([1, 2, 3])
>>> b = np.array([2, 3, 4])
>>> np.vstack((a,b))
array([[1, 2, 3],
    [2, 3, 4]])
>>> a = np.array([[1], [2], [3]])
>>> b = np.array([[2], [3], [4]])
>>> np.vstack((a,b))
array([[1],
    [2],
    [3],
    [2],
    [3],
    [4]])
```


## Joining arrays

```
ma.column_stack(tup) Stack 1-D arrays as columns into a 2-D array.
ma.concatenate(arrays[, axis]) Concatenate a sequence of arrays along the given axis.
ma.dstack(tup) Stack arrays in sequence depth wise (along third axis).
ma.hstack(tup) Stack arrays in sequence horizontally (column wise).
ma.vstack(tup) Stack arrays in sequence vertically (row wise).
numpy.ma.column_stack(tup)
```

Stack 1-D arrays as columns into a 2-D array.
Take a sequence of 1-D arrays and stack them as columns to make a single 2-D array. 2-D arrays are stacked as-is, just like with hstack. 1-D arrays are turned into 2-D columns first.

## Parameters

tup : sequence of 1-D or 2-D arrays.
Arrays to stack. All of them must have the same first dimension.

## Returns

stacked : 2-D array
The array formed by stacking the given arrays.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.column_stack((a,b))
array([[1, 2],
    [2, 3],
    [3, 4]])
```

numpy.ma.concatenate (arrays, axis=0)
Concatenate a sequence of arrays along the given axis.

## Parameters

arrays : sequence of array_like
The arrays must have the same shape, except in the dimension corresponding to axis (the first, by default).
axis : int, optional
The axis along which the arrays will be joined. Default is 0 .

## Returns

result : MaskedArray
The concatenated array with any masked entries preserved.

## See Also:

```
numpy.concatenate
```

Equivalent function in the top-level NumPy module.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.arange(3)
>>> a[1] = ma.masked
>>> b = ma.arange (2, 5)
>>> a
masked_array(data = [0 -- 2],
    mask = [False True False],
    fill_value = 999999)
>>> b
masked_array(data = [2 3 4 4],
    mask = False,
    fill_value = 999999)
>>> ma.concatenate([a, b])
masked_array(data = [0 -- 2 2 3 4 4}
    mask = [False True False False False False],
    fill_value = 999999)
numpy.ma.dstack (tup)
```

Stack arrays in sequence depth wise (along third axis).
Takes a sequence of arrays and stack them along the third axis to make a single array. Rebuilds arrays divided by dsplit. This is a simple way to stack 2D arrays (images) into a single 3D array for processing.

## Parameters

tup : sequence of arrays
Arrays to stack. All of them must have the same shape along all but the third axis.

## Returns

 stacked : ndarrayThe array formed by stacking the given arrays.

## See Also:

```
vstack
    Stack along first axis.
hstack
    Stack along second axis.
concatenate
    Join arrays.
dsplit
    Split array along third axis.
```


## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.dstack((a,b))
array([[[1, 2],
    [2, 3],
    [3, 4]]])
>>> a = np.array([[1],[2],[3]])
>>> b = np.array([[2],[3],[4]])
>>> np.dstack((a,b))
array([[[1, 2]],
            [[2, 3]],
            [[3, 4]]])
```

numpy.ma.hstack (tup)

Stack arrays in sequence horizontally (column wise).
Take a sequence of arrays and stack them horizontally to make a single array. Rebuild arrays divided by hsplit.

## Parameters

tup : sequence of ndarrays
All arrays must have the same shape along all but the second axis.

## Returns

stacked : ndarray
The array formed by stacking the given arrays.

## See Also:

vstack
Stack arrays in sequence vertically (row wise).
dstack
Stack arrays in sequence depth wise (along third axis).
concatenate
Join a sequence of arrays together.
hsplit
Split array along second axis.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.hstack((a,b))
array([1, 2, 3, 2, 3, 4])
>>> a = np.array([[1],[2],[3]])
>>> b = np.array([[2],[3],[4]])
>>> np.hstack((a,b))
array([[1, 2],
    [2, 3],
    [3, 4]])
numpy.ma.vstack(tup)
```

Stack arrays in sequence vertically (row wise).
Take a sequence of arrays and stack them vertically to make a single array. Rebuild arrays divided by vsplit.

## Parameters

tup : sequence of ndarrays
Tuple containing arrays to be stacked. The arrays must have the same shape along all but the first axis.

## Returns

## stacked : ndarray

The array formed by stacking the given arrays.

## See Also:

```
hstack
```

    Stack arrays in sequence horizontally (column wise).
    dstack

Stack arrays in sequence depth wise (along third dimension).
concatenate
Join a sequence of arrays together.
vsplit
Split array into a list of multiple sub-arrays vertically.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array([1, 2, 3])
>>> b = np.array([2, 3, 4])
>>> np.vstack((a,b))
array([[1, 2, 3],
    [2, 3, 4]])
>>> a = np.array([[1], [2], [3]])
>>> b = np.array([[2], [3], [4]])
>>> np.vstack((a,b))
array([[1],
    [2],
    [3],
    [2],
    [3],
    [4]])
```


## Operations on masks

## Creating a mask

```
ma.make_mask(m[, copy, shrink, dtype]) Create a boolean mask from an array.
ma.make_mask_none(newshape[, dtype]) Return a boolean mask of the given shape, filled with False.
ma.mask_or(m1, m2[, copy, shrink]) Combine two masks with the logical_or operator.
ma.make_mask_descr(ndtype) Construct a dtype description list from a given dtype.
```

numpy.ma.make_mask ( $m$, copy=False, shrink=True, dtype=<type 'numpy.bool_'>)
Create a boolean mask from an array.
Return $m$ as a boolean mask, creating a copy if necessary or requested. The function can accept any sequence that is convertible to integers, or nomask. Does not require that contents must be 0 s and 1 s , values of 0 are interepreted as False, everything else as True.

## Parameters

m : array_like
Potential mask.
copy : bool, optional
Whether to return a copy of $m$ (True) or $m$ itself (False).
shrink : bool, optional
Whether to shrink $m$ to nomask if all its values are False.
dtype : dtype, optional
Data-type of the output mask. By default, the output mask has a dtype of MaskType (bool). If the dtype is flexible, each field has a boolean dtype.

## Returns

result : ndarray
A boolean mask derived from $m$.
Examples

```
>>> import numpy.ma as ma
>>> m = [True, False, True, True]
>>> ma.make_mask(m)
array([ True, False, True, True], dtype=bool)
>>> m = [1, 0, 1, 1]
>>> ma.make_mask(m)
array([ True, False, True, True], dtype=bool)
>>> m = [1, 0, 2, -3]
>>> ma.make_mask(m)
array([ True, False, True, True], dtype=bool)
```

Effect of the shrink parameter.

```
>>> m = np.zeros(4)
>>> m
array([ 0., 0., 0., 0.])
>>> ma.make_mask(m)
False
>>> ma.make_mask(m, shrink=False)
array([False, False, False, False], dtype=bool)
```

Using a flexible dtype.

```
>>> m=[1, 0, 1, 1]
>>> n = [0, 1, 0, 0]
>>> arr = []
>>> for man, mouse in zip(m, n):
... arr.append((man, mouse))
>>> arr
[(1, 0), (0, 1), (1, 0), (1, 0)]
>>> dtype = np.dtype({'names':['man', 'mouse'],
    'formats':[np.int, np.int]})
>>> arr = np.array(arr, dtype=dtype)
>>> arr
array([(1, 0), (0, 1), (1, 0), (1, 0)],
    dtype=[('man', '<i4'), ('mouse', '<i4')])
>>> ma.make_mask(arr, dtype=dtype)
array([(True, False), (False, True), (True, False), (True, False)],
    dtype=[('man', '|b1'), ('mouse', '|b1')])
```

numpy.ma.make_mask_none (newshape, dtype=None)
Return a boolean mask of the given shape, filled with False.
This function returns a boolean ndarray with all entries False, that can be used in common mask manipulations.
If a complex dtype is specified, the type of each field is converted to a boolean type.

## Parameters

newshape : tuple
A tuple indicating the shape of the mask.
dtype: \{None, dtype\}, optional :
If None, use a MaskType instance. Otherwise, use a new datatype with the same fields as dtype, converted to boolean types.

## Returns

result : ndarray
An ndarray of appropriate shape and dtype, filled with False.

## See Also:

make_mask
Create a boolean mask from an array.
make_mask_descr
Construct a dtype description list from a given dtype.

## Examples

```
>>> import numpy.ma as ma
>>> ma.make_mask_none((3,))
array([False, False, False], dtype=bool)
```

Defining a more complex dtype.

```
>>> dtype = np.dtype({'names':['foo', 'bar'],
    'formats':[np.float32, np.int]})
>>> dtype
dtype([('foo', '<f4'), ('bar', '<i4')])
>>> ma.make_mask_none((3,), dtype=dtype)
array([(False, False), (False, False), (False, False)],
    dtype=[('foo', '|b1'), ('bar', '|b1')])
```

numpy.ma.mask_or ( $m 1, m 2$, copy=False, shrink=True)
Combine two masks with the logical_or operator.
The result may be a view on $m 1$ or $m 2$ if the other is nomask (i.e. False).

## Parameters

m1, m2 : array_like
Input masks.
copy : bool, optional
If copy is False and one of the inputs is nomask, return a view of the other input mask. Defaults to False.
shrink : bool, optional
Whether to shrink the output to nomask if all its values are False. Defaults to True.

## Returns

mask : output mask
The result masks values that are masked in either $m 1$ or $m 2$.

## Raises

## ValueError :

If $m 1$ and $m 2$ have different flexible dtypes.

## Examples

```
>>> m1 = np.ma.make_mask([0, 1, 1, 0])
>>> m2 = np.ma.make_mask([1, 0, 0, 0])
>>> np.ma.mask_or(m1, m2)
array([ True, True, True, False], dtype=bool)
```

numpy.ma.make_mask_descr (ndtype)

Construct a dtype description list from a given dtype.

Returns a new dtype object, with the type of all fields in ndtype to a boolean type. Field names are not altered.

## Parameters <br> ndtype : dtype

The dtype to convert.

## Returns

result : dtype
A dtype that looks like ndtype, the type of all fields is boolean.

## Examples

```
>>> import numpy.ma as ma
>>> dtype = np.dtype({'names':['foo', 'bar'],
    'formats':[np.float32, np.int]})
>>> dtype
dtype([('foo', '<f4'), ('bar', '<i4')])
>>> ma.make_mask_descr(dtype)
dtype([('foo', '|b1'), ('bar', '|b1')])
>>> ma.make_mask_descr(np.float32)
<type 'numpy.bool_'>
```


## Accessing a mask

| ma.getmask(a) | Return the mask of a masked array, or nomask. |
| :--- | :--- |
| ma.getmaskarray (arr) | Return the mask of a masked array, or full boolean array of False. |
| ma.masked_array.mask | Mask |

## numpy.ma.getmask (a)

Return the mask of a masked array, or nomask.
Return the mask of $a$ as an ndarray if $a$ is a MaskedArray and the mask is not nomask, else return nomask. To guarantee a full array of booleans of the same shape as a, use getmaskarray.

## Parameters

a : array_like
Input MaskedArray for which the mask is required.

## See Also:

getdata
Return the data of a masked array as an ndarray.
getmaskarray
Return the mask of a masked array, or full array of False.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.masked_equal([[1,2],[3,4]], 2)
>>> a
masked_array(data =
            [[1 --]
            [[3 4]],
                mask =
            [[False True]
            [False False]],
                fill_value=999999)
```

```
>>> ma.getmask(a)
array([[False, True],
    [False, False]], dtype=bool)
```

Equivalently use the MaskedArray mask attribute.

```
>>> a.mask
array([[False, True],
    [False, False]], dtype=bool)
```

Result when mask $==$ nomask

```
>>> b = ma.masked_array([[1,2],[3,4]])
>>> b
masked_array(data =
    [[\begin{array}{ll}{1}&{2}\end{array}]
    [3 4]],
            mask =
    False,
            fill_value=999999)
>>> ma.nomask
False
>>> ma.getmask(b) == ma.nomask
True
>>> b.mask == ma.nomask
True
```

numpy.ma.getmaskarray (arr)
Return the mask of a masked array, or full boolean array of False.
Return the mask of arr as an ndarray if arr is a MaskedArray and the mask is not nomask, else return a full boolean array of False of the same shape as arr.

## Parameters

arr : array_like
Input MaskedArray for which the mask is required.

## See Also:

getmask
Return the mask of a masked array, or nomask.
getdata
Return the data of a masked array as an ndarray.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.masked_equal([[1,2],[3,4]], 2)
>>> a
masked_array(data =
    [[1 -- ]
    [3 4]],
                mask =
    [[False True]
    [False False]],
                fill_value=999999)
>>> ma.getmaskarray(a)
```

```
array([[False, True],
    [False, False]], dtype=bool)
```

Result when mask $==$ nomask

```
>>> b = ma.masked_array([[1,2], [3,4]])
>>> b
masked_array(data =
    [[lll
    [3 4]],
            mask =
    False,
            fill_value=999999)
>>> >ma.getmaskarray(b)
array([[False, False],
            [False, False]], dtype=bool)
```

masked_array.mask
Mask

## Finding masked data

```
ma.flatnotmasked_contiguous(a) Find contiguous unmasked data in a masked array along the given axis.
ma.flatnotmasked_edges(a) Find the indices of the first and last unmasked values.
ma.notmasked_contiguous(a[, axis]) Find contiguous unmasked data in a masked array along the given axis.
ma.notmasked__edges(a[, axis])
Find the indices of the first and last unmasked values along an axis.
```


## numpy.ma.flatnotmasked_contiguous $(a)$

Find contiguous unmasked data in a masked array along the given axis.

## Parameters

a : narray
The input array.

## Returns

slice_list : list
A sorted sequence of slices (start index, end index).

## See Also:

```
flatnotmasked_edges, notmasked_contiguous, notmasked_edges, clump_masked,
clump_unmasked
```


## Notes

Only accepts 2-D arrays at most.

## Examples

```
>>> a = np.ma.arange(10)
>>> np.ma.extras.flatnotmasked_contiguous(a)
slice(0, 10, None)
>>> mask = (a<3) | (a > 8) | (a == 5)
>>> a[mask] = np.ma.masked
>>> np.array(a[~a.mask])
array([3, 4, 6, 7, 8])
```

```
>>> np.ma.extras.flatnotmasked_contiguous(a)
[slice(3, 5, None), slice(6, 9, None)]
>>> a[:] = np.ma.masked
>>> print np.ma.extras.flatnotmasked_edges(a)
None
```

numpy.ma.flatnotmasked_edges (a)

Find the indices of the first and last unmasked values.
Expects a 1-D MaskedArray, returns None if all values are masked.

## Parameters

arr : array_like
Input 1-D MaskedArray

## Returns

edges : ndarray or None
The indices of first and last non-masked value in the array. Returns None if all values are masked.

## See Also:

```
flatnotmasked_contiguous, notmasked_contiguous, notmasked_edges, clump_masked,
clump_unmasked
```


## Notes

Only accepts 1-D arrays.

## Examples

```
>>> a = np.ma.arange(10)
>>> flatnotmasked_edges(a)
[0,-1]
>>> mask = (a<3) | (a > 8) | (a == 5)
>>> a[mask] = np.ma.masked
>>> np.array(a[~a.mask])
array([3, 4, 6, 7, 8])
>>> flatnotmasked_edges(a)
array([3, 8])
>>> a[:] = np.ma.masked
>>> print flatnotmasked_edges(ma)
None
```

numpy.ma.notmasked_contiguous (a, axis=None)

Find contiguous unmasked data in a masked array along the given axis.

## Parameters

a : array_like
The input array.
axis : int, optional
Axis along which to perform the operation. If None (default), applies to a flattened version of the array.

## Returns

endpoints : list
A list of slices (start and end indexes) of unmasked indexes in the array.

## See Also:

```
flatnotmasked_edges, flatnotmasked_contiguous, notmasked_edges, clump_masked,
clump_unmasked
```


## Notes

Only accepts 2-D arrays at most.
Examples

```
>>> a = np.arange(9).reshape((3, 3))
>>> mask = np.zeros_like(a)
>>> mask[1:, 1:] = 1
>>> ma = np.ma.array(a, mask=mask)
>>> np.array(ma[~ma.mask])
array([0, 1, 2, 3, 6])
>>> np.ma.extras.notmasked_contiguous(ma)
[slice(0, 4, None), slice(6, 7, None)]
```

numpy.ma.notmasked_edges (a, axis=None)
Find the indices of the first and last unmasked values along an axis.
If all values are masked, return None. Otherwise, return a list of two tuples, corresponding to the indices of the first and last unmasked values respectively.

## Parameters

a : array_like
The input array.
axis : int, optional
Axis along which to perform the operation. If None (default), applies to a flattened version of the array.

## Returns

edges : ndarray or list
An array of start and end indexes if there are any masked data in the array. If there are no masked data in the array, edges is a list of the first and last index.

## See Also:

flatnotmasked_contiguous, flatnotmasked_edges, notmasked_contiguous, clump_masked, clump_unmasked

## Examples

```
>>> a = np.arange(9).reshape((3, 3))
>>> m = np.zeros_like(a)
>>> m[1:, 1:] = 1
>>> am = np.ma.array(a, mask=m)
>>> np.array(am[~am.mask])
array([0, 1, 2, 3, 6])
```

```
>>> np.ma.extras.notmasked_edges(ma)
array([0, 6])
```

Modifying a mask

```
ma.mask_cols(a[,axis]) Mask columns of a 2D array that contain masked values.
ma.mask_or(m1, m2[, copy, shrink]) Combine two masks with the logical_or operator.
ma.mask_rowcols(a[, axis]) Mask rows and/or columns of a 2D array that contain masked values.
ma.mask_rows(a[, axis]) Mask rows of a 2D array that contain masked values.
ma.harden_mask(self) Force the mask to hard.
ma.soften_mask(self) Force the mask to soft.
ma.MaskedArray.harden_mask() Force the mask to hard.
ma.MaskedArray.soften_mask() Force the mask to soft.
ma.MaskedArray.shrink_mask() Reduce a mask to nomask when possible.
ma.MaskedArray.unshare_mask() Copy the mask and set the sharedmask flag to False.
```

numpy.ma.mask_cols (a, axis=None)
Mask columns of a 2D array that contain masked values.
This function is a shortcut to mask_rowcols with axis equal to 1 .

## See Also:

mask_rowcols
Mask rows and/or columns of a 2D array.
masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.zeros((3, 3), dtype=np.int)
>>> a[1, 1] = 1
>>> a
array([[0, 0, 0],
            [0, 1, 0],
            [0, 0, 0]])
>>> a = ma.masked_equal(a, 1)
>>> a
masked_array(data =
    [[00 0 0]
    [0 -- 0]
    [0}00<0]]
                mask =
            [[False False False]
            [False True False]
            [False False False]],
                    fill_value=999999)
>>> ma.mask_cols(a)
masked_array(data =
            [[0 -- 0]
            [0 -- 0]
            [0 -- 0]],
                mask =
            [[False True False]
            [False True False]
```

[False True False]],
fill_value=999999)
numpy.ma.mask_or ( $m 1, m 2$, copy=False, shrink=True $)$
Combine two masks with the logical_or operator.
The result may be a view on $m 1$ or $m 2$ if the other is nomask (i.e. False).

## Parameters

m1, m2 : array_like
Input masks.
copy : bool, optional
If copy is False and one of the inputs is nomask, return a view of the other input mask. Defaults to False.
shrink : bool, optional
Whether to shrink the output to nomask if all its values are False. Defaults to True.

## Returns

mask : output mask
The result masks values that are masked in either $m 1$ or $m 2$.

## Raises

ValueError :
If $m 1$ and $m 2$ have different flexible dtypes.

## Examples

```
>>> m1 = np.ma.make_mask([0, 1, 1, 0])
>>> m2 = np.ma.make_mask([1, 0, 0, 0])
>>> np.ma.mask_or(m1, m2)
array([ True, True, True, False], dtype=bool)
```

numpy.ma.mask_rowcols (a, axis=None)
Mask rows and/or columns of a 2D array that contain masked values.
Mask whole rows and/or columns of a 2D array that contain masked values. The masking behavior is selected using the axis parameter.
-If axis is None, rows and columns are masked.
-If axis is 0 , only rows are masked.
-If axis is 1 or -1 , only columns are masked.

## Parameters

a : array_like, MaskedArray
The array to mask. If not a MaskedArray instance (or if no array elements are masked). The result is a MaskedArray with mask set to nomask (False). Must be a 2D array.
axis : int, optional
Axis along which to perform the operation. If None, applies to a flattened version of the array.

## Returns

a: MaskedArray

A modified version of the input array, masked depending on the value of the axis parameter.

## Raises

## NotImplementedError :

If input array $a$ is not 2D.

## See Also:

mask_rows
Mask rows of a 2D array that contain masked values.
mask_cols
Mask cols of a 2D array that contain masked values.
masked_where
Mask where a condition is met.

## Notes

The input array's mask is modified by this function.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.zeros((3, 3), dtype=np.int)
>>> a[1, 1] = 1
>>> a
array([[0, 0, 0],
    [0, 1, 0],
    [0, 0, 0]])
>>> a = ma.masked_equal(a, 1)
>>> a
masked_array(data =
    [[0 0 0]
    [0 -- 0]
    [0 0 0]],
                mask =
    [[False False False]
    [False True False]
    [False False False]],
            fill_value=999999)
>>> ma.mask_rowcols(a)
masked_array(data =
    [[0 -- 0]
    [-- -- --]
    [0 -- 0]],
            mask =
    [[False True False]
    [ True True True]
    [False True False]],
            fill_value=999999)
```

numpy.ma.mask_rows (a, axis=None)

Mask rows of a 2D array that contain masked values.
This function is a shortcut to mask_rowcols with axis equal to 0 .

## See Also:

```
mask_rowcols
```

Mask rows and/or columns of a 2D array.
masked_where
Mask where a condition is met.
Examples

```
>>> import numpy.ma as ma
>>> a = np.zeros((3, 3), dtype=np.int)
>>> a[1, 1] = 1
>>> a
array([[0, 0, 0],
                    [0, 1, 0],
    [0, 0, 0]])
>>> a = ma.masked_equal(a, 1)
>>> a
masked_array(data =
    [[0 0 0]
    [0 -- 0]
    [0 0 0]],
                mask =
    [[False False False]
    [False True False]
    [False False False]],
            fill_value=999999)
>>> ma.mask_rows(a)
masked_array(data =
    [[0 0 0]
    [-- -- --]
    [0 0 0]],
            mask =
    [[False False False]
    [ True True True]
    [False False False]],
            fill_value=999999)
```

numpy.ma. harden_mask (self)

Force the mask to hard.
Whether the mask of a masked array is hard or soft is determined by its hardmask property. harden_mask sets hardmask to True.

See Also:
hardmask
numpy.ma.soften_mask (self )
Force the mask to soft.
Whether the mask of a masked array is hard or soft is determined by its hardmask property. soften_mask sets hardmask to False.

## See Also:

hardmask
MaskedArray.harden_mask()
Force the mask to hard.
Whether the mask of a masked array is hard or soft is determined by its hardmask property. harden_mask sets hardmask to True.

## See Also:

hardmask
MaskedArray.soften_mask()
Force the mask to soft.
Whether the mask of a masked array is hard or soft is determined by its hardmask property. soften_mask sets hardmask to False.

## See Also:

hardmask
MaskedArray.shrink_mask()
Reduce a mask to nomask when possible.

## Parameters

None :
Returns
None :

## Examples

```
>>> x = np.ma.array([[1,2 ], [3, 4]], mask=[0]*4)
>>> x.mask
array([[False, False],
                    [False, False]], dtype=bool)
>>> x.shrink_mask()
>>> x.mask
False
```

MaskedArray.unshare_mask()
Copy the mask and set the sharedmask flag to False.
Whether the mask is shared between masked arrays can be seen from the sharedmask property. unshare_mask ensures the mask is not shared. A copy of the mask is only made if it was shared.

## See Also:

sharedmask

## Conversion operations

```
> to a masked array
    ma.asarray(a[, dtype, order])
    ma.asanyarray(a[, dtype])
        Convert the input to a masked array of the given data-type.
    Convert the input to a masked array, conserving subclasses.
    ma.fix_invalid(a[, mask, copy, fill_value])
        Return input with invalid data masked and replaced by a fill
        value.
    ma.masked_equal(x, value[, copy])
    Mask an array where equal to a given value.
    ma.masked_greater(x, value[, copy])
    Mask an array where greater than a given value.
    ma.masked_greater_equal(x, value[,
    copy])
    ma.masked_inside(x, v1, v2[, copy])
    ma.masked_invalid(a[, copy])
    ma.masked_less(x, value[, copy])
    ma.masked_less_equal(x, value[, copy])
    ma.masked_not_equal(x, value[, copy])
    ma.masked_object(x, value[, copy, shrink])
    ma.masked_outside(x, v1, v2[, copy])
    ma.masked_values(x, value[, rtol, atol, ...])
    ma.masked_where(condition, a[, copy]) Mask an array where a condition is met.
        Mask an array where greater than or equal to a given value.
    Mask an array inside a given interval.
    Mask an array where invalid values occur (NaNs or infs).
        Mask an array where less than a given value.
        Mask an array where less than or equal to a given value.
    Mask the array }x\mathrm{ where the data are exactly equal to value.
        Mask an array outside a given interval.
    Mask using floating point equality.
```

numpy.ma. asarray ( $a$, dtype=None, order $=$ None )

Convert the input to a masked array of the given data-type.
No copy is performed if the input is already an ndarray. If $a$ is a subclass of MaskedArray, a base class MaskedArray is returned.

## Parameters

a : array_like
Input data, in any form that can be converted to a masked array. This includes lists, lists of tuples, tuples, tuples of tuples, tuples of lists, ndarrays and masked arrays.
dtype : dtype, optional
By default, the data-type is inferred from the input data.
order : \{ 'C', 'F'\}, optional
Whether to use row-major ('C') or column-major ('FORTRAN') memory representation. Default is ' C '.

## Returns

```
        out : MaskedArray
```

Masked array interpretation of $a$.

## See Also:

## asanyarray

Similar to asarray, but conserves subclasses.

## Examples

```
>>> x = np.arange(10.).reshape(2, 5)
>>> x
array([[ 0., 1., 2., 3., 4.],
    [ 5., 6., 7., 8., 9.]])
>>> np.ma.asarray(x)
```

```
masked_array(data =
    [[ 0. 1. 2. 3. 4.]
    [ 5. 6. 7. 8. 9.]],
                        mask =
    False,
        fill_value = 1e+20)
>>> type(np.ma.asarray(x))
<class 'numpy.ma.core.MaskedArray'>
```

numpy.ma. asanyarray ( $a$, dtype $=$ None )
Convert the input to a masked array, conserving subclasses.
If $a$ is a subclass of MaskedArray, its class is conserved. No copy is performed if the input is already an ndarray.

## Parameters

a : array_like
Input data, in any form that can be converted to an array.
dtype : dtype, optional
By default, the data-type is inferred from the input data.
order : \{‘C', 'F'\}, optional
Whether to use row-major ('C') or column-major ('FORTRAN') memory representation. Default is ' C '.

## Returns

out : MaskedArray
MaskedArray interpretation of $a$.

## See Also:

asarray
Similar to asanyarray, but does not conserve subclass.

## Examples

```
>>> x = np.arange(10.).reshape(2, 5)
>>> x
array([[ 0., 1., 2., 3., 4.],
    [ 5., 6., 7., 8., 9.]])
>>> np.ma.asanyarray(x)
masked_array(data =
    [[ 0. 1. 2. 3. 4.]
    [ 5. 6. 7. 8. 9.]],
        mask =
        False,
            fill_value = 1e+20)
        >>> type(np.ma.asanyarray(x))
        <class ' numpy.ma.core.MaskedArray'>
numpy.ma.fix_invalid(a,mask=False, copy=True,fill_value=None)
    Return input with invalid data masked and replaced by a fill value.
Invalid data means values of nan, inf, etc.
```


## Parameters

a : array_like

Input array, a (subclass of) ndarray.
copy : bool, optional
Whether to use a copy of $a$ (True) or to fix $a$ in place (False). Default is True.
fill_value : scalar, optional
Value used for fixing invalid data. Default is None, in which case the a.fill_value is used.

## Returns

b : MaskedArray
The input array with invalid entries fixed.

## Notes

A copy is performed by default.

## Examples

```
>>> x = np.ma.array([1., -1, np.nan, np.inf], mask=[1] + [0]*3)
>>> x
masked_array(data = [-- -1.0 nan inf],
            mask = [ True False False False],
    fill_value = 1e+20)
>>> np.ma.fix_invalid(x)
masked_array(data = [-- -1.0 -- --],
            mask = [ True False True True],
    fill_value = 1e+20)
>>> fixed = np.ma.fix_invalid(x)
>>> fixed.data
array([ 1.00000000e+00, -1.00000000e+00, 1.00000000e+20,
    1.00000000e+20])
>>> x.data
array([ 1., -1., NaN, Inf])
```

numpy.ma.masked_equal ( $x$, value, copy=True)
Mask an array where equal to a given value.
This function is a shortcut to masked_where, with condition $=(x==$ value). For floating point arrays, consider using masked_values ( $x$, value).

## See Also:

masked_where

## Mask where a condition is met.

masked_values
Mask using floating point equality.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_equal(a, 2)
masked_array(data = [0 1 -- 3],
```

```
mask = [False False True False],
fill_value=999999)
```

numpy.ma.masked_greater ( $x$, value, copy=True)
Mask an array where greater than a given value.
This function is a shortcut to masked_where, with condition $=(x>$ value $)$.

## See Also:

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_greater(a, 2)
masked_array(data = [0 1 2 --],
    mask = [False False False True],
    fill_value=999999)
```

numpy.ma.masked_greater_equal ( $x$, value, copy=True)
Mask an array where greater than or equal to a given value.
This function is a shortcut to masked_where, with condition $=(x>=$ value $)$.

## See Also:

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_greater_equal(a, 2)
masked_array(data = [0 1 -- --],
    mask = [False False True True],
    fill_value=999999)
```

numpy.ma.masked_inside ( $x, v 1, v 2$, copy=True)
Mask an array inside a given interval.
Shortcut to masked_where, where condition is True for $x$ inside the interval [v1,v2] (v1 $<=\mathrm{x}<=\mathrm{v} 2$ ). The boundaries $v 1$ and $v 2$ can be given in either order.

## See Also:

masked_where
Mask where a condition is met.

## Notes

The array $x$ is prefilled with its filling value.

## Examples

```
>>> import numpy.ma as ma
>>> x = [0.31, 1.2, 0.01, 0.2, -0.4, -1.1]
>>> ma.masked_inside(x, -0.3, 0.3)
masked_array(data = [0.31 1.2 -- -- -0.4 -1.1],
    mask = [False False True True False False],
    fill_value=1e+20)
```

The order of $v l$ and $v 2$ doesn't matter.

```
>>> ma.masked_inside(x, 0.3, -0.3)
masked_array(data = [0.31 1.2 -- -- -0.4 -1.1],
    mask = [False False True True False False],
    fill_value=1e+20)
```

numpy.ma.masked_invalid(a, copy=True)
Mask an array where invalid values occur (NaNs or infs).
This function is a shortcut to masked_where, with condition $=\sim(n p . i s f i n i t e(a))$. Any pre-existing mask is conserved. Only applies to arrays with a dtype where NaNs or infs make sense (i.e. floating point types), but accepts any array_like object.

## See Also:

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(5, dtype=np.float)
>>> a[2] = np.NaN
>>> a[3] = np.PINF
>>> a
array([ 0., 1., NaN, Inf, 4.])
>>> ma.masked_invalid(a)
masked_array(data = [0.0 1.0 -- -- 4.0],
            mask = [False False True True False],
            fill_value=1e+20)
```

numpy.ma.masked_less ( $x$, value, copy=True)
Mask an array where less than a given value.
This function is a shortcut to masked_where, with condition $=(x<$ value $)$.

## See Also:

```
masked_where
```

Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_less(a, 2)
masked_array(data = [-- -- 2 3],
```

```
mask = [ True True False False],
fill_value=999999)
```

numpy.ma.masked_less_equal ( $x$, value, copy=True)
Mask an array where less than or equal to a given value.
This function is a shortcut to masked_where, with condition $=(\mathrm{x}<=$ value $)$.

## See Also:

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_less_equal(a, 2)
masked_array(data = [-- -- -- 3],
    mask = [ True True True False],
    fill_value=999999)
```

numpy.ma.masked_not_equal ( $x$, value, copy=True)

Mask an array where not equal to a given value.
This function is a shortcut to masked_where, with condition $=(x!=$ value $)$.

## See Also:

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_not_equal(a, 2)
masked_array(data = [-- -- 2 --],
    mask = [ True True False True],
    fill_value=999999)
```

numpy.ma.masked_object ( $x$, value, copy=True, shrink=True)
Mask the array $x$ where the data are exactly equal to value.
This function is similar to masked_values, but only suitable for object arrays: for floating point, use masked_values instead.

## Parameters

$\mathbf{x}$ : array_like
Array to mask
value : object
Comparison value
copy : \{True, False\}, optional

Whether to return a copy of $x$.
shrink: \{True, False $\}$, optional
Whether to collapse a mask full of False to nomask

## Returns

result : MaskedArray
The result of masking $x$ where equal to value.

## See Also:

masked_where
Mask where a condition is met.
masked_equal
Mask where equal to a given value (integers).
masked_values
Mask using floating point equality.

## Examples

```
>>> import numpy.ma as ma
>>> food = np.array(['green_eggs', 'ham'], dtype=object)
>>> # don't eat spoiled food
>>> eat = ma.masked_object(food, 'green_eggs')
>>> print eat
[-- ham]
>>> # plain ol' ham is boring
>>> fresh_food = np.array(['cheese', 'ham', 'pineapple'], dtype=object)
>>> eat = ma.masked_object(fresh_food, 'green_eggs')
>>> print eat
[cheese ham pineapple]
```

Note that mask is set to nomask if possible.

```
>>> eat
masked_array(data = [cheese ham pineapple],
        mask = False,
        fill_value=?)
```

numpy.ma.masked_outside ( $x, v 1, v 2$, copy=True)

Mask an array outside a given interval.
Shortcut to masked_where, where condition is True for $x$ outside the interval [v1,v2] ( $\mathrm{x}<\mathrm{v} 1) \mid(\mathrm{x}>\mathrm{v} 2)$. The boundaries $v 1$ and $v 2$ can be given in either order.

## See Also:

## masked_where

Mask where a condition is met.

## Notes

The array $x$ is prefilled with its filling value.

## Examples

```
>>> import numpy.ma as ma
>>> x = [0.31, 1.2, 0.01, 0.2, -0.4, -1.1]
>>> ma.masked_outside(x, -0.3, 0.3)
masked_array(data = [-- -- 0.01 0.2 -- --],
    mask = [ True True False False True True],
    fill_value=1e+20)
```

The order of $v 1$ and $v 2$ doesn't matter.

```
>>> ma.masked_outside(x, 0.3, -0.3)
masked_array(data = [-- -- 0.01 0.2 -- --],
    mask = [ True True False False True True],
    fill_value=1e+20)
```

numpy.ma.masked_values $(x, \quad$ value, $\quad$ rtol $=1.0000000000000001 e-05, \quad$ atol $=1 e-08, \quad$ copy $=$ True, shrink=True)
Mask using floating point equality.
Return a MaskedArray, masked where the data in array $x$ are approximately equal to value, i.e. where the following condition is True
(abs(x - value) <= atol+rtol*abs(value))
The fill_value is set to value and the mask is set to nomask if possible. For integers, consider using masked_equal.

## Parameters

$\mathbf{x}$ : array_like
Array to mask.
value : float
Masking value.
rtol : float, optional
Tolerance parameter.
atol : float, optional
Tolerance parameter (1e-8).
copy : bool, optional
Whether to return a copy of $x$.
shrink : bool, optional
Whether to collapse a mask full of False to nomask.

## Returns

result : MaskedArray
The result of masking $x$ where approximately equal to value.

## See Also:

masked_where
Mask where a condition is met.
masked_equal
Mask where equal to a given value (integers).

## Examples

```
>>> import numpy.ma as ma
>>> x = np.array([1, 1.1, 2, 1.1, 3])
>>> ma.masked_values(x, 1.1)
masked_array(data = [1.0 -- 2.0 -- 3.0],
    mask = [False True False True False],
    fill_value=1.1)
```

Note that mask is set to nomask if possible.

```
>>> ma.masked_values(x, 1.5)
masked_array(data = [ 1. 1.1 2. 1.1 3. ],
    mask = False,
    fill_value=1.5)
```

For integers, the fill value will be different in general to the result of masked_equal.

```
>>> x = np.arange(5)
>>> x
array([0, 1, 2, 3, 4])
>>> ma.masked_values(x, 2)
masked_array(data = [0 1 -- 3 4],
    mask = [False False True False False],
    fill_value=2)
>>> ma.masked_equal(x, 2)
masked_array(data = [0 1 -- 3 4],
    mask = [False False True False False],
    fill_value=999999)
```

numpy.ma.masked_where (condition, $a$, copy=True)

Mask an array where a condition is met.
Return $a$ as an array masked where condition is True. Any masked values of $a$ or condition are also masked in the output.

## Parameters

condition : array_like
Masking condition. When condition tests floating point values for equality, consider using masked_values instead.
a : array_like
Array to mask.
copy : bool
If True (default) make a copy of $a$ in the result. If False modify $a$ in place and return a view.

## Returns

result : MaskedArray
The result of masking $a$ where condition is True.

## See Also:

masked_values
Mask using floating point equality.
masked_equal
Mask where equal to a given value.

```
masked_not_equal
```

Mask where not equal to a given value.

```
masked_less_equal
```

Mask where less than or equal to a given value.
masked_greater_equal
Mask where greater than or equal to a given value.
masked_less
Mask where less than a given value.
masked_greater
Mask where greater than a given value.
masked_inside
Mask inside a given interval.

```
masked outside
```

Mask outside a given interval.
masked_invalid
Mask invalid values (NaNs or infs).

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_where(a <= 2, a)
masked_array(data = [-- -- -- 3],
    mask = [ True True True False],
    fill_value=999999)
```

Mask array $b$ conditional on $a$.

```
>>> b = ['a', 'b', 'c', 'd']
>>> ma.masked_where(a == 2, b)
masked_array(data = [a b -- d],
    mask = [False False True False],
    fill_value=N/A)
```

Effect of the copy argument.

```
>>> c = ma.masked_where(a <= 2, a)
>>> c
masked_array(data = [-- -- -- 3],
    mask = [ True True True False],
    fill_value=999999)
>>> c[0] = 99
>>> c
masked_array(data = [99 -- -- 3],
    mask = [False True True False],
    fill_value=999999)
>>> a
array([0, 1, 2, 3])
>>> c = ma.masked_where(a <= 2, a, copy=False)
>>> c[0] = 99
>>> c
masked_array(data = [99 -- -- 3],
```

```
    mask = [False True True False],
    fill_value=999999)
>>> a
array([99, 1, 2, 3])
```

When condition or $a$ contain masked values.

```
>>> a = np.arange(4)
>>> a = ma.masked_where(a == 2, a)
>>> a
masked_array(data = [0 1 -- 3],
    mask = [False False True False],
    fill_value=999999)
>>> b = np.arange(4)
>>> b = ma.masked_where(b == 0, b)
>>> b
masked_array(data = [-- 1 2 3}]
    mask = [ True False False False],
    fill_value=999999)
>>> ma.masked_where(a == 3, b)
masked_array(data = [-- 1 -- --],
    mask = [ True False True True],
    fill_value=999999)
```


## $>$ to a ndarray

| ma.compress_cols(a) | Suppress whole columns of a 2-D array that contain masked values. |
| :--- | :--- |
| ma.compress_rowcols(x[, axis]) | Suppress the rows and/or columns of a 2-D array that contain |
| ma.compress_rows(a) | Suppress whole rows of a 2-D array that contain masked values. |
| ma.compressed(x) | Return all the non-masked data as a 1-D array. |
| ma.filled(a[, fill_value]) | Return input as an array with masked data replaced by a fill value. |
| ma.MaskedArray.compressed() | Return all the non-masked data as a 1-D array. |
| ma.MaskedArray.filled([fill_value]) | Return a copy of self, with masked values filled with a given value. |
| numpy.ma.compress_cols $(a)$ |  |

Suppress whole columns of a 2-D array that contain masked values.
This is equivalent to np.ma.extras.compress_rowcols(a, 1), see extras.compress_rowcols for details.

See Also:
extras.compress_rowcols
numpy.ma.compress_rowcols ( $x$, axis=None)
Suppress the rows and/or columns of a 2-D array that contain masked values.
The suppression behavior is selected with the axis parameter.
-If axis is None, both rows and columns are suppressed.
-If axis is 0 , only rows are suppressed.
-If axis is 1 or -1 , only columns are suppressed.

## Parameters

axis : int, optional
Axis along which to perform the operation. Default is None.

## Returns

compressed_array : ndarray
The compressed array.

## Examples

```
>>> x = np.ma.array(np.arange(9).reshape(3, 3), mask=[[1, 0, 0],
... [1,0,0],
... [0, 0, 0]])
>>> x
masked_array(data =
    [[-- 1 2]
    [-- 4 5]
    [\begin{array}{lll}{6}&{7}&{8}\end{array}],
                mask =
    [[ True False False]
    [ True False False]
    [False False False]],
            fill_value = 999999)
>>> np.ma.extras.compress_rowcols(x)
array([[7, 8]])
>>> np.ma.extras.compress_rowcols(x, 0)
array([[6, 7, 8]])
>>> np.ma.extras.compress_rowcols(x, 1)
array([[1, 2],
    [4, 5],
    [7, 8]])
```

numpy.ma.compress_rows (a)

Suppress whole rows of a 2-D array that contain masked values.
This is equivalent to np.ma.extras.compress_rowcols (a, 0), see extras.compress_rowcols for details.

## See Also:

extras.compress_rowcols
numpy.ma. compressed $(x)$
Return all the non-masked data as a 1-D array.
This function is equivalent to calling the "compressed" method of a MaskedArray, see MaskedArray.compressed for details.

See Also:

MaskedArray. compressed
Equivalent method.
numpy.ma. $\mathbf{f i l l e d}(a$, fill_value $=$ None $)$
Return input as an array with masked data replaced by a fill value.
If $a$ is not a MaskedArray, $a$ itself is returned. If $a$ is a MaskedArray and fill_value is None, fill_value is set to a.fill_value.

## Parameters

a : MaskedArray or array_like
An input object.
fill_value : scalar, optional
Filling value. Default is None.

## Returns

a : ndarray
The filled array.

## See Also:

compressed

## Examples

```
>>> x = np.ma.array(np.arange(9).reshape(3, 3), mask=[[1, 0, 0],
... [1, 0, 0],
\cdots. [0, 0, 0]])
>>> x.filled()
array([[999999, 1, 2],
    [999999, 4, 5],
    [ 6, 7, 8]])
```

MaskedArray. compressed()

Return all the non-masked data as a 1-D array.

## Returns

data : ndarray
A new ndarray holding the non-masked data is returned.

## Notes

The result is not a MaskedArray!

## Examples

```
>>> x = np.ma.array(np.arange(5), mask=[0]*2 + [1]*3)
>>> x.compressed()
array([0, 1])
>>> type(x.compressed())
<type 'numpy.ndarray'>
MaskedArray.filled(fill_value=None)
```

Return a copy of self, with masked values filled with a given value.

## Parameters

fill_value : scalar, optional
The value to use for invalid entries (None by default). If None, the fill_value attribute of the array is used instead.

## Returns

filled_array : ndarray
A copy of self with invalid entries replaced by fill_value (be it the function argument or the attribute of self.

## Notes

The result is not a MaskedArray!

## Examples

```
>>> x = np.ma.array([1,2,3,4,5], mask=[0,0,1,0,1], fill_value=-999)
>>> x.filled()
array([1, 2, -999, 4, -999])
>>> type(x.filled())
<type 'numpy.ndarray'>
```

Subclassing is preserved. This means that if the data part of the masked array is a matrix, filled returns a matrix:

```
>>> x = np.ma.array(np.matrix([[1, 2], [3, 4]]), mask=[[0, 1], [1, 0]])
>>> x.filled()
matrix([[ 1, 999999],
    [999999, 4]])
```

> to another object
ma.MaskedArray.tofile(fid[, sep, Save a masked array to a file in binary format.
format])
ma.MaskedArray.tolist([fill_value]) Return the data portion of the masked array as a hierarchical
Python list.
ma.MaskedArray.torecords()
ma.MaskedArray.tostring([fill_value, Return the array data as a string containing the raw bytes in the
order])
array.

MaskedArray.tofile (fid, sep='', format='\%s')
Save a masked array to a file in binary format.
Warning: This function is not implemented yet

## Raises

## NotImplementedError :

When tofile is called.
MaskedArray.tolist (fill_value=None)
Return the data portion of the masked array as a hierarchical Python list.
Data items are converted to the nearest compatible Python type. Masked values are converted to fill_value. If fill_value is None, the corresponding entries in the output list will be None.

## Parameters

fill_value : scalar, optional
The value to use for invalid entries. Default is None.

## Returns

result : list
The Python list representation of the masked array.

## Examples

>>> $x=n p . m a . \operatorname{array}([[1,2,3],[4,5,6],[7,8,9]], \operatorname{mask}=[0]+[1,0] * 4)$
>>> x.tolist()
[[1, None, 3], [None, 5, None], [7, None, 9]]
>>> x.tolist(-999)
$[[1,-999,3],[-999,5,-999],[7,-999,9]]$
MaskedArray.torecords()
Transforms a masked array into a flexible-type array.

The flexible type array that is returned will have two fields:
-the _dat a field stores the _data part of the array.
-the _mask field stores the _mask part of the array.

## Parameters

None :

## Returns

record : ndarray
A new flexible-type ndarray with two fields: the first element containing a value, the second element containing the corresponding mask boolean. The returned record shape matches self.shape.

## Notes

A side-effect of transforming a masked array into a flexible ndarray is that meta information (fill_value, ...) will be lost.

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 --]
    [7 -- 9]]
>>> print x.toflex()
[[(1, False) (2, True) (3, False)]
    [(4, True) (5, False) (6, True)]
    [(7, False) (8, True) (9, False)]]
```

MaskedArray.tostring (fill_value=None, order='C')
Return the array data as a string containing the raw bytes in the array.
The array is filled with a fill value before the string conversion.

## Parameters

 fill_value : scalar, optionalValue used to fill in the masked values. Deafult is None, in which case MaskedArray.fill_value is used.
order : \{ 'C','F', $A$ ' $\}$, optional
Order of the data item in the copy. Default is ' C '.

- ' C ' - C order (row major).
- 'F' - Fortran order (column major).
- 'A' - Any, current order of array.
- None - Same as ' $A$ '.


## See Also:

ndarray.tostring, tolist, tofile

## Notes

As for ndarray.tostring, information about the shape, dtype, etc., but also about fill_value, will be lost.

## Examples

```
>>> x = np.ma.array(np.array([[1, 2], [3, 4]]), mask=[[0, 1], [1, 0]])
>>> x.tostring()
'\x01\x00\x00\x00?B\x0f\x00?B\x0f\x00\x04\x00\x00\x00'
```


## Pickling and unpickling

```
ma.dump(a, F) Pickle a masked array to a file.
ma.dumps(a) Return a string corresponding to the pickling of a masked array.
ma.load(F) Wrapper around cPickle.load which accepts either a file-like object
ma.loads(strg) Load a pickle from the current string.
```

numpy.ma. dump ( $a, F$ )

Pickle a masked array to a file.
This is a wrapper around cPickle.dump.

## Parameters

a : MaskedArray
The array to be pickled.
F : str or file-like object
The file to pickle $a$ to. If a string, the full path to the file.
numpy.ma.dumps (a)
Return a string corresponding to the pickling of a masked array.
This is a wrapper around cPickle.dumps.

## Parameters

a : MaskedArray
The array for which the string representation of the pickle is returned.
numpy.ma.load (F)
Wrapper around CPickle.load which accepts either a file-like object or a filename.

## Parameters

F : str or file
The file or file name to load.

## See Also:

dump
Pickle an array

## Notes

This is different from numpy. load, which does not use cPickle but loads the NumPy binary .npy format.

```
numpy.ma.loads (strg)
```

Load a pickle from the current string.
The result of cPickle.loads (strg) is returned.

## Parameters

strg : str
The string to load.

## See Also:

dumps
Return a string corresponding to the pickling of a masked array.

## Filling a masked array

```
ma.common_fill_value(a,b) Return the common filling value of two masked arrays, if any.
ma.default_fill_value(obj) Return the default fill value for the argument object.
ma.maximum_fill_value(obj) Return the minimum value that can be represented by the dtype of
an object.
ma.maximum_fill_value(obj) Return the minimum value that can be represented by the dtype of
an object.
ma.set_fill_value(a,fill_value) Set the filling value of a, if a is a masked array.
ma.MaskedArray.get_fill_value() Return the filling value of the masked array.
ma.MaskedArray.set_fill_value([val&ef)the filling value of the masked array.
ma.MaskedArray.fill_value Filling value.
```

numpy.ma.common_fill_value $(a, b)$
Return the common filling value of two masked arrays, if any.
If a.fill_value == b.fill_value, return the fill value, otherwise return None.

## Parameters

a, b: MaskedArray
The masked arrays for which to compare fill values.

## Returns

fill_value : scalar or None
The common fill value, or None.

## Examples

```
>>> x = np.ma.array([0, 1.], fill_value=3)
>>> y = np.ma.array([0, 1.], fill_value=3)
>>> np.ma.common_fill_value(x, y)
3.0
```

numpy.ma.default_fill_value (obj)

Return the default fill value for the argument object.
The default filling value depends on the datatype of the input array or the type of the input scalar:

| datatype | default |
| :--- | :--- |
| bool | True |
| int | 999999 |
| float | $1 . \mathrm{e} 20$ |
| complex | $1 . \mathrm{e} 20+0 \mathrm{j}$ |
| object | '?' |
| string | 'N/A' |

## Parameters

obj : ndarray, dtype or scalar
The array data-type or scalar for which the default fill value is returned.

## Returns

fill_value : scalar
The default fill value.

## Examples

```
>>> np.ma.default_fill_value(1)
999999
>>> np.ma.default_fill_value(np.array([1.1, 2., np.pi]))
1e+20
>>> np.ma.default_fill_value(np.dtype(complex))
(1e+20+0j)
```

numpy.ma.maximum_fill_value (obj)

Return the minimum value that can be represented by the dtype of an object.
This function is useful for calculating a fill value suitable for taking the maximum of an array with a given dtype.

## Parameters

obj : \{ndarray, dtype\}
An object that can be queried for it's numeric type.

## Returns

val : scalar
The minimum representable value

## Raises

TypeError :
If $o b j$ isn't a suitable numeric type.

## See Also:

minimum_fill_value
The inverse function.
set_fill_value
Set the filling value of a masked array.
MaskedArray.fill_value
Return current fill value.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.int8()
>>> ma.maximum_fill_value(a)
-128
>>> a = np.int32()
>>> ma.maximum_fill_value(a)
-2147483648
```

An array of numeric data can also be passed.

```
>>> a = np.array([1, 2, 3], dtype=np.int8)
>>> ma.maximum_fill_value(a)
-128
>>> a = np.array([1, 2, 3], dtype=np.float32)
>>> ma.maximum_fill_value(a)
-inf
```

numpy.ma.maximum_fill_value (obj)
Return the minimum value that can be represented by the dtype of an object.
This function is useful for calculating a fill value suitable for taking the maximum of an array with a given dtype.

## Parameters

obj : \{ndarray, dtype\}
An object that can be queried for it's numeric type.

## Returns

val : scalar
The minimum representable value.

## Raises

TypeError :
If $o b j$ isn't a suitable numeric type.

## See Also:

minimum_fill_value
The inverse function.

```
set_fill_value
```

Set the filling value of a masked array.
MaskedArray.fill_value
Return current fill value.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.int8()
>>> ma.maximum_fill_value(a)
-128
>>> a = np.int32()
>>> ma.maximum_fill_value(a)
-2147483648
```

An array of numeric data can also be passed.

```
>>> a = np.array([1, 2, 3], dtype=np.int8)
>>> ma.maximum_fill_value(a)
-128
>>> a = np.array([1, 2, 3], dtype=np.float32)
>>> ma.maximum_fill_value(a)
-inf
numpy.ma.set_fill_value(a,fill_value)
```

Set the filling value of $a$, if $a$ is a masked array.
This function changes the fill value of the masked array $a$ in place. If $a$ is not a masked array, the function returns silently, without doing anything.

## Parameters

a: array_like
Input array.
fill_value : dtype
Filling value. A consistency test is performed to make sure the value is compatible with the dtype of $a$.

## Returns

None :

Nothing returned by this function.

## See Also:

maximum_fill_value
Return the default fill value for a dtype.
MaskedArray.fill_value
Return current fill value.
MaskedArray.set_fill_value
Equivalent method.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(5)
>>> a
array([0, 1, 2, 3, 4])
>>> a = ma.masked_where(a < 3, a)
>>> a
masked_array(data = [-- -- -- 3 4],
    mask = [ True True True False False],
    fill_value=999999)
>>> ma.set_fill_value(a, -999)
>>> a
masked_array(data = [-- -- -- 3 4],
    mask = [ True True True False False],
    fill_value=-999)
```

Nothing happens if $a$ is not a masked array.

```
>>> a = range(5)
>>> a
[0, 1, 2, 3, 4]
>>> ma.set_fill_value(a, 100)
>>> a
[0, 1, 2, 3, 4]
>>> a = np.arange(5)
>>> a
array([0, 1, 2, 3, 4])
>>> ma.set_fill_value(a, 100)
>>> a
array([0, 1, 2, 3, 4])
```

MaskedArray.get_fill_value()

Return the filling value of the masked array.

## Returns

fill_value : scalar
The filling value.

## Examples

```
>>> for dt in [np.int32, np.int64, np.float64, np.complex128]:
... np.ma.array([0, 1], dtype=dt).get_fill_value()
999999
999999
```

```
1e+20
(1e+20+0j)
>>> x = np.ma.array([0, 1.], fill_value=-np.inf)
>>> x.get_fill_value()
-inf
MaskedArray.set_fill_value (value=None)
Set the filling value of the masked array.
```


## Parameters

value : scalar, optional
The new filling value. Default is None, in which case a default based on the data type is used.

## See Also:

ma.set_fill_value
Equivalent function.

## Examples

```
>>> x = np.ma.array([0, 1.], fill_value=-np.inf)
>>> x.fill_value
-inf
>>> x.set_fill_value(np.pi)
>>> x.fill_value
3.1415926535897931
```

Reset to default:
>>> x.set_fill_value()
>>> x.fill_value
$1 \mathrm{e}+20$
MaskedArray.fill_value
Filling value.

## Masked arrays arithmetics

## Arithmetics

| ma. anom(self[, axis, dtype]) | Compute the anomalies (deviations from the arithmetic mean) along the given axis. |
| :---: | :---: |
| ma. anomalies(self[, axis, dtype]) | Compute the anomalies (deviations from the arithmetic mean) along the given axis. |
| ma. average(a[, axis, weights, returned]) | Return the weighted average of array over the given axis. |
| ma.conjugate() | Return the complex conjugate, element-wise. |
| ma.corrcoef(x[, y, rowvar, bias, ...]) | Return correlation coefficients of the input array. |
| ma. $\operatorname{cov}(x[, y$, rowvar, bias, allow_masked, ddof]) | Estimate the covariance matrix. |
| ma. cumsum(self[, axis, dtype, o | Return the cumulative sum of the elements along the given axis. |
| ma. cumprod(self[, axis, dtype, out]) | Return the cumulative product of the elements along the given axis. |
| ma.mean(self[, axis, dtype, out]) | Returns the average of the array elements. |
| ma.median(a[, axis, out, overwrite_input]) | Compute the median along the specified axis. |
| ma.power(a, b[, third]) | Returns element-wise base array raised to power from second array. |
| ma.prod(self[, axis, dtype, out]) | Return the product of the array elements over the given axis. |
| ma.std(self[, axis, dtype, out, ddof]) | Compute the standard deviation along the specified axis. |
| ma. sum(self[, axis, dtype, out]) | Return the sum of the array elements over the given axis. |
| ma.var(self[, axis, dtype, out, ddof]) | Compute the variance along the specified axis. |
| ma.MaskedArray.anom([axis, dtype]) | Compute the anomalies (deviations from the arithmetic mean) along the given axis. |
| ma. MaskedArray.cumprod([axis, dtype, out]) | Return the cumulative product of the elements along the given axis. |
| ma.MaskedArray. cumsum([axis, dtype, out]) | Return the cumulative sum of the elements along the given axis. |
| ma.MaskedArray.mean([axis, dtype, out]) | Returns the average of the array elements. |
| ma.MaskedArray.prod([axis, dtype, out]) | Return the product of the array elements over the given axis. |
| ma.MaskedArray.std([axis, dtype, out, ddof]) | Compute the standard deviation along the specified axis. |
| ma.MaskedArray.sum([axis, dtype, out]) | Return the sum of the array elements over the given axis. |
| ma.MaskedArray.var([axis, dtype, out, ddof]) | Compute the variance along the specified axis. |

numpy .ma. anom (self, axis=None, dtype=None)
Compute the anomalies (deviations from the arithmetic mean) along the given axis.
Returns an array of anomalies, with the same shape as the input and where the arithmetic mean is computed along the given axis.

## Parameters

axis : int, optional
Axis over which the anomalies are taken. The default is to use the mean of the flattened array as reference.
dtype : dtype, optional
Type to use in computing the variance. For arrays of integer type
the default is float 32 ; for arrays of float types it is the same as the array type.

## See Also:

mean
Compute the mean of the array.

## Examples

```
>>> a = np.ma.array([1,2,3])
>>> a.anom()
masked_array(data = [-1. 0. 1.],
                    mask = False,
    fill_value = 1e+20)
```

numpy.ma. anomalies (self, axis=None, dtype=None)
Compute the anomalies (deviations from the arithmetic mean) along the given axis.
Returns an array of anomalies, with the same shape as the input and where the arithmetic mean is computed along the given axis.

## Parameters

axis : int, optional
Axis over which the anomalies are taken. The default is to use the mean of the flattened array as reference.
dtype : dtype, optional
Type to use in computing the variance. For arrays of integer type
the default is float 32 ; for arrays of float types it is the same as the array type.
See Also:
mean
Compute the mean of the array.
Examples
$\ggg a=n p \cdot m a \cdot \operatorname{array}([1,2,3])$
>>> a.anom()
masked_array (data $=[-1.0 .1$.$] ,$
mask $=$ False,
fill_value = 1e+20)
numpy.ma. average ( $a$, axis=None, weights=None, returned $=$ False )

Return the weighted average of array over the given axis.

## Parameters

a : array_like
Data to be averaged. Masked entries are not taken into account in the computation.
axis : int, optional
Axis along which the variance is computed. The default is to compute the variance of the flattened array.
weights : array_like, optional
The importance that each element has in the computation of the average. The weights array can either be 1-D (in which case its length must be the size of $a$ along the given axis) or of the same shape as $a$. If weights=None, then all data in $a$ are assumed to have a weight equal to one.
returned : bool, optional
Flag indicating whether a tuple (result, sum of weights) should be returned as output (True), or just the result (False). Default is False.

## Returns

average, [sum_of_weights] : (tuple of) scalar or MaskedArray
The average along the specified axis. When returned is True, return a tuple with the average as the first element and the sum of the weights as the second element. The return type is $n p$.float64 if $a$ is of integer type, otherwise it is of the same type as $a$. If returned, sum_of_weights is of the same type as average.

## Examples

```
>>> a = np.ma.array([1., 2., 3., 4.], mask=[False, False, True, True])
>>> np.ma.average(a, weights=[3, 1, 0, 0])
1.25
>>> x = np.ma.arange(6.).reshape(3, 2)
>>> print x
[[ 0. 1.]
    [ 2. 3.]
    [ 4. 5.]]
>>> avg, sumweights = np.ma.average(x, axis=0, weights=[1, 2, 3],
... returned=True)
>>> print avg
[2.66666666667 3.66666666667]
```

numpy.ma. conjugate ( $x[$, out $]$ )
Return the complex conjugate, element-wise.
The complex conjugate of a complex number is obtained by changing the sign of its imaginary part.

## Parameters

$\mathbf{x}$ : array_like
Input value.

## Returns

$\mathbf{y}$ : ndarray
The complex conjugate of $x$, with same dtype as $y$.

## Examples

```
>>> np.conjugate(1+2j)
(1-2j)
>>> x = np.eye(2) + 1j * np.eye(2)
>>> np.conjugate(x)
array([[ 1.-1.j, 0.-0.j],
    [ 0.-0.j, 1.-1.j]])
```

numpy.ma.corrcoef ( $x, y=$ None, rowvar=True, bias=False, allow_masked=True, ddof=None)

Return correlation coefficients of the input array.
Except for the handling of missing data this function does the same as numpy. corrcoef. For more details and examples, see numpy. corrcoef.

## Parameters

$\mathbf{x}$ : array_like

A 1-D or 2-D array containing multiple variables and observations. Each row of $x$ represents a variable, and each column a single observation of all those variables. Also see rowvar below.
$\mathbf{y}$ : array_like, optional
An additional set of variables and observations. $y$ has the same shape as $x$.
rowvar : bool, optional
If rowvar is True (default), then each row represents a variable, with observations in the columns. Otherwise, the relationship is transposed: each column represents a variable, while the rows contain observations.
bias : bool, optional
Default normalization (False) is by ( $\mathrm{N}-1$ ), where N is the number of observations given (unbiased estimate). If bias is 1, then normalization is by N. This keyword can be overridden by the keyword ddof in numpy versions $>=1.5$.
allow_masked : bool, optional
If True, masked values are propagated pair-wise: if a value is masked in $x$, the corresponding value is masked in $y$. If False, raises an exception.
ddof : \{None, int \}, optional
New in version 1.5. If not None normalization is by ( $N$ - ddof), where $N$ is the number of observations; this overrides the value implied by bias. The default value is None.

## See Also:

numpy. corrcoef
Equivalent function in top-level NumPy module.
cov
Estimate the covariance matrix.
numpy.ma.cov ( $x, y=$ None, rowvar=True, bias=False, allow_masked=True, $d d o f=$ None $)$
Estimate the covariance matrix.
Except for the handling of missing data this function does the same as numpy.cov. For more details and examples, see numpy.cov.
By default, masked values are recognized as such. If $x$ and $y$ have the same shape, a common mask is allocated: if $x[i, j]$ is masked, then $y[i, j]$ will also be masked. Setting allow_masked to False will raise an exception if values are missing in either of the input arrays.

## Parameters

$\mathbf{x}$ : array_like
A 1-D or 2-D array containing multiple variables and observations. Each row of $x$ represents a variable, and each column a single observation of all those variables. Also see rowvar below.
$\mathbf{y}$ : array_like, optional
An additional set of variables and observations. $y$ has the same form as $x$.
rowvar : bool, optional

If rowvar is True (default), then each row represents a variable, with observations in the columns. Otherwise, the relationship is transposed: each column represents a variable, while the rows contain observations.
bias : bool, optional
Default normalization (False) is by ( $\mathrm{N}-1$ ), where N is the number of observations given (unbiased estimate). If bias is True, then normalization is by N. This keyword can be overridden by the keyword ddof in numpy versions $>=1.5$.
allow_masked : bool, optional
If True, masked values are propagated pair-wise: if a value is masked in $x$, the corresponding value is masked in $y$. If False, raises a ValueError exception when some values are missing.
ddof : \{None, int \}, optional
New in version 1.5. If not None normalization is by ( $N$ - ddof), where $N$ is the number of observations; this overrides the value implied by bias. The default value is None.

## Raises

## ValueError: :

Raised if some values are missing and allow_masked is False.

## See Also:

numpy.cov
numpy.ma.cumsum (self, axis=None, dtype=None, out=None)
Return the cumulative sum of the elements along the given axis. The cumulative sum is calculated over the flattened array by default, otherwise over the specified axis.
Masked values are set to 0 internally during the computation. However, their position is saved, and the result will be masked at the same locations.

## Parameters

axis : $\{$ None, -1 , int \}, optional
Axis along which the sum is computed. The default (axis = None) is to compute over the flattened array. axis may be negative, in which case it counts from the last to the first axis.
dtype: \{None, dtype\}, optional
Type of the returned array and of the accumulator in which the elements are summed. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

cumsum : ndarray.
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## Notes

The mask is lost if out is not a valid MaskedArray !
Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> marr = np.ma.array(np.arange(10), mask=[0,0,0,1,1,1,0,0,0,0])
>>> print marr.cumsum()
[0 1 3 -- -- -- 9 16 24 33]
```

numpy.ma. cumprod (self, axis=None, dtype=None, out=None)
Return the cumulative product of the elements along the given axis. The cumulative product is taken over the flattened array by default, otherwise over the specified axis.

Masked values are set to 1 internally during the computation. However, their position is saved, and the result will be masked at the same locations.

## Parameters

axis: \{None, -1 , int \}, optional
Axis along which the product is computed. The default (axis $=$ None) is to compute over the flattened array.
dtype : \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are multiplied. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

cumprod : ndarray
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## Notes

The mask is lost if out is not a valid MaskedArray!
Arithmetic is modular when using integer types, and no error is raised on overflow.
numpy.ma.mean (self, axis=None, dtype=None, out=None)
Returns the average of the array elements.
Masked entries are ignored. The average is taken over the flattened array by default, otherwise over the specified axis. Refer to numpy . mean for the full documentation.

## Parameters

a : array_like
Array containing numbers whose mean is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional

Axis along which the means are computed. The default is to compute the mean of the flattened array.
dtype : dtype, optional
Type to use in computing the mean. For integer inputs, the default is float64; for floating point, inputs it is the same as the input dtype.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type will be cast if necessary.

## Returns

mean : ndarray, see dtype parameter above
If out=None, returns a new array containing the mean values, otherwise a reference to the output array is returned.

## See Also:

numpy.ma.mean
Equivalent function.
numpy.mean
Equivalent function on non-masked arrays.
numpy.ma.average
Weighted average.

## Examples

```
>>> a = np.ma.array([1,2,3], mask=[False, False, True])
>>> a
masked_array(data = [1 2 --],
                    mask = [False False True],
            fill_value = 999999)
>>> a.mean()
1.5
```

numpy.ma.median (a, axis=None, out=None, overwrite_input=False)
Compute the median along the specified axis.
Returns the median of the array elements.

## Parameters

a : array_like
Input array or object that can be converted to an array.
axis : int, optional
Axis along which the medians are computed. The default (None) is to compute the median along a flattened version of the array.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.
overwrite_input : bool, optional
If True, then allow use of memory of input array (a) for calculations. The input array will be modified by the call to median. This will save memory when you do not need to
preserve the contents of the input array. Treat the input as undefined, but it will probably be fully or partially sorted. Default is False. Note that, if overwrite_input is True, and the input is not already an ndarray, an error will be raised.

## Returns

median : ndarray
A new array holding the result is returned unless out is specified, in which case a reference to out is returned. Return data-type is float64 for integers and floats smaller than float64, or the input data-type, otherwise.

## See Also:

mean

## Notes

Given a vector V with N non masked values, the median of V is the middle value of a sorted copy of $\mathrm{V}(\mathrm{Vs})$ - i.e. $\operatorname{Vs}[(N-1) / 2]$, when $N$ is odd, or $\{\operatorname{Vs}[N / 2-1]+\operatorname{Vs}[N / 2]\} / 2$ when $N$ is even.

## Examples

```
>>> x = np.ma.array(np.arange(8), mask=[0]*4 + [1]*4)
>>> np.ma.extras.median(x)
1.5
>>> x = np.ma.array(np.arange(10).reshape(2, 5), mask=[0]*6 + [1]*4)
>>> np.ma.extras.median(x)
2.5
>>> np.ma.extras.median(x, axis=-1, overwrite_input=True)
masked_array(data = [ 2. 5.],
            mask = False,
    fill_value = le+20)
```

numpy.ma.power ( $a, b$, third=None)
Returns element-wise base array raised to power from second array.
This is the masked array version of numpy . power. For details see numpy . power.

## See Also:

numpy.power

## Notes

The out argument to numpy. power is not supported, third has to be None.
numpy.ma.prod (self, axis=None, dtype=None, out=None)
Return the product of the array elements over the given axis. Masked elements are set to 1 internally for computation.

## Parameters

axis: \{None, int \}, optional
Axis over which the product is taken. If None is used, then the product is over all the array elements.
dtype : \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are multiplied. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : \{None, array\}, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type will be cast if necessary.

## Returns

product_along_axis : \{array, scalar\}, see dtype parameter above.
Returns an array whose shape is the same as a with the specified axis removed. Returns a 0d array when a is 1 d or axis=None. Returns a reference to the specified output array if specified.

## See Also:

prod
equivalent function

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> np.prod([1.,2.])
2.0
>>> np.prod([1.,2.], dtype=np.int32)
2
>>> np.prod([[1.,2.],[3.,4.]])
24.0
>>> np.prod([[1.,2.],[3.,4.]], axis=1)
array([ 2., 12.])
```

numpy.ma.std (self, axis=None, dtype=None, out=None, $d d o f=0$ )
Compute the standard deviation along the specified axis.
Returns the standard deviation, a measure of the spread of a distribution, of the array elements. The standard deviation is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Calculate the standard deviation of these values.
axis : int, optional
Axis along which the standard deviation is computed. The default is to compute the standard deviation of the flattened array.
dtype : dtype, optional
Type to use in computing the standard deviation. For arrays of integer type the default is float 64 , for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type (of the calculated values) will be cast if necessary.
ddof : int, optional
Means Delta Degrees of Freedom. The divisor used in calculations is N - ddof, where N represents the number of elements. By default ddof is zero.

## Returns

standard_deviation : ndarray, see dtype parameter above.
If out is None, return a new array containing the standard deviation, otherwise return a reference to the output array.

## See Also:

var, mean

## numpy.doc.ufuncs

Section "Output arguments"

## Notes

The standard deviation is the square root of the average of the squared deviations from the mean, i.e., std $=$ sqrt (mean (abs ( $x-x$.mean()) **2)).
The average squared deviation is normally calculated as $\mathrm{x} \cdot \operatorname{sum}() / \mathrm{N}$, where $\mathrm{N}=\operatorname{len}(\mathrm{x}) \cdot$ If, however, $d d o f$ is specified, the divisor N - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of the infinite population. ddo $\mathrm{f}=0$ provides a maximum likelihood estimate of the variance for normally distributed variables. The standard deviation computed in this function is the square root of the estimated variance, so even with ddo $f=1$, it will not be an unbiased estimate of the standard deviation per se.
Note that, for complex numbers, std takes the absolute value before squaring, so that the result is always real and nonnegative.
For floating-point input, the std is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higheraccuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.std(a)
1.1180339887498949
>>> np.std(a, axis=0)
array([ 1., 1.])
>>> np.std(a, axis=1)
array([ 0.5, 0.5])
```

In single precision, $\operatorname{std}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.std(a)
0.45172946707416706
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.std(a, dtype=np.float64)
0.449999999925552653
```

numpy .ma. sum (self, axis=None, dtype=None, out=None)
Return the sum of the array elements over the given axis. Masked elements are set to 0 internally.

## Parameters

axis : $\{$ None, -1 , int $\}$, optional

Axis along which the sum is computed. The default (axis $=$ None) is to compute over the flattened array.
dtype : \{None, dtype \}, optional
Determines the type of the returned array and of the accumulator where the elements are summed. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : \{None, ndarray \}, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

sum_along_axis : MaskedArray or scalar
An array with the same shape as self, with the specified axis removed. If self is a $0-\mathrm{d}$ array, or if axis is None, a scalar is returned. If an output array is specified, a reference to out is returned.

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 --]
    [7 -- 9]]
>>> print x.sum()
25
>>> print x.sum(axis=1)
[4 5 16]
>>> print x.sum(axis=0)
[8 5 12]
>>> print type(x.sum(axis=0, dtype=np.int64)[0])
<type 'numpy.int64'>
numpy.ma. var (self, axis=None, dtype=None, out=None, ddof=0)
Compute the variance along the specified axis.
```

Returns the variance of the array elements, a measure of the spread of a distribution. The variance is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Array containing numbers whose variance is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the variance is computed. The default is to compute the variance of the flattened array.
dtype : data-type, optional
Type to use in computing the variance. For arrays of integer type the default is float 32 ; for arrays of float types it is the same as the array type.
out : ndarray, optional

Alternate output array in which to place the result. It must have the same shape as the expected output, but the type is cast if necessary.
ddof : int, optional
"Delta Degrees of Freedom": the divisor used in the calculation is N - ddof, where N represents the number of elements. By default ddof is zero.

## Returns

variance : ndarray, see dtype parameter above
If out=None, returns a new array containing the variance; otherwise, a reference to the output array is returned.

## See Also:

std
Standard deviation
mean
Average
numpy. doc. ufuncs
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## Notes

The variance is the average of the squared deviations from the mean, i.e., var $=$ mean (abs ( $x-$ $x . \operatorname{mean}()) * * 2)$.

The mean is normally calculated as $x . \operatorname{sum}() / N$, where $N=\operatorname{len}(x)$. If, however, $d d o f$ is specified, the divisor $N$ - ddof is used instead. In standard statistical practice, ddof $=1$ provides an unbiased estimator of the variance of a hypothetical infinite population. ddof $=0$ provides a maximum likelihood estimate of the variance for normally distributed variables.

Note that for complex numbers, the absolute value is taken before squaring, so that the result is always real and nonnegative.

For floating-point input, the variance is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1,2],[3,4]])
>>> np.var(a)
1.25
>>> np.var(a,0)
array([ 1., 1.])
>>> np.var(a,1)
array([ 0.25, 0.25])
```

In single precision, $\operatorname{var}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.var(a)
0.20405951142311096
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.var(a, dtype=np.float64)
0.202499999932997387
>>> ((1-0.55)**2 + (0.1-0.55)**2)/2
0.202500000000000001
MaskedArray.anom (axis=None,dtype=None)
```

Compute the anomalies (deviations from the arithmetic mean) along the given axis.
Returns an array of anomalies, with the same shape as the input and where the arithmetic mean is computed along the given axis.

## Parameters

axis : int, optional
Axis over which the anomalies are taken. The default is to use the mean of the flattened array as reference.
dtype : dtype, optional

## Type to use in computing the variance. For arrays of integer type

the default is float32; for arrays of float types it is the same as the array type.

## See Also:

mean
Compute the mean of the array.

## Examples

```
>>> a = np.ma.array([1,2,3])
>>> a.anom()
masked_array(data = [-1. 0. 1.],
                    mask = False,
fill_value = 1e+20)
```

MaskedArray. cumprod (axis=None, dtype=None, out=None)

Return the cumulative product of the elements along the given axis. The cumulative product is taken over the flattened array by default, otherwise over the specified axis.
Masked values are set to 1 internally during the computation. However, their position is saved, and the result will be masked at the same locations.

## Parameters

axis : $\{$ None, -1 , int $\}$, optional
Axis along which the product is computed. The default (axis $=$ None) is to compute over the flattened array.
dtype : \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are multiplied. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

cumprod : ndarray

A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## Notes

The mask is lost if out is not a valid MaskedArray!
Arithmetic is modular when using integer types, and no error is raised on overflow.
MaskedArray. cumsum (axis=None, dtype=None, out=None)
Return the cumulative sum of the elements along the given axis. The cumulative sum is calculated over the flattened array by default, otherwise over the specified axis.

Masked values are set to 0 internally during the computation. However, their position is saved, and the result will be masked at the same locations.

## Parameters

axis : \{None, -1 , int \}, optional
Axis along which the sum is computed. The default (axis = None) is to compute over the flattened array. axis may be negative, in which case it counts from the last to the first axis.
dtype: \{None, dtype\}, optional
Type of the returned array and of the accumulator in which the elements are summed. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

cumsum : ndarray.
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## Notes

The mask is lost if out is not a valid MaskedArray !
Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> marr = np.ma.array(np.arange(10), mask=[0,0,0,1,1,1,0,0,0,0])
>>> print marr.cumsum()
[0 1 3 -- -- -- 9 16 24 33]
```

MaskedArray.mean (axis=None, dtype=None, out=None)
Returns the average of the array elements.
Masked entries are ignored. The average is taken over the flattened array by default, otherwise over the specified axis. Refer to numpy . mean for the full documentation.

## Parameters

a : array_like
Array containing numbers whose mean is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the means are computed. The default is to compute the mean of the flattened array.
dtype : dtype, optional
Type to use in computing the mean. For integer inputs, the default is float64; for floating point, inputs it is the same as the input dtype.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type will be cast if necessary.

## Returns

mean : ndarray, see dtype parameter above
If out=None, returns a new array containing the mean values, otherwise a reference to the output array is returned.

## See Also:

```
numpy.ma.mean
```

Equivalent function.
numpy.mean
Equivalent function on non-masked arrays.

```
numpy.ma.average
    Weighted average.
```


## Examples

```
>>> a = np.ma.array([1,2,3], mask=[False, False, True])
>>> a
masked_array(data = [1 2 --],
                            mask = [False False True],
            fill_value = 999999)
>>> a.mean()
1.5
MaskedArray.prod (axis=None,dtype=None, out=None)
```

Return the product of the array elements over the given axis. Masked elements are set to 1 internally for computation.

## Parameters

axis : \{None, int \}, optional
Axis over which the product is taken. If None is used, then the product is over all the array elements.
dtype : \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are multiplied. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : \{None, array \}, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type will be cast if necessary.

## Returns

product_along_axis : \{array, scalar\}, see dtype parameter above.
Returns an array whose shape is the same as a with the specified axis removed. Returns a 0d array when a is 1 d or axis=None. Returns a reference to the specified output array if specified.

## See Also:

prod
equivalent function

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> np.prod([1.,2.])
2.0
>>> np.prod([1.,2.], dtype=np.int32)
2
>>> np.prod([[1.,2.],[3.,4.]])
24.0
>>> np.prod([[1.,2.],[3.,4.]], axis=1)
array([ 2., 12.])
```

MaskedArray.std (axis=None, dtype=None, out=None, $d d o f=0$ )

Compute the standard deviation along the specified axis.
Returns the standard deviation, a measure of the spread of a distribution, of the array elements. The standard deviation is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Calculate the standard deviation of these values.
axis : int, optional
Axis along which the standard deviation is computed. The default is to compute the standard deviation of the flattened array.
dtype : dtype, optional
Type to use in computing the standard deviation. For arrays of integer type the default is float64, for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type (of the calculated values) will be cast if necessary.
ddof : int, optional
Means Delta Degrees of Freedom. The divisor used in calculations is N - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

standard_deviation : ndarray, see dtype parameter above.
If out is None, return a new array containing the standard deviation, otherwise return a reference to the output array.

## See Also:

var, mean

## numpy.doc.ufuncs

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## Notes

The standard deviation is the square root of the average of the squared deviations from the mean, i.e., std $=$ sqrt (mean (abs ( $\mathrm{x}-\mathrm{x} . \mathrm{mean}(\mathrm{)}) * * 2$ )).

The average squared deviation is normally calculated as $\mathrm{x} . \operatorname{sum}() / \mathrm{N}$, where $\mathrm{N}=$ len(x). If, however, $d d o f$ is specified, the divisor N - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of the infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables. The standard deviation computed in this function is the square root of the estimated variance, so even with ddof=1, it will not be an unbiased estimate of the standard deviation per se.

Note that, for complex numbers, std takes the absolute value before squaring, so that the result is always real and nonnegative.

For floating-point input, the std is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higheraccuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.std(a)
1.1180339887498949
>>> np.std(a, axis=0)
array([ 1., 1.])
>>> np.std(a, axis=1)
array([ 0.5, 0.5])
```

In single precision, std() can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.std(a)
0.45172946707416706
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.std(a, dtype=np.float64)
0.449999999925552653
```

MaskedArray.sum (axis=None, dtype=None, out=None)
Return the sum of the array elements over the given axis. Masked elements are set to 0 internally.

## Parameters

axis : $\{$ None, -1 , int $\}$, optional
Axis along which the sum is computed. The default (axis $=$ None) is to compute over the flattened array.
dtype : \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are summed. If dtype has the value None and the type of a is an integer type of precision
less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : \{None, ndarray \}, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

sum_along_axis : MaskedArray or scalar
An array with the same shape as self, with the specified axis removed. If self is a $0-\mathrm{d}$ array, or if axis is None, a scalar is returned. If an output array is specified, a reference to out is returned.

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 [-- 3]
    [-- 5 --]
    [7 -- 9]]
>>> print x.sum()
25
>>> print x.sum(axis=1)
[4 5 16]
>>> print x.sum(axis=0)
[8 5 12]
>>> print type(x.sum(axis=0, dtype=np.int64)[0])
<type 'numpy.int64'>
```

MaskedArray.var (axis=None, dtype=None, out=None, $d d o f=0$ )

Compute the variance along the specified axis.
Returns the variance of the array elements, a measure of the spread of a distribution. The variance is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a: array_like
Array containing numbers whose variance is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the variance is computed. The default is to compute the variance of the flattened array.
dtype : data-type, optional
Type to use in computing the variance. For arrays of integer type the default is float32; for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output, but the type is cast if necessary.
ddof : int, optional
"Delta Degrees of Freedom": the divisor used in the calculation is N - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

variance : ndarray, see dtype parameter above
If out=None, returns a new array containing the variance; otherwise, a reference to the output array is returned.

## See Also:

std
Standard deviation

## mean

Average
numpy.doc.ufuncs
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## Notes

The variance is the average of the squared deviations from the mean, i.e., var $=$ mean $(a b s(x-$ x.mean ()) **2).

The mean is normally calculated as $\mathrm{x} . \operatorname{sum}() / \mathrm{N}$, where $\mathrm{N}=$ len (x). If, however, ddof is specified, the divisor N - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of a hypothetical infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables.

Note that for complex numbers, the absolute value is taken before squaring, so that the result is always real and nonnegative.
For floating-point input, the variance is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float 32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1,2],[3,4]])
>>> np.var(a)
1.25
>>> np.var(a,0)
array([ 1., 1.])
>>> np.var(a,1)
array([ 0.25, 0.25])
```

In single precision, var() can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.var(a)
0.20405951142311096
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.var(a, dtype=np.float64)
0.202499999932997387
>>> ((1-0.55)**2 + (0.1-0.55)**2)/2
0.202500000000000001
```


## Minimum/maximum

| ma.argmax(a[, axis, fill_value]) | Function version of the eponymous method. |
| :---: | :---: |
| ma.argmin(a[, axis, fill_value]) | Returns array of indices of the maximum values along the given axis. |
| ma.max(obj[, axis, out, fill_value]) | Return the maximum along a given axis. |
| ma.min(obj[, axis, out, fill_value]) | Return the minimum along a given axis. |
| ma.ptp(obj[, axis, out, fill_value]) | Return (maximum - minimum) along the the given dimension (i.e. |
| ma.MaskedArray.argmax([axis, fill_value, out]) | Returns array of indices of the maximum values along the given axis. |
| ma.MaskedArray.argmin([axis, fill_value, out]) | Return array of indices to the minimum values along the given axis. |
| ```ma.MaskedArray.max([axis, out, fill_value])``` | Return the maximum along a given axis. |
| ma.MaskedArray.min([axis, out, fill_value]) | Return the minimum along a given axis. |
| ma.MaskedArray.ptp([axis, out, fill_value]) | Return (maximum - minimum) along the the given dimension (i.e. |

numpy .ma. argmax (a, axis=None, fill_value=None)
Function version of the eponymous method.
numpy.ma.argmin (a, axis=None, fill_value=None)
Returns array of indices of the maximum values along the given axis. Masked values are treated as if they had the value fill_value.

## Parameters

axis : \{None, integer \}
If None, the index is into the flattened array, otherwise along the specified axis
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, the output of maximum_fill_value(self._data) is used instead.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

index_array : \{integer_array\}
Examples

```
>>> a = np.arange(6).reshape (2, 3)
>>> a.argmax()
5
>>> a.argmax(0)
array([1, 1, 1])
>>> a.argmax(1)
array([2, 2])
```

numpy.ma. $\max (o b j$, axis=None, out=None, fill_value=None)
Return the maximum along a given axis.

## Parameters

axis : \{None, int \}, optional

Axis along which to operate. By default, axis is None and the flattened input is used. out : array_like, optional

Alternative output array in which to place the result. Must be of the same shape and buffer length as the expected output.
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, use the output of maximum_fill_value().

## Returns

amax : array_like
New array holding the result. If out was specified, out is returned.

## See Also:

maximum_fill_value
Returns the maximum filling value for a given datatype.
numpy.ma.min (obj, axis=None, out=None, fill_value=None)
Return the minimum along a given axis.

## Parameters

axis: \{None, int \}, optional
Axis along which to operate. By default, axis is None and the flattened input is used.
out : array_like, optional
Alternative output array in which to place the result. Must be of the same shape and buffer length as the expected output.
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, use the output of minimum_fill_value.

## Returns

amin : array_like
New array holding the result. If out was specified, out is returned.
See Also:
minimum_fill_value
Returns the minimum filling value for a given datatype.
numpy.ma.ptp (obj, axis=None, out=None, fill_value=None)
Return (maximum - minimum) along the the given dimension (i.e. peak-to-peak value).

## Parameters

axis : \{None, int \}, optional
Axis along which to find the peaks. If None (default) the flattened array is used.
out : \{None, array_like\}, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.
fill_value : \{var\}, optional
Value used to fill in the masked values.

## Returns

ptp : ndarray.
A new array holding the result, unless out was specified, in which case a reference to out is returned.
MaskedArray .argmax (axis=None, fill_value=None, out=None)
Returns array of indices of the maximum values along the given axis. Masked values are treated as if they had the value fill_value.

## Parameters

axis : \{None, integer\}
If None, the index is into the flattened array, otherwise along the specified axis
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, the output of maximum_fill_value(self._data) is used instead.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

index_array : \{integer_array\}

## Examples

```
>>> a = np.arange (6).reshape (2,3)
>>> a.argmax()
5
>>> a.argmax(0)
array([1, 1, 1])
>>> a.argmax(1)
array([2, 2])
```

MaskedArray.argmin (axis=None, fill_value=None, out=None)
Return array of indices to the minimum values along the given axis.

## Parameters

axis : \{None, integer\}
If None, the index is into the flattened array, otherwise along the specified axis
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, the output of minimum_fill_value(self._data) is used instead.
out : \{None, array\}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

\{ndarray, scalar\} :
If multi-dimension input, returns a new ndarray of indices to the minimum values along the given axis. Otherwise, returns a scalar of index to the minimum values along the given axis.

## Examples

```
>>> x = np.ma.array(arange(4), mask=[1,1,0,0])
>>> x.shape = (2,2)
>>> print x
[[-- --]
    [2 3]]
>>> print x.argmin(axis=0, fill_value=-1)
[0 0]
>>> print x.argmin(axis=0, fill_value=9)
[1 1]
MaskedArray.max (axis=None,out=None,fill_value=None)
```

Return the maximum along a given axis.

## Parameters

axis : \{None, int \}, optional
Axis along which to operate. By default, axis is None and the flattened input is used.
out : array_like, optional
Alternative output array in which to place the result. Must be of the same shape and buffer length as the expected output.
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, use the output of maximum_fill_value().

## Returns

amax : array_like
New array holding the result. If out was specified, out is returned.

## See Also:

maximum_fill_value
Returns the maximum filling value for a given datatype.
MaskedArray.min (axis=None, out=None, fill_value=None $)$
Return the minimum along a given axis.

## Parameters

axis: \{None, int \}, optional
Axis along which to operate. By default, axis is None and the flattened input is used.
out : array_like, optional
Alternative output array in which to place the result. Must be of the same shape and buffer length as the expected output.
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, use the output of minimum_fill_value.

## Returns

amin : array_like
New array holding the result. If out was specified, out is returned.

## See Also:

minimum_fill_value
Returns the minimum filling value for a given datatype.
MaskedArray.ptp (axis=None, out=None, fill_value=None)
Return (maximum - minimum) along the the given dimension (i.e. peak-to-peak value).

## Parameters

axis: \{None, int \}, optional
Axis along which to find the peaks. If None (default) the flattened array is used.
out : \{None, array_like \}, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.
fill_value : \{var\}, optional
Value used to fill in the masked values.

## Returns

ptp : ndarray.
A new array holding the result, unless out was specified, in which case a reference to out is returned.

## Sorting

ma.argsort(a[, axis, kind, order, fill_value]) Return an ndarray of indices that sort the array along the specified axis.
ma. sort(a[, axis, kind, order, endwith, ...])
Sort the array, in-place
ma.MaskedArray.argsort([axis, kind,
Return an ndarray of indices that sort the array along the specified axis.
order, ...])
ma.MaskedArray. sort([axis, kind, order, Sort the array, in-place
...])
numpy.ma. argsort ( $a$, axis=None, kind='quicksort', order=None, fill_value=None)
Return an ndarray of indices that sort the array along the specified axis. Masked values are filled beforehand to fill_value.

## Parameters

axis : int, optional
Axis along which to sort. The default is -1 (last axis). If None, the flattened array is used.
fill_value : var, optional
Value used to fill the array before sorting. The default is the fill_value attribute of the input array.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## Returns

index_array : ndarray, int

Array of indices that sort $a$ along the specified axis. In other words, a [index_array] yields a sorted $a$.

## See Also:

## sort

Describes sorting algorithms used.

## lexsort

Indirect stable sort with multiple keys.

## ndarray.sort

Inplace sort.

## Notes

See sort for notes on the different sorting algorithms.

## Examples

```
>>> a = np.ma.array([3,2,1], mask=[False, False, True])
>>> a
masked_array(data = [3 2 --],
                    mask = [False False True],
    fill_value = 999999)
>>> a.argsort()
array([1, 0, 2])
```

numpy.ma.sort ( $a$, axis=-1, kind='quicksort', order=None, endwith=True, fill_value=None )
Sort the array, in-place

## Parameters

a : array_like
Array to be sorted.
axis : int, optional
Axis along which to sort. If None, the array is flattened before sorting. The default is -1 , which sorts along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is a structured array, this argument specifies which fields to compare first, second, and so on. This list does not need to include all of the fields.
endwith : \{True, False\}, optional
Whether missing values (if any) should be forced in the upper indices (at the end of the array) (True) or lower indices (at the beginning).
fill_value : \{var\}, optional
Value used internally for the masked values. If fill_value is not None, it supersedes endwith.

## Returns

sorted_array : ndarray
Array of the same type and shape as $a$.

## See Also:

## ndarray.sort

Method to sort an array in-place.
argsort
Indirect sort.

## lexsort

Indirect stable sort on multiple keys.

```
searchsorted
```

Find elements in a sorted array.

## Notes

See sort for notes on the different sorting algorithms.

## Examples

```
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # Default
>>> a.sort()
>>> print a
[1 3 5 -- --]
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # Put missing values in the front
>>> a.sort(endwith=False)
>>> print a
[-- -- 1 3 5]
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # fill_value takes over endwith
>>> a.sort(endwith=False, fill_value=3)
>>> print a
[1 -- -- 3 5]
```

MaskedArray. argsort ( axis=None, kind='quicksort', order=None, fill_value=None )

Return an ndarray of indices that sort the array along the specified axis. Masked values are filled beforehand to fill_value.

## Parameters

axis : int, optional
Axis along which to sort. The default is -1 (last axis). If None, the flattened array is used.
fill_value : var, optional
Value used to fill the array before sorting. The default is the fill_value attribute of the input array.
kind : \{ 'quicksort', 'mergesort', 'heapsort'\}, optional
Sorting algorithm.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## Returns

index_array : ndarray, int
Array of indices that sort $a$ along the specified axis. In other words, a [index_array] yields a sorted $a$.

## See Also:

sort
Describes sorting algorithms used.

## lexsort

Indirect stable sort with multiple keys.
ndarray.sort
Inplace sort.

## Notes

See sort for notes on the different sorting algorithms.

## Examples

```
>>> a = np.ma.array([3,2,1], mask=[False, False, True])
>>> a
masked_array(data = [3 2 --],
    mask = [False False True],
    fill_value = 999999)
>>> a.argsort()
array([1, 0, 2])
MaskedArray.sort (axis=-1, kind='quicksort', order=None, endwith=True, fill_value=None)
```

Sort the array, in-place

## Parameters

a: array_like
Array to be sorted.
axis : int, optional
Axis along which to sort. If None, the array is flattened before sorting. The default is -1 , which sorts along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is a structured array, this argument specifies which fields to compare first, second, and so on. This list does not need to include all of the fields.
endwith : \{True, False \}, optional
Whether missing values (if any) should be forced in the upper indices (at the end of the array) (True) or lower indices (at the beginning).
fill_value : \{var\}, optional
Value used internally for the masked values. If fill_value is not None, it supersedes endwith.

## Returns

sorted_array : ndarray
Array of the same type and shape as $a$.

## See Also:

```
ndarray.sort
```

Method to sort an array in-place.
argsort
Indirect sort.

## lexsort

Indirect stable sort on multiple keys.
searchsorted
Find elements in a sorted array.

## Notes

See sort for notes on the different sorting algorithms.

## Examples

```
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # Default
>>> a.sort()
>>> print a
[1 [3 5 -- --]
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # Put missing values in the front
>>> a.sort(endwith=False)
>>> print a
[-- -- 1 3 5]
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # fill_value takes over endwith
>>> a.sort(endwith=False, fill_value=3)
>>> print a
[1 -- -- 3 5]
```


## Algebra

```
ma.diag(v[, k])
ma.dot(a, b[, strict])
ma.identity(n[, dtype])
ma.inner(a,b)
ma.innerproduct(a,b)
ma.outer(a,b)
ma.outerproduct(a, b)
ma.trace(self[, offset, axis1, axis2, ...])
ma.transpose(a[, axes])
ma.MaskedArray.trace([offset, axis1, axis2, ...])
ma.MaskedArray.transpose(*axes)
Extract a diagonal or construct a diagonal array.
Return the dot product of two arrays.
Return the identity array.
Inner product of two arrays.
Inner product of two arrays.
Compute the outer product of two vectors.
Compute the outer product of two vectors.
Return the sum along diagonals of the array.
Permute the dimensions of an array.
Return the sum along diagonals of the array.
Returns a view of the array with axes transposed.
numpy.ma.diag ( v, k=0)
```

Extract a diagonal or construct a diagonal array.

This function is the equivalent of numpy. diag that takes masked values into account, see numpy. diag for details.

See Also:
numpy. diag
Equivalent function for ndarrays.
numpy.ma.dot ( $a, b$, strict=False)
Return the dot product of two arrays.
Note: Works only with 2-D arrays at the moment.
This function is the equivalent of numpy. dot that takes masked values into account, see numpy. dot for details.

## Parameters

$\mathbf{a}, \mathbf{b}$ : ndarray
Inputs arrays.
strict : bool, optional
Whether masked data are propagated (True) or set to 0 (False) for the computation. Default is False. Propagating the mask means that if a masked value appears in a row or column, the whole row or column is considered masked.

## See Also:

numpy.dot
Equivalent function for ndarrays.

## Examples

```
>>> a = ma.array([[1, 2, 3], [4, 5, 6]], mask=[[1, 0, 0], [0, 0, 0]])
>>> b = ma.array([[1, 2], [3, 4], [5, 6]], mask=[[1, 0], [0, 0], [0, 0]])
>>> np.ma.dot(a, b)
masked_array(data =
    [[21 26]
    [45 64]],
                mask =
            [[False False]
            [False False]],
                    fill_value = 999999)
>>> np.ma.dot(a, b, strict=True)
masked_array(data =
    [[-- -- ]
    [-- 64]],
            mask =
    [[ True True]
    [ True False]],
            fill_value = 999999)
numpy.ma.identity(n,dtype=None)
    Return the identity array.
The identity array is a square array with ones on the main diagonal.
```


## Parameters

n : int

Number of rows (and columns) in $n \times n$ output.
dtype : data-type, optional
Data-type of the output. Defaults to float.

## Returns

 out : ndarray$n \times n$ array with its main diagonal set to one, and all other elements 0.

## Examples

```
>>> np.identity(3)
array([[ 1., 0., 0.],
    [ 0., 1., 0.],
    [ 0., 0., 1.]])
```

numpy.ma.inner $(a, b)$
Inner product of two arrays.

Ordinary inner product of vectors for 1-D arrays (without complex conjugation), in higher dimensions a sum product over the last axes.

## Parameters

## $\mathbf{a}, \mathbf{b}:$ array_like

If $a$ and $b$ are nonscalar, their last dimensions of must match.

## Returns

out : ndarray
out.shape $=$ a.shape $[:-1]+$ b.shape $[:-1]$

## Raises

ValueError :
If the last dimension of $a$ and $b$ has different size.

## See Also:

## tensordot

Sum products over arbitrary axes.
dot
Generalised matrix product, using second last dimension of $b$.
einsum
Einstein summation convention.

## Notes

Masked values are replaced by 0 .

## Examples

Ordinary inner product for vectors:

```
>>> a = np.array([1,2,3])
>>> b = np.array([0,1,0])
>>> np.inner(a, b)
2
```

A multidimensional example:

```
>>> a = np.arange(24).reshape((2,3,4))
>>> b = np.arange(4)
>>> np.inner(a, b)
array([[ 14, 38, 62],
    [ 86, 110, 134]])
```

An example where $b$ is a scalar:

```
>>> np.inner(np.eye(2), 7)
array([[ 7., 0.],
    [ 0., 7.]])
```

numpy.ma.innerproduct ( $a, b$ )

Inner product of two arrays.
Ordinary inner product of vectors for 1-D arrays (without complex conjugation), in higher dimensions a sum product over the last axes.

## Parameters

$\mathbf{a}, \mathbf{b}$ : array_like
If $a$ and $b$ are nonscalar, their last dimensions of must match.

## Returns

out : ndarray
out.shape $=$ a.shape $[:-1]+$ b.shape $[:-1]$

## Raises

## ValueError :

If the last dimension of $a$ and $b$ has different size.

## See Also:

## tensordot

Sum products over arbitrary axes.
dot
Generalised matrix product, using second last dimension of $b$.

## einsum

Einstein summation convention.

## Notes

Masked values are replaced by 0 .

## Examples

Ordinary inner product for vectors:

```
>>> a = np.array([1,2,3])
>>> b = np.array([0,1,0])
>>> np.inner(a, b)
2
```

A multidimensional example:

```
>>> a = np.arange(24).reshape((2,3,4))
>>> b = np.arange(4)
>>> np.inner(a, b)
```

```
array([[ 14, 38, 62],
    [ 86, 110, 134]])
```

An example where $b$ is a scalar:

```
>>> np.inner(np.eye(2), 7)
array([[ 7., 0.],
    [ 0., 7.]])
```

numpy.ma.outer ( $a, b$ )
Compute the outer product of two vectors.
Given two vectors, $a=[a 0, a 1, \ldots, a M]$ and $b=[b 0, b 1, \ldots, b N]$, the outer product [R47] is:

```
[[a0*b0 a0*bl ... a0*bN ]
    [a1*b0 .
    [ ...
    [aM*b0 aM*bN ]]
```


## Parameters

a, b: array_like, shape (M,), (N,)
First and second input vectors. Inputs are flattened if they are not already 1-dimensional.

## Returns

out : ndarray, shape ( $\mathrm{M}, \mathrm{N}$ )

```
out[i, j] = a[i] * b[j]
```


## See Also:

inner, einsum

## Notes

Masked values are replaced by 0 .

## References

[R47]

## Examples

Make a (very coarse) grid for computing a Mandelbrot set:

```
>>> rl = np.outer(np.ones((5,)), np.linspace(-2, 2, 5))
>>> rl
array([[-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.]])
>>> im = np.outer(1j*np.linspace(2, -2, 5), np.ones((5,)))
>>> im
array([[ 0.+2.j, 0.+2.j, 0.+2.j, 0.+2.j, 0.+2.j],
    [ 0.+1.j, 0.+1.j, 0.+1.j, 0.+1.j, 0.+1.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
    [ 0.-1.j, 0.-1.j, 0.-1.j, 0.-1.j, 0.-1.j],
    [0.-2.j, 0.-2.j, 0.-2.j, 0.-2.j, 0.-2.j]])
>>> grid = rl + im
```

```
>>> grid
array([[-2.+2.j, -1.+2.j, 0.+2.j, 1.+2.j, 2.+2.j],
    [-2.+1.j, -1.+1.j, 0.+1.j, 1.+1.j, 2.+1.j],
    [-2.+0.j, -1.+0.j, 0.+0.j, 1.+0.j, 2.+0.j],
    [-2.-1.j, -1.-1.j, 0.-1.j, 1.-1.j, 2.-1.j],
    [-2.-2.j, -1.-2.j, 0.-2.j, 1.-2.j, 2.-2.j]])
```

An example using a "vector" of letters:

```
>>> x = np.array(['a', 'b', 'c'], dtype=object)
>>> np.outer(x, [1, 2, 3])
array([[a, aa, aaa],
    [b, bb, b.b.b],
    [c, cc, ccc]], dtype=object)
```

numpy.ma.outerproduct ( $a, b$ )

Compute the outer product of two vectors.
Given two vectors, $\mathrm{a}=[\mathrm{a} 0, \mathrm{a} 1, \ldots, \mathrm{aM}]$ and $\mathrm{b}=[\mathrm{b} 0, \mathrm{~b} 1, \ldots, \mathrm{bN}]$, the outer product [R48] is:

```
[[a0*b0 a0*b1 ... a0*bN ]
    [a1*b0
    [ ...
    [aM*b0 aM*bN ]]
```


## Parameters

a, b: array_like, shape (M,), (N,)
First and second input vectors. Inputs are flattened if they are not already 1-dimensional.

## Returns

$$
\text { out : ndarray, shape }(\mathrm{M}, \mathrm{~N})
$$

```
out[i, j] = a[i] * b[j]
```


## See Also:

```
inner, einsum
```


## Notes

Masked values are replaced by 0 .

## References

[R48]

## Examples

Make a (very coarse) grid for computing a Mandelbrot set:

```
>>> rl = np.outer(np.ones((5,)), np.linspace(-2, 2, 5))
>>> rl
array([[-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.]])
>>> im = np.outer(1j*np.linspace(2, -2, 5), np.ones((5,)))
>>> im
```

```
array([[ 0.+2.j, 0.+2.j, 0.+2.j, 0.+2.j, 0.+2.j],
    [ 0.+1.j, 0.+1.j, 0.+1.j, 0.+1.j, 0.+1.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
    [ 0.-1.j, 0.-1.j, 0.-1.j, 0.-1.j, 0.-1.j],
    [ 0.-2.j, 0.-2.j, 0.-2.j, 0.-2.j, 0.-2.j]])
>>> grid = rl + im
>>> grid
array([[-2.+2.j, -1.+2.j, 0.+2.j, 1.+2.j, 2.+2.j],
    [-2.+1.j, -1.+1.j, 0.+1.j, 1.+1.j, 2.+1.j],
    [-2.+0.j, -1.+0.j, 0.+0.j, 1.+0.j, 2.+0.j],
    [-2.-1.j, -1.-1.j, 0.-1.j, 1.-1.j, 2.-1.j],
    [-2.-2.j, -1.-2.j, 0.-2.j, 1.-2.j, 2.-2.j]])
```

An example using a "vector" of letters:

```
>>> x = np.array(['a', 'b', 'c'], dtype=object)
>>> np.outer(x, [1, 2, 3])
array([[a, aa, aaa],
    [b, bb, b.b.b],
    [c, cc, ccc]], dtype=object)
```

numpy.ma.trace (self, offset=0, axis $1=0$, axis $2=1$, dtype $=$ None, out=None) a.trace(offset=0, axisl=0, axis $2=1$, dtype $=$ None, out $=$ None )

Return the sum along diagonals of the array.
Refer to numpy. trace for full documentation.

## See Also:

numpy.trace equivalent function
numpy.ma.transpose ( $a$, axes=None)
Permute the dimensions of an array.
This function is exactly equivalent to numpy. transpose.
See Also:
numpy.transpose
Equivalent function in top-level NumPy module.

## Examples

```
>>> import numpy.ma as ma
>>> x = ma.arange(4).reshape((2,2))
>>> x[1, 1] = ma.masked
>>>> x
masked_array(data =
    [[0 1]
    [2 --]],
                mask =
            [[False False]
    [False True]],
                    fill_value = 999999)
>>> ma.transpose(x)
masked_array(data =
    [[ll 2]
```

```
    [1 --]]
            mask =
    [[False False]
    [False True]],
        fill_value = 999999)
MaskedArray.trace (offset=0, axis 1=0, axis 2=1, dtype =None, out=None)
Return the sum along diagonals of the array.
Refer to numpy. trace for full documentation.
```


## See Also:

numpy.trace
equivalent function

## MaskedArray.transpose (*axes)

Returns a view of the array with axes transposed.
For a 1-D array, this has no effect. (To change between column and row vectors, first cast the 1-D array into a matrix object.) For a 2-D array, this is the usual matrix transpose. For an n-D array, if axes are given, their order indicates how the axes are permuted (see Examples). If axes are not provided and a.shape $=(i[0], i[1]$, $\ldots \quad i[n-2], i[n-1])$, then a.transpose().shape $=(i[n-1], i[n-2], \ldots \quad i[1]$, i[0]).

## Parameters

axes : None, tuple of ints, or $n$ ints

- None or no argument: reverses the order of the axes.
- tuple of ints: $i$ in the $j$-th place in the tuple means $a$ 's $i$-th axis becomes $a$. transpose()'s $j$-th axis.
- $n$ ints: same as an n-tuple of the same ints (this form is intended simply as a "convenience" alternative to the tuple form)


## Returns

out : ndarray
View of $a$, with axes suitably permuted.

## See Also:

## ndarray. $T$

Array property returning the array transposed.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> a
array([[1, 2],
            [3, 4]])
>>> a.transpose()
array([[1, 3],
    [2, 4]])
>>> a.transpose((1, 0))
array([[1, 3],
    [2, 4]])
>>> a.transpose(1, 0)
```

```
array([[1, 3],
    [2, 4]])
```


## Polynomial fit

| ma.vander(x[, n]) | Generate a Van der Monde matrix. |
| :--- | :--- |
| ma.polyfit(x, y, deg[, rcond, full $])$ | Least squares polynomial fit. |

numpy.ma. vander ( $x, n=$ None)
Generate a Van der Monde matrix.
The columns of the output matrix are decreasing powers of the input vector. Specifically, the $i$-th output column is the input vector raised element-wise to the power of $\mathrm{N}-\mathrm{i}-1$. Such a matrix with a geometric progression in each row is named for Alexandre-Theophile Vandermonde.

## Parameters

$\mathbf{x}$ : array_like
1-D input array.

## $\mathbf{N}$ : int, optional

Order of (number of columns in) the output. If $N$ is not specified, a square array is returned ( $\mathrm{N}=$ len ( x$)$ ).

## Returns

out : ndarray
Van der Monde matrix of order $N$. The first column is $x^{\wedge}(N-1)$, the second $x^{\wedge}(N-2)$ and so forth.

## Notes

Masked values in the input array result in rows of zeros.

## Examples

```
>>> x = np.array([1, 2, 3, 5])
>>> N = 3
>>> np.vander(x, N)
array([[ 1, 1, 1],
    [4, 2, 1],
    [ 9, 3, 1],
    [25, 5, 1]])
>>> np.column_stack([x**(N-1-i) for i in range(N)])
array([[ 1, 1, 1],
    [4, 2, 1],
    [ 9, 3, 1],
    [25, 5, 1]])
>>> x = np.array([1, 2, 3, 5])
>>> np.vander(x)
array([[[ 1, 1, 1, 1],
    [ 8, 4, 2, 1],
    [ 27, 9, 3, 1],
    [125, 25, 5, 1]])
```

The determinant of a square Vandermonde matrix is the product of the differences between the values of the input vector:

```
>>> np.linalg.det(np.vander(x))
48.0000000000000043
>>>}(5-3)*(5-2)*(5-1)*(3-2)*(3-1)*(2-1
48
```

numpy.ma.polyfit ( $x, y, d e g$, rcond=None, full=False)

Least squares polynomial fit.
Fit a polynomial $p(x)=p[0] * x * * \operatorname{deg}+\ldots+\mathrm{p}[$ deg $]$ of degree deg to points $(x, y)$. Returns a vector of coefficients $p$ that minimises the squared error.

## Parameters

$\mathbf{x}$ : array_like, shape (M,)
$x$-coordinates of the $M$ sample points (x[i], y[i]).
$\mathbf{y}$ : array_like, shape (M,) or (M, K)
$y$-coordinates of the sample points. Several data sets of sample points sharing the same $x$-coordinates can be fitted at once by passing in a 2D-array that contains one dataset per column.
deg : int
Degree of the fitting polynomial
rcond : float, optional
Relative condition number of the fit. Singular values smaller than this relative to the largest singular value will be ignored. The default value is len $(x) * e p s$, where eps is the relative precision of the float type, about $2 \mathrm{e}-16$ in most cases.
full : bool, optional
Switch determining nature of return value. When it is False (the default) just the coefficients are returned, when True diagnostic information from the singular value decomposition is also returned.

## Returns

$\mathbf{p}$ : ndarray, shape (M,) or (M, K)
Polynomial coefficients, highest power first. If $y$ was 2-D, the coefficients for $k$-th data set are in $p[:, k]$.
residuals, rank, singular_values, rcond : present only if full $=$ True
Residuals of the least-squares fit, the effective rank of the scaled Vandermonde coefficient matrix, its singular values, and the specified value of rcond. For more details, see linalg.lstsq.

## Warns

## RankWarning :

The rank of the coefficient matrix in the least-squares fit is deficient. The warning is only raised if full = False.

The warnings can be turned off by

```
>>> import warnings
>>> warnings.simplefilter('ignore', np.RankWarningl)
```

See Also:

## polyval

Computes polynomial values.

## linalg.lstsq

Computes a least-squares fit.
scipy.interpolate.UnivariateSpline
Computes spline fits.

## Notes

Any masked values in x is propagated in y , and vice-versa.

## References

[R49], [R50]

## Examples

```
>>> x = np.array([0.0, 1.0, 2.0, 3.0, 4.0, 5.0])
>>> y = np.array([0.0, 0.8, 0.9, 0.1, -0.8, -1.0])
>>> z = np.polyfit(x, y, 3)
>>> z
array([ 0.08703704, -0.81349206, 1.69312169, -0.03968254])
```

It is convenient to use polyld objects for dealing with polynomials:

```
>>> p = np.poly1d(z)
>>> p(0.5)
0.6143849206349179
>>> p(3.5)
-0.34732142857143039
>>> p(10)
22.579365079365115
```

High-order polynomials may oscillate wildly:

```
>>> p30 = np.polyld(np.polyfit(x, y, 30))
/... RankWarning: Polyfit may be poorly conditioned...
>>> p30(4)
-0.80000000000000204
>>> p30(5)
-0.99999999999999445
>>> p30(4.5)
-0.10547061179440398
```

Illustration:

```
>>> import matplotlib.pyplot as plt
>>> xp = np.linspace(-2, 6, 100)
>>> plt.plot(x, y, '.', xp, p(xp), '-', xp, p30(xp), '--')
[<matplotlib.lines.Line2D object at 0x...>, <matplotlib.lines.Line2D object at 0x...>, <matpld
>>> plt.ylim(-2,2)
(-2, 2)
>>> plt.show()
```



## Clipping and rounding

| ma.around | Round an array to the given number of decimals. |
| :--- | :--- |
| ma.clip(a, a_min, a_max[,out]) | Clip (limit) the values in an array. |
| ma.round(a[, decimals, out $])$ | Return a copy of a, rounded to 'decimals' places. |
| ma.MaskedArray.clip(a_min, a_max[, | Return an array whose values are limited to [a_min, <br> out] $)$ |
| ma.MaskedArray.round([decimals, out $])$ | Return $a$ with each element rounded to the given number of <br> decimals. |

numpy.ma. around
Round an array to the given number of decimals.
Refer to around for full documentation.

## See Also:

around
equivalent function
numpy.ma.clip (a, a_min, a_max, out=None)
Clip (limit) the values in an array.
Given an interval, values outside the interval are clipped to the interval edges. For example, if an interval of $[0,1]$ is specified, values smaller than 0 become 0 , and values larger than 1 become 1 .

## Parameters

a : array_like
Array containing elements to clip.
a_min : scalar or array_like
Minimum value.
a_max : scalar or array_like
Maximum value. If $a \_m i n$ or $a \_m a x$ are array_like, then they will be broadcasted to the shape of $a$.
out : ndarray, optional

The results will be placed in this array. It may be the input array for in-place clipping. out must be of the right shape to hold the output. Its type is preserved.

## Returns

clipped_array : ndarray
An array with the elements of $a$, but where values $<a_{-} \min$ are replaced with $a \_$min, and those $>a \_m a x$ with $a \_m a x$.

## See Also:

numpy.doc.ufuncs
Section "Output arguments"

## Examples

```
>>> a = np.arange(10)
>>> np.clip(a, 1, 8)
array([1, 1, 2, 3, 4, 5, 6, 7, 8, 8])
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, 3, 6, out=a)
array([3, 3, 3, 3, 4, 5, 6, 6, 6, 6])
>>> a = np.arange(10)
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, [3,4,1,1,1,4,4,4,4,4], 8)
array([3, 4, 2, 3, 4, 5, 6, 7, 8, 8])
```

numpy.ma.round ( $a$, decimals $=0$, out $=$ None )
Return a copy of a, rounded to 'decimals' places.
When 'decimals' is negative, it specifies the number of positions to the left of the decimal point. The real and imaginary parts of complex numbers are rounded separately. Nothing is done if the array is not of float type and 'decimals' is greater than or equal to 0 .

## Parameters

decimals : int
Number of decimals to round to. May be negative.
out : array_like
Existing array to use for output. If not given, returns a default copy of a.

## Notes

If out is given and does not have a mask attribute, the mask of a is lost!
MaskedArray.clip (a_min, a_max, out=None)
Return an array whose values are limited to [a_min, a_max].
Refer to numpy.clip for full documentation.

## See Also:

numpy.clip
equivalent function
MaskedArray.round (decimals $=0$, out $=$ None)
Return $a$ with each element rounded to the given number of decimals.

Refer to numpy . around for full documentation.
See Also:
numpy. around
equivalent function

## Miscellanea

| ma.allequal(a, b[, fill_value]) | Return True if all entries of a and b are equal, using |
| :---: | :---: |
| ma.allclose( $\mathrm{a}, \mathrm{b}[$, masked_equal, rtol, atol]) | Returns True if two arrays are element-wise equal within a tolerance. |
| ma.apply_along_axis(func1d, axis, arr, ...) | Apply a function to 1-D slices along the given axis. |
| ma.arange([dtype]) | Return evenly spaced values within a given interval. |
| ma.choose(indices, choices[, out, mode]) | Use an index array to construct a new array from a set of choices. |
| ma.ediffld(arr[, to_end, to_begin]) | Compute the differences between consecutive elements of an array. |
| ma.indices(dimensions[, dtype]) | Return an array representing the indices of a grid. |
| ma.where(condition[, x, y]) | Return a masked array with elements from x or y , depending on condition. |

numpy.ma. allequal ( $a, b$, fill_value $=$ True $)$
Return True if all entries of $a$ and $b$ are equal, using fill_value as a truth value where either or both are masked.

## Parameters

$\mathbf{a}, \mathbf{b}:$ array_like
Input arrays to compare.
fill_value : bool, optional
Whether masked values in a or b are considered equal (True) or not (False).

## Returns

$\mathbf{y}$ : bool
Returns True if the two arrays are equal within the given tolerance, False otherwise. If either array contains NaN , then False is returned.

## See Also:

```
all, any, numpy.ma.allclose
```


## Examples

```
>>> a = ma.array([1e10, 1e-7, 42.0], mask=[0, 0, 1])
>>> a
masked_array(data = [10000000000.0 1e-07 --],
            mask = [False False True],
            fill_value=1e+20)
>>> b = array([1e10, 1e-7, -42.0])
>>> b
array([ 1.00000000e+10, 1.00000000e-07, -4.20000000e+01])
>>> ma.allequal(a, b, fill_value=False)
False
>>> ma.allequal(a, b)
True
```

numpy.ma.allclose ( $a, b$, masked_equal=True, rtol $=1.0000000000000001 e-05$, atol $=1 e-08$ )
Returns True if two arrays are element-wise equal within a tolerance.

This function is equivalent to allclose except that masked values are treated as equal (default) or unequal, depending on the masked_equal argument.

## Parameters

$\mathbf{a}, \mathbf{b}:$ array_like
Input arrays to compare.
masked_equal : bool, optional
Whether masked values in $a$ and $b$ are considered equal (True) or not (False). They are considered equal by default.
rtol : float, optional
Relative tolerance. The relative difference is equal to rtol * b. Default is $1 \mathrm{e}-5$.
atol : float, optional
Absolute tolerance. The absolute difference is equal to atol. Default is 1e-8.

## Returns

$\mathbf{y}$ : bool
Returns True if the two arrays are equal within the given tolerance, False otherwise. If either array contains NaN , then False is returned.

## See Also:

all, any
numpy.allclose
the non-masked allclose.

## Notes

If the following equation is element-wise True, then allclose returns True:

```
absolute(`a` - `b`) <= (`atol` + `rtol` * absolute(`b`))
```

Return True if all elements of $a$ and $b$ are equal subject to given tolerances.

## Examples

```
>>> a = ma.array([1e10, 1e-7, 42.0], mask=[0, 0, 1])
>>> a
masked_array(data = [10000000000.0 1e-07 -- ],
            mask = [False False True],
            fill_value = 1e+20)
>>> b = ma.array([1e10, 1e-8, -42.0], mask=[0, 0, 1])
>>> ma.allclose(a, b)
False
>>> a = ma.array([1e10, 1e-8, 42.0], mask=[0, 0, 1])
>>> b = ma.array([1.00001e10, 1e-9, -42.0], mask=[0, 0, 1])
>>> ma.allclose(a, b)
True
>>> ma.allclose(a, b, masked_equal=False)
False
```

Masked values are not compared directly.

```
>>> a = ma.array([1e10, 1e-8, 42.0], mask=[0, 0, 1])
>>> b = ma.array([1.00001e10, 1e-9, 42.0], mask=[0, 0, 1])
>>> ma.allclose(a, b)
True
>>> ma.allclose(a, b, masked_equal=False)
False
```

numpy.ma.apply_along_axis (funcld, axis, arr, *args, **kwargs)
Apply a function to 1-D slices along the given axis.

Execute funcld( $a$, *args) where funcld operates on 1-D arrays and $a$ is a 1-D slice of arr along axis.

## Parameters

func1d : function
This function should accept 1-D arrays. It is applied to 1-D slices of arr along the specified axis.
axis : integer
Axis along which $a r r$ is sliced.
arr : ndarray
Input array.
args : any
Additional arguments to funcld.

## Returns

outarr : ndarray
The output array. The shape of outarr is identical to the shape of arr, except along the axis dimension, where the length of outarr is equal to the size of the return value of funcld. If funcld returns a scalar outarr will have one fewer dimensions than arr.

## See Also:

## apply_over_axes

Apply a function repeatedly over multiple axes.

## Examples

```
>>> def my_func(a):
... """Average first and last element of a I-D array"""
... return (a[0] + a[-1]) * 0.5
>>> b = np.array([[1,2,3], [4,5,6], [7, 8, 9]])
>>> np.apply_along_axis(my_func, 0, b)
array([ 4., 5., 6.])
>>> np.apply_along_axis(my_func, 1, b)
array([ 2., 5., 8.])
```

For a function that doesn't return a scalar, the number of dimensions in outarr is the same as arr.

```
>>> def new_func(a):
... """Divide elements of a by 2."""
... return a * 0.5
>>> b = np.array([[1,2,3], [4,5,6], [7, 8, 9]])
>>> np.apply_along_axis(new_func, 0, b)
array([[ 0.5, 1. , 1.5],
```

```
[ 2. , 2.5, 3. ],
[ 3.5, 4. , 4.5]])
```

numpy.ma. arange ([start], stop $[$, step $]$, dtype $=$ None )
Return evenly spaced values within a given interval.
Values are generated within the half-open interval [start, stop) (in other words, the interval including start but excluding stop). For integer arguments the function is equivalent to the Python built-in range function, but returns a ndarray rather than a list.

When using a non-integer step, such as 0.1 , the results will often not be consistent. It is better to use linspace for these cases.

## Parameters

start : number, optional
Start of interval. The interval includes this value. The default start value is 0 .
stop : number
End of interval. The interval does not include this value, except in some cases where step is not an integer and floating point round-off affects the length of out.
step : number, optional
Spacing between values. For any output out, this is the distance between two adjacent values, out [i+1] - out [i]. The default step size is 1. If step is specified, start must also be given.
dtype : dtype
The type of the output array. If dtype is not given, infer the data type from the other input arguments.

## Returns

out : ndarray
Array of evenly spaced values.
For floating point arguments, the length of the result is ceil((stop start)/step). Because of floating point overflow, this rule may result in the last element of out being greater than stop.

## See Also:

## linspace

Evenly spaced numbers with careful handling of endpoints.
ogrid
Arrays of evenly spaced numbers in N -dimensions
mgrid
Grid-shaped arrays of evenly spaced numbers in N -dimensions

## Examples

```
>>> np.arange(3)
array([0, 1, 2])
>>> np.arange(3.0)
array([ 0., 1., 2.])
>>> np.arange (3,7)
array([3, 4, 5, 6])
```

```
>>> np.arange(3,7,2)
array([3, 5])
```

numpy.ma. choose (indices, choices, out=None, mode='raise')
Use an index array to construct a new array from a set of choices.
Given an array of integers and a set of $n$ choice arrays, this method will create a new array that merges each of the choice arrays. Where a value in $a$ is $i$, the new array will have the value that choices[i] contains in the same place.

## Parameters

a : ndarray of ints
This array must contain integers in [0, $n-1]$, where $n$ is the number of choices.
choices : sequence of arrays
Choice arrays. The index array and all of the choices should be broadcastable to the same shape.
out : array, optional
If provided, the result will be inserted into this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' : raise an error
- 'wrap' : wrap around
- 'clip' : clip to the range


## Returns

merged_array : array

## See Also:

choose
equivalent function

## Examples

```
>>> choice = np.array([[1,1,1], [2,2,2], [3,3,3]])
>>> a = np.array([2, 1, 0])
>>> np.ma.choose(a, choice)
masked_array(data = [3 2 1],
            mask = False,
            fill_value=999999)
```

numpy.ma.ediff1d (arr, to_end=None, to_begin=None)
Compute the differences between consecutive elements of an array.
This function is the equivalent of numpy.ediffid that takes masked values into account, see numpy.ediffid for details.

## See Also:

numpy.ediff1d
Equivalent function for ndarrays.
numpy.ma.indices (dimensions, dtype=<type 'int'>)
Return an array representing the indices of a grid.
Compute an array where the subarrays contain index values $0,1, \ldots$ varying only along the corresponding axis.

## Parameters

dimensions : sequence of ints
The shape of the grid.
dtype : dtype, optional
Data type of the result.

## Returns

grid : ndarray
The array of grid indices, grid.shape = (len(dimensions), $)+$ tuple(dimensions).

## See Also:

mgrid, meshgrid

## Notes

The output shape is obtained by prepending the number of dimensions in front of the tuple of dimensions, i.e. if dimensions is a tuple ( $r 0, \ldots, r N-1$ ) of length $N$, the output shape is ( $N, r 0, \ldots, r N-1$ ).
The subarrays grid[k] contains the $N$-D array of indices along the $k-t h$ axis. Explicitly:

```
grid[k,i0,i1,...,iN-1] = ik
```


## Examples

```
>>> grid = np.indices((2, 3))
>>> grid.shape
(2, 2, 3)
>>> grid[0] # row indices
array([[0, 0, 0],
            [1, 1, 1]])
>>> grid[1] # column indices
array([[0, 1, 2],
    [0, 1, 2]])
```

The indices can be used as an index into an array.

```
>>> x = np.arange (20).reshape(5, 4)
>>> row, col = np.indices((2, 3))
>>> x[row, col]
array([[0, 1, 2],
    [4, 5, 6]])
```

Note that it would be more straightforward in the above example to extract the required elements directly with $x[: 2,: 3]$.
numpy.ma. where (condition, $x=$ None, $y=$ None)
Return a masked array with elements from x or y , depending on condition.
Returns a masked array, shaped like condition, where the elements are from $x$ when condition is True, and from $y$ otherwise. If neither $x$ nor $y$ are given, the function returns a tuple of indices where condition is True (the result of condition. nonzero()).

## Parameters

condition : array_like, bool
The condition to meet. For each True element, yield the corresponding element from $x$, otherwise from $y$.
$\mathbf{x}, \mathbf{y}$ : array_like, optional
Values from which to choose. $x$ and $y$ need to have the same shape as condition, or be broadcast-able to that shape.

## Returns

out : MaskedArray or tuple of ndarrays
The resulting masked array if $x$ and $y$ were given, otherwise the result of condition.nonzero().

## See Also:

numpy. where
Equivalent function in the top-level NumPy module.

## Examples

```
>>> x = np.ma.array(np.arange(9.).reshape(3, 3), mask=[[0, 1, 0],
... [1, 0, 1],
>>> print x
[[0.0 -- 2.0]
    [-- 4.0 --]
    [6.0 -- 8.0]]
>>> np.ma.where(x > 5) # return the indices where x > 5
(array([2, 2]), array([0, 2]))
>>> print np.ma.where(x > 5, x, -3.1416)
[[-3.1416 -- -3.1416]
    [-- -3.1416 --]
    [6.0 -- 8.0]]
```


### 1.7 The Array Interface

Note: This page describes the numpy-specific API for accessing the contents of a numpy array from other C extensions. PEP 3118 - The Revised Buffer Protocol introduces similar, standardized API to Python 2.6 and 3.0 for any extension module to use. Cython's buffer array support uses the PEP 3118 API ; see the Cython numpy tutorial. Cython provides a way to write code that supports the buffer protocol with Python versions older than 2.6 because it has a backward-compatible implementation utilizing the legacy array interface described here.

## version

3
The array interface (sometimes called array protocol) was created in 2005 as a means for array-like Python objects to re-use each other's data buffers intelligently whenever possible. The homogeneous N -dimensional array interface is a default mechanism for objects to share N-dimensional array memory and information. The interface consists of a Python-side and a C -side using two attributes. Objects wishing to be considered an N -dimensional array in application code should support at least one of these attributes. Objects wishing to support an N -dimensional array in application code should look for at least one of these attributes and use the information provided appropriately.

This interface describes homogeneous arrays in the sense that each item of the array has the same "type". This type can be very simple or it can be a quite arbitrary and complicated C-like structure.
There are two ways to use the interface: A Python side and a C-side. Both are separate attributes.

### 1.7.1 Python side

This approach to the interface consists of the object having an $\qquad$ array_interface $\qquad$ attribute.

## _array_interface__

A dictionary of items (3 required and 5 optional). The optional keys in the dictionary have implied defaults if they are not provided.

The keys are:
shape (required)
Tuple whose elements are the array size in each dimension. Each entry is an integer (a Python int or long). Note that these integers could be larger than the platform "int" or "long" could hold (a Python int is a C long). It is up to the code using this attribute to handle this appropriately; either by raising an error when overflow is possible, or by using Py_LONG_LONG as the C type for the shapes.
typestr (required)
A string providing the basic type of the homogenous array The basic string format consists of 3 parts: a character describing the byteorder of the data (<: little-endian, >: big-endian, ।: not-relevant), a character code giving the basic type of the array, and an integer providing the number of bytes the type uses.

The basic type character codes are:

| t | Bit field (following integer gives the number of bits in the bit field). |
| :---: | :--- |
| b | Boolean (integer type where all values are only True or False) |
| i | Integer |
| u | Unsigned integer |
| f | Floating point |
| c | Complex floating point |
| O | Object (i.e. the memory contains a pointer to PyOb ject) |
| S | String (fixed-length sequence of char) |
| U | Unicode (fixed-length sequence of Py_UNICODE) |
| V | Other (void - each item is a fixed-size chunk of memory) |

descr (optional)
A list of tuples providing a more detailed description of the memory layout for each item in the homogeneous array. Each tuple in the list has two or three elements. Normally, this attribute would be used when typestr is $\mathrm{V}[0-9]+$, but this is not a requirement. The only requirement is that the number of bytes represented in the typestr key is the same as the total number of bytes represented here. The idea is to support descriptions of C-like structs (records) that make up array elements. The elements of each tuple in the list are
1.A string providing a name associated with this portion of the record. This could also be a tuple of ('full name', 'basic_name') where basic name would be a valid Python variable name representing the full name of the field.
2.Either a basic-type description string as in typestr or another list (for nested records)
3.An optional shape tuple providing how many times this part of the record should be repeated. No repeats are assumed if this is not given. Very complicated structures can be described using this
generic interface. Notice, however, that each element of the array is still of the same data-type. Some examples of using this interface are given below.

Default: [(", typestr)]
data (optional)
A 2-tuple whose first argument is an integer (a long integer if necessary) that points to the data-area storing the array contents. This pointer must point to the first element of data (in other words any offset is always ignored in this case). The second entry in the tuple is a read-only flag (true means the data area is read-only).

This attribute can also be an object exposing the buffer interface which will be used to share the data. If this key is not present (or returns None), then memory sharing will be done through the buffer interface of the object itself. In this case, the offset key can be used to indicate the start of the buffer. A reference to the object exposing the array interface must be stored by the new object if the memory area is to be secured.

Default: None
strides (optional)
Either None to indicate a C-style contiguous array or a Tuple of strides which provides the number of bytes needed to jump to the next array element in the corresponding dimension. Each entry must be an integer (a Python int or long). As with shape, the values may be larger than can be represented by a C "int" or "long"; the calling code should handle this appropiately, either by raising an error, or by using Py_LONG_LONG in C. The default is None which implies a C-style contiguous memory buffer. In this model, the last dimension of the array varies the fastest. For example, the default strides tuple for an object whose array entries are 8 bytes long and whose shape is $(10,20,30)$ would be $(4800,240,8)$

Default: None (C-style contiguous)
mask (optional)
None or an object exposing the array interface. All elements of the mask array should be interpreted only as true or not true indicating which elements of this array are valid. The shape of this object should be "broadcastable" to the shape of the original array.

Default: None (All array values are valid)
offset (optional)
An integer offset into the array data region. This can only be used when data is None or returns a buffer object.
Default: 0 .
version (required)
An integer showing the version of the interface (i.e. 3 for this version). Be careful not to use this to invalidate objects exposing future versions of the interface.

### 1.7.2 C-struct access

This approach to the array interface allows for faster access to an array using only one attribute lookup and a welldefined C-structure.

```
__array_struct__
```

A PyCObject whose voidptr member contains a pointer to a filled PyArrayInterface structure. Memory for the structure is dynamically created and the PyCObject is also created with an appropriate destructor so the retriever of this attribute simply has to apply Py_DECREF to the object returned by this
attribute when it is finished. Also, either the data needs to be copied out, or a reference to the object exposing this attribute must be held to ensure the data is not freed. Objects exposing the $\qquad$ array_struct $\qquad$ interface must also not reallocate their memory if other objects are referencing them.

The PyArrayInterface structure is defined in numpy/ndarrayobject.h as:

```
typedef struct {
    int two; /* contains the integer 2 -- simple sanity check */
    int nd; /* number of dimensions */
    char typekind; /* kind in array --- character code of typestr */
    int itemsize; /* size of each element */
    int flags; /* flags indicating how the data should be interpreted */
    /* must set ARR_HAS_DESCR bit to validate descr */
    Py_intptr_t *shape; /* A length-nd array of shape information */
    Py_intptr_t *strides; /* A length-nd array of stride information */
    void *data; /* A pointer to the first element of the array */
    PyObject *descr; /* NULL or data-description (same as descr key
    of __array_interface__) -- must set ARR_HAS_DESCR
    flag or this will be ignored. */
} PyArrayInterface;
```

The flags member may consist of 5 bits showing how the data should be interpreted and one bit showing how the Interface should be interpreted. The data-bits are CONTIGUOUS (0x1), FORTRAN (0x2), ALIGNED (0x100), NOTSWAPPED ( $0 \times 200$ ), and WRITEABLE ( 0 x 400 ). A final flag ARR_HAS_DESCR (0x800) indicates whether or not this structure has the arrdescr field. The field should not be accessed unless this flag is present.

## New since June 16, 2006:

In the past most implementations used the "desc" member of the PyCObject itself (do not confuse this with the "descr" member of the PyArrayInterface structure above - they are two separate things) to hold the pointer to the object exposing the interface. This is now an explicit part of the interface. Be sure to own a reference to the object when the PyCObject is created using PyCObject_FromVoidPtrAndDesc.

### 1.7.3 Type description examples

For clarity it is useful to provide some examples of the type description and corresponding __array_interface__ 'descr' entries. Thanks to Scott Gilbert for these examples:

In every case, the 'descr' key is optional, but of course provides more information which may be important for various applications:

```
* Float data
    typestr == '>f4'
    descr == [('','>f4')]
* Complex double
    typestr == '>c8'
    descr == [('real','>f4'), ('imag','>f4')]
* RGB Pixel data
    typestr == '|V3'
    descr == [('r','|u1'), ('g','|u1'), ('b','|ul')]
* Mixed endian (weird but could happen).
    typestr == '|V8' (or '>u8')
    descr == [('big','>i4'), ('little','<i4')]
* Nested structure
```

```
    struct {
        int ival;
        struct {
            unsigned short sval;
            unsigned char bval;
            unsigned char cval;
        } sub;
}
typestr == '|V8' (or '<u8' if you want)
descr == [('ival','<i4'), ('sub', [('sval','<u2'), ('bval','|ul'), ('cval','|ul') ]) ]
* Nested array
    struct {
        int ival;
        double data[16*4];
    }
    typestr == '|V516'
    descr == [('ival','>i4'), ('data','>f8',(16,4))]
* Padded structure
    struct {
        int ival;
        double dval;
    }
    typestr == '|V16'
    descr == [('ival','>i4'),('','|V4'),('dval','>f8')]
```

It should be clear that any record type could be described using this interface.

### 1.7.4 Differences with Array interface (Version 2)

The version 2 interface was very similar. The differences were largely asthetic. In particular:

1. The PyArrayInterface structure had no descr member at the end (and therefore no flag ARR_HAS_DESCR)
2. The desc member of the PyCObject returned from __array_struct__ was not specified. Usually, it was the object exposing the array (so that a reference to it could be kept and destroyed when the C-object was destroyed). Now it must be a tuple whose first element is a string with "PyArrayInterface Version \#" and whose second element is the object exposing the array.
3. The tuple returned from __array_interface__['data'] used to be a hex-string (now it is an integer or a long integer).
4. There was no __array_interface__ attribute instead all of the keys (except for version) in the __array_interface dictionary were their own attribute: Thus to obtain the Python-side information you had to access separately the attributes:

- __array_data__
- __array_shape__
- __array_strides__
- __array_typestr__
- __array_descr__
- __array_offset _
- __array_mask__


## UNIVERSAL FUNCTIONS (UFUNC)

A universal function (or ufunc for short) is a function that operates on ndarrays in an element-by-element fashion, supporting array broadcasting, type casting, and several other standard features. That is, a ufunc is a "vectorized" wrapper for a function that takes a fixed number of scalar inputs and produces a fixed number of scalar outputs.

In Numpy, universal functions are instances of the numpy. ufunc class. Many of the built-in functions are implemented in compiled C code, but ufunc instances can also be produced using the frompyfunc factory function.

### 2.1 Broadcasting

Each universal function takes array inputs and produces array outputs by performing the core function element-wise on the inputs. Standard broadcasting rules are applied so that inputs not sharing exactly the same shapes can still be usefully operated on. Broadcasting can be understood by four rules:

1. All input arrays with ndim smaller than the input array of largest ndim, have 1's prepended to their shapes.
2. The size in each dimension of the output shape is the maximum of all the input sizes in that dimension.
3. An input can be used in the calculation if its size in a particular dimension either matches the output size in that dimension, or has value exactly 1.
4. If an input has a dimension size of 1 in its shape, the first data entry in that dimension will be used for all calculations along that dimension. In other words, the stepping machinery of the ufunc will simply not step along that dimension (the stride will be 0 for that dimension).

Broadcasting is used throughout NumPy to decide how to handle disparately shaped arrays; for example, all arithmetic operations $(+,-, *, \ldots)$ between ndarrays broadcast the arrays before operation. A set of arrays is called "broadcastable" to the same shape if the above rules produce a valid result, i.e., one of the following is true:

1. The arrays all have exactly the same shape.
2. The arrays all have the same number of dimensions and the length of each dimensions is either a common length or 1 .
3. The arrays that have too few dimensions can have their shapes prepended with a dimension of length 1 to satisfy property 2.

## Example

If a . shape is $(5,1), \mathrm{b}$. shape is $(1,6), \mathrm{c}$. shape is $(6$,$) and \mathrm{d}$. shape is () so that $d$ is a scalar, then $a, b, c$, and $d$ are all broadcastable to dimension $(5,6)$; and

- $a$ acts like $\mathrm{a}(5,6)$ array where $a[:, 0]$ is broadcast to the other columns,
- $b$ acts like $\mathrm{a}(5,6)$ array where $\mathrm{b}[0,:]$ is broadcast to the other rows,
- $c$ acts like a $(1,6)$ array and therefore like a $(5,6)$ array where $c[:]$ is broadcast to every row, and finally,
- $d$ acts like a $(5,6)$ array where the single value is repeated.


### 2.2 Output type determination

The output of the ufunc (and its methods) is not necessarily an ndarray, if all input arguments are not ndarrays.
All output arrays will be passed to the __array_prepare__ and __array_wrap__ methods of the input (besides ndarrays, and scalars) that defines it and has the highest__array_priority__ of any other input to the universal function. The default __array_priority__ of the ndarray is 0.0 , and the default __array_priority__ of a subtype is 1.0. Matrices have __array_priority__ equal to 10.0.

All ufuncs can also take output arguments. If necessary, output will be cast to the data-type(s) of the provided output array(s). If a class with an ___array__ method is used for the output, results will be written to the object returned by __array__. Then, if the class also has an __array_prepare__ method, it is called so metadata may be determined based on the context of the ufunc (the context consisting of the ufunc itself, the arguments passed to the ufunc, and the ufunc domain.) The array object returned by __array_prepare__ is passed to the ufunc for computation. Finally, if the class also has an __array_wrap__ method, the returned ndarray result will be passed to that method just before passing control back to the caller.

### 2.3 Use of internal buffers

Internally, buffers are used for misaligned data, swapped data, and data that has to be converted from one data type to another. The size of internal buffers is settable on a per-thread basis. There can be up to $2\left(n_{\text {inputs }}+n_{\text {outputs }}\right)$ buffers of the specified size created to handle the data from all the inputs and outputs of a ufunc. The default size of a buffer is 10,000 elements. Whenever buffer-based calculation would be needed, but all input arrays are smaller than the buffer size, those misbehaved or incorrectly-typed arrays will be copied before the calculation proceeds. Adjusting the size of the buffer may therefore alter the speed at which ufunc calculations of various sorts are completed. A simple interface for setting this variable is accessible using the function

[^1]Set the size of the buffer used in ufuncs.

## Parameters

size : int
Size of buffer.

### 2.4 Error handling

Universal functions can trip special floating-point status registers in your hardware (such as divide-by-zero). If available on your platform, these registers will be regularly checked during calculation. Error handling is controlled on a per-thread basis, and can be configured using the functions
seterr([all, divide, over, under, invalid]) Set how floating-point errors are handled.
seterrcall(func) Set the floating-point error callback function or log object.
numpy.seterr (all=None, divide $=$ None, over $=$ None, under $=$ None, invalid=None)
Set how floating-point errors are handled.

Note that operations on integer scalar types (such as int16) are handled like floating point, and are affected by these settings.

## Parameters

all : \{ 'ignore', 'warn', 'raise', 'call', 'print', 'log'\}, optional
Set treatment for all types of floating-point errors at once:

- ignore: Take no action when the exception occurs.
- warn: Print a RuntimeWarning (via the Python warnings module).
- raise: Raise a FloatingPointError.
- call: Call a function specified using the seterrcall function.
- print: Print a warning directly to stdout.
- log: Record error in a Log object specified by seterrcall.

The default is not to change the current behavior.
divide : \{ 'ignore', 'warn', 'raise', 'call', 'print', 'log' \}, optional
Treatment for division by zero.
over : \{ 'ignore', 'warn', 'raise', 'call', 'print', 'log'\}, optional
Treatment for floating-point overflow.
under : \{ 'ignore’, 'warn', 'raise', 'call', 'print', 'log' \}, optional
Treatment for floating-point underflow.
invalid : \{ 'ignore', 'warn', 'raise', 'call', 'print', 'log'\}, optional
Treatment for invalid floating-point operation.

## Returns

old_settings : dict
Dictionary containing the old settings.

## See Also:

seterrcall
Set a callback function for the 'call' mode.

```
geterr, geterrcall
```


## Notes

The floating-point exceptions are defined in the IEEE 754 standard [1]:
-Division by zero: infinite result obtained from finite numbers.

- Overflow: result too large to be expressed.
-Underflow: result so close to zero that some precision was lost.
-Invalid operation: result is not an expressible number, typically indicates that a NaN was produced.


## Examples

```
>>> old_settings = np.seterr(all='ignore') #seterr to known value
>>> np.seterr(over='raise')
{'over': 'ignore', 'divide': 'ignore', 'invalid': 'ignore',
    'under': 'ignore'}
>>> np.seterr(all='ignore') # reset to default
{'over': 'raise', 'divide': 'ignore', 'invalid': 'ignore', 'under': 'ignore'}
>>> np.int16(32000) * np.int16(3)
30464
>>> old_settings = np.seterr(all='warn', over='raise')
>>> np.int16(32000) * np.int16(3)
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
FloatingPointError: overflow encountered in short_scalars
>>> old_settings = np.seterr(all='print')
>>> np.geterr()
{'over': 'print', 'divide': 'print', 'invalid': 'print', 'under': 'print'}
>>> np.int16(32000) * np.int16(3)
Warning: overflow encountered in short_scalars
30464
```

numpy.seterrcall (func)

Set the floating-point error callback function or log object.
There are two ways to capture floating-point error messages. The first is to set the error-handler to 'call', using seterr. Then, set the function to call using this function.
The second is to set the error-handler to 'log', using seterr. Floating-point errors then trigger a call to the 'write' method of the provided object.

## Parameters

func : callable f(err, flag) or object with write method
Function to call upon floating-point errors ('call'-mode) or object whose 'write' method is used to log such message ('log'-mode).

The call function takes two arguments. The first is the type of error (one of "divide", "over", "under", or "invalid"), and the second is the status flag. The flag is a byte, whose least-significant bits indicate the status:
[0 0 0 0 invalid over under invalid]
In other words, flags $=$ divide +2 *over +4 *under +8 *invalid.
If an object is provided, its write method should take one argument, a string.

## Returns

 h : callable, log instance or NoneThe old error handler.

## See Also:

```
seterr,geterr,geterrcall
```


## Examples

Callback upon error:

```
>>> def err_handler(type, flag):
... print "Floating point error (%S), with flag %s" % (type, flag)
...
>>> saved_handler = np.seterrcall(err_handler)
>>> save_err = np.seterr(all='call')
>>> np.array([1, 2, 3]) / 0.0
Floating point error (divide by zero), with flag 1
array([ Inf, Inf, Inf])
>>> np.seterrcall(saved_handler)
<function err_handler at 0x...>
>>> np.seterr(**save_err)
{'over': 'call', 'divide': 'call', 'invalid': 'call', 'under': 'call'}
```

Log error message:

```
>>> class Log(object):
... def write(self, msg):
... print "LOG: %S" % msg
...
>>> log = Log()
>>> saved_handler = np.seterrcall(log)
>>> save_err = np.seterr(all=' log')
>>> np.array([1, 2, 3]) / 0.0
LOG: Warning: divide by zero encountered in divide
<BLANKLINE>
array([ Inf, Inf, Inf])
>>> np.seterrcall(saved_handler)
<__main__.Log object at 0x...>
>>> np.seterr(**save_err)
{'over': ' log', 'divide': 'log', 'invalid': ' log', 'under': 'log' }
```


### 2.5 Casting Rules

At the core of every ufunc is a one-dimensional strided loop that implements the actual function for a specific type combination. When a ufunc is created, it is given a static list of inner loops and a corresponding list of type signatures over which the ufunc operates. The ufunc machinery uses this list to determine which inner loop to use for a particular case. You can inspect the .types attribute for a particular ufunc to see which type combinations have a defined inner loop and which output type they produce (character codes are used in said output for brevity).

Casting must be done on one or more of the inputs whenever the ufunc does not have a core loop implementation for the input types provided. If an implementation for the input types cannot be found, then the algorithm searches for an implementation with a type signature to which all of the inputs can be cast "safely." The first one it finds in its internal list of loops is selected and performed, after all necessary type casting. Recall that internal copies during ufuncs (even for casting) are limited to the size of an internal buffer (which is user settable).
Note: Universal functions in NumPy are flexible enough to have mixed type signatures. Thus, for example, a universal function could be defined that works with floating-point and integer values. See ldexp for an example.

By the above description, the casting rules are essentially implemented by the question of when a data type can be cast "safely" to another data type. The answer to this question can be determined in Python with a function call:
can_cast (fromtype, totype). The Figure below shows the results of this call for the 24 internally supported types on the author's 64-bit system. You can generate this table for your system with the code given in the Figure.

## Figure

Code segment showing the "can cast safely" table for a 32-bit system.

```
>>> def print_table(ntypes):
... print 'X',
... for char in ntypes: print char,
... print
... for row in ntypes:
... print row,
... for col in ntypes:
... print int(np.can_cast(row, col)),
... print
>>> print_table(np.typecodes['All'])
X ? b h i l q p B H I L Q P e f d g F D G S U V O Mm
? 1
b
h
i}0
1}0
q}0
p
B
H
I
L
Q 0
P
e
f 0}0
d
g}0
F
D
G 0}0
S
U O
V 0
O
M 0
m}0
```

You should note that, while included in the table for completeness, the ' S ', ' U ', and ' V ' types cannot be operated on by ufuncs. Also, note that on a 32-bit system the integer types may have different sizes, resulting in a slightly altered table.

Mixed scalar-array operations use a different set of casting rules that ensure that a scalar cannot "upcast" an array unless the scalar is of a fundamentally different kind of data (i.e., under a different hierarchy in the data-type hierarchy) than the array. This rule enables you to use scalar constants in your code (which, as Python types, are interpreted accordingly in ufuncs) without worrying about whether the precision of the scalar constant will cause upcasting on your large (small precision) array.

## 2.6 ufunc

### 2.6.1 Optional keyword arguments

All ufuncs take optional keyword arguments. These represent rather advanced usage and will not typically be used by most Numpy users. sig

Either a data-type, a tuple of data-types, or a special signature string indicating the input and output types of a ufunc. This argument allows you to provide a specific signature for the $1-\mathrm{d}$ loop to use in the underlying calculation. If the loop specified does not exist for the ufunc, then a TypeError is raised. Normally, a suitable loop is found automatically by comparing the input types with what is available and searching for a loop with data-types to which all inputs can be cast safely. This keyword argument lets you bypass that search and choose a particular loop. A list of available signatures is provided by the types attribute of the ufunc object.
extobj
a list of length 1,2 , or 3 specifying the ufunc buffer-size, the error mode integer, and the error callback function. Normally, these values are looked up in a thread-specific dictionary. Passing them here circumvents that look up and uses the low-level specification provided for the error mode. This may be useful, for example, as an optimization for calculations requiring many ufunc calls on small arrays in a loop.

### 2.6.2 Attributes

There are some informational attributes that universal functions possess. None of the attributes can be set.
__doc_ A docstring for each ufunc. The first part of the docstring is dynamically generated from the number of outputs, the name, and the number of inputs. The second part of the docstring is provided at creation time and stored with the ufunc.
name The name of the ufunc.

| ufunc.nin | The number of inputs. |
| :--- | :--- |
| ufunc.nout | The number of outputs. |
| ufunc.nargs | The number of arguments. |
| ufunc.ntypes | The number of types. |
| ufunc.types | Returns a list with types grouped input->output. |
| ufunc.identity | The identity value. |

ufunc.nin
The number of inputs.
Data attribute containing the number of arguments the ufunc treats as input.

## Examples

```
>>> np.add.nin
2
>>> np.multiply.nin
2
>>> np.power.nin
2
>>> np.exp.nin
1
```

ufunc.nout

The number of outputs.

Data attribute containing the number of arguments the ufunc treats as output.

## Notes

Since all ufuncs can take output arguments, this will always be (at least) 1.

## Examples

```
>>> np.add.nout
1
>>> np.multiply.nout
1
>>> np.power.nout
1
>>> np.exp.nout
1
The number of arguments.
```

ufunc.nargs

Data attribute containing the number of arguments the ufunc takes, including optional ones.

## Notes

Typically this value will be one more than what you might expect because all ufuncs take the optional "out" argument.

## Examples

```
        >>> np.add.nargs
```

        3
        >>> np.multiply.nargs
        3
        >>> np.power.nargs
        3
        >>> np.exp.nargs
        2
    ufunc.ntypes

The number of types.
The number of numerical NumPy types - of which there are 18 total - on which the ufunc can operate.

## See Also:

numpy.ufunc.types

## Examples

```
>>> np.add.ntypes
18
>>> np.multiply.ntypes
18
>>> np.power.ntypes
17
>>> np.exp.ntypes
7
>>> np.remainder.ntypes
14
```

ufunc.types

Returns a list with types grouped input->output.

Data attribute listing the data-type "Domain-Range" groupings the ufunc can deliver. The data-types are given using the character codes.

## See Also:

numpy.ufunc.ntypes

## Examples

```
>>> np.add.types
['??->?', 'bb->b', 'BB->B', 'hh->h', 'HH->H', 'ii->i', 'II->I', 'll-> '',
'LL->L', 'qq->q', 'QQ->Q', 'ff->f', 'dd->d', 'gg->g', 'FF->F', 'DD->D',
'GG->G', 'OO->O' ]
>>> np.multiply.types
['??->?', 'bb->b', 'BB->B', 'hh->h' , 'HH->H', 'ii->i', 'II->I', 'll->l',
'LL->L', 'qq->q', 'QQ->Q', 'ff->f', 'dd->d', 'gg->g', 'FF->F', 'DD->D',
'GG->G', 'OO->O']
>>> np.power.types
['bb->b', 'BB->B', 'hh->h', 'HH->H', 'ii->i', 'II->I',' 'll->l', 'LL->L',
'qq->q', 'QQ->Q', 'ff->f', 'dd->d', 'gg->g', 'FF->E', 'DD->D', 'GG->G',
'OO->O' ]
>>> np.exp.types
['f->f', 'd->d', 'g->g', 'F->F', 'D->D', 'G->G', 'O->O']
>>> np.remainder.types
['bb->b', 'BB->B', 'hh->h', 'HH->H', 'ii->i', 'II->I', 'll->l', 'LL->L',
'qq->q', 'QQ->Q', 'ff->f', 'dd->d', 'gg->g', 'OO->O']
```


## ufunc.identity

The identity value.
Data attribute containing the identity element for the ufunc, if it has one. If it does not, the attribute value is None.

## Examples

```
>>> np.add.identity
0
>>> np.multiply.identity
1
>>> np.power.identity
1
>>> print np.exp.identity
None
```


### 2.6.3 Methods

All ufuncs have four methods. However, these methods only make sense on ufuncs that take two input arguments and return one output argument. Attempting to call these methods on other ufuncs will cause a ValueError. The reduce-like methods all take an axis keyword and a dtype keyword, and the arrays must all have dimension >= 1 . The axis keyword specifies the axis of the array over which the reduction will take place and may be negative, but must be an integer. The dtype keyword allows you to manage a very common problem that arises when naively using \{op\}.reduce. Sometimes you may have an array of a certain data type and wish to add up all of its elements, but the result does not fit into the data type of the array. This commonly happens if you have an array of single-byte integers. The dtype keyword allows you to alter the data type over which the reduction takes place (and therefore
the type of the output). Thus, you can ensure that the output is a data type with precision large enough to handle your output. The responsibility of altering the reduce type is mostly up to you. There is one exception: if no dtype is given for a reduction on the "add" or "multiply" operations, then if the input type is an integer (or Boolean) data-type and smaller than the size of the int_data type, it will be internally upcast to the int_ (or uint) data-type. ufunc.reduce(a[, axis, dtype, out]) Reduces $a$ 's dimension by one, by applying ufunc along one axis. ufunc.accumulate(array[, axis, dtype, out]) Accumulate the result of applying the operator to all elements. ufunc.reduceat(a, indices[, axis, dtype, out]) Performs a (local) reduce with specified slices over a single axis. ufunc.outer(A, B)

Apply the ufunc $o p$ to all pairs $(\mathrm{a}, \mathrm{b})$ with a in $A$ and b in $B$.
ufunc.reduce ( $a$, axis=0, dtype $=$ None, out $=$ None )
Reduces $a$ 's dimension by one, by applying ufunc along one axis.
Let $a . s h a p e=\left(N_{0}, \ldots, N_{i}, \ldots, N_{M-1}\right)$. Then ufunc.reduce $(a$, axis $=i)\left[k_{0}, . ., k_{i-1}, k_{i+1}, . ., k_{M-1}\right]=$ the result of iterating $j$ over range $\left(N_{i}\right)$, cumulatively applying ufunc to each $a\left[k_{0}, . ., k_{i-1}, j, k_{i+1}, . ., k_{M-1}\right]$. For a one-dimensional array, reduce produces results equivalent to:

```
r = op.identity # op = ufunc
for i in xrange(len(A)):
    r =op(r, A[i])
return r
```

For example, add.reduce() is equivalent to sum().

## Parameters

a: array_like
The array to act on.
axis : int, optional
The axis along which to apply the reduction.
dtype : data-type code, optional
The type used to represent the intermediate results. Defaults to the data-type of the output array if this is provided, or the data-type of the input array if no output array is provided.
out : ndarray, optional
A location into which the result is stored. If not provided, a freshly-allocated array is returned.

## Returns

$\mathbf{r}$ : ndarray
The reduced array. If out was supplied, $r$ is a reference to it.

## Examples

```
>>> np.multiply.reduce([2,3,5])
30
```

A multi-dimensional array example:

```
>>> X = np.arange(8).reshape((2,2,2))
>>> X
array([[[0, 1],
            [2, 3]],
            [[4, 5],
            [6, 7]]])
>>> np.add.reduce(X, 0)
array([[ 4, 6],
```

```
    [ 8, 10]])
>>> np.add.reduce(X) # confirm: default axis value is 0
array([[ 4, 6],
    [ 8, 10]])
>>> np.add.reduce(X, 1)
array([[ 2, 4],
    [10, 12]])
>>> np.add.reduce(X, 2)
array([[ 1, 5],
    [ 9, 13]])
ufunc.accumulate (array, axis=0,dtype=None, out=None)
Accumulate the result of applying the operator to all elements.
For a one-dimensional array, accumulate produces results equivalent to:
```

```
r = np.empty(len(A))
```

r = np.empty(len(A))
t = op.identity \# op = the ufunc being applied to A's elements
t = op.identity \# op = the ufunc being applied to A's elements
for i in xrange(len(A)):
for i in xrange(len(A)):
t = op(t, A[i])
t = op(t, A[i])
r[i] = t
r[i] = t
return r

```
return r
```

For example, add.accumulate() is equivalent to np.cumsum().
For a multi-dimensional array, accumulate is applied along only one axis (axis zero by default; see Examples below) so repeated use is necessary if one wants to accumulate over multiple axes.

## Parameters

array : array_like
The array to act on.
axis : int, optional
The axis along which to apply the accumulation; default is zero.
dtype : data-type code, optional
The data-type used to represent the intermediate results. Defaults to the data-type of the output array if such is provided, or the the data-type of the input array if no output array is provided.
out : ndarray, optional
A location into which the result is stored. If not provided a freshly-allocated array is returned.

## Returns

r: ndarray
The accumulated values. If out was supplied, $r$ is a reference to out.

## Examples

1-D array examples:

```
>>> np.add.accumulate([2, 3, 5])
array([ 2, 5, 10])
>>> np.multiply.accumulate([2, 3, 5])
array([ 2, 6, 30])
```

2-D array examples:

```
>>> I = np.eye(2)
>>> I
array([[ 1., 0.],
    [ 0., 1.]])
```

Accumulate along axis 0 (rows), down columns:

```
>>> np.add.accumulate(I, 0)
array([[ 1., 0.],
    [ 1., 1.]])
>>> np.add.accumulate(I) # no axis specified = axis zero
array([[ 1., 0.],
    [ 1., 1.]])
```

Accumulate along axis 1 (columns), through rows:

```
>>> np.add.accumulate(I, 1)
array([[ 1., 1.],
    [ 0., 1.]])
```

ufunc.reduceat ( $a$, indices, axis=0, dtype $=$ None, out $=$ None )
Performs a (local) reduce with specified slices over a single axis.
Foriin range (len(indices)), reduceat computes ufunc.reduce (a[indices[i]:indices[i+1]]), which becomes the i-th generalized "row" parallel to axis in the final result (i.e., in a 2-D array, for example, if axis $=0$, it becomes the i-th row, but if axis $=1$, it becomes the i-th column). There are two exceptions to this:
-when $i=$ len(indices) -1 (so for the last index), indices [i+1] = a.shape[axis].
-if indices[i] >= indices[i + 1], the i-th generalized "row" is simply a[indices[i]].
The shape of the output depends on the size of indices, and may be larger than $a$ (this happens if len(indices) > a.shape[axis]).

## Parameters

a : array_like
The array to act on.
indices : array_like
Paired indices, comma separated (not colon), specifying slices to reduce.
axis : int, optional
The axis along which to apply the reduceat.
dtype : data-type code, optional
The type used to represent the intermediate results. Defaults to the data type of the output array if this is provided, or the data type of the input array if no output array is provided.
out : ndarray, optional
A location into which the result is stored. If not provided a freshly-allocated array is returned.

## Returns

r: ndarray
The reduced values. If out was supplied, $r$ is a reference to out.

## Notes

## A descriptive example:

If $a$ is $1-\mathrm{D}$, the function ufunc.accumulate( $(a)$ is the same as ufunc.reduceat (a, indices) [::2] where indices is range (len (array) - 1) with a zero placed in every other element: indices = zeros (2 * len(a) - 1), indices[1::2] = range(1, len(a)).

Don't be fooled by this attribute's name: reduceat $(a)$ is not necessarily smaller than $a$.

## Examples

To take the running sum of four successive values:

```
>>> np.add.reduceat(np.arange(8),[0,4, 1,5, 2,6, 3,7]) [::2]
array([ 6, 10, 14, 18])
```

A 2-D example:

```
>>> x = np.linspace(0, 15, 16).reshape (4,4)
>>> x
array([[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.],
    [ 12., 13., 14., 15.]])
# reduce such that the result has the following five rows:
# [row1 + row2 + row3]
# [row4]
# [row2]
# [row3]
# [row1 + row2 + row3 + row4]
>>> np.add.reduceat(x, [0, 3, 1, 2, 0])
array([[ 12., 15., 18., 21.],
    [ 12., 13., 14., 15.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.],
    [ 24., 28., 32., 36.]])
# reduce such that result has the following two columns:
# [col1 * col2 * col3, col4]
>>> np.multiply.reduceat(x, [0, 3], 1)
array([[ 0., 3.],
    [ 120., 7.],
    [ 720., 11.],
    [ 2184., 15.]])
```

ufunc.outer ( $A, B$ )

Apply the ufunc $o p$ to all pairs $(\mathrm{a}, \mathrm{b})$ with a in $A$ and b in $B$.
Let $M=A$. ndim, $N=B$. ndim. Then the result, $C$, of op. outer $(A, B)$ is an array of dimension $M+N$ such that:

$$
C\left[i_{0}, \ldots, i_{M-1}, j_{0}, \ldots, j_{N-1}\right]=o p\left(A\left[i_{0}, \ldots, i_{M-1}\right], B\left[j_{0}, \ldots, j_{N-1}\right]\right)
$$

For $A$ and $B$ one-dimensional, this is equivalent to:

```
r = empty(len(A),len(B))
for i in xrange(len(A)):
    for j in xrange(len(B)):
        r[i,j] = op(A[i], B[j]) # op = ufunc in question
```


## Parameters

A : array_like
First array
B : array_like
Second array

## Returns

r: ndarray
Output array

## See Also:

numpy.outer

## Examples

```
>>> np.multiply.outer([1, 2, 3], [4, 5, 6])
array([[ 4, 5, 6],
    [ 8, 10, 12],
    [12, 15, 18]])
```

A multi-dimensional example:

```
>>>A = np.array([[1, 2, 3], [4, 5, 6]])
>>> A.shape
(2, 3)
>>> B = np.array([[1, 2, 3, 4]])
>>> B.shape
(1, 4)
>>> C = np.multiply.outer(A, B)
>>> C.shape; C
(2, 3, 1, 4)
array([[[[[ 1, 2, 3, 4]],
    [[ 2, 4, 6, 8]],
    [[[3, 6, 9, 12]]],
    [[[[4, 8, 12, 16]],
    [[ 5, 10, 15, 20]],
    [[ 6, 12, 18, 24]]]])
```

Warning: A reduce-like operation on an array with a data-type that has a range "too small" to handle the result will silently wrap. One should use dtype to increase the size of the data-type over which reduction takes place.

### 2.7 Available ufuncs

There are currently more than 60 universal functions defined in numpy on one or more types, covering a wide variety of operations. Some of these ufuncs are called automatically on arrays when the relevant infix notation is used (e.g., add ( $\mathrm{a}, \mathrm{b}$ ) is called internally when $\mathrm{a}+\mathrm{b}$ is written and $a$ or $b$ is an ndarray). Nevertheless, you may still want
to use the ufunc call in order to use the optional output argument(s) to place the output(s) in an object (or objects) of your choice.

Recall that each ufunc operates element-by-element. Therefore, each ufunc will be described as if acting on a set of scalar inputs to return a set of scalar outputs.

Note: The ufunc still returns its output(s) even if you use the optional output argument(s).

### 2.7.1 Math operations

| add(x1) | Add arguments element-wise. |
| :---: | :---: |
| subtract(x1) | Subtract arguments, element-wise. |
| multiply(x1) | Multiply arguments element-wise. |
| divide(x1) | Divide arguments element-wise. |
| logaddexp(x1) | Logarithm of the sum of exponentiations of the inputs. |
| logaddexp2(x1) | Logarithm of the sum of exponentiations of the inputs in base-2. |
| true_divide(x1) | Returns a true division of the inputs, element-wise. |
| floor_divide(x1) | Return the largest integer smaller or equal to the division of the inputs. |
| negative() | Returns an array with the negative of each element of the original array. |
| power(x1) | First array elements raised to powers from second array, element-wise. |
| remainder(x1) | Return element-wise remainder of division. |
| $\bmod (\mathrm{x} 1)$ | Return element-wise remainder of division. |
| fmod(x1) | Return the element-wise remainder of division. |
| absolute() | Calculate the absolute value element-wise. |
| rint() | Round elements of the array to the nearest integer. |
| sign() | Returns an element-wise indication of the sign of a number. |
| conj() | Return the complex conjugate, element-wise. |
| $\exp ()$ | Calculate the exponential of all elements in the input array. |
| exp2() | Calculate $2{ }^{* *} p$ for all $p$ in the input array. |
| $\log ()$ | Natural logarithm, element-wise. |
| $\log 2()$ | Base-2 logarithm of $x$. |
| $\log 10()$ | Return the base 10 logarithm of the input array, element-wise. |
| expm1() | Calculate $\exp (\mathrm{x})-1$ for all elements in the array. |
| $\operatorname{log1p()}$ | Return the natural logarithm of one plus the input array, element-wise. |
| sqrt() | Return the positive square-root of an array, element-wise. |
| square() | Return the element-wise square of the input. |
| reciprocal() | Return the reciprocal of the argument, element-wise. |
| ones_like() | Returns an array of ones with the same shape and type as a given array. |

Tip: The optional output arguments can be used to help you save memory for large calculations. If your arrays are large, complicated expressions can take longer than absolutely necessary due to the creation and (later) destruction of temporary calculation spaces. For example, the expression $G=a * b+c$ is equivalent to $t 1=A * B ; G=$ $T 1+C$; del t1. It will be more quickly executed as $G=A * B ; \operatorname{add}(G, C, G)$ which is the same as $G$ $=A * B ; G+=C$.

### 2.7.2 Trigonometric functions

All trigonometric functions use radians when an angle is called for. The ratio of degrees to radians is $180^{\circ} / \pi$.

| $\sin ()$ | Trigonometric sine, element-wise. |
| :--- | :--- |
| $\cos ()$ | Cosine elementwise. |
| $\tan ()$ | Compute tangent element-wise. |
| $\arcsin ()$ | Inverse sine, element-wise. |
| $\arccos ()$ | Trigonometric inverse cosine, element-wise. |
| $\arctan ()$ | Trigonometric inverse tangent, element-wise. |
| $\arctan 2(\mathrm{x} 1)$ | Element-wise arc tangent of x1/x2 choosing the quadrant correctly. |
| hypot(x1) | Given the "legs" of a right triangle, return its hypotenuse. |
| $\sinh ()$ | Hyperbolic sine, element-wise. |
| $\cosh ()$ | Hyperbolic cosine, element-wise. |
| $\tanh ()$ | Compute hyperbolic tangent element-wise. |
| $\operatorname{arcsinh}()$ | Inverse hyperbolic sine elementwise. |
| $\operatorname{arccosh}()$ | Inverse hyperbolic cosine, elementwise. |
| $\operatorname{arctanh}()$ | Inverse hyperbolic tangent elementwise. |
| $\operatorname{deg} 2 r a d()$ | Convert angles from degrees to radians. |
| $\operatorname{rad2deg}()$ | Convert angles from radians to degrees. |

### 2.7.3 Bit-twiddling functions

These function all require integer arguments and they manipulate the bit-pattern of those arguments.

| bitwise_and(x1) | Compute the bit-wise AND of two arrays element-wise. |
| :--- | :--- |
| bitwise_or(x1) | Compute the bit-wise OR of two arrays element-wise. |
| bitwise_xor(x1) | Compute the bit-wise XOR of two arrays element-wise. |
| invert() | Compute bit-wise inversion, or bit-wise NOT, element-wise. |
| left_shift(x1) | Shift the bits of an integer to the left. |
| right_shift(x1) | Shift the bits of an integer to the right. |

### 2.7.4 Comparison functions

| greater(x1) | Return the truth value of $(x 1>x 2)$ element-wise. |
| :--- | :--- |
| greater_equal(x1) | Return the truth value of $(x 1>=x 2)$ element-wise. |
| less(x1) | Return the truth value of $(x 1<x 2)$ element-wise. |
| less_equal(x1) | Return the truth value of $(x 1=<x 2)$ element-wise. |
| not_equal(x1) | Return $(x 1!=x 2)$ element-wise. |
| equal(x1) | Return $(x 1==x 2)$ element-wise. |

Warning: Do not use the Python keywords and and or to combine logical array expressions. These keywords will test the truth value of the entire array (not element-by-element as you might expect). Use the bitwise operators \& and I instead.

| logical_and(x1) | Compute the truth value of x1 AND x2 elementwise. |
| :--- | :--- |
| logical_or(x1) | Compute the truth value of x1 OR x2 elementwise. |
| logical_xor(x1) | Compute the truth value of x1 XOR x2, element-wise. |
| logical_not() | Compute the truth value of NOT x elementwise. |

Warning: The bit-wise operators \& and I are the proper way to perform element-by-element array comparisons. Be sure you understand the operator precedence: $(a>2) \&(a<5)$ is the proper syntax because $a>2$ $\& a<5$ will result in an error due to the fact that $2 \& a$ is evaluated first.

[^2]Tip: The Python function max () will find the maximum over a one-dimensional array, but it will do so using a slower sequence interface. The reduce method of the maximum ufunc is much faster. Also, the max () method will not give answers you might expect for arrays with greater than one dimension. The reduce method of minimum also allows you to compute a total minimum over an array.

```
minimum(x1) Element-wise minimum of array elements.
```

Warning: the behavior of maximum ( $a, b$ ) is different than that of max ( $a, b$ ). As a ufunc, maximum ( $a$, b) performs an element-by-element comparison of $a$ and $b$ and chooses each element of the result according to which element in the two arrays is larger. In contrast, $\max (\mathrm{a}, \mathrm{b})$ treats the objects $a$ and $b$ as a whole, looks at the (total) truth value of $\mathrm{a}>\mathrm{b}$ and uses it to return either $a$ or $b$ (as a whole). A similar difference exists between minimum ( $\mathrm{a}, \mathrm{b}$ ) andmin( $\mathrm{a}, \mathrm{b})$.

### 2.7.5 Floating functions

Recall that all of these functions work element-by-element over an array, returning an array output. The description details only a single operation.

| isreal(x) | Returns a bool array, where True if input element is real. |
| :--- | :--- |
| iscomplex(x) | Returns a bool array, where True if input element is complex. |
| isfinite() | Test element-wise for finite-ness (not infinity or not Not a Number). |
| isinf() | Test element-wise for positive or negative infinity. |
| isnan() | Test element-wise for Not a Number (NaN), return result as a bool array. |
| signbit() | Returns element-wise True where signbit is set (less than zero). |
| copysign(x1) | Change the sign of x1 to that of x2, element-wise. |
| nextafter(x1) | Return the next representable floating-point value after x1 in the direction of x2 element-wise. |
| modf(out1) | Return the fractional and integral parts of an array, element-wise. |
| ldexp(x1) | Compute $y=x 1 * 2^{* * x} 2$. |
| frexp(out1) | Split the number, x, into a normalized fraction (y1) and exponent (y2) |
| fmod(x1) | Return the element-wise remainder of division. |
| floor() | Return the floor of the input, element-wise. |
| $\operatorname{ceil()}$ | Return the ceiling of the input, element-wise. |
| $\operatorname{trunc}()$ | Return the truncated value of the input, element-wise. |

## ROUTINES

In this chapter routine docstrings are presented, grouped by functionality. Many docstrings contain example code, which demonstrates basic usage of the routine. The examples assume that NumPy is imported with:

```
>>> import numpy as np
```

A convenient way to execute examples is the \%doctest_mode mode of IPython, which allows for pasting of multiline examples and preserves indentation.

### 3.1 Array creation routines

## See Also:

Array creation

### 3.1.1 Ones and zeros

| empty(shape[, dtype, order]) | Return a new array of given shape and type, without initializing entries. |
| :---: | :---: |
| empty_like(a[, dtype, order, subok]) | Return a new array with the same shape and type as a given array. |
| eye(N[, M, k, dtype]) | Return a 2-D array with ones on the diagonal and zeros elsewhere. |
| identity(n[, dtype]) | Return the identity array. |
| ones(shape[, dtype, order]) | Return a new array of given shape and type, filled with ones. |
| ones_like() | Returns an array of ones with the same shape and type as a given array. |
| zeros(shape[, dtype, order]) | Return a new array of given shape and type, filled with zeros. |
| zeros_like(a[, dtype, order, subok]) | Return an array of zeros with the same shape and type as a given array. |
| numpy . empty (shape, dtype=float, order ${ }^{\prime} C^{\prime}$ ) |  |
| Return a new array of given shape and type, without initializing entries. |  |
| Parameters |  |
| shape : int or tuple of int |  |
| Shape of the empty array |  |
| dtype : data-type, optional |  |
| Desired output data-type. |  |
| order : $\{$ ' C ', ' F ' $\}$, optional |  |
| Whether to store multic order in memory. | -dimensional data in C (row-major) or Fortran (column-major) |

## See Also:

```
empty_like,zeros,ones
```


## Notes

empty, unlike zeros, does not set the array values to zero, and may therefore be marginally faster. On the other hand, it requires the user to manually set all the values in the array, and should be used with caution.

## Examples

```
>>> np.empty([2, 2])
array([[ -9.74499359e+001, 6.69583040e-309],
    [ 2.13182611e-314, 3.06959433e-309]]) #random
>>> np.empty([2, 2], dtype=int)
array([[-1073741821, -1067949133],
    [496041986, 19249760]]) #random
```

numpy.empty_like ( $a$, dtype=None, order='K', subok=True)

Return a new array with the same shape and type as a given array.

## Parameters

a : array_like
The shape and data-type of $a$ define these same attributes of the returned array. dtype : data-type, optional

Overrides the data type of the result.
order : \{ ' $C$ ', ' $F$ ', ' $A$ ', or ' $K$ ' \}, optional
Overrides the memory layout of the result. ' $C$ ' means $C$-order, ' $F$ ' means F-order, ' $A$ ' means ' $F$ ' if a is Fortran contiguous, ' $C$ ' otherwise. ' $K$ ' means match the layout of a as closely as possible.
subok: bool, optional.
If True, then the newly created array will use the sub-class type of ' $a$ ', otherwise it will be a base-class array. Defaults to True.

## Returns

 out : ndarrayArray of uninitialized (arbitrary) data with the same shape and type as $a$.

## See Also:

ones_like
Return an array of ones with shape and type of input.
zeros_like
Return an array of zeros with shape and type of input.
empty
Return a new uninitialized array.
ones
Return a new array setting values to one.
zeros
Return a new array setting values to zero.

## Notes

This function does not initialize the returned array; to do that use zeros_like or ones_like instead. It may be marginally faster than the functions that do set the array values.

## Examples

```
>>> a = ([1,2,3], [4,5,6]) # a is array-like
>>> np.empty_like(a)
array([[-1073741821, -1073741821, 3], #random
    [ 0, 0, -1073741821]])
>>> a = np.array([[1., 2., 3.],[4.,5.,6.]])
>>> np.empty_like(a)
array([[ -2.00000715e+000, 1.48219694e-323, -2.00000572e+000],#random
    [ 4.38791518e-305, -2.00000715e+000, 4.17269252e-309]])
```

numpy . eye ( $N, M=$ None, $k=0$, dtype $=<$ type 'float' $>$ )

Return a 2-D array with ones on the diagonal and zeros elsewhere.

## Parameters

$\mathbf{N}$ : int
Number of rows in the output.
M : int, optional
Number of columns in the output. If None, defaults to $N$.
k: int, optional
Index of the diagonal: 0 (the default) refers to the main diagonal, a positive value refers to an upper diagonal, and a negative value to a lower diagonal.
dtype : data-type, optional
Data-type of the returned array.

## Returns

I : ndarray of shape ( $\mathrm{N}, \mathrm{M}$ )
An array where all elements are equal to zero, except for the $k$-th diagonal, whose values are equal to one.

## See Also:

identity
(almost) equivalent function
diag
diagonal 2-D array from a 1-D array specified by the user.

## Examples

```
>>> np.eye(2, dtype=int)
array([[1, 0],
                    [0, 1]])
>>> np.eye(3, k=1)
array([[ 0., 1., 0.],
            [ 0., 0., 1.],
            [ 0., 0., 0.]])
```

numpy.identity ( $n$, dtype=None)
Return the identity array.

The identity array is a square array with ones on the main diagonal.

## Parameters

$\mathbf{n}$ : int
Number of rows (and columns) in $n \times n$ output.
dtype : data-type, optional
Data-type of the output. Defaults to float.

## Returns

out : ndarray
$n \times n$ array with its main diagonal set to one, and all other elements 0.

## Examples

```
>>> np.identity(3)
array([[ 1., 0., 0.],
    [ 0., 1., 0.],
    [ 0., 0., 1.]])
```

numpy. ones (shape, dtype $=$ None, order $=$ ' $C^{\prime}$ )
Return a new array of given shape and type, filled with ones.
Please refer to the documentation for zeros for further details.

## See Also:

```
zeros,ones_like
```


## Examples

```
>>> np.ones(5)
array([ 1., 1., 1., 1., 1.])
>>> np.ones((5,), dtype=np.int)
array([1, 1, 1, 1, 1])
>>> np.ones((2, 1))
array([[ 1.],
            [ 1.]])
>>> s = (2,2)
>>> np.ones(s)
array([[ 1., 1.],
            [ 1., 1.]])
```

numpy. ones_like ( $x[$, out $]$ )

Returns an array of ones with the same shape and type as a given array.
Equivalent to a.copy ().fill(1).
Please refer to the documentation for zeros_like for further details.

## See Also:

zeros_like, ones

## Examples

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
>>> np.ones_like(a)
array([[1, 1, 1],
    [1, 1, 1]])
```

numpy.zeros (shape, dtype=float, order='C')

Return a new array of given shape and type, filled with zeros.

## Parameters

shape : int or sequence of ints
Shape of the new array, e.g., $(2,3)$ or 2.
dtype : data-type, optional
The desired data-type for the array, e.g., numpy.int 8 . Default is numpy.float 64.
order : \{ 'C', 'F' \}, optional
Whether to store multidimensional data in C - or Fortran-contiguous (row- or columnwise) order in memory.

## Returns

out : ndarray
Array of zeros with the given shape, dtype, and order.

## See Also:

## zeros_like

Return an array of zeros with shape and type of input.

## ones_like

Return an array of ones with shape and type of input.
empty_like
Return an empty array with shape and type of input.
ones
Return a new array setting values to one.
empty
Return a new uninitialized array.

## Examples

```
>>> np.zeros(5)
array([ 0., 0., 0., 0., 0.])
>>> np.zeros((5,), dtype=numpy.int)
array([0, 0, 0, 0, 0])
>>> np.zeros((2, 1))
array([[ 0.],
                    [ 0.]])
>>> s = (2,2)
>>> np.zeros(s)
array([[ 0., 0.],
            [ 0., 0.]])
```

```
>>> np.zeros((2,), dtype=[('x', 'i4'), ('y', 'i4')]) # custom dtype
array([(0, 0), (0, 0)],
    dtype=[('x', '<i4'), ('y', '<i4')])
```

numpy.zeros_like ( $a$, dtype $=$ None, order $=$ ' $K$ ', subok=True )

Return an array of zeros with the same shape and type as a given array.
With default parameters, is equivalent to a.copy ().fill(0).

## Parameters

a : array_like
The shape and data-type of $a$ define these same attributes of the returned array.
dtype : data-type, optional
Overrides the data type of the result.
order : \{ ' $C$ ', ' $F$ ', ' $A$ ', or ' $K$ ' \}, optional
Overrides the memory layout of the result. 'C' means C-order, ' F ' means F -order, ' A ' means ' F ' if $a$ is Fortran contiguous, ' C ' otherwise. ' K ' means match the layout of $a$ as closely as possible.

## Returns

out : ndarray
Array of zeros with the same shape and type as $a$.
See Also:
ones_like
Return an array of ones with shape and type of input.
empty_like
Return an empty array with shape and type of input.
zeros
Return a new array setting values to zero.
ones
Return a new array setting values to one.
empty
Return a new uninitialized array.

## Examples

```
>>> x = np.arange(6)
>>> x = x.reshape((2, 3))
>>> x
array([[0, 1, 2],
                    [3, 4, 5]])
>>> np.zeros_like(x)
array([[0, 0, 0],
                    [0, 0, 0]])
>>> y = np.arange(3, dtype=np.float)
>>> y
array([ 0., 1., 2.])
>>> np.zeros_like(y)
array([ 0., 0., 0.])
```


### 3.1.2 From existing data

```
array(object[, dtype, copy, order, subok,
ndmin])
asarray(a[, dtype, order]) Convert the input to an array.
asanyarray(a[, dtype, order])
ascontiguousarray(a[, dtype])
asmatrix(data[, dtype])
copy(a)
frombuffer(buffer[, dtype, count, offset])
fromfile(file[, dtype, count, sep])
fromfunction(function, shape, **kwargs)
fromiter(iterable, dtype[, count])
fromstring(string[, dtype, count, sep])
```

Create an array.

Convert the input to an array.
Convert the input to an ndarray, but pass ndarray subclasses through.
Return a contiguous array in memory (C order).
Interpret the input as a matrix.
Return an array copy of the given object.
Interpret a buffer as a 1-dimensional array.
Construct an array from data in a text or binary file.
Construct an array by executing a function over each coordinate.
Create a new 1-dimensional array from an iterable object. A new 1-D array initialized from raw binary or text data in a string.

```
loadtxt(fname[, dtype, comments, delimiter, Load data from a text file.
...])
```

numpy . array (object, dtype=None, copy=True, order=None, subok=False, ndmin=0)
Create an array.

## Parameters

object : array_like
An array, any object exposing the array interface, an object whose $\qquad$ array method returns an array, or any (nested) sequence.
dtype : data-type, optional
The desired data-type for the array. If not given, then the type will be determined as the minimum type required to hold the objects in the sequence. This argument can only be used to 'upcast' the array. For downcasting, use the .astype(t) method.
copy : bool, optional
If true (default), then the object is copied. Otherwise, a copy will only be made if __array__ returns a copy, if obj is a nested sequence, or if a copy is needed to satisfy any of the other requirements (dtype, order, etc.).
order : \{ 'C', 'F', 'A'\}, optional
Specify the order of the array. If order is ' C ' (default), then the array will be in C contiguous order (last-index varies the fastest). If order is ' F ', then the returned array will be in Fortran-contiguous order (first-index varies the fastest). If order is ' $A$ ', then the returned array may be in any order (either C-, Fortran-contiguous, or even discontiguous).
subok: bool, optional
If True, then sub-classes will be passed-through, otherwise the returned array will be forced to be a base-class array (default).
ndmin : int, optional
Specifies the minimum number of dimensions that the resulting array should have. Ones will be pre-pended to the shape as needed to meet this requirement.

## Returns

out : ndarray

An array object satisfying the specified requirements.

## See Also:

```
empty, empty_like, zeros, zeros_like,ones,ones_like, fill
```


## Examples

```
>>> np.array([1, 2, 3])
array([1, 2, 3])
```

Upcasting:

```
>>> np.array([1, 2, 3.0])
array([ 1., 2., 3.])
```

More than one dimension:

```
>>> np.array([[1, 2], [3, 4]])
array([[1, 2],
    [3, 4]])
```

Minimum dimensions 2:

```
>>> np.array([1, 2, 3], ndmin=2)
array([[1, 2, 3]])
```

Type provided:

```
>>> np.array([1, 2, 3], dtype=complex)
array([ 1.+0.j, 2.+0.j, 3.+0.j])
```

Data-type consisting of more than one element:

```
>>> x = np.array([(1,2), (3,4)],dtype=[('a','<i4'),('b','<i4')])
>>> x['a']
array([1, 3])
```

Creating an array from sub-classes:

```
>>> np.array(np.mat('1 2; 3 4'))
array([[1, 2],
    [3, 4]])
>>> np.array(np.mat('1 2; 3 4'), subok=True)
matrix([[1, 2],
    [3, 4]])
```

numpy . asarray ( $a$, dtype $=$ None, order $=$ None )
Convert the input to an array.

## Parameters

a : array_like
Input data, in any form that can be converted to an array. This includes lists, lists of tuples, tuples, tuples of tuples, tuples of lists and ndarrays.
dtype : data-type, optional
By default, the data-type is inferred from the input data.
order : \{ 'C', 'F' \}, optional

Whether to use row-major ('C') or column-major ('F' for FORTRAN) memory representation. Defaults to ' C '.

## Returns

```
out : ndarray
```

Array interpretation of $a$. No copy is performed if the input is already an ndarray. If $a$ is a subclass of ndarray, a base class ndarray is returned.

## See Also:

## asanyarray

Similar function which passes through subclasses.

```
ascontiguousarray
```

Convert input to a contiguous array.

```
asfarray
```

Convert input to a floating point ndarray.

```
asfortranarray
```

Convert input to an ndarray with column-major memory order.

## asarray_chkfinite

Similar function which checks input for NaNs and Infs.

## fromiter

Create an array from an iterator.

## fromfunction

Construct an array by executing a function on grid positions.

## Examples

Convert a list into an array:

```
>>> a = [1, 2]
>>> np.asarray(a)
array([1, 2])
```

Existing arrays are not copied:

```
>>> a = np.array([1, 2])
>>> np.asarray(a) is a
True
```

If dtype is set, array is copied only if dtype does not match:

```
>>> a = np.array([1, 2], dtype=np.float32)
>>> np.asarray(a, dtype=np.float32) is a
True
>>> np.asarray(a, dtype=np.float64) is a
False
```

Contrary to asanyarray, ndarray subclasses are not passed through:

```
>>> issubclass(np.matrix, np.ndarray)
True
>>> a = np.matrix([[1, 2]])
>>> np.asarray(a) is a
False
```

```
>>> np.asanyarray(a) is a
```

True
numpy . asanyarray ( $a$, dtype $=$ None, order $=$ None )
Convert the input to an ndarray, but pass ndarray subclasses through.

## Parameters

a : array_like
Input data, in any form that can be converted to an array. This includes scalars, lists, lists of tuples, tuples, tuples of tuples, tuples of lists, and ndarrays.
dtype : data-type, optional
By default, the data-type is inferred from the input data.
order : \{ 'C', 'F'\}, optional
Whether to use row-major ('C') or column-major (' F ') memory representation. Defaults to ' C '.

## Returns

out : ndarray or an ndarray subclass
Array interpretation of $a$. If $a$ is an ndarray or a subclass of ndarray, it is returned as-is and no copy is performed.

## See Also:

## asarray

Similar function which always returns ndarrays.

## ascontiguousarray

Convert input to a contiguous array.
asfarray
Convert input to a floating point ndarray.
asfortranarray
Convert input to an ndarray with column-major memory order.
asarray_chkfinite
Similar function which checks input for NaNs and Infs.
fromiter
Create an array from an iterator.
fromfunction
Construct an array by executing a function on grid positions.

## Examples

Convert a list into an array:

```
>>> a = [1, 2]
>>> np.asanyarray(a)
array([1, 2])
```

Instances of ndarray subclasses are passed through as-is:

```
>>> a = np.matrix([1, 2])
>>> np.asanyarray(a) is a
True
```

numpy.ascontiguousarray ( $a$, dtype $=$ None )
Return a contiguous array in memory ( C order).

## Parameters

a : array_like
Input array. dtype : str or dtype object, optional

Data-type of returned array.

## Returns

out : ndarray
Contiguous array of same shape and content as $a$, with type dtype if specified.

## See Also:

asfortranarray
Convert input to an ndarray with column-major memory order.
require
Return an ndarray that satisfies requirements.
ndarray.flags
Information about the memory layout of the array.

## Examples

```
>>> x = np.arange(6).reshape (2,3)
>>> np.ascontiguousarray(x, dtype=np.float32)
array([[ 0., 1., 2.],
            [ 3., 4., 5.]], dtype=float32)
>>> x.flags['C_CONTIGUOUS']
True
```

numpy.asmatrix (data, dtype=None)

Interpret the input as a matrix.
Unlike matrix, asmatrix does not make a copy if the input is already a matrix or an ndarray. Equivalent to matrix(data, copy=False).

## Parameters

data : array_like
Input data.

## Returns

mat : matrix
data interpreted as a matrix.

## Examples

```
>>> x = np.array([[1, 2], [3, 4]])
>>> m = np.asmatrix(x)
>>> x[0,0] = 5
```

```
>>> m
matrix([[5, 2],
    [3, 4]])
```

numpy. copy (a)

Return an array copy of the given object.

## Parameters

a: array_like
Input data.

## Returns

arr : ndarray
Array interpretation of $a$.

## Notes

This is equivalent to

```
>>> np.array(a, copy=True)
```


## Examples

Create an array x , with a reference y and a copy z :

```
>>> x = np.array([1, 2, 3])
>>> y = x
>>> z = np.copy(x)
```

Note that, when we modify $\mathrm{x}, \mathrm{y}$ changes, but not z :

```
>>> x[0] = 10
>>> x[0] == y[0]
True
>>> x[0] == z[0]
False
```

numpy . frombuffer (buffer, dtype=float, count $=-1$, offset=0)
Interpret a buffer as a 1-dimensional array.

## Parameters

buffer : buffer_like
An object that exposes the buffer interface.
dtype : data-type, optional
Data-type of the returned array; default: float.
count : int, optional
Number of items to read. -1 means all data in the buffer.
offset : int, optional
Start reading the buffer from this offset; default: 0 .

## Notes

If the buffer has data that is not in machine byte-order, this should be specified as part of the data-type, e.g.:

```
>>> dt = np.dtype(int)
>>> dt = dt.newbyteorder('>')
>>> np.frombuffer(buf, dtype=dt)
```

The data of the resulting array will not be byteswapped, but will be interpreted correctly.

## Examples

```
>>> s = 'hello world'
>>> np.frombuffer(s, dtype='S1', count=5, offset=6)
array(['w', 'o', 'r', 'l', 'd'],
    dtype='|S1')
```

numpy.fromfile (file, dtype=float, count=-1, sep=' ')

Construct an array from data in a text or binary file.
A highly efficient way of reading binary data with a known data-type, as well as parsing simply formatted text files. Data written using the tofile method can be read using this function.

## Parameters

file : file or str
Open file object or filename.
dtype : data-type
Data type of the returned array. For binary files, it is used to determine the size and byte-order of the items in the file.
count : int
Number of items to read. -1 means all items (i.e., the complete file).
sep : str
Separator between items if file is a text file. Empty ("") separator means the file should be treated as binary. Spaces ("") in the separator match zero or more whitespace characters. A separator consisting only of spaces must match at least one whitespace.

## See Also:

```
load, save, ndarray.tofile
```

loadtxt
More flexible way of loading data from a text file.

## Notes

Do not rely on the combination of tofile and fromfile for data storage, as the binary files generated are are not platform independent. In particular, no byte-order or data-type information is saved. Data can be stored in the platform independent . npy format using save and load instead.

## Examples

Construct an ndarray:

```
>>> dt = np.dtype([('time', [('min', int), ('sec', int)]),
... ('temp', float)])
>>> x = np.zeros((1,), dtype=dt)
>>> x['time']['min'] = 10; x['temp'] = 98.25
>>> x
array([((10, 0), 98.25)],
    dtype=[('time', [('min', '<i4'), ('sec', '<i4')]), ('temp', '<f8')])
```

Save the raw data to disk:

```
>>> import os
>>> fname = os.tmpnam()
>>> x.tofile(fname)
```

Read the raw data from disk:

```
>>> np.fromfile(fname, dtype=dt)
array([((10, 0), 98.25)],
    dtype=[('time', [('min', '<i4'), ('sec', '<i4')]), ('temp', '<f8')])
```

The recommended way to store and load data:

```
>>> np.save(fname, x)
>>> np.load(fname + '.npy')
array([((10, 0), 98.25)],
    dtype=[('time', [('min', '<i4'), ('sec', '<i4')]), ('temp', '<f8')])
```

numpy.fromfunction (function, shape, **kwargs)
Construct an array by executing a function over each coordinate.
The resulting array therefore has a value $f n(x, y, z)$ at coordinate $(x, y, z)$.

## Parameters

function : callable
The function is called with N parameters, each of which represents the coordinates of the array varying along a specific axis. For example, if shape were $(2,2)$, then the parameters would be two arrays, $[[0,0],[1,1]]$ and $[[0,1],[0,1]]$. function must be capable of operating on arrays, and should return a scalar value.
shape : ( N, ) tuple of ints
Shape of the output array, which also determines the shape of the coordinate arrays passed to function.
dtype : data-type, optional
Data-type of the coordinate arrays passed to function. By default, dtype is float.

## Returns

out : any
The result of the call to function is passed back directly. Therefore the type and shape of out is completely determined by function.

See Also:

```
indices,meshgrid
```


## Notes

Keywords other than shape and dtype are passed to function.

## Examples

```
>>> np.fromfunction(lambda i, j: i == j, (3, 3), dtype=int)
array([[ True, False, False],
    [False, True, False],
    [False, False, True]], dtype=bool)
```

```
>>> np.fromfunction(lambda i, j: i + j, (3, 3), dtype=int)
array([[0, 1, 2],
    [1, 2, 3],
    [2, 3, 4]])
```

numpy.fromiter (iterable, dtype, count=-1)

Create a new 1-dimensional array from an iterable object.

## Parameters

iterable : iterable object
An iterable object providing data for the array.
dtype : data-type
The data-type of the returned array.
count : int, optional
The number of items to read from iterable. The default is -1 , which means all data is read.

## Returns

out : ndarray
The output array.

## Notes

Specify count to improve performance. It allows fromiter to pre-allocate the output array, instead of resizing it on demand.

## Examples

```
>>> iterable = (x*x for x in range(5))
>>> np.fromiter(iterable, np.float)
array([ 0., 1., 4., 9., 16.])
```

numpy.fromstring (string, dtype=float, count=-1, sep='")
A new 1-D array initialized from raw binary or text data in a string.

## Parameters

string : str
A string containing the data.
dtype : data-type, optional
The data type of the array; default: float. For binary input data, the data must be in exactly this format.
count : int, optional
Read this number of dtype elements from the data. If this is negative (the default), the count will be determined from the length of the data.
sep : str, optional
If not provided or, equivalently, the empty string, the data will be interpreted as binary data; otherwise, as ASCII text with decimal numbers. Also in this latter case, this argument is interpreted as the string separating numbers in the data; extra whitespace between elements is also ignored.

## Returns

arr : ndarray
The constructed array.

## Raises

## ValueError :

If the string is not the correct size to satisfy the requested dtype and count.

## See Also:

```
frombuffer,fromfile, fromiter
```


## Examples

```
>>> np.fromstring('\x01\x02', dtype=np.uint8)
array([1, 2], dtype=uint8)
>>> np.fromstring('1 2', dtype=int, sep=' ')
array([1, 2])
>>> np.fromstring('1, 2', dtype=int, sep=',')
array([1, 2])
>>> np.fromstring('\x01\x02\x03\x04\x05', dtype=np.uint8, count=3)
array([1, 2, 3], dtype=uint8)
```

numpy.loadtxt (fname, dtype=<type 'float'>, comments='\#', delimiter=None, converters=None, skiprows $=0$, usecols $=$ None, unpack $=$ False, , $d$ min $=0$ )
Load data from a text file.
Each row in the text file must have the same number of values.

## Parameters

fname : file or str
File, filename, or generator to read. If the filename extension is.$g z$ or .bz2, the file is first decompressed. Note that generators should return byte strings for Python 3 k .
dtype : data-type, optional
Data-type of the resulting array; default: float. If this is a record data-type, the resulting array will be 1 -dimensional, and each row will be interpreted as an element of the array. In this case, the number of columns used must match the number of fields in the datatype.
comments : str, optional
The character used to indicate the start of a comment; default: '\#'.
delimiter : str, optional
The string used to separate values. By default, this is any whitespace.
converters : dict, optional
A dictionary mapping column number to a function that will convert that column to a float. E.g., if column 0 is a date string: converters $=\{0$ : datestr2num $\}$. Converters can also be used to provide a default value for missing data (but see also genfromtxt): converters $=\{3:$ lambda s: float(s.strip() or 0) \}. Default: None.
skiprows: int, optional
Skip the first skiprows lines; default: 0 .
usecols : sequence, optional

Which columns to read, with 0 being the first. For example, usecols $=(1,4,5)$ will extract the 2 nd, 5th and 6 th columns. The default, None, results in all columns being read.
unpack : bool, optional
If True, the returned array is transposed, so that arguments may be unpacked using x , y, $z=$ loadtxt (...). When used with a record data-type, arrays are returned for each field. Default is False.
ndmin : int, optional
The returned array must have at least $n d \min$ dimensions. Legal values: 0 (default), 1 or 2. .. versionadded:: 1.6.0

## Returns

out : ndarray
Data read from the text file.

## See Also:

```
load, fromstring, fromregex
```

genfromtxt

Load data with missing values handled as specified.
scipy.io.loadmat
reads MATLAB data files

## Notes

This function aims to be a fast reader for simply formatted files. The genfromtxt function provides more sophisticated handling of, e.g., lines with missing values.

## Examples

```
>>> from StringIO import StringIO # StringIO behaves like a file object
>>> c = StringIO("0 1\n2 3")
>>> np.loadtxt(c)
array([[ 0., 1.],
    [ 2., 3.]])
>>> d = StringIO("M 21 72\nF 35 58")
>>> np.loadtxt(d, dtype={'names': ('gender', 'age', 'weight'),
... 'formats': ('S1', 'i4', 'f4')})
array([('M', 21, 72.0), ('F', 35, 58.0)],
    dtype=[('gender', '|S1'), ('age', '<i4'), ('weight', '<f4')])
>>> c = StringIO("1,0,2\n3,0,4")
>>> x, y = np.loadtxt(c, delimiter=',', usecols=(0, 2), unpack=True)
>>> x
array([ 1., 3.])
>>> y
array([ 2., 4.])
```


### 3.1.3 Creating record arrays (numpy .rec)

Note: numpy.rec is the preferred alias for numpy.core.records.

```
core.records.array(obj[, dtype, shape, ...]
core.records.fromarrays(arrayList[, dtype,
...])
core.records.fromrecords(recList[, dtype,
...])
core.records.fromstring(datastring[, dtype,
...])
core.records.fromfile(fd[, dtype, shape,
...])
core.records.fromarrays(arrayList[, dtype, ...])
core.records.fromrecords(recList[, dtype, ...])
core.records.fromstring(datastring[, dtype, ...])
core.records.fromfile(fd[, dtype, shape, ...])
```

Construct a record array from a wide-variety of objects. create a record array from a (flat) list of arrays create a recarray from a list of records in text form create a (read-only) record array from binary data contained in
Create an array from binary file data
numpy.core.records.array (obj, dtype $=$ None, shape $=$ None, offset $=0$, strides $=$ None, formats $=$ None, names $=$ None, titles $=$ None, aligned $=$ False, byteorder $=$ None, copy=True) Construct a record array from a wide-variety of objects.
numpy. core.records.fromarrays (arrayList, dtype=None, shape=None, formats=None, names $=$ None, titles $=$ None, aligned $=$ False, byteorder $=$ None )
create a record array from a (flat) list of arrays

```
>>> x1=np.array([1,2,3,4])
>>> x2=np.array(['a','dd','xyz','12'])
>>> x3=np.array([1.1,2,3,4])
>>> r = np.core.records.fromarrays([x1,x2,x3],names=' a,b,c')
>>> print r[1]
(2, 'dd', 2.0)
>>> x1[1]=34
>>> r.a
array([1, 2, 3, 4])
```

numpy.core.records.fromrecords (recList, dtype=None, shape=None, formats=None, names $=$ None, titles $=$ None, aligned $=$ False, byteorder $=$ None )
create a recarray from a list of records in text form
The data in the same field can be heterogeneous, they will be promoted to the highest data type. This method is intended for creating smaller record arrays. If used to create large array without formats defined
$\mathrm{r}=$ fromrecords([(2,3.,'abc') $\left.]^{*} 100000\right)$
it can be slow.
If formats is None, then this will auto-detect formats. Use list of tuples rather than list of lists for faster processing.

```
>>> r=np.core.records.fromrecords([(456,'dbe',1.2),(2,'de',1.3)],
... names=' col1,col2,col3')
>>> print r[0]
(456, 'dbe', 1.2)
>>> r.col1
array([456, 2])
>>> r.col2
chararray(['dbe', 'de'],
            dtype='|S3')
>>> import cPickle
>>> print cPickle.loads(cPickle.dumps(r))
[(456, 'dbe', 1.2) (2, 'de', 1.3)]
```

numpy.core.records.fromstring (datastring, dtype $=$ None, shape $=$ None, offset $=$, , formats $=$ None, names=None, titles=None, aligned=False, byteorder=None)
create a (read-only) record array from binary data contained in a string
numpy.core.records.fromfile (fd, dtype=None, shape=None, offset=0, formats=None, names $=$ None, titles $=$ None, aligned $=$ False, byteorder=None)
Create an array from binary file data
If file is a string then that file is opened, else it is assumed to be a file object.

```
>>> from tempfile import TemporaryFile
>>> a = np.empty(10,dtype='f8,i4,a5')
>>> a[5] = (0.5,10,' abcde')
>>>
>>> fd=TemporaryFile()
>>> a = a.newbyteorder('<')
>>> a.tofile(fd)
>>>
>>> fd.seek(0)
>>> r=np.core.records.fromfile(fd, formats='f8,i4,a5', shape=10,
... byteorder='<')
>>> print r[5]
(0.5, 10, 'abcde')
>>> r.shape
(10,)
```


### 3.1.4 Creating character arrays (numpy . char)

Note: numpy.char is the preferred alias for numpy.core.defchararray.
core.defchararray.array(obj[, itemsize, Create a chararray.
...])
core.defchararray. asarray(obj[, Convert the input to a chararray, copying the data only if
itemsize, ...]) necessary.
numpy. core.defchararray. array (obj, itemsize $=$ None, copy $=$ True, unicode $=$ None, order $=$ None )
Create a chararray.
Note: This class is provided for numarray backward-compatibility. New code (not concerned with numarray compatibility) should use arrays of type string_ or unicode_ and use the free functions in numpy. char for fast vectorized string operations instead.

Versus a regular Numpy array of type str or unicode, this class adds the following functionality:
1.values automatically have whitespace removed from the end when indexed
2.comparison operators automatically remove whitespace from the end when comparing values
3.vectorized string operations are provided as methods (e.g. str.endswith) and infix operators (e.g. + , *, \%)

## Parameters

obj : array of str or unicode-like
itemsize : int, optional
itemsize is the number of characters per scalar in the resulting array. If itemsize is None, and obj is an object array or a Python list, the itemsize will be automatically determined. If itemsize is provided and obj is of type str or unicode, then the obj string will be chunked into itemsize pieces.
copy : bool, optional

If true (default), then the object is copied. Otherwise, a copy will only be made if
$\qquad$ _ returns a copy, if obj is a nested sequence, or if a copy is needed to satisfy any of the other requirements (itemsize, unicode, order, etc.).
unicode : bool, optional
When true, the resulting chararray can contain Unicode characters, when false only 8 -bit characters. If unicode is None and obj is one of the following:

- a chararray,
- an ndarray of type str or unicode
- a Python str or unicode object,
then the unicode setting of the output array will be automatically determined.
order : \{ ' $C$ ', ' $F$ ', 'A' $\}$, optional
Specify the order of the array. If order is ' $C$ ' (default), then the array will be in $C$ contiguous order (last-index varies the fastest). If order is ' F ', then the returned array will be in Fortran-contiguous order (first-index varies the fastest). If order is ' A ', then the returned array may be in any order (either C-, Fortran-contiguous, or even discontiguous).
numpy.core.defchararray.asarray (obj, itemsize $=$ None, unicode $=$ None, order $=$ None)
Convert the input to a chararray, copying the data only if necessary.
Versus a regular Numpy array of type str or unicode, this class adds the following functionality:
1.values automatically have whitespace removed from the end when indexed
2.comparison operators automatically remove whitespace from the end when comparing values
3.vectorized string operations are provided as methods (e.g. str.endswith) and infix operators (e.g. +, *, \%)


## Parameters

obj : array of str or unicode-like
itemsize : int, optional
itemsize is the number of characters per scalar in the resulting array. If itemsize is None, and obj is an object array or a Python list, the itemsize will be automatically determined. If itemsize is provided and obj is of type str or unicode, then the obj string will be chunked into itemsize pieces.
unicode : bool, optional
When true, the resulting chararray can contain Unicode characters, when false only 8 -bit characters. If unicode is None and obj is one of the following:

- a chararray,
- an ndarray of type str or 'unicode'
- a Python str or unicode object,
then the unicode setting of the output array will be automatically determined.
order : \{ 'C', 'F'\}, optional
Specify the order of the array. If order is ' C ' (default), then the array will be in C contiguous order (last-index varies the fastest). If order is ' F ', then the returned array will be in Fortran-contiguous order (first-index varies the fastest).


### 3.1.5 Numerical ranges

```
arange([dtype])
linspace(start, stop[, num, endpoint,
retstep])
logspace(start, stop[, num, endpoint,
base])
meshgrid(x,y) Return coordinate matrices from two coordinate vectors.
mgrid nd_grid instance which returns a dense multi-dimensional
ogrid
Return evenly spaced values within a given interval.
Return evenly spaced numbers over a specified interval.
Return numbers spaced evenly on a log scale.
Return coordinate matrices from two coordinate vectors.
nd_grid instance which returns a dense multi-dimensional "meshgrid".
\(n d \_\)grid instance which returns an open multi-dimensional "meshgrid".
```

numpy . arange ([start $]$, stop $[$, step $]$, dtype $=$ None )
Return evenly spaced values within a given interval.
Values are generated within the half-open interval [start, stop) (in other words, the interval including start but excluding stop). For integer arguments the function is equivalent to the Python built-in range function, but returns a ndarray rather than a list.

When using a non-integer step, such as 0.1 , the results will often not be consistent. It is better to use linspace for these cases.

## Parameters

start : number, optional
Start of interval. The interval includes this value. The default start value is 0 .
stop : number
End of interval. The interval does not include this value, except in some cases where step is not an integer and floating point round-off affects the length of out.
step : number, optional
Spacing between values. For any output out, this is the distance between two adjacent values, out [i+1] - out [i]. The default step size is 1. If step is specified, start must also be given.
dtype : dtype
The type of the output array. If dtype is not given, infer the data type from the other input arguments.

## Returns

out : ndarray
Array of evenly spaced values.
For floating point arguments, the length of the result is ceil((stop start)/step). Because of floating point overflow, this rule may result in the last element of out being greater than stop.

## See Also:

linspace
Evenly spaced numbers with careful handling of endpoints.
ogrid
Arrays of evenly spaced numbers in N -dimensions
mgrid
Grid-shaped arrays of evenly spaced numbers in N -dimensions

## Examples

```
>>> np.arange(3)
array([0, 1, 2])
>>> np.arange(3.0)
array([ 0., 1., 2.])
>>> np.arange (3,7)
array([3, 4, 5, 6])
>>> np.arange (3,7,2)
array([3, 5])
```

numpy. linspace (start, stop, num=50, endpoint=True, retstep $=$ False)
Return evenly spaced numbers over a specified interval.
Returns num evenly spaced samples, calculated over the interval [start, stop].
The endpoint of the interval can optionally be excluded.

## Parameters

start : scalar
The starting value of the sequence.
stop : scalar
The end value of the sequence, unless endpoint is set to False. In that case, the sequence consists of all but the last of num +1 evenly spaced samples, so that stop is excluded. Note that the step size changes when endpoint is False.
num : int, optional
Number of samples to generate. Default is 50.
endpoint : bool, optional
If True, stop is the last sample. Otherwise, it is not included. Default is True.
retstep : bool, optional
If True, return (samples, step), where step is the spacing between samples.

## Returns

samples : ndarray
There are num equally spaced samples in the closed interval [start, stop] or the half-open interval [start, stop) (depending on whether endpoint is True or False).
step : float (only if retstep is True)
Size of spacing between samples.

## See Also:

arange
Similiar to linspace, but uses a step size (instead of the number of samples).
logspace
Samples uniformly distributed in log space.

## Examples

```
>>> np.linspace(2.0, 3.0, num=5)
    array([ 2. , 2.25, 2.5 , 2.75, 3. ])
>>> np.linspace(2.0, 3.0, num=5, endpoint=False)
    array([ 2. , 2.2, 2.4, 2.6, 2.8])
>>> np.linspace(2.0, 3.0, num=5, retstep=True)
    (array([ 2. , 2.25, 2.5, 2.75, 3. ]), 0.25)
```

Graphical illustration:

```
>>> import matplotlib.pyplot as plt
>>> N = 8
>>> y = np.zeros(N)
>>> x1 = np.linspace(0, 10, N, endpoint=True)
>>> x2 = np.linspace(0, 10, N, endpoint=False)
>>> plt.plot(x1, y, 'o')
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.plot(x2, y + 0.5, 'o')
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.ylim([-0.5, 1])
(-0.5, 1)
>>> plt.show()
```


numpy.logspace (start, stop, num=50, endpoint=True, base=10.0)
Return numbers spaced evenly on a log scale.
In linear space, the sequence starts at base ** start (base to the power of start) and ends with base ** stop (see endpoint below).

## Parameters

start : float
base ** start is the starting value of the sequence.
stop : float
base ** stop is the final value of the sequence, unless endpoint is False. In that case, num +1 values are spaced over the interval in log-space, of which all but the last (a sequence of length num) are returned.
num : integer, optional
Number of samples to generate. Default is 50 .
endpoint : boolean, optional
If true, stop is the last sample. Otherwise, it is not included. Default is True.
base : float, optional
The base of the log space. The step size between the elements in $\ln$ (samples) / ln (base) (or log_base (samples) ) is uniform. Default is 10.0.

## Returns

samples : ndarray num samples, equally spaced on a log scale.

## See Also:

## arange

Similiar to linspace, with the step size specified instead of the number of samples. Note that, when used with a float endpoint, the endpoint may or may not be included.

## linspace

Similar to logspace, but with the samples uniformly distributed in linear space, instead of log space.

## Notes

Logspace is equivalent to the code

```
>>> y = np.linspace(start, stop, num=num, endpoint=endpoint)
>>> power(base, y)
..
```


## Examples

```
>>> np.logspace(2.0, 3.0, num=4)
    array([ 100. , 215.443469 , 464.15888336, 1000. ])
>>> np.logspace(2.0, 3.0, num=4, endpoint=False)
    array([ 100. , 177.827941 , 316.22776602, 562.34132519])
>>> np.logspace(2.0, 3.0, num=4, base=2.0)
    array([ 4. , 5.0396842 , 6.34960421, 8. ])
```

Graphical illustration:

```
>>> import matplotlib.pyplot as plt
>>> N = 10
>>> x1 = np.logspace(0.1, 1, N, endpoint=True)
>>> x2 = np.logspace(0.1, 1, N, endpoint=False)
>>> y = np.zeros(N)
>>> plt.plot(x1, y, 'o')
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.plot(x2, y + 0.5, 'o')
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.ylim([-0.5, 1])
(-0.5, 1)
>>> plt.show()
```


numpy.meshgrid ( $x, y$ )
Return coordinate matrices from two coordinate vectors.

## Parameters

$\mathbf{x}, \mathbf{y}$ : ndarray
Two 1-D arrays representing the x and y coordinates of a grid.

## Returns

$\mathbf{X}, \mathbf{Y}$ : ndarray
For vectors $x, y$ with lengths $\mathrm{Nx}=\mathrm{len}(\mathrm{x})$ and $\mathrm{Ny}=1 \mathrm{len}(\mathrm{y})$, return $X, Y$ where $X$ and $Y$ are ( $\mathrm{Ny}, \mathrm{Nx}$ ) shaped arrays with the elements of $x$ and y repeated to fill the matrix along the first dimension for $x$, the second for $y$.

## See Also:

## index_tricks.mgrid

Construct a multi-dimensional "meshgrid" using indexing notation.

## index_tricks.ogrid

Construct an open multi-dimensional "meshgrid" using indexing notation.

## Examples

```
>>> X, Y = np.meshgrid([1,2,3], [4,5,6,7])
>>> X
array([[1, 2, 3],
    [1, 2, 3],
    [1, 2, 3],
    [1, 2, 3]])
>>> Y
array([[4, 4, 4],
    [5, 5, 5],
    [6, 6, 6],
    [7, 7, 7]])
```

meshgrid is very useful to evaluate functions on a grid.

```
>>> x = np.arange(-5, 5, 0.1)
>>> y = np.arange(-5, 5, 0.1)
>>> xx, yy = np.meshgrid(x, y)
>>> z = np.sin(xx**2+yy**2)/(xx**2+yy**2)
```

numpy.mgrid
$n d \_g r i d$ instance which returns a dense multi-dimensional "meshgrid".

An instance of numpy.lib.index_tricks.nd_grid which returns an dense (or fleshed out) mesh-grid when indexed, so that each returned argument has the same shape. The dimensions and number of the output arrays are equal to the number of indexing dimensions. If the step length is not a complex number, then the stop is not inclusive.

However, if the step length is a complex number (e.g. 5j), then the integer part of its magnitude is interpreted as specifying the number of points to create between the start and stop values, where the stop value is inclusive.

## Returns

mesh-grid 'ndarrays' all of the same dimensions :

## See Also:

numpy.lib.index_tricks.nd_grid
class of ogrid and mgrid objects
ogrid
like mgrid but returns open (not fleshed out) mesh grids
$r_{-}$
array concatenator

## Examples

```
>>> np.mgrid[0:5,0:5]
array([[[0, 0, 0, 0, 0],
            [1, 1, 1, 1, 1],
            [2, 2, 2, 2, 2],
            [3, 3, 3, 3, 3],
            [4, 4, 4, 4, 4]],
            [[0, 1, 2, 3, 4],
                    [0, 1, 2, 3, 4],
                    [0, 1, 2, 3, 4],
                    [0, 1, 2, 3, 4],
            [0, 1, 2, 3, 4]]])
        >>> np.mgrid[-1:1:5j]
        array([-1. , -0.5, 0. , 0.5, 1. ])
```


## numpy.ogrid

$n d \_$grid instance which returns an open multi-dimensional "meshgrid".
An instance of numpy.lib.index_tricks.nd_grid which returns an open (i.e. not fleshed out) meshgrid when indexed, so that only one dimension of each returned array is greater than 1 . The dimension and number of the output arrays are equal to the number of indexing dimensions. If the step length is not a complex number, then the stop is not inclusive.

However, if the step length is a complex number (e.g. 5j), then the integer part of its magnitude is interpreted as specifying the number of points to create between the start and stop values, where the stop value is inclusive.

## Returns <br> mesh-grid 'ndarrays' with only one dimension :math:'neq 1' :

## See Also:

```
np.lib.index_tricks.nd_grid
    class of ogrid and mgrid objects
mgrid
    like ogrid but returns dense (or fleshed out) mesh grids
r_
    array concatenator
```


## Examples

```
>>> from numpy import ogrid
```

>>> ogrid[-1:1:5j]
array ([-1. , -0.5, 0. , 0.5, 1. ])
>>> ogrid[0:5,0:5]
[array([[0],
[1],
[2],
[3],
[4]]), $\operatorname{array}([[0,1,2,3,4]])]$

### 3.1.6 Building matrices

| $\operatorname{diag}(\mathrm{v}[, \mathrm{k}])$ | Extract a diagonal or construct a diagonal array. |
| :--- | :--- |
| $\operatorname{diagflat}(\mathrm{v}[, \mathrm{k}])$ | Create a two-dimensional array with the flattened input as a diagonal. |
| $\operatorname{tri}(\mathrm{N}[, \mathrm{M}, \mathrm{k}, \mathrm{dtype}])$ | An array with ones at and below the given diagonal and zeros elsewhere. |
| $\operatorname{tril}(\mathrm{m}[, \mathrm{k}])$ | Lower triangle of an array. |
| $\operatorname{triu}(\mathrm{m}[, \mathrm{k}])$ | Upper triangle of an array. |
| $\operatorname{vander}(\mathrm{x}[, \mathrm{N}])$ | Generate a Van der Monde matrix. |

## numpy.diag ( $v, k=0$ )

Extract a diagonal or construct a diagonal array

## Parameters

$\mathbf{v}$ : array_like
If $v$ is a 2-D array, return a copy of its $k$-th diagonal. If $v$ is a 1-D array, return a 2-D array with $v$ on the $k$-th diagonal.
k: int, optional
Diagonal in question. The default is 0 . Use $k>0$ for diagonals above the main diagonal, and $k<0$ for diagonals below the main diagonal.

## Returns

out : ndarray
The extracted diagonal or constructed diagonal array.

## See Also:

diagonal
Return specified diagonals.
diagflat
Create a 2-D array with the flattened input as a diagonal.
trace
Sum along diagonals.

```
triu
    Upper triangle of an array.
tril
    Lower triange of an array.
Examples
```

```
>>> x = np.arange (9).reshape((3,3))
>>> x
array([[0, 1, 2],
[3, 4, 5],
[6, 7, 8]])
```

>>> np.diag(x)
array([0, 4, 8])
>>> np.diag(x, k=1)
array ([1, 5])
>>> np.diag(x, k=-1)
array ([3, 7])
>>> np.diag(np.diag(x))
array([[0, 0, 0],
$[0,4,0]$,
[0, 0, 8]])
numpy.diagflat ( $v, k=0$ )

Create a two-dimensional array with the flattened input as a diagonal.

## Parameters

$\mathbf{v}$ : array_like
Input data, which is flattened and set as the $k$-th diagonal of the output.
$\mathbf{k}$ : int, optional
Diagonal to set; 0 , the default, corresponds to the "main" diagonal, a positive (negative) $k$ giving the number of the diagonal above (below) the main.

## Returns

out : ndarray
The 2-D output array.

## See Also:

diag
MATLAB work-alike for 1-D and 2-D arrays.
diagonal
Return specified diagonals.

## trace

Sum along diagonals.

## Examples

```
>>> np.diagflat([[1,2], [3,4]])
array([[1, 0, 0, 0],
    [0, 2, 0, 0],
```

$[0,0,3,0]$,
$[0,0,0,4]])$

```
>>> np.diagflat([1,2], 1)
array([[0, 1, 0],
    [0, 0, 2],
    [0, 0, 0]])
```

numpy.tri ( $N, M=$ None, $k=0$, dtype=<type 'float'>)
An array with ones at and below the given diagonal and zeros elsewhere.

## Parameters

$\mathbf{N}$ : int
Number of rows in the array.
M : int, optional
Number of columns in the array. By default, $M$ is taken equal to $N$.
k: int, optional
The sub-diagonal at and below which the array is filled. $k=0$ is the main diagonal, while $k<0$ is below it, and $k>0$ is above. The default is 0 .
dtype : dtype, optional
Data type of the returned array. The default is float.

## Returns

$\mathbf{T}$ : ndarray of shape ( $\mathrm{N}, \mathrm{M}$ )
Array with its lower triangle filled with ones and zero elsewhere; in other words $\mathrm{T}[\mathrm{i}, \mathrm{j}]==1$ for $i<=j+\mathrm{k}, 0$ otherwise.

## Examples

```
>>> np.tri(3, 5, 2, dtype=int)
array([[1, 1, 1, 0, 0],
                    [1, 1, 1, 1, 0],
            [1, 1, 1, 1, 1]])
>>> np.tri(3, 5, -1)
array([[ 0., 0., 0., 0., 0.],
    [ 1., 0., 0., 0., 0.],
    [ 1., 1., 0., 0., 0.]])
```

numpy.tril ( $m, k=0$ )

Lower triangle of an array.
Return a copy of an array with elements above the $k$-th diagonal zeroed.

## Parameters

$\mathbf{m}$ : array_like, shape ( $\mathrm{M}, \mathrm{N}$ )
Input array.
$\mathbf{k}$ : int, optional
Diagonal above which to zero elements. $k=0$ (the default) is the main diagonal, $k<0$ is below it and $k>0$ is above.

## Returns

$\mathbf{L}$ : ndarray, shape ( $\mathrm{M}, \mathrm{N}$ )

Lower triangle of $m$, of same shape and data-type as $m$.

## See Also:

triu
same thing, only for the upper triangle

## Examples

```
>> np.tril([[1,2,3],[4,5,6],[7,8,9],[10,11,12]], -1)
array([[ 0, 0, 0],
    [4, 0, 0],
    [7, 8, 0],
    [10, 11, 12]])
```

numpy.triu ( $m, k=0$ )
Upper triangle of an array.
Return a copy of a matrix with the elements below the $k$-th diagonal zeroed.
Please refer to the documentation for tril for further details.

## See Also:

tril
lower triangle of an array

## Examples

```
>>> np.triu([[1,2,3],[4,5,6],[7,8,9],[10,11,12]], -1)
array([[ 1, 2, 3],
    [4, 5, 6],
    [ 0, 8, 9],
    [ 0, 0, 12]])
```

numpy . vander ( $x, N=N o n e$ )
Generate a Van der Monde matrix.
The columns of the output matrix are decreasing powers of the input vector. Specifically, the $i$-th output column is the input vector raised element-wise to the power of $\mathrm{N}-\mathrm{i}-1$. Such a matrix with a geometric progression in each row is named for Alexandre-Theophile Vandermonde.

## Parameters

$\mathbf{x}$ : array_like
1-D input array.
$\mathbf{N}$ : int, optional
Order of (number of columns in) the output. If $N$ is not specified, a square array is returned ( $\mathrm{N}=\operatorname{len}(\mathrm{x})$ ).

## Returns

out : ndarray
Van der Monde matrix of order $N$. The first column is $x^{\wedge}(N-1)$, the second $x^{\wedge}(N-2)$ and so forth.

## Examples

```
>>> x = np.array([1, 2, 3, 5])
>>> N = 3
>>> np.vander(x, N)
array([[ 1, 1, 1],
    [ 4, 2, 1],
    [ 9, 3, 1],
    [25, 5, 1]])
>>> np.column_stack([x**(N-1-i) for i in range(N)])
array([[ 1, 1, 1],
    [ 4, 2, 1],
    [ 9, 3, 1],
    [25, 5, 1]])
>>> x = np.array([1, 2, 3, 5])
>>> np.vander(x)
array([[ 1, 1, 1, 1],
    [ 8, 4, 2, 1],
    [ 27, 9, 3, 1],
    [125, 25, 5, 1]])
```

The determinant of a square Vandermonde matrix is the product of the differences between the values of the input vector:

```
>>> np.linalg.det(np.vander(x))
48.000000000000043
>>> (5-3)*(5-2)*(5-1)*(3-2)*(3-1)*(2-1)
48
```


### 3.1.7 The Matrix class

| mat(data[, dtype]) | Interpret the input as a matrix. |
| :--- | :--- |
| bmat(obj[, ldict, gdict]) | Build a matrix object from a string, nested sequence, or array. |

numpy .mat (data, dtype=None)
Interpret the input as a matrix.
Unlike matrix, asmatrix does not make a copy if the input is already a matrix or an ndarray. Equivalent to matrix(data, copy=False).

## Parameters

## data : array_like

Input data.

## Returns

## mat : matrix

 data interpreted as a matrix.
## Examples

```
>>> x = np.array([[1, 2], [3, 4]])
>>> m = np.asmatrix(x)
>>> x[0,0] = 5
```

>>> m
matrix([[5, 2],

$$
[3,4]])
$$

numpy .bmat (obj, ldict=None, gdict=None)
Build a matrix object from a string, nested sequence, or array.

## Parameters

obj : str or array_like
Input data. Names of variables in the current scope may be referenced, even if obj is a string.

## Returns

out : matrix
Returns a matrix object, which is a specialized 2-D array.

## See Also:

matrix

## Examples

```
>>> A = np.mat('1 1; 1 1')
>>> B = np.mat('2 2; 2 2')
>>> C = np.mat('3 4; 5 6')
>>> D = np.mat('7 8; 9 0')
```

All the following expressions construct the same block matrix:

```
>>> np.bmat([[A, B], [C, D]])
matrix([[1, 1, 2, 2],
    [1, 1, 2, 2],
    [3, 4, 7, 8],
    [5, 6, 9, 0]])
>>> np.bmat(np.r_[np.c_[A, B], np.c_[C, D]])
matrix([[1, 1, 2, 2],
    [1, 1, 2, 2],
    [3, 4, 7, 8],
    [5, 6, 9, 0]])
>>> np.bmat('A,B; C,D')
matrix([[1, 1, 2, 2],
    [1, 1, 2, 2],
    [3, 4, 7, 8],
    [5, 6, 9, 0]])
```


### 3.2 Array manipulation routines

### 3.2.1 Changing array shape

```
reshape(a, newshape[, order]) Gives a new shape to an array without changing its data.
ravel(a[, order]) Return a flattened array.
ndarray.flat A 1-D iterator over the array.
ndarray.flatten([order]) Return a copy of the array collapsed into one dimension.
numpy. reshape ( \(a\), newshape, order \(=\) ' \(C\) ')
```

Gives a new shape to an array without changing its data.

## Parameters

a : array_like
Array to be reshaped.
newshape : int or tuple of ints
The new shape should be compatible with the original shape. If an integer, then the result will be a 1-D array of that length. One shape dimension can be -1 . In this case, the value is inferred from the length of the array and remaining dimensions.
order : \{ 'C', 'F', 'A'\}, optional
Determines whether the array data should be viewed as in C (row-major) order, FORTRAN (column-major) order, or the C/FORTRAN order should be preserved.

## Returns

reshaped_array : ndarray
This will be a new view object if possible; otherwise, it will be a copy.

## See Also:

```
ndarray.reshape
```

Equivalent method.

## Notes

It is not always possible to change the shape of an array without copying the data. If you want an error to be raise if the data is copied, you should assign the new shape to the shape attribute of the array:

```
>>> a = np.zeros((10, 2))
# A transpose make the array non-contiguous
>>> b = a.T
# Taking a view makes it possible to modify the shape without modiying the
# initial object.
>>> c = b.view()
>>> c.shape = (20)
AttributeError: incompatible shape for a non-contiguous array
```


## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> np.reshape(a, 6)
array([1, 2, 3, 4, 5, 6])
>>> np.reshape(a, 6, order=' F')
array([1, 4, 2, 5, 3, 6])
>>> np.reshape(a, (3,-1)) # the unspecified value is inferred to be 2
array([[1, 2],
    [3, 4],
    [5, 6]])
```

numpy.ravel ( $a$, order=' $C^{\prime}$ )

Return a flattened array.
A 1-D array, containing the elements of the input, is returned. A copy is made only if needed.

## Parameters

a : array_like

Input array. The elements in a are read in the order specified by order, and packed as a 1-D array.
order : \{ 'C',' F ', ' A ', ' K ' $\}$, optional
The elements of a are read in this order. ' C ' means to view the elements in C (rowmajor) order. ' F ' means to view the elements in Fortran (column-major) order. ' A ' means to view the elements in ' F ' order if a is Fortran contiguous, ' C ' order otherwise. ' $K$ ' means to view the elements in the order they occur in memory, except for reversing the data when strides are negative. By default, ' C ' order is used.

## Returns

1d_array : ndarray
Output of the same dtype as $a$, and of shape (a.size(), ).

## See Also:

```
ndarray.flat
```

1-D iterator over an array.
ndarray.flatten
1-D array copy of the elements of an array in row-major order.

## Notes

In row-major order, the row index varies the slowest, and the column index the quickest. This can be generalized to multiple dimensions, where row-major order implies that the index along the first axis varies slowest, and the index along the last quickest. The opposite holds for Fortran-, or column-major, mode.

## Examples

It is equivalent to reshape ( -1 , order=order).

```
>>> x = np.array([[1, 2, 3], [4, 5, 6]])
>>> print np.ravel(x)
[1 2 3 4 5 6]
>>> print x.reshape(-1)
[1 2 3 4 5 6]
>>> print np.ravel(x, order='F')
[14 4 2 5 3 6
```

When order is ' A ', it will preserve the array's ' C ' or ' F ' ordering:

```
>>> print np.ravel(x.T)
[1 4 2 5 5 6]
>>> print np.ravel(x.T, order='A')
[1 2 3 4 5 6]
```

When order is ' $K$ ', it will preserve orderings that are neither ' $C$ ' nor ' $F$ ', but won't reverse axes:

```
>>> a = np.arange(3)[::-1]; a
array([2, 1, 0])
>>> a.ravel(order='C')
array([2, 1, 0])
>>> a.ravel(order='K')
array([2, 1, 0])
```

```
>>> a = np.arange(12).reshape(2,3,2).swapaxes(1,2); a
array([[[ 0, 2, 4],
            [ 1, 3, 5]],
    [[ 6, 8, 10],
    [ 7, 9, 11]]])
>>> a.ravel(order='C')
array([ 0, 2, 4, 1, 3, 5, 6, 8, 10, 7, 9, 11])
>>> a.ravel(order=' K')
array([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11])
```

ndarray.flat

A 1-D iterator over the array.
This is a numpy.flat iter instance, which acts similarly to, but is not a subclass of, Python's built-in iterator object.

## See Also:

## flatten

Return a copy of the array collapsed into one dimension.
flatiter

## Examples

```
>>> x = np.arange(1, 7).reshape(2, 3)
>>> x
array([[1, 2, 3],
                    [4, 5, 6]])
>>> x.flat[3]
4
>>> x.T
array([[1, 4],
                    [2, 5],
                    [3, 6]])
>>> x.T.flat[3]
5
>>> type(x.flat)
<type 'numpy.flatiter'>
```

An assignment example:

```
>>> x.flat = 3; x
array([[3, 3, 3],
    [3, 3, 3]])
>>> x.flat[[1,4]] = 1; x
array([[3, 1, 3],
    [3, 1, 3]])
```

ndarray. flatten (order=' $C^{\prime}$ )

Return a copy of the array collapsed into one dimension.

## Parameters

order : \{ 'C', 'F', 'A'\}, optional
Whether to flatten in C (row-major), Fortran (column-major) order, or preserve the $\mathrm{C} /$ Fortran ordering from $a$. The default is ' C '.

## Returns

y : ndarray

A copy of the input array, flattened to one dimension.

## See Also:

ravel
Return a flattened array.
flat
A 1-D flat iterator over the array.

## Examples

```
>>> a = np.array([[1,2], [3,4]])
>>> a.flatten()
array([1, 2, 3, 4])
>>> a.flatten('F')
array([1, 3, 2, 4])
```


### 3.2.2 Transpose-like operations

| rollaxis(a, axis[, start]) | Roll the specified axis backwards, until it lies in a given position. |
| :--- | :--- |
| swapaxes(a, axis1, axis2) | Interchange two axes of an array. |
| ndarray.T | Same as self.transpose(), except that self is returned if self.ndim < 2. |
| transpose(a[, axes]) | Permute the dimensions of an array. |

numpy.rollaxis (a, axis, start=0)

Roll the specified axis backwards, until it lies in a given position.

## Parameters

a : ndarray
Input array.
axis: int
The axis to roll backwards. The positions of the other axes do not change relative to one another.
start : int, optional
The axis is rolled until it lies before this position. The default, 0 , results in a "complete" roll.

## Returns

res: ndarray
Output array.

## See Also:

roll
Roll the elements of an array by a number of positions along a given axis.
Examples

```
>>> a = np.ones((3,4,5,6))
>>> np.rollaxis(a, 3, 1).shape
(3, 6, 4, 5)
>>> np.rollaxis(a, 2).shape
(5, 3, 4, 6)
```

```
>>> np.rollaxis(a, 1, 4).shape
```

$(3,5,6,4)$
numpy.swapaxes (a, axis1, axis2)
Interchange two axes of an array.

## Parameters

a : array_like
Input array.
axis1 : int
First axis.
axis2 : int
Second axis.

## Returns

a_swapped : ndarray
If $a$ is an ndarray, then a view of $a$ is returned; otherwise a new array is created.

## Examples

```
>>> x = np.array([[1,2,3]])
>>> np.swapaxes(x,0,1)
array([[1],
[2],
[3]])
>>> x = np.array([[[0,1],[2,3]],[[4,5],[6,7]]])
>>> x
array([[[0, 1],
    [2, 3]],
    [[4, 5],
            [6, 7]]])
>>> np.swapaxes(x,0,2)
array([[[0, 4],
            [2, 6]],
            [[1, 5],
            [3, 7]]])
```

ndarray. $\mathbf{T}$

Same as self.transpose(), except that self is returned if self.ndim $<2$.

## Examples

```
>>> x = np.array([[1.,2.],[3.,4.]])
>>> x
array([[ 1., 2.],
    [ 3., 4.]])
>>> x.T
array([[ 1., 3.],
            [ 2., 4.]])
>>> x = np.array([1.,2.,3.,4.])
>>> x
array([ 1., 2., 3., 4.])
```

```
>>> x.T
array([ 1., 2., 3., 4.])
numpy.transpose (a,axes=None)
Permute the dimensions of an array.
```


## Parameters

a : array_like
Input array.
axes : list of ints, optional
By default, reverse the dimensions, otherwise permute the axes according to the values given.

## Returns

p : ndarray
$a$ with its axes permuted. A view is returned whenever possible.

## See Also:

rollaxis
Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
    [2, 3]])
>>> np.transpose(x)
array([[0, 2],
            [1, 3]])
>>> x = np.ones((1, 2, 3))
>>> np.transpose(x, (1, 0, 2)).shape
(2, 1, 3)
```


### 3.2.3 Changing number of dimensions

```
atleast_1d(*arys) Convert inputs to arrays with at least one dimension.
atleast_2d(*arys) View inputs as arrays with at least two dimensions.
atleast_3d(*arys) View inputs as arrays with at least three dimensions.
broadcast Produce an object that mimics broadcasting.
broadcast_arrays(*args) Broadcast any number of arrays against each other.
expand_dims(a,axis) Expand the shape of an array.
squeeze(a) Remove single-dimensional entries from the shape of an array.
```

numpy.atleast_1d(*arys)

Convert inputs to arrays with at least one dimension.
Scalar inputs are converted to 1-dimensional arrays, whilst higher-dimensional inputs are preserved.

```
Parameters
array1, array2, ... : array_like
```

One or more input arrays.

## Returns

ret : ndarray
An array, or sequence of arrays, each with a.ndim $>=1$. Copies are made only if necessary.

## See Also:

```
atleast_2d,atleast_3d
```


## Examples

```
>>> np.atleast_1d(1.0)
array([ 1.])
>>> x = np.arange(9.0).reshape (3,3)
>>> np.atleast_1d(x)
array([[ 0., 1., 2.],
    [ 3., 4., 5.],
    [ 6., 7., 8.]])
>>> np.atleast_1d(x) is x
True
>>> np.atleast_1d(1, [3, 4])
[array([1]), array([3, 4])]
numpy.atleast_2d(*arys)
```

View inputs as arrays with at least two dimensions.

## Parameters

array1, array2, ... : array_like
One or more array-like sequences. Non-array inputs are converted to arrays. Arrays that already have two or more dimensions are preserved.

## Returns

res, res2, ... : ndarray
An array, or tuple of arrays, each with a.ndim $>=2$. Copies are avoided where possible, and views with two or more dimensions are returned.

## See Also:

atleast_1d, atleast_3d
Examples

```
>>> np.atleast_2d(3.0)
array([[ 3.]])
>>> x = np.arange(3.0)
>>> np.atleast_2d(x)
array([[ 0., 1., 2.]])
>>> np.atleast_2d(x).base is x
True
>>> np.atleast_2d(1, [1, 2], [[1, 2]])
[array([[1]]), array([[1, 2]]), array([[1, 2]])]
```

numpy.atleast_3d(*arys)

View inputs as arrays with at least three dimensions.

## Parameters

array1, array2, ... : array_like
One or more array-like sequences. Non-array inputs are converted to arrays. Arrays that already have three or more dimensions are preserved.

## Returns

res1, res2, ... : ndarray
An array, or tuple of arrays, each with a.ndim $>=3$. Copies are avoided where possible, and views with three or more dimensions are returned. For example, a 1-D array of shape ( N, ) becomes a view of shape ( $1, \mathrm{~N}, 1$ ), and a 2-D array of shape $(\mathrm{M}, \mathrm{N})$ becomes a view of shape ( $\mathrm{M}, \mathrm{N}, ~ 1$ ).

## See Also:

```
atleast_1d,atleast_2d
```


## Examples

```
>>> np.atleast_3d(3.0)
array([[[ 3.]]])
>>> x = np.arange(3.0)
>>> np.atleast_3d(x).shape
(1, 3, 1)
>>> x = np.arange(12.0).reshape(4,3)
>>> np.atleast_3d(x).shape
(4, 3, 1)
>>> np.atleast_3d(x).base is x
True
>>> for arr in np.atleast_3d([1, 2], [[1, 2]], [[[1, 2]]]):
... print arr, arr.shape
...
[[ [1]
    [2]]] (1, 2, 1)
[ [ [1]
    [2]]] (1, 2, 1)
[[[[1 2]]] (1, 1, 2)
```


## class numpy.broadcast

Produce an object that mimics broadcasting.

## Parameters

in1, in2, ... : array_like
Input parameters.

## Returns

b : broadcast object
Broadcast the input parameters against one another, and return an object that encapsulates the result. Amongst others, it has shape and nd properties, and may be used as an iterator.

## Examples

Manually adding two vectors, using broadcasting:

```
>>> x = np.array([[1], [2], [3]])
>>> y = np.array([4, 5, 6])
>>> b = np.broadcast(x, y)
>>> out = np.empty(b.shape)
>>> out.flat = [u+v for (u,v) in b]
>>> out
array([[ 5., 6., 7.],
    [ 6., 7., 8.],
    [ 7., 8., 9.]])
```

Compare against built-in broadcasting:

```
>>> x + y
array([[5, 6, 7],
    [6, 7, 8],
    [7, 8, 9]])
```


## Methods

next
reset
numpy.broadcast_arrays (*args)

Broadcast any number of arrays against each other.

## Parameters

'*args' : array_likes
The arrays to broadcast.

## Returns

broadcasted : list of arrays
These arrays are views on the original arrays. They are typically not contiguous. Furthermore, more than one element of a broadcasted array may refer to a single memory location. If you need to write to the arrays, make copies first.

## Examples

```
>>> x = np.array([[1,2,3]])
>>> y = np.array([[1],[2],[3]])
>>> np.broadcast_arrays(x, y)
[array([[1, 2, 3],
    [1, 2, 3],
    [1, 2, 3]]), array([[1, 1, 1],
    [2, 2, 2],
    [3, 3, 3]])]
```

Here is a useful idiom for getting contiguous copies instead of non-contiguous views.

```
>>> map(np.array, np.broadcast_arrays(x, y))
[array([[1, 2, 3],
    [1, 2, 3],
    [1, 2, 3]]), array([[1, 1, 1],
    [2, 2, 2],
    [3, 3, 3]])]
numpy.expand_dims (a,axis)
Expand the shape of an array.
```

Insert a new axis, corresponding to a given position in the array shape.

## Parameters

a: array_like
Input array.
axis: int
Position (amongst axes) where new axis is to be inserted.

## Returns

res: ndarray
Output array. The number of dimensions is one greater than that of the input array.

## See Also:

```
doc.indexing, atleast_1d,atleast_2d,atleast_3d
```


## Examples

```
>>> x = np.array([1,2])
>>> x.shape
(2,)
```

The following is equivalent to $x[n p . n e w a x i s,:]$ or $x[n p . n e w a x i s]$ :

```
>>> y = np.expand_dims(x, axis=0)
>>> y
array([[1, 2]])
>>> y.shape
(1, 2)
>>> y = np.expand_dims(x, axis=1) # Equivalent to x[:,newaxis]
>>> y
array([[1],
    [2]])
>>> y.shape
(2, 1)
```

Note that some examples may use None instead of np. newaxis. These are the same objects:

```
>>> np.newaxis is None
True
```

numpy.squeeze (a)

Remove single-dimensional entries from the shape of an array.

## Parameters

a : array_like
Input data.

## Returns

squeezed : ndarray
The input array, but with with all dimensions of length 1 removed. Whenever possible, a view on $a$ is returned.

## Examples

```
>>> x = np.array([[[0], [1], [2]]])
>>> x.shape
(1, 3, 1)
>>> np.squeeze(x).shape
(3,)
```


### 3.2.4 Changing kind of array

| asarray(a[, dtype, order $])$ | Convert the input to an array. |
| :--- | :--- |
| asanyarray(a[, dtype, order $])$ | Convert the input to an ndarray, but pass ndarray subclasses through. |
| asmatrix(data[, dtype] $)$ | Interpret the input as a matrix. |
| asfarray(a[, dtype $])$ | Return an array converted to a float type. |
| asfortranarray(a[, dtype]) | Return an array laid out in Fortran order in memory. |
| asscalar(a) | Convert an array of size 1 to its scalar equivalent. |
| require(a[, dtype, requirements]) | Return an ndarray of the provided type that satisfies requirements. |

numpy . asarray ( $a$, dtype $=$ None, order $=$ None )
Convert the input to an array.

## Parameters

a : array_like
Input data, in any form that can be converted to an array. This includes lists, lists of tuples, tuples, tuples of tuples, tuples of lists and ndarrays.
dtype : data-type, optional
By default, the data-type is inferred from the input data.
order : \{ 'C', 'F' \}, optional
Whether to use row-major (' $C$ ') or column-major (' $F$ ' for FORTRAN) memory representation. Defaults to ' C '.

Returns
out : ndarray
Array interpretation of $a$. No copy is performed if the input is already an ndarray. If $a$ is a subclass of ndarray, a base class ndarray is returned.

See Also:
asanyarray
Similar function which passes through subclasses.
ascontiguousarray
Convert input to a contiguous array.
asfarray
Convert input to a floating point ndarray.
asfortranarray
Convert input to an ndarray with column-major memory order.
asarray_chkfinite
Similar function which checks input for NaNs and Infs.
fromiter
Create an array from an iterator.

## fromfunction

Construct an array by executing a function on grid positions.

## Examples

Convert a list into an array:

```
>>> a = [1, 2]
>>> np.asarray(a)
array([1, 2])
```

Existing arrays are not copied:

```
>>> a = np.array([1, 2])
>>> np.asarray(a) is a
True
```

If dtype is set, array is copied only if dtype does not match:

```
>>> a = np.array([1, 2], dtype=np.float32)
>>> np.asarray(a, dtype=np.float32) is a
True
>>> np.asarray(a, dtype=np.float64) is a
False
```

Contrary to asanyarray, ndarray subclasses are not passed through:

```
>>> issubclass(np.matrix, np.ndarray)
True
>>> a = np.matrix([[1, 2]])
>>> np.asarray(a) is a
False
>>> np.asanyarray(a) is a
True
```

numpy . asanyarray ( $a$, dtype $=$ None, order $=$ None )
Convert the input to an ndarray, but pass ndarray subclasses through.

## Parameters

a : array_like
Input data, in any form that can be converted to an array. This includes scalars, lists, lists of tuples, tuples, tuples of tuples, tuples of lists, and ndarrays.
dtype : data-type, optional
By default, the data-type is inferred from the input data.
order : \{ 'C', 'F' \}, optional
Whether to use row-major ('C') or column-major (' F ') memory representation. Defaults to ' C '.

## Returns

out : ndarray or an ndarray subclass
Array interpretation of $a$. If $a$ is an ndarray or a subclass of ndarray, it is returned as-is and no copy is performed.

## See Also:

## asarray

Similar function which always returns ndarrays.

## ascontiguousarray

Convert input to a contiguous array.
asfarray
Convert input to a floating point ndarray.
asfortranarray
Convert input to an ndarray with column-major memory order.

## asarray_chkfinite

Similar function which checks input for NaNs and Infs.

## fromiter

Create an array from an iterator.

## fromfunction

Construct an array by executing a function on grid positions.

## Examples

Convert a list into an array:

```
>>> a=[1, 2]
>>> np.asanyarray(a)
array([1, 2])
```

Instances of ndarray subclasses are passed through as-is:

```
>>> a = np.matrix([1, 2])
>>> np.asanyarray(a) is a
True
```

numpy.asmatrix (data, dtype=None)

Interpret the input as a matrix.
Unlike matrix, asmatrix does not make a copy if the input is already a matrix or an ndarray. Equivalent to matrix(data, copy=False).

## Parameters

data : array_like
Input data.

## Returns

mat : matrix
data interpreted as a matrix.

## Examples

```
>>> x = np.array([[1, 2], [3, 4]])
>>> m = np.asmatrix(x)
>>> x[0,0] = 5
>>> m
matrix([[5, 2],
                    [3, 4]])
```

numpy.asfarray (a, dtype=<type 'numpy.float64'>)
Return an array converted to a float type.

## Parameters

a : array_like
The input array.
dtype : str or dtype object, optional
Float type code to coerce input array $a$. If dtype is one of the 'int' dtypes, it is replaced with float64.

## Returns

out : ndarray
The input $a$ as a float ndarray.

## Examples

```
>>> np.asfarray([2, 3])
array([ 2., 3.])
>>> np.asfarray([2, 3], dtype='float')
array([ 2., 3.])
>>> np.asfarray([2, 3], dtype='int8')
array([ 2., 3.])
```

numpy.asfortranarray ( $a$, dtype=None)

Return an array laid out in Fortran order in memory.

## Parameters

a: array_like
Input array.
dtype : str or dtype object, optional
By default, the data-type is inferred from the input data.

## Returns

out : ndarray
The input $a$ in Fortran, or column-major, order.
See Also:

## ascontiguousarray

Convert input to a contiguous ( C order) array.

## asanyarray

Convert input to an ndarray with either row or column-major memory order.
require
Return an ndarray that satisfies requirements.
ndarray.flags
Information about the memory layout of the array.

## Examples

```
>>> x = np.arange (6).reshape (2,3)
>>> y = np.asfortranarray(x)
>>> x.flags['F_CONTIGUOUS']
False
>>> y.flags['F_CONTIGUOUS']
True
```

numpy.asscalar (a)
Convert an array of size 1 to its scalar equivalent.

## Parameters

a : ndarray
Input array of size 1.

## Returns

out : scalar
Scalar representation of $a$. The input data type is preserved.

## Examples

>>> np.asscalar(np.array([24]))
24
numpy . require ( $a$, dtype $=$ None, requirements $=$ None )
Return an ndarray of the provided type that satisfies requirements.
This function is useful to be sure that an array with the correct flags is returned for passing to compiled code (perhaps through ctypes).

## Parameters

a : array_like
The object to be converted to a type-and-requirement-satisfying array.
dtype : data-type
The required data-type, the default data-type is float64).
requirements : str or list of str
The requirements list can be any of the following

- 'F_CONTIGUOUS' ('F') - ensure a Fortran-contiguous array
- 'C_CONTIGUOUS' ('C') - ensure a C-contiguous array
- 'ALIGNED' ('A') - ensure a data-type aligned array
- 'WRITEABLE’ ('W') - ensure a writable array
- 'OWNDATA' ('O') - ensure an array that owns its own data


## See Also:

asarray
Convert input to an ndarray.
asanyarray
Convert to an ndarray, but pass through ndarray subclasses.
ascontiguousarray
Convert input to a contiguous array.
asfortranarray
Convert input to an ndarray with column-major memory order.
ndarray.flags
Information about the memory layout of the array.

## Notes

The returned array will be guaranteed to have the listed requirements by making a copy if needed.

## Examples

```
>>> x = np.arange (6).reshape (2,3)
>>> x.flags
    C_CONTIGUOUS : True
    F_CONTIGUOUS : False
    OWNDATA : False
    WRITEABLE : True
    ALIGNED : True
    UPDATEIFCOPY : False
>>> y = np.require(x, dtype=np.float 32, requirements=['A', 'O', 'W', 'F'])
>>> y.flags
    C_CONTIGUOUS : False
    F_CONTIGUOUS : True
    OWNDATA : True
    WRITEABLE : True
    ALIGNED : True
    UPDATEIFCOPY : False
```


### 3.2.5 Joining arrays

```
column_stack(tup) Stack 1-D arrays as columns into a 2-D array.
concatenate(a1, a2[, axis]) Join a sequence of arrays together.
dstack(tup) Stack arrays in sequence depth wise (along third axis).
hstack(tup) Stack arrays in sequence horizontally (column wise).
vstack(tup) Stack arrays in sequence vertically (row wise).
```

numpy.column_stack (tup)

Stack 1-D arrays as columns into a 2-D array.
Take a sequence of 1-D arrays and stack them as columns to make a single 2-D array. 2-D arrays are stacked as-is, just like with hstack. 1-D arrays are turned into 2-D columns first.

## Parameters

tup : sequence of 1-D or 2-D arrays.
Arrays to stack. All of them must have the same first dimension.

## Returns

stacked : 2-D array
The array formed by stacking the given arrays.

## See Also:

hstack, vstack, concatenate

## Notes

This function is equivalent to np. vstack (tup).T.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.column_stack((a,b))
array([[1, 2],
    [2, 3],
    [3, 4]])
```

numpy. concatenate ((a1, a2, ...), axis=0)
Join a sequence of arrays together.

## Parameters

$\mathbf{a 1}, \mathbf{a} 2, \ldots$ : sequence of array_like
The arrays must have the same shape, except in the dimension corresponding to axis (the first, by default).
axis : int, optional
The axis along which the arrays will be joined. Default is 0 .

## Returns

res : ndarray
The concatenated array.

## See Also:

ma. concatenate
Concatenate function that preserves input masks.
array_split
Split an array into multiple sub-arrays of equal or near-equal size.
split
Split array into a list of multiple sub-arrays of equal size.
hsplit
Split array into multiple sub-arrays horizontally (column wise)
vsplit
Split array into multiple sub-arrays vertically (row wise)
dsplit
Split array into multiple sub-arrays along the 3rd axis (depth).
hstack
Stack arrays in sequence horizontally (column wise)
vstack
Stack arrays in sequence vertically (row wise)
dstack
Stack arrays in sequence depth wise (along third dimension)

## Notes

When one or more of the arrays to be concatenated is a MaskedArray, this function will return a MaskedArray object instead of an ndarray, but the input masks are not preserved. In cases where a MaskedArray is expected as input, use the ma.concatenate function from the masked array module instead.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> b = np.array([[5, 6]])
>>> np.concatenate((a, b), axis=0)
array([[1, 2],
    [3, 4],
    [5, 6]])
>>> np.concatenate((a, b.T), axis=1)
array([[1, 2, 5],
    [3, 4, 6]])
```

This function will not preserve masking of MaskedArray inputs.

```
>>> a = np.ma.arange(3)
>>> a[1] = np.ma.masked
>>> b = np.arange (2, 5)
>>> a
masked_array(data = [0 -- 2],
    mask = [False True False],
    fill_value = 999999)
>>> b
array([2, 3, 4])
>>> np.concatenate([a, b])
masked_array(data = [llllllll}01
            mask = False,
    fill_value = 999999)
>>> np.ma.concatenate([a, b])
masked_array(data = [0 -- 2 2 3 4 ] ,
            mask = [False True False False False False],
    fill_value = 999999)
```

numpy.dstack (tup)

Stack arrays in sequence depth wise (along third axis).
Takes a sequence of arrays and stack them along the third axis to make a single array. Rebuilds arrays divided by dsplit. This is a simple way to stack 2D arrays (images) into a single 3D array for processing.

## Parameters

tup : sequence of arrays
Arrays to stack. All of them must have the same shape along all but the third axis.

## Returns

## stacked : ndarray

The array formed by stacking the given arrays.

## See Also:

```
vstack
```

Stack along first axis.

```
hstack
```

Stack along second axis.
concatenate
Join arrays.
dsplit
Split array along third axis.

## Notes

Equivalent to np.concatenate(tup, axis=2).

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.dstack((a,b))
array([[[1, 2],
    [2, 3],
    [3, 4]]])
>>> a = np.array([[1],[2],[3]])
>>> b = np.array([[2],[3],[4]])
>>> np.dstack((a,b))
array([[[1, 2]],
    [[2, 3]],
    [[3, 4]]])
```

numpy.hstack (tup)

Stack arrays in sequence horizontally (column wise).
Take a sequence of arrays and stack them horizontally to make a single array. Rebuild arrays divided by hsplit.

## Parameters

tup : sequence of ndarrays
All arrays must have the same shape along all but the second axis.

## Returns

stacked : ndarray
The array formed by stacking the given arrays.

## See Also:

vstack
Stack arrays in sequence vertically (row wise).
dstack
Stack arrays in sequence depth wise (along third axis).
concatenate
Join a sequence of arrays together.
hsplit
Split array along second axis.

## Notes

Equivalent to np.concatenate (tup, axis=1)

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.hstack((a,b))
array([1, 2, 3, 2, 3, 4])
>>> a = np.array([[1],[2],[3]])
>>> b = np.array([[2],[3],[4]])
>>> np.hstack((a,b))
```

```
array([[1, 2],
    [2, 3],
    [3, 4]])
```

numpy.vstack (tup)
Stack arrays in sequence vertically (row wise).
Take a sequence of arrays and stack them vertically to make a single array. Rebuild arrays divided by vsplit.

## Parameters

tup : sequence of ndarrays
Tuple containing arrays to be stacked. The arrays must have the same shape along all but the first axis.

## Returns

 stacked : ndarrayThe array formed by stacking the given arrays.

## See Also:

hstack
Stack arrays in sequence horizontally (column wise).
dstack
Stack arrays in sequence depth wise (along third dimension).
concatenate
Join a sequence of arrays together.
vsplit
Split array into a list of multiple sub-arrays vertically.

## Notes

Equivalent to np.concatenate (tup, axis=0)

## Examples

```
>>> a = np.array([1, 2, 3])
>>> b = np.array([2, 3, 4])
>>> np.vstack((a,b))
array([[1, 2, 3],
    [2, 3, 4]])
>>> a = np.array([[1], [2], [3]])
>>> b = np.array([[2], [3], [4]])
>>> np.vstack((a,b))
array([[1],
            [2],
            [3],
            [2],
            [3],
            [4]])
```


### 3.2.6 Splitting arrays

```
array_split(ary, indices_or_sections[, axis]) Split an array into multiple sub-arrays of equal or near-equal size.
dsplit(ary, indices_or_sections) Split array into multiple sub-arrays along the 3rd axis (depth).
hsplit(ary, indices_or_sections)
split(ary, indices_or_sections[, axis])
vsplit(ary, indices_or_sections)
Split an array into multiple sub-arrays horizontally (column-wise).
Split an array into multiple sub-arrays of equal size.
Split an array into multiple sub-arrays vertically (row-wise).
```

numpy.array_split (ary, indices_or_sections, axis=0)
Split an array into multiple sub-arrays of equal or near-equal size.
Please refer to the split documentation. The only difference between these functions is that array_split allows indices_or_sections to be an integer that does not equally divide the axis.

## See Also:

split
Split array into multiple sub-arrays of equal size.

## Examples

```
>>> x = np.arange(8.0)
>>> np.array_split(x, 3)
            [array([ 0., 1., 2.]), array([ 3., 4., 5.]), array([ 6., 7.])]
```

numpy.dsplit (ary, indices_or_sections)
Split array into multiple sub-arrays along the 3rd axis (depth).
Please refer to the split documentation. $d s$ slit is equivalent to $s p l i t$ with axis=2, the array is always split along the third axis provided the array dimension is greater than or equal to 3 .

## See Also:

split
Split an array into multiple sub-arrays of equal size.

## Examples

```
>>> x = np.arange(16.0).reshape(2, 2, 4)
>>> x
array([[[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.]],
    [[[ 8., 9., 10., 11.],
            [ 12., 13., 14., 15.]]])
>>> np.dsplit(x, 2)
[array([[[ 0., 1.],
            [ 4., 5.]],
            [[[ 8., 9.],
            [ 12., 13.]]]),
            array([[[[ 2., 3.],
                    [ 6., 7.]],
            [[ 10., 11.],
                    [ 14., 15.]]])]
>>> np.dsplit(x, np.array([3, 6]))
[array([[[ 0., 1., 2.],
            [ 4., 5., 6.]],
            [[[ 8., 9., 10.],
            [ 12., 13., 14.]]]),
        array([[[[ 3.],
```

```
    [ 7.]],
    [[ 11.],
    [ 15.]]]),
array([], dtype=float64)]
```


## numpy.hsplit (ary, indices_or_sections)

Split an array into multiple sub-arrays horizontally (column-wise).
Please refer to the split documentation. hsplit is equivalent to split with axis=1, the array is always split along the second axis regardless of the array dimension.

## See Also:

```
split
```

Split an array into multiple sub-arrays of equal size.

## Examples

```
>>> x = np.arange(16.0).reshape(4, 4)
>>> x
array([[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.],
    [ 12., 13., 14., 15.]])
>>> np.hsplit(x, 2)
[array([[ 0., 1.],
    [ 4., 5.],
    [ 8., 9.],
    [ 12., 13.]]),
        array([[ 2., 3.],
                            [ 6., 7.],
                    [ 10., 11.],
                            [ 14., 15.]])]
>>> np.hsplit(x, np.array([3, 6]))
[array([[ 0., 1., 2.],
                            [ 4., 5., 6.],
                            [ 8., 9., 10.],
                            [ 12., 13., 14.]]),
        array([[ 3.],
                            [ 7.],
                            [ 11.],
                            [ 15.]]),
        array([], dtype=float64)]
```

With a higher dimensional array the split is still along the second axis.

```
>>> x = np.arange(8.0).reshape(2, 2, 2)
>>> x
array([[[ 0., 1.],
    [ 2., 3.]],
    [[ 4., 5.],
    [ 6., 7.]]])
>>> np.hsplit(x, 2)
[array([[[ 0., 1.]],
    [[ 4., 5.]]]),
        array([[[ 2., 3.]],
    [[ 6., 7.]]])]
```

```
numpy.split (ary, indices_or_sections, axis=0)
```

Split an array into multiple sub-arrays of equal size.

## Parameters

ary : ndarray
Array to be divided into sub-arrays.
indices_or_sections : int or 1-D array
If indices_or_sections is an integer, N , the array will be divided into N equal arrays along axis. If such a split is not possible, an error is raised.

If indices_or_sections is a 1-D array of sorted integers, the entries indicate where along axis the array is split. For example, [2, 3] would, for axis=0, result in

- ary[:2]
- ary[2:3]
- ary[3:]

If an index exceeds the dimension of the array along axis, an empty sub-array is returned correspondingly.
axis : int, optional
The axis along which to split, default is 0 .

## Returns

sub-arrays : list of ndarrays
A list of sub-arrays.

## Raises

ValueError :
If indices_or_sections is given as an integer, but a split does not result in equal division.

## See Also:

array_split
Split an array into multiple sub-arrays of equal or near-equal size. Does not raise an exception if an equal division cannot be made.
hsplit
Split array into multiple sub-arrays horizontally (column-wise).
vsplit
Split array into multiple sub-arrays vertically (row wise).
dsplit
Split array into multiple sub-arrays along the 3rd axis (depth).
concatenate
Join arrays together.
hstack
Stack arrays in sequence horizontally (column wise).
vstack
Stack arrays in sequence vertically (row wise).
dstack
Stack arrays in sequence depth wise (along third dimension).

## Examples

```
>>> x = np.arange(9.0)
>>> np.split(x, 3)
[array([ 0., 1., 2.]), array([ 3., 4., 5.]), array([ 6., 7., 8.])]
>>> x = np.arange(8.0)
>>> np.split(x, [3, 5, 6, 10])
[array([ 0., 1., 2.]),
    array([ 3., 4.]),
    array([ 5.]),
    array([ 6., 7.]),
    array([], dtype=float64)]
```

numpy.vsplit (ary, indices_or_sections)

Split an array into multiple sub-arrays vertically (row-wise).
Please refer to the split documentation. vsplit is equivalent to split with axis=0 (default), the array is always split along the first axis regardless of the array dimension.

## See Also:

split
Split an array into multiple sub-arrays of equal size.

## Examples

```
>>> x = np.arange(16.0).reshape(4, 4)
>>> x
array([[[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.],
    [ 12., 13., 14., 15.]])
>>> np.vsplit(x, 2)
[array([[ 0., 1., 2., 3.],
    [4., 5., 6., 7.]]),
    array([[[ 8., 9., 10., 11.],
    [ 12., 13., 14., 15.]])]
>>> np.vsplit(x, np.array([3, 6]))
[array([[[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.]]),
    array([[ 12., 13., 14., 15.]]),
    array([], dtype=float64)]
```

With a higher dimensional array the split is still along the first axis.

```
>>> x = np.arange(8.0).reshape(2, 2, 2)
>>> x
array([[[ 0., 1.],
    [ 2., 3.]],
    [[ 4., 5.],
    [ 6., 7.]]])
>>> np.vsplit(x, 2)
[array([[[ 0., 1.],
            [ 2., 3.]]]),
    array([[[ 4., 5.],
    [ 6., 7.]]])]
```


### 3.2.7 Tiling arrays

```
tile(A, reps) Construct an array by repeating A the number of times given by reps.
repeat(a, repeats[, axis]) Repeat elements of an array.
```

numpy.tile ( $A$, reps)
Construct an array by repeating A the number of times given by reps.
If reps has length $d$, the result will have dimension of max ( $\mathrm{d}, \mathrm{A}$. ndim).
If A. ndim $<\mathrm{d}, A$ is promoted to be d-dimensional by prepending new axes. So a shape (3,) array is promoted to $(1,3)$ for 2-D replication, or shape $(1,1,3)$ for 3-D replication. If this is not the desired behavior, promote $A$ to d-dimensions manually before calling this function.

If A. ndim $>\mathrm{d}$, reps is promoted to $A$.ndim by pre-pending 1 's to it. Thus for an $A$ of shape $(2,3,4,5)$, a reps of $(2,2)$ is treated as $(1,1,2,2)$.

## Parameters

A : array_like
The input array.
reps : array_like
The number of repetitions of $A$ along each axis.

## Returns

c : ndarray
The tiled output array.

## See Also:

## repeat

Repeat elements of an array.

## Examples

```
>>> a = np.array([0, 1, 2])
>>> np.tile(a, 2)
array([0, 1, 2, 0, 1, 2])
>>> np.tile(a, (2, 2))
array([[0, 1, 2, 0, 1, 2],
                    [0, 1, 2, 0, 1, 2]])
>>> np.tile(a, (2, 1, 2))
array([[[0, 1, 2, 0, 1, 2]],
    [[0, 1, 2, 0, 1, 2]]])
>>> b = np.array([[1, 2], [3, 4]])
>>> np.tile(b, 2)
array([[1, 2, 1, 2],
    [3, 4, 3, 4]])
>>> np.tile(b, (2, 1))
array([[1, 2],
    [3, 4],
    [1, 2],
            [3, 4]])
```

numpy.repeat ( $a$, repeats, axis=None)

Repeat elements of an array.

## Parameters

a : array_like
Input array.
repeats : \{int, array of ints \}
The number of repetitions for each element. repeats is broadcasted to fit the shape of the given axis.
axis : int, optional
The axis along which to repeat values. By default, use the flattened input array, and return a flat output array.

## Returns

repeated_array : ndarray
Output array which has the same shape as $a$, except along the given axis.

## See Also:

tile
Tile an array.

## Examples

```
>>> x = np.array([[1,2],[3,4]])
>>> np.repeat (x, 2)
array([1, 1, 2, 2, 3, 3, 4, 4])
>>> np.repeat(x, 3, axis=1)
array([[1, 1, 1, 2, 2, 2],
    [3, 3, 3, 4, 4, 4]])
>>> np.repeat(x, [1, 2], axis=0)
array([[1, 2],
    [3, 4],
    [3, 4]])
```


### 3.2.8 Adding and removing elements

```
delete(arr, obj[, axis])
insert(arr, obj, values[, axis])
append(arr, values[, axis])
resize(a,new_shape)
trim_zeros(filt[, trim])
unique(ar[, return_index, return_inverse])
```

Return a new array with sub-arrays along an axis deleted.
Insert values along the given axis before the given indices. Append values to the end of an array.
Return a new array with the specified shape.
Trim the leading and/or trailing zeros from a 1-D array or sequence.
Find the unique elements of an array.

```
numpy. delete (arr, obj, axis=None)
Return a new array with sub-arrays along an axis deleted.
```


## Parameters

```
arr : array_like
Input array.
obj : slice, int or array of ints
Indicate which sub-arrays to remove.
axis : int, optional
```

The axis along which to delete the subarray defined by obj. If axis is None, obj is applied to the flattened array.

## Returns

 out : ndarrayA copy of arr with the elements specified by obj removed. Note that delete does not occur in-place. If axis is None, out is a flattened array.

## See Also:

```
insert
```

Insert elements into an array.
append
Append elements at the end of an array.

## Examples

```
>>> arr = np.array([[1,2,3,4], [5,6,7,8], [9,10,11,12]])
>>> arr
array([[ 1, 2, 3, 4],
    [ 5, 6, 7, 8],
    [ 9, 10, 11, 12]])
>>> np.delete(arr, 1, 0)
array([[ 1, 2, 3, 4],
    [ 9, 10, 11, 12]])
>>> np.delete(arr, np.s_[::2], 1)
array([[ 2, 4],
    [ 6, 8],
    [10, 12]])
>>> np.delete(arr, [1,3,5], None)
array([ 1, 3, 5, 7, 8, 9, 10, 11, 12])
```

numpy.insert (arr, obj, values, axis=None)
Insert values along the given axis before the given indices.

## Parameters

arr : array_like
Input array.
obj : int, slice or sequence of ints
Object that defines the index or indices before which values is inserted.
values : array_like
Values to insert into arr. If the type of values is different from that of arr, values is converted to the type of arr .
axis : int, optional
Axis along which to insert values. If axis is None then arr is flattened first.

## Returns

out : ndarray
A copy of arr with values inserted. Note that insert does not occur in-place: a new array is returned. If axis is None, out is a flattened array.

## See Also:

append
Append elements at the end of an array.
delete
Delete elements from an array.

## Examples

```
>> a = np.array([[1, 1], [2, 2], [3, 3]])
>>> a
array([[1, 1],
    [2, 2],
    [3, 3]])
>>> np.insert(a, 1, 5)
array([1, 5, 1, 2, 2, 3, 3])
>>> np.insert(a, 1, 5, axis=1)
array([[1, 5, 1],
    [2, 5, 2],
    [3, 5, 3]])
>>> b = a.flatten()
>>> b
array([1, 1, 2, 2, 3, 3])
>>> np.insert(b, [2, 2], [5, 6])
array([1, 1, 5, 6, 2, 2, 3, 3])
>>> np.insert(b, slice(2, 4), [5, 6])
array([1, 1, 5, 2, 6, 2, 3, 3])
>>> np.insert(b, [2, 2], [7.13, False]) # type casting
array([1, 1, 7, 0, 2, 2, 3, 3])
>>> x = np.arange(8).reshape (2, 4)
>>> idx = (1, 3)
>>> np.insert(x, idx, 999, axis=1)
array([[ 0, 999, 1, 2, 999, 3],
    [4, 999, 5, 6, 999, 7]])
```

numpy . append (arr, values, axis=None)
Append values to the end of an array.

## Parameters

arr : array_like
Values are appended to a copy of this array.
values : array_like
These values are appended to a copy of arr. It must be of the correct shape (the same shape as arr, excluding axis). If axis is not specified, values can be any shape and will be flattened before use.
axis : int, optional
The axis along which values are appended. If axis is not given, both arr and values are flattened before use.

## Returns

out : ndarray

A copy of arr with values appended to axis. Note that append does not occur in-place: a new array is allocated and filled. If axis is None, out is a flattened array.

## See Also:

## insert

Insert elements into an array.
delete
Delete elements from an array.

## Examples

```
>>> np.append([1, 2, 3], [[4, 5, 6], [7, 8, 9]])
array([1, 2, 3, 4, 5, 6, 7, 8, 9])
```

When axis is specified, values must have the correct shape.

```
>>> np.append([[1, 2, 3], [4, 5, 6]], [[7, 8, 9]], axis=0)
array([[1, 2, 3],
    [4, 5, 6],
    [7, 8, 9]])
>>> np.append([[1, 2, 3], [4, 5, 6]], [7, 8, 9], axis=0)
Traceback (most recent call last):
ValueError: arrays must have same number of dimensions
numpy.resize(a,new_shape)
```

Return a new array with the specified shape.
If the new array is larger than the original array, then the new array is filled with repeated copies of $a$. Note that this behavior is different from a.resize(new_shape) which fills with zeros instead of repeated copies of $a$.

## Parameters

## a : array_like

Array to be resized.
new_shape : int or tuple of int
Shape of resized array.

## Returns

reshaped_array : ndarray
The new array is formed from the data in the old array, repeated if necessary to fill out the required number of elements. The data are repeated in the order that they are stored in memory.

## See Also:

ndarray.resize
resize an array in-place.

## Examples

```
>>> a=np.array([[0,1],[2,3]])
>>> np.resize(a,(1,4))
array([[0, 1, 2, 3]])
>>> np.resize(a, (2,4))
array([[0, 1, 2, 3],
    [0, 1, 2, 3]])
```

numpy.trim_zeros (filt, trim='fb')
Trim the leading and/or trailing zeros from a 1-D array or sequence.

## Parameters

filt : 1-D array or sequence
Input array.
trim : str, optional
A string with ' $f$ ' representing trim from front and ' $b$ ' to trim from back. Default is ' fb ', trim zeros from both front and back of the array.

## Returns

trimmed : 1-D array or sequence
The result of trimming the input. The input data type is preserved.

## Examples

```
>>> a = np.array((0, 0, 0, 1, 2, 3, 0, 2, 1, 0))
>>> np.trim_zeros(a)
array([1, 2, 3, 0, 2, 1])
>>> np.trim_zeros(a, 'b')
array([0, 0, 0, 1, 2, 3, 0, 2, 1])
```

The input data type is preserved, list/tuple in means list/tuple out.
>>> np.trim_zeros([0, 1, 2, 0])
[1, 2]
numpy.unique (ar, return_index=False, return_inverse=False)
Find the unique elements of an array.
Returns the sorted unique elements of an array. There are two optional outputs in addition to the unique elements: the indices of the input array that give the unique values, and the indices of the unique array that reconstruct the input array.

## Parameters

ar : array_like
Input array. This will be flattened if it is not already 1-D.
return_index : bool, optional
If True, also return the indices of $a r$ that result in the unique array.
return_inverse : bool, optional
If True, also return the indices of the unique array that can be used to reconstruct $a r$.

## Returns

unique : ndarray
The sorted unique values.
unique_indices : ndarray, optional
The indices of the unique values in the (flattened) original array. Only provided if return_index is True.
unique_inverse : ndarray, optional

The indices to reconstruct the (flattened) original array from the unique array. Only provided if return_inverse is True.

## See Also:

## numpy.lib.arraysetops

Module with a number of other functions for performing set operations on arrays.

## Examples

```
>>> np.unique([1, 1, 2, 2, 3, 3])
array([1, 2, 3])
>>> a = np.array([[1, 1], [2, 3]])
>>> np.unique(a)
array([1, 2, 3])
```

Return the indices of the original array that give the unique values:

```
>>> a = np.array(['a', 'b', 'b', 'c', 'a'])
>>> u, indices = np.unique(a, return_index=True)
>>> u
array(['a', 'b', 'c'],
    dtype='|S1')
>>> indices
array([0, 1, 3])
>>> a[indices]
array(['a', 'b', 'c'],
    dtype='|S1')
```

Reconstruct the input array from the unique values:

```
>>> a = np.array([1, 2, 6, 4, 2, 3, 2])
>>> u, indices = np.unique(a, return_inverse=True)
>>> u
array([1, 2, 3, 4, 6])
>>> indices
array([0, 1, 4, 3, 1, 2, 1])
>>> u[indices]
array([1, 2, 6, 4, 2, 3, 2])
```


### 3.2.9 Rearranging elements

| fliplr $(\mathrm{m})$ | Flip array in the left/right direction. |
| :--- | :--- |
| flipud(m) | Flip array in the up/down direction. |
| reshape $(a$, newshape[, order $])$ | Gives a new shape to an array without changing its data. |
| $\operatorname{roll}(\mathrm{a}$, shift $[$, axis $])$ | Roll array elements along a given axis. |
| $\operatorname{rot} 90(\mathrm{~m}[, \mathrm{k}])$ | Rotate an array by 90 degrees in the counter-clockwise direction. |

numpy.fliplr(m)
Flip array in the left/right direction.
Flip the entries in each row in the left/right direction. Columns are preserved, but appear in a different order than before.

## Parameters <br> m : array_like <br> Input array.

## Returns

f: ndarray
A view of $m$ with the columns reversed. Since a view is returned, this operation is $\mathcal{O}(1)$.

## See Also:

flipud
Flip array in the up/down direction.
rot 90
Rotate array counterclockwise.

## Notes

Equivalent to $\mathrm{A}[:,::-1]$. Does not require the array to be two-dimensional.

## Examples

```
>>> A = np.diag([1.,2.,3.])
>>> A
array([[ 1., 0., 0.],
    [ 0., 2., 0.],
    [0., 0., 3.]])
>>> np.fliplr(A)
array([[ 0., 0., 1.],
    [ 0., 2., 0.],
    [ 3., 0., 0.]])
>>> A = np.random.randn (2,3,5)
>>> np.all(np.fliplr(A)==A[:,::-1,...])
True
```

numpy.flipud ( $m$ )

Flip array in the up/down direction.
Flip the entries in each column in the up/down direction. Rows are preserved, but appear in a different order than before.

## Parameters

m : array_like
Input array.

## Returns

out : array_like
A view of $m$ with the rows reversed. Since a view is returned, this operation is $\mathcal{O}(1)$.

## See Also:

## fliplr

Flip array in the left/right direction.
rot 90
Rotate array counterclockwise.

## Notes

Equivalent to $\mathrm{A}[::-1, \ldots]$. Does not require the array to be two-dimensional.

## Examples

```
>>> A = np.diag([1.0, 2, 3])
>>> A
array([[ 1., 0., 0.],
    [ 0., 2., 0.],
    [ 0., 0., 3.]])
>>> np.flipud(A)
array([[ 0., 0., 3.],
    [ 0., 2., 0.],
    [ 1., 0., 0.]])
>>> A = np.random.randn (2, 3,5)
>>> np.all(np.flipud(A)==A[::-1,...])
True
>>> np.flipud([1,2])
array([2, 1])
numpy.reshape (a,newshape, order='C')
```

Gives a new shape to an array without changing its data.

## Parameters

a : array_like
Array to be reshaped.
newshape : int or tuple of ints
The new shape should be compatible with the original shape. If an integer, then the result will be a 1-D array of that length. One shape dimension can be -1 . In this case, the value is inferred from the length of the array and remaining dimensions.
order : \{ ' C ', ' F ', ' $A$ ' \}, optional
Determines whether the array data should be viewed as in C (row-major) order, FORTRAN (column-major) order, or the C/FORTRAN order should be preserved.

## Returns

reshaped_array : ndarray
This will be a new view object if possible; otherwise, it will be a copy.

## See Also:

```
ndarray.reshape
```

Equivalent method.

## Notes

It is not always possible to change the shape of an array without copying the data. If you want an error to be raise if the data is copied, you should assign the new shape to the shape attribute of the array:

```
>>> a = np.zeros((10, 2))
# A transpose make the array non-contiguous
>>> b = a.T
# Taking a view makes it possible to modify the shape without modiying the
# initial object.
>>> c = b.view()
>>> c.shape = (20)
AttributeError: incompatible shape for a non-contiguous array
```


## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> np.reshape(a, 6)
array([1, 2, 3, 4, 5, 6])
>>> np.reshape(a, 6, order=' F')
array([1, 4, 2, 5, 3, 6])
>>> np.reshape(a, (3,-1)) # the unspecified value is inferred to be 2
array([[1, 2],
    [3, 4],
    [5, 6]])
```

numpy.roll (a, shift, axis=None)

Roll array elements along a given axis.
Elements that roll beyond the last position are re-introduced at the first.

## Parameters

a: array_like
Input array.
shift : int
The number of places by which elements are shifted.
axis : int, optional
The axis along which elements are shifted. By default, the array is flattened before shifting, after which the original shape is restored.

## Returns

res: ndarray
Output array, with the same shape as $a$.

## See Also:

rollaxis
Roll the specified axis backwards, until it lies in a given position.

## Examples

```
>>> x = np.arange(10)
>>> np.roll(x, 2)
array([8, 9, 0, 1, 2, 3, 4, 5, 6, 7])
>>> x2 = np.reshape(x, (2,5))
>>> x2
array([[0, 1, 2, 3, 4],
    [5, 6, 7, 8, 9]])
>>> np.roll(x2, 1)
array([[9, 0, 1, 2, 3],
    [4, 5, 6, 7, 8]])
>>> np.roll(x2, 1, axis=0)
array([[5, 6, 7, 8, 9],
    [0, 1, 2, 3, 4]])
>>> np.roll(x2, 1, axis=1)
array([[4, 0, 1, 2, 3],
    [9, 5, 6, 7, 8]])
```

numpy $\operatorname{rot} 90(m, k=1)$
Rotate an array by 90 degrees in the counter-clockwise direction.
The first two dimensions are rotated; therefore, the array must be at least 2-D.

## Parameters

m : array_like
Array of two or more dimensions.
$\mathbf{k}$ : integer
Number of times the array is rotated by 90 degrees.

## Returns

$\mathbf{y}$ : ndarray
Rotated array.

## See Also:

fliplr
Flip an array horizontally.
flipud
Flip an array vertically.

## Examples

```
>>> m = np.array([[1,2],[3,4]], int)
>>> m
array([[1, 2],
            [3, 4]])
>>> np.rot90(m)
array([[2, 4],
            [1, 3]])
>>> np.rot90(m, 2)
array([[4, 3],
    [2, 1]])
```


### 3.3 Indexing routines

See Also:<br>Indexing

### 3.3.1 Generating index arrays

| C_ | Translates slice objects to concatenation along the second axis. |
| :---: | :---: |
| $r_{\text {_ }}$ | Translates slice objects to concatenation along the first axis. |
| S_ | A nicer way to build up index tuples for arrays. |
| nonzero(a) | Return the indices of the elements that are non-zero. |
| where(condition, x ) | Return elements, either from $x$ or $y$, depending on condition. |
| indices(dimensions[, dtype]) | Return an array representing the indices of a grid. |
| ix_(*args) | Construct an open mesh from multiple sequences. |
| ogrid | $n d \_$grid instance which returns an open multi-dimensional "meshgrid". |
| ravel_multi_index(multi_index, dims[, mode, ...]) | Converts a tuple of index arrays into an array of flat indices, applying boundary modes to the multi-index. |
| unravel_index(indices, dims[, order]) | Converts a flat index or array of flat indices into a tuple of coordinate arrays. |
| diag_indices(n[, ndim]) | Return the indices to access the main diagonal of an array. |
| diag_indices_from(arr) | Return the indices to access the main diagonal of an $n$-dimensional array. |
| mask_indices(n, mask_func[, k]) | Return the indices to access ( $\mathrm{n}, \mathrm{n}$ ) arrays, given a masking function. |
| tril_indices(n[, k]) | Return the indices for the lower-triangle of an ( $n, n$ ) array. |
| tril_indices_from(arr[, k]) | Return the indices for the lower-triangle of arr. |
| triu_indices( n [, k]) | Return the indices for the upper-triangle of an ( $n, n$ ) array. |
| triu_indices_from(arr[, k]) | Return the indices for the upper-triangle of an ( $n, n$ ) array. |

This is short-hand for np. $r_{-}\left[{ }^{\prime}-1,2,0^{\prime}\right.$, index expression], which is useful because of its common occurrence. In particular, arrays will be stacked along their last axis after being upgraded to at least 2-D with 1's post-pended to the shape (column vectors made out of 1-D arrays).
For detailed documentation, see $r_{-}$.

## Examples

```
>>> np.c_[np.array([[1,2,3]]), 0, 0, np.array([[4,5,6]])]
array([[1, 2, 3, 0, 0, 4, 5, 6]])
```

numpy. $\mathbf{r}_{-}$
Translates slice objects to concatenation along the first axis.
This is a simple way to build up arrays quickly. There are two use cases.
1.If the index expression contains comma separated arrays, then stack them along their first axis.
2.If the index expression contains slice notation or scalars then create a 1-D array with a range indicated by the slice notation.
If slice notation is used, the syntax start:stop:step is equivalent to np.arange (start, stop, step) inside of the brackets. However, if step is an imaginary number (i.e. 100 j ) then its integer portion is interpreted as a number-of-points desired and the start and stop are inclusive. In other words start: stop: stepj is interpreted as np. linspace (start, stop, step, endpoint=1) inside of the brackets. After expansion of slice notation, all comma separated sequences are concatenated together.

Optional character strings placed as the first element of the index expression can be used to change the output. The strings ' $r$ ' or ' $c$ ' result in matrix output. If the result is $1-\mathrm{D}$ and ' $r$ ' is specified a $1 \times \mathrm{N}$ (row) matrix is produced. If the result is 1-D and ' c ' is specified, then a $\mathrm{N} \times 1$ (column) matrix is produced. If the result is 2-D then both provide the same matrix result.

A string integer specifies which axis to stack multiple comma separated arrays along. A string of two commaseparated integers allows indication of the minimum number of dimensions to force each entry into as the second integer (the axis to concatenate along is still the first integer).

A string with three comma-separated integers allows specification of the axis to concatenate along, the minimum number of dimensions to force the entries to, and which axis should contain the start of the arrays which are less than the specified number of dimensions. In other words the third integer allows you to specify where the 1 's should be placed in the shape of the arrays that have their shapes upgraded. By default, they are placed in the front of the shape tuple. The third argument allows you to specify where the start of the array should be instead. Thus, a third argument of ' 0 ' would place the 1 's at the end of the array shape. Negative integers specify where in the new shape tuple the last dimension of upgraded arrays should be placed, so the default is ' -1 '.

## Parameters

Not a function, so takes no parameters :

## Returns

A concatenated ndarray or matrix. :

## See Also:

concatenate
Join a sequence of arrays together.
C-
Translates slice objects to concatenation along the second axis.

## Examples

```
>>> np.r_[np.array([1,2,3]), 0, 0, np.array([4,5,6])]
array([1, 2, 3, 0, 0, 4, 5, 6])
>>> np.r_[-1:1:6j, [0]*3, 5, 6]
array([-1. , -0.6, -0.2, 0.2, 0.6, 1., 0., 0., 0., 5., 6. ])
```

String integers specify the axis to concatenate along or the minimum number of dimensions to force entries into.

```
>>> a = np.array([[0, 1, 2], [3, 4, 5]])
>>> np.r_['-1', a, a] # concatenate along last axis
array([[0, 1, 2, 0, 1, 2],
    [3, 4, 5, 3, 4, 5]])
>>> np.r_['0,2', [1,2,3], [4,5,6]] # concatenate along first axis, dim>=2
array([[1, 2, 3],
    [4, 5, 6]])
>>> np.r_['0,2,0', [1,2,3], [4,5,6]]
array([[1],
    [2],
    [3],
    [4],
    [5],
    [6]])
>>> np.r_['1,2,0', [1,2,3], [4,5,6]]
array([[1, 4],
    [2, 5],
    [3, 6]])
```

Using ' $r$ ' or ' $c$ ' as a first string argument creates a matrix.

```
>>> np.r_['r', [1,2,3], [4,5,6]]
matrix([[1, 2, 3, 4, 5, 6]])
```

numpy.s_
A nicer way to build up index tuples for arrays.
Note: Use one of the two predefined instances index_exp or $s_{-}$rather than directly using IndexExpression.
For any index combination, including slicing and axis insertion, a[indices] is the same as a [np.index_exp[indices]] for any array $a$. However, np.index_exp [indices] can be used anywhere in Python code and returns a tuple of slice objects that can be used in the construction of complex index expressions.

## Parameters

## maketuple : bool

If True, always returns a tuple.

## See Also:

## index_exp

Predefined instance that always returns a tuple: index_exp = IndexExpression(maketuple=True).
s_
Predefined instance without tuple conversion: $s_{-}=$IndexExpression( maketuple=False ).

## Notes

You can do all this with slice() plus a few special objects, but there's a lot to remember and this version is simpler because it uses the standard array indexing syntax.

## Examples

```
>>> np.s_[2::2]
slice(2, None, 2)
>>> np.index_exp[2::2]
(slice(2, None, 2),)
>>> np.array([0, 1, 2, 3, 4])[np.s_[2::2]]
array([2, 4])
numpy.nonzero (a)
Return the indices of the elements that are non-zero.
```

Returns a tuple of arrays, one for each dimension of $a$, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

```
a[nonzero(a)]
```

To group the indices by element, rather than dimension, use:
transpose (nonzero(a))
The result of this is always a 2-D array, with a row for each non-zero element.

## Parameters

a: array_like
Input array.

## Returns

tuple_of_arrays : tuple
Indices of elements that are non-zero.

## See Also:

## flatnonzero

Return indices that are non-zero in the flattened version of the input array.

```
ndarray.nonzero
```

Equivalent ndarray method.

```
count_nonzero
```

Counts the number of non-zero elements in the input array.

## Examples

```
>>> x = np.eye(3)
>>> x
array([[ 1., 0., 0.],
    [ 0., 1., 0.],
    [ 0., 0., 1.]])
>>> np.nonzero(x)
(array([0, 1, 2]), array([0, 1, 2]))
>>> x[np.nonzero(x)]
array([ 1., 1., 1.])
>>> np.transpose(np.nonzero(x))
array([[0, 0],
    [1, 1],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , np.nonzero( $a>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a = np.array([[1,2,3],[4,5,6],[7, 8,9]])
>>> a > 3
array([[False, False, False],
    [ True, True, True],
    [ True, True, True]], dtype=bool)
>>> np.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the boolean array can also be called.

```
>>> (a > 3).nonzero()
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

numpy . where (condition $[, x, y]$ )
Return elements, either from $x$ or $y$, depending on condition.
If only condition is given, return condition.nonzero().

## Parameters

condition : array_like, bool
When True, yield $x$, otherwise yield $y$.
$\mathbf{x , ~ y}$ : array_like, optional
Values from which to choose. $x$ and $y$ need to have the same shape as condition.

## Returns

out : ndarray or tuple of ndarrays
If both $x$ and $y$ are specified, the output array contains elements of $x$ where condition is True, and elements from $y$ elsewhere.

If only condition is given, return the tuple condition. nonzero(), the indices where condition is True.

## See Also:

```
nonzero, choose
```


## Notes

If $x$ and $y$ are given and input arrays are 1-D, where is equivalent to:

```
[xv if c else yv for (c,xv,yv) in zip(condition,x,y)]
```


## Examples

```
>>> np.where([[True, False], [True, True]],
... [[1, 2], [3, 4]],
... [[9, 8], [7, 6]])
array([[1, 8],
    [3, 4]])
>>> np.where([[0, 1], [1, 0]])
(array([0, 1]), array([1, 0]))
>>> x = np.arange(9.).reshape(3, 3)
>>> np.where( x > 5 )
(array([2, 2, 2]), array([0, 1, 2]))
>> x[np.where( x > 3.0 )] # Note: result is 1D.
array([ 4., 5., 6., 7., 8.])
>>> np.where(x < 5, x, -1) # Note: broadcasting.
array([[ 0., 1., 2.],
    [ 3., 4., -1.],
    [-1., -1., -1.]])
```

numpy.indices (dimensions, dtype $=<$ type 'int'> )

Return an array representing the indices of a grid.
Compute an array where the subarrays contain index values $0,1, \ldots$ varying only along the corresponding axis.

## Parameters

dimensions : sequence of ints
The shape of the grid.
dtype : dtype, optional
Data type of the result.

## Returns

grid : ndarray
The array of grid indices, grid.shape = (len(dimensions), ) + tuple(dimensions).

## See Also:

mgrid, meshgrid

## Notes

The output shape is obtained by prepending the number of dimensions in front of the tuple of dimensions, i.e. if dimensions is a tuple ( $r 0, \ldots, r N-1$ ) of length $N$, the output shape is ( $N, r 0, \ldots, r N-1$ ).

The subarrays grid[k] contains the $\mathrm{N}-\mathrm{D}$ array of indices along the $\mathrm{k}-\mathrm{th}$ axis. Explicitly:

```
grid[k,i0,i1,...,iN-1] = ik
```


## Examples

```
>>> grid = np.indices((2, 3))
>>> grid.shape
(2, 2, 3)
>>> grid[0] # row indices
array([[0, 0, 0],
    [1, 1, 1]])
>>> grid[1] # column indices
array([[0, 1, 2],
    [0, 1, 2]])
```

The indices can be used as an index into an array.

```
>>> x = np.arange (20).reshape(5, 4)
>>> row, col = np.indices((2, 3))
>>> x[row, col]
array([[0, 1, 2],
    [4, 5, 6]])
```

Note that it would be more straightforward in the above example to extract the required elements directly with $x[: 2,: 3]$.

```
numpy.ix_(*args)
```

Construct an open mesh from multiple sequences.
This function takes N 1-D sequences and returns N outputs with N dimensions each, such that the shape is 1 in all but one dimension and the dimension with the non-unit shape value cycles through all N dimensions.

Using ix_ one can quickly construct index arrays that will index the cross product. $a\left[n p . i x \_([1,3],[2,5])\right]$ returns the array $[[a[1,2] a[1,5]],[a[3,2] a[3,5]]]$.

## Parameters

args : 1-D sequences

## Returns

out : tuple of ndarrays
N arrays with N dimensions each, with N the number of input sequences. Together these arrays form an open mesh.

## See Also:

ogrid, mgrid, meshgrid

## Examples

```
>>> a = np.arange(10).reshape(2, 5)
>>> a
array([[0, 1, 2, 3, 4],
    [5, 6, 7, 8, 9]])
>>> ixgrid = np.ix_([0,1], [2,4])
>>> ixgrid
(array([[0],
    [1]]), array([[2, 4]]))
>>> ixgrid[0].shape, ixgrid[1].shape
((2, 1), (1, 2))
>>> a[ixgrid]
```

```
array([[2, 4],
    [7, 9]])
```

numpy.ogrid
$n d \_$grid instance which returns an open multi-dimensional "meshgrid".
An instance of numpy.lib.index_tricks.nd_grid which returns an open (i.e. not fleshed out) meshgrid when indexed, so that only one dimension of each returned array is greater than 1 . The dimension and number of the output arrays are equal to the number of indexing dimensions. If the step length is not a complex number, then the stop is not inclusive.

However, if the step length is a complex number (e.g. 5j), then the integer part of its magnitude is interpreted as specifying the number of points to create between the start and stop values, where the stop value is inclusive.

## Returns <br> mesh-grid 'ndarrays' with only one dimension :math:'neq 1' :

## See Also:

np.lib.index_tricks.nd_grid
class of ogrid and mgrid objects
mgrid
like ogrid but returns dense (or fleshed out) mesh grids
$r_{-}$
array concatenator

## Examples

```
        >>> from numpy import ogrid
        >>> ogrid[-1:1:5j]
        array([-1. , -0.5, 0. , 0.5, 1. ])
        >>> ogrid[0:5,0:5]
        [array([[0],
            [1],
            [2],
            [3],
            [4]]), array([[0, 1, 2, 3, 4]])]
```

numpy.ravel_multi_index (multi_index, dims, mode='raise', order=' 'C')

Converts a tuple of index arrays into an array of flat indices, applying boundary modes to the multi-index.

## Parameters

multi_index : tuple of array_like
A tuple of integer arrays, one array for each dimension.
dims : tuple of ints
The shape of array into which the indices from multi_index apply.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices are handled. Can specify either one mode or a tuple of modes, one mode per index.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range

In 'clip' mode, a negative index which would normally wrap will clip to 0 instead.
order : \{ 'C', 'F' \}, optional
Determines whether the multi-index should be viewed as indexing in C (row-major) order or FORTRAN (column-major) order.

## Returns

raveled_indices : ndarray
An array of indices into the flattened version of an array of dimensions dims.

## See Also:

```
unravel_index
```


## Notes

New in version 1.6.0.

## Examples

```
>>> arr = np.array([[3,6,6],[4,5,1]])
>>> np.ravel_multi_index(arr, (7,6))
array([22, 41, 37])
>>> np.ravel_multi_index(arr, (7,6), order=' F')
array([31, 41, 13])
>>> np.ravel_multi_index(arr, (4,6), mode='clip')
array([22, 23, 19])
>>> np.ravel_multi_index(arr, (4,4), mode=('clip','wrap'))
array([12, 13, 13])
>>> np.ravel_multi_index((3,1,4,1), (6,7,8,9))
1621
```

numpy.unravel_index (indices, dims, order='C')
Converts a flat index or array of flat indices into a tuple of coordinate arrays.

## Parameters

indices : array_like
An integer array whose elements are indices into the flattened version of an array of dimensions dims. Before version 1.6.0, this function accepted just one index value.
dims : tuple of ints
The shape of the array to use for unraveling indices.
order : \{ 'C', 'F'\}, optional
New in version 1.6.0. Determines whether the indices should be viewed as indexing in C (row-major) order or FORTRAN (column-major) order.

## Returns

unraveled_coords : tuple of ndarray
Each array in the tuple has the same shape as the indices array.

## See Also:

```
ravel_multi_index
```


## Examples

```
>>> np.unravel_index([22, 41, 37], (7,6))
    (array([3, 6, 6]), array([4, 5, 1]))
>>> np.unravel_index([31, 41, 13], (7,6), order='F')
    (array([3, 6, 6]), array([4, 5, 1]))
>>> np.unravel_index(1621, (6,7,8,9))
(3, 1, 4, 1)
```

numpy.diag_indices ( $n$, ndim=2)

Return the indices to access the main diagonal of an array.
This returns a tuple of indices that can be used to access the main diagonal of an array $a$ with a. ndim $>=2$ dimensions and shape $(\mathrm{n}, \mathrm{n}, \ldots, \mathrm{n})$. For a. ndim $=2$ this is the usual diagonal, for a.ndim $>2$ this is the set of indices to access a [i, i, ..., i] for $i=[0 \ldots n-1]$.

## Parameters

$\mathbf{n}$ : int
The size, along each dimension, of the arrays for which the returned indices can be used.
ndim : int, optional
The number of dimensions.

## See Also:

```
diag_indices_from
```


## Notes

New in version 1.4.0.

## Examples

Create a set of indices to access the diagonal of a $(4,4)$ array:

```
>>> di = np.diag_indices(4)
>>> di
(array([0, 1, 2, 3]), array([0, 1, 2, 3]))
>>> a = np.arange(16).reshape(4, 4)
>>> a
array([[ 0, 1, 2, 3],
    [4, 5, 6, 7],
    [ 8, 9, 10, 11],
    [12, 13, 14, 15]])
>>> a[di] = 100
>>> a
array([[100, 1, 2, 3],
    [ 4, 100, 6, 7],
    [ 8, 9, 100, 11],
    [ 12, 13, 14, 100]])
```

Now, we create indices to manipulate a 3-D array:

```
>>> d3 = np.diag_indices(2, 3)
>>> d3
(array([0, 1]), array([0, 1]), array([0, 1]))
```

And use it to set the diagonal of an array of zeros to 1 :

```
>>> a = np.zeros((2, 2, 2), dtype=np.int)
>>> a[d3] = 1
>>> a
array([[[1, 0],
    [0, 0]],
    [[0, 0],
        [0, 1]]])
```

numpy.diag_indices_from (arr)
Return the indices to access the main diagonal of an n-dimensional array.
See diag_indices for full details.

## Parameters

arr : array, at least 2-D

## See Also:

```
diag_indices
```


## Notes

New in version 1.4.0
numpy.mask_indices ( $n$, mask_func, $k=0$ )
Return the indices to access ( $\mathrm{n}, \mathrm{n}$ ) arrays, given a masking function.
Assume mask_func is a function that, for a square array a of size ( $\mathrm{n}, \mathrm{n}$ ) with a possible offset argument $k$, when called as mask_func ( $\mathrm{a}, \mathrm{k}$ ) returns a new array with zeros in certain locations (functions like triu or tril do precisely this). Then this function returns the indices where the non-zero values would be located.

## Parameters

$\mathbf{n}$ : int
The returned indices will be valid to access arrays of shape ( $n, n$ ).
mask_func : callable
A function whose call signature is similar to that of triu, tril. That is, mask_func ( x ,
$k$ ) returns a boolean array, shaped like $x . k$ is an optional argument to the function.
k: scalar
An optional argument which is passed through to mask_func. Functions like triu, tril take a second argument that is interpreted as an offset.

## Returns

indices : tuple of arrays.
The $n$ arrays of indices corresponding to the locations where mask_func (np.ones ( $n, n$ ) ), k) is True.

## See Also:

triu,tril,triu_indices,tril_indices

## Notes

New in version 1.4.0.

## Examples

These are the indices that would allow you to access the upper triangular part of any $3 \times 3$ array:

```
>>> iu = np.mask_indices(3, np.triu)
```

For example, if $a$ is a $3 \times 3$ array:

```
>>> a = np.arange(9).reshape(3, 3)
>>> a
array([[0, 1, 2],
    [3, 4, 5],
    [6, 7, 8]])
>>> a[iu]
array([0, 1, 2, 4, 5, 8])
```

An offset can be passed also to the masking function. This gets us the indices starting on the first diagonal right of the main one:

```
>>> iu1 = np.mask_indices(3, np.triu, 1)
```

with which we now extract only three elements:

```
>>> a[iul]
```

array([1, 2, 5])
numpy.tril_indices ( $n, k=0$ )
Return the indices for the lower-triangle of an ( $\mathrm{n}, \mathrm{n}$ ) array.

## Parameters

$\mathbf{n}$ : int
The row dimension of the square arrays for which the returned indices will be valid.
$\mathbf{k}$ : int, optional
Diagonal offset (see tril for details).

## Returns

inds : tuple of arrays
The indices for the triangle. The returned tuple contains two arrays, each with the indices along one dimension of the array.

## See Also:

triu_indices
similar function, for upper-triangular.
mask_indices
generic function accepting an arbitrary mask function.
tril,triu

## Notes

New in version 1.4.0.

## Examples

Compute two different sets of indices to access 4 x 4 arrays, one for the lower triangular part starting at the main diagonal, and one starting two diagonals further right:

```
>>> il1 = np.tril_indices(4)
>>> il2 = np.tril_indices(4, 2)
```

Here is how they can be used with a sample array:

```
>>> a = np.arange(16).reshape(4, 4)
>>> a
array([[ 0, 1, 2, 3],
    [ 4, 5, 6, 7],
    [ 8, 9, 10, 11],
    [12, 13, 14, 15]])
```

Both for indexing:

```
>>> a[il1]
array([ 0, 4, 5, 8, 9, 10, 12, 13, 14, 15])
```

And for assigning values:

```
>>> a[il1] = -1
>>> a
array([[-1, 1, 2, 3],
    [-1, -1, 6, 7],
    [-1, -1, -1, 11],
    [-1, -1, -1, -1]])
```

These cover almost the whole array (two diagonals right of the main one):

```
>>> a[il2] = -10
>>> a
array([[-10, -10, -10, 3],
    [-10, -10, -10, -10],
    [-10, -10, -10, -10],
    [-10, -10, -10, -10]])
```

numpy.tril_indices_from (arr, $k=0$ )

Return the indices for the lower-triangle of arr.
See tril_indices for full details.

## Parameters

arr : array_like
The indices will be valid for square arrays whose dimensions are the same as arr.
k: int, optional
Diagonal offset (see tril for details).

## See Also:

tril_indices,tril

## Notes

New in version 1.4.0.
numpy.triu_indices ( $n, k=0$ )
Return the indices for the upper-triangle of an ( $\mathrm{n}, \mathrm{n}$ ) array.

## Parameters

$\mathbf{n}$ : int
The size of the arrays for which the returned indices will be valid.
$\mathbf{k}$ : int, optional

Diagonal offset (see triu for details).

## Returns

inds : tuple of arrays
The indices for the triangle. The returned tuple contains two arrays, each with the indices along one dimension of the array.

## See Also:

tril_indices
similar function, for lower-triangular.
mask_indices
generic function accepting an arbitrary mask function.
triu, tril

## Notes

New in version 1.4.0.

## Examples

Compute two different sets of indices to access $4 \times 4$ arrays, one for the upper triangular part starting at the main diagonal, and one starting two diagonals further right:

```
>>> iul = np.triu_indices(4)
>>> iu2 = np.triu_indices(4, 2)
```

Here is how they can be used with a sample array:

```
>>> a = np.arange(16).reshape(4, 4)
>>> a
array([[ 0, 1, 2, 3],
    [ 4, 5, 6, 7],
    [ 8, 9, 10, 11],
    [12, 13, 14, 15]])
```

Both for indexing:

```
>>> a[iu1]
array([ 0, 1, 2, 3, 5, 6, 7, 10, 11, 15])
```

And for assigning values:

```
>>> a[iul] = -1
>>> a
array([[-1, -1, -1, -1],
    [ 4, -1, -1, -1],
    [ 8, 9, -1, -1],
    [12, 13, 14, -1]])
```

These cover only a small part of the whole array (two diagonals right of the main one):

```
>>> a[iu2] = -10
>>> a
array([[ -1, -1, -10, -10],
    [ 4, -1, -1, -10],
    [ 8, 9, -1, -1],
    [ 12, 13, 14, -1]])
```

```
numpy.triu_indices_from(arr, k=0)
```

Return the indices for the upper-triangle of an ( $n, n$ ) array.
See triu_indices for full details.

## Parameters

arr : array_like
The indices will be valid for square arrays whose dimensions are the same as arr.
k: int, optional
Diagonal offset (see triu for details).

## See Also:

triu_indices, triu

## Notes

New in version 1.4.0.

### 3.3.2 Indexing-like operations

```
take(a, indices[, axis, out, mode]) Take elements from an array along an axis.
choose(a, choices[, out, mode]) Construct an array from an index array and a set of arrays to choose from.
compress(condition, a[, axis, out])
diag(v[, k])
diagonal(a[, offset, axis1, axis2]) Return specified diagonals.
Return selected slices of an array along given axis.
Extract a diagonal or construct a diagonal array.
select(condlist, choicelist[, default]) Return an array drawn from elements in choicelist, depending on conditions.
```

numpy.take ( $a$, indices, axis=None, out=None, mode='raise')

Take elements from an array along an axis.
This function does the same thing as "fancy" indexing (indexing arrays using arrays); however, it can be easier to use if you need elements along a given axis.

## Parameters

a : array_like
The source array.
indices : array_like
The indices of the values to extract.
axis : int, optional
The axis over which to select values. By default, the flattened input array is used.
out : ndarray, optional
If provided, the result will be placed in this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## Returns

subarray : ndarray
The returned array has the same type as $a$.

```
See Also:
ndarray.take
    equivalent method
Examples
>>> a = [4, 3, 5, 7, 6, 8]
>>> indices = [0, 1, 4]
>>> np.take(a, indices)
array([4, 3, 6])
```

In this example if $a$ is an ndarray, "fancy" indexing can be used.

```
>>> a = np.array(a)
>>> a[indices]
array([4, 3, 6])
```

numpy. choose ( $a$, choices, out=None, mode='raise')
Construct an array from an index array and a set of arrays to choose from.
First of all, if confused or uncertain, definitely look at the Examples - in its full generality, this function is less simple than it might seem from the following code description (below ndi = numpy. lib. index_tricks):

```
np.choose(a,c) == np.array([c[a[I]][I] for I in ndi.ndindex(a.shape)]).
```

But this omits some subtleties. Here is a fully general summary:
Given an "index" array ( $a$ ) of integers and a sequence of $n$ arrays (choices), $a$ and each choice array are first broadcast, as necessary, to arrays of a common shape; calling these Ba and Bchoices $[i], i=0, \ldots, n-1$ we have that, necessarily, Ba.shape == Bchoices[i].shape for each $i$. Then, a new array with shape Ba.shape is created as follows:
-if mode=raise (the default), then, first of all, each element of $a$ (and thus $B a$ ) must be in the range $[0$, $n-1$ ]; now, suppose that $i$ (in that range) is the value at the ( $j 0, j 1, \ldots, j m$ ) position in $B a$ - then the value at the same position in the new array is the value in Bchoices $[i]$ at that same position;
-if mode=wrap, values in $a$ (and thus $B a$ ) may be any (signed) integer; modular arithmetic is used to map integers outside the range [ $0, n-1$ ] back into that range; and then the new array is constructed as above;
-if mode $=$ clip, values in $a$ (and thus $B a$ ) may be any (signed) integer; negative integers are mapped to 0 ; values greater than $n-1$ are mapped to $n-l$; and then the new array is constructed as above.

## Parameters

a : int array
This array must contain integers in [0, $n-1]$, where $n$ is the number of choices, unless mode=wrap or mode=clip, in which cases any integers are permissible.
choices : sequence of arrays

Choice arrays. $a$ and all of the choices must be broadcastable to the same shape. If choices is itself an array (not recommended), then its outermost dimension (i.e., the one corresponding to choices.shape[0]) is taken as defining the "sequence".
out : array, optional
If provided, the result will be inserted into this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise' (default), 'wrap', 'clip' \}, optional
Specifies how indices outside [ $0, n-1]$ will be treated:

- 'raise' : an exception is raised
- 'wrap' : value becomes value $\bmod n$
- 'clip' : values $<0$ are mapped to 0 , values $>\mathrm{n}-1$ are mapped to $\mathrm{n}-1$


## Returns

merged_array : array
The merged result.

## Raises

## ValueError: shape mismatch :

If $a$ and each choice array are not all broadcastable to the same shape.

## See Also:

```
ndarray.choose
```

equivalent method

## Notes

To reduce the chance of misinterpretation, even though the following "abuse" is nominally supported, choices should neither be, nor be thought of as, a single array, i.e., the outermost sequence-like container should be either a list or a tuple.

## Examples

```
>>> choices = [[0, 1, 2, 3], [10, 11, 12, 13],
... [20, 21, 22, 23], [30, 31, 32, 33]]
>>> np.choose([2, 3, 1, 0], choices
... # the first element of the result will be the first element of the
... # third (2+1) "array" in choices, namely, 20; the second element
... # will be the second element of the fourth (3+1) choice array, i.e.,
... # 31, etc.
... )
array([20, 31, 12, 3])
>>> np.choose([2, 4, 1, 0], choices, mode='clip') # 4 goes to 3 (4-1)
array([20, 31, 12, 3])
>>> # because there are 4 choice arrays
>>> np.choose([2, 4, 1, 0], choices, mode='wrap') # 4 goes to (4 mod 4)
array([20, 1, 12, 3])
>>> # i.e., 0
```

A couple examples illustrating how choose broadcasts:

```
>>> a = [[1, 0, 1], [0, 1, 0], [1, 0, 1]]
>>> choices = [-10, 10]
>>> np.choose(a, choices)
array([[ 10, -10, 10],
    [-10, 10, -10],
    [ 10, -10, 10]])
>>> # With thanks to Anne Archibald
>>> a = np.array([0, 1]).reshape((2,1,1))
>>> c1 = np.array([1, 2, 3]).reshape((1,3,1))
>>> c2 = np.array([-1, -2, -3, -4, -5]).reshape((1,1,5))
>>> np.choose(a, (c1, c2)) # result is 2x3x5, res[0,:,:]=c1, res[1,:,:]=c2
array([[[ 1, 1, 1, 1, 1],
    [ 2, 2, 2, 2, 2],
    [ 3, 3, 3, 3, 3]],
    [[-1, -2, -3, -4, -5],
    [-1, -2, -3, -4, -5],
    [-1, -2, -3, -4, -5]]])
```

numpy. compress (condition, a, axis=None, out=None)
Return selected slices of an array along given axis.
When working along a given axis, a slice along that axis is returned in output for each index where condition evaluates to True. When working on a 1-D array, compress is equivalent to extract.

## Parameters

condition : 1-D array of bools
Array that selects which entries to return. If len(condition) is less than the size of $a$ along the given axis, then output is truncated to the length of the condition array.
a : array_like
Array from which to extract a part.
axis : int, optional
Axis along which to take slices. If None (default), work on the flattened array.
out : ndarray, optional
Output array. Its type is preserved and it must be of the right shape to hold the output.

## Returns

compressed_array : ndarray
A copy of $a$ without the slices along axis for which condition is false.

## See Also:

take, choose, diag, diagonal, select
ndarray. compress
Equivalent method.
numpy. doc. ufuncs
Section "Output arguments"

## Examples

```
>>> a = np.array([[1, 2], [3, 4], [5, 6]])
>>> a
array([[1, 2],
```

```
    3, 4],
    [5, 6]])
>>> np.compress([0, 1], a, axis=0)
array([[3, 4]])
>>> np.compress([False, True, True], a, axis=0)
array([[3, 4],
    [5, 6]])
>>> np.compress([False, True], a, axis=1)
array([[2],
    [4],
    [6]])
```

Working on the flattened array does not return slices along an axis but selects elements.

```
>>> np.compress([False, True], a)
array([2])
numpy.diag ( v, k=0)
```

Extract a diagonal or construct a diagonal array

## Parameters

$\mathbf{v}$ : array_like
If $v$ is a 2-D array, return a copy of its $k$-th diagonal. If $v$ is a 1-D array, return a 2-D array with $v$ on the $k$-th diagonal.
$\mathbf{k}$ : int, optional
Diagonal in question. The default is 0 . Use $k>0$ for diagonals above the main diagonal, and $k<0$ for diagonals below the main diagonal.

## Returns

 out : ndarrayThe extracted diagonal or constructed diagonal array.

## See Also:

diagonal
Return specified diagonals.
diagflat
Create a 2-D array with the flattened input as a diagonal.

## trace

Sum along diagonals.

## triu

Upper triangle of an array.
tril
Lower triange of an array.

## Examples

```
>>> x = np.arange(9).reshape((3,3))
>>> x
array([[0, 1, 2],
                    [3, 4, 5],
                    [6, 7, 8]])
```

```
>>> np.diag(x)
array([0, 4, 8])
>>> np.diag(x, k=1)
array([1, 5])
>>> np.diag(x, k=-1)
array([3, 7])
>>> np.diag(np.diag(x))
array([[0, 0, 0],
    [0, 4, 0],
    [0, 0, 8]])
```

numpy.diagonal (a, offset $=0$, axis $1=0$, axis $2=1$ )

Return specified diagonals.
If $a$ is 2-D, returns the diagonal of $a$ with the given offset, i.e., the collection of elements of the form a [i, i+offset]. If $a$ has more than two dimensions, then the axes specified by axisl and axis 2 are used to determine the 2-D sub-array whose diagonal is returned. The shape of the resulting array can be determined by removing axis1 and axis2 and appending an index to the right equal to the size of the resulting diagonals.

## Parameters

a : array_like
Array from which the diagonals are taken.
offset : int, optional
Offset of the diagonal from the main diagonal. Can be positive or negative. Defaults to main diagonal (0).
axis1 : int, optional
Axis to be used as the first axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults to first axis (0).
axis2 : int, optional
Axis to be used as the second axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults to second axis (1).

## Returns

array_of_diagonals : ndarray
If $a$ is 2-D, a 1-D array containing the diagonal is returned. If the dimension of $a$ is larger, then an array of diagonals is returned, "packed" from left-most dimension to right-most (e.g., if $a$ is 3-D, then the diagonals are "packed" along rows).

## Raises

ValueError :
If the dimension of $a$ is less than 2 .

## See Also:

diag
MATLAB work-a-like for 1-D and 2-D arrays.
diagflat
Create diagonal arrays.
trace
Sum along diagonals.

## Examples

```
>>> a = np.arange(4).reshape(2,2)
>>> a
array([[0, 1],
    [2, 3]])
>>> a.diagonal()
array([0, 3])
>>> a.diagonal(1)
array([1])
```

A 3-D example:

```
>>> a = np.arange(8).reshape(2,2,2); a
array([[[0, 1],
    [2, 3]],
    [[4, 5],
    [6, 7]]])
>>> a.diagonal(0, # Main diagonals of two arrays created by skipping
... 0, # across the outer(left)-most axis last and
... 1) # the "middle" (row) axis first.
array([[0, 6],
    [1, 7]])
```

The sub-arrays whose main diagonals we just obtained; note that each corresponds to fixing the right-most (column) axis, and that the diagonals are "packed" in rows.

```
>>> a[:,:,0] # main diagonal is [0 6]
array([[0, 2],
    [4, 6]])
>>> a[:,:,1] # main diagonal is [1 7]
array([[1, 3],
    [5, 7]])
```

numpy.select (condlist, choicelist, default=0)

Return an array drawn from elements in choicelist, depending on conditions.

## Parameters

condlist : list of bool ndarrays
The list of conditions which determine from which array in choicelist the output elements are taken. When multiple conditions are satisfied, the first one encountered in condlist is used.
choicelist : list of ndarrays
The list of arrays from which the output elements are taken. It has to be of the same length as condlist.
default : scalar, optional
The element inserted in output when all conditions evaluate to False.

## Returns

output : ndarray
The output at position $m$ is the $m$-th element of the array in choicelist where the $m$-th element of the corresponding array in condlist is True.

## See Also:

## where

Return elements from one of two arrays depending on condition.

```
take, choose, compress, diag, diagonal
```


## Examples

```
>>> x = np.arange(10)
>>> condlist = [x<3, x>5]
>>> choicelist = [x, x**2]
>>> np.select(condlist, choicelist)
array([ 0, 1, 2, 0, 0, 0, 36, 49, 64, 81])
```


### 3.3.3 Inserting data into arrays

$$
\begin{array}{ll}
\hline \text { place(arr, mask, vals) } & \text { Change elements of an array based on conditional and input values. } \\
\text { put(a, ind, v[, mode]) } & \text { Replaces specified elements of an array with given values. } \\
\text { putmask(a, mask, values) } & \text { Changes elements of an array based on conditional and input values. } \\
\text { fill_diagonal(a, val) } & \text { Fill the main diagonal of the given array of any dimensionality. } \\
\hline
\end{array}
$$

numpy.place (arr, mask, vals)
Change elements of an array based on conditional and input values.
Similar to np. putmask (arr, mask, vals), the difference is that place uses the first N elements of vals, where N is the number of True values in mask, while putmask uses the elements where mask is True.

Note that extract does the exact opposite of place.

## Parameters

arr : array_like
Array to put data into.
mask : array_like
Boolean mask array. Must have the same size as $a$.
vals: 1-D sequence
Values to put into $a$. Only the first N elements are used, where N is the number of True values in mask. If vals is smaller than N it will be repeated.

## See Also:

putmask, put, take, extract

## Examples

```
>>> arr = np.arange(6).reshape (2, 3)
>>> np.place(arr, arr>2, [44, 55])
>>> arr
array([[ 0, 1, 2],
    [44, 55, 44]])
```

numpy .put ( $a$, ind, $v$, mode $=$ 'raise')
Replaces specified elements of an array with given values.
The indexing works on the flattened target array. put is roughly equivalent to:

```
a.flat[ind] = v
```


## Parameters

a : ndarray
Target array.
ind : array_like
Target indices, interpreted as integers.
$\mathbf{v}$ : array_like
Values to place in $a$ at target indices. If $v$ is shorter than ind it will be repeated as necessary.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' - raise an error (default)
- 'wrap' - wrap around
- 'clip' - clip to the range
'clip' mode means that all indices that are too large are replaced by the index that addresses the last element along that axis. Note that this disables indexing with negative numbers.


## See Also:

putmask, place

## Examples

```
>>> a = np.arange(5)
>>> np.put(a, [0, 2], [-44, -55])
>>> a
array([-44, 1, -55, 3, 4])
>>> a = np.arange(5)
>>> np.put(a, 22, -5, mode='clip')
>>> a
array([ 0, 1, 2, 3, -5])
```

numpy.putmask (a, mask, values)
Changes elements of an array based on conditional and input values.
Sets a.flat[n] = values[n] for each $n$ where mask.flat [n]==True.
If values is not the same size as $a$ and mask then it will repeat. This gives behavior different from a [mask] = values.

## Parameters

a : array_like
Target array.
mask : array_like
Boolean mask array. It has to be the same shape as $a$.
values : array_like
Values to put into $a$ where mask is True. If values is smaller than $a$ it will be repeated.

## See Also:

```
place, put,take
```


## Examples

```
>>> x = np.arange (6).reshape (2, 3)
>>> np.putmask(x, x>2, x**2)
>>> x
array([[ 0, 1, 2],
    [ 9, 16, 25]])
```

If values is smaller than $a$ it is repeated:

```
>>> x = np.arange(5)
>>> np.putmask(x, x>1, [-33, -44])
>>> x
array([ 0, 1, -33, -44, -33])
```

numpy.fill_diagonal ( $a$, val)
Fill the main diagonal of the given array of any dimensionality.
For an array $a$ with a.ndim $>2$, the diagonal is the list of locations with indices a[i, i, ..., i] all identical. This function modifies the input array in-place, it does not return a value.

## Parameters

a : array, at least 2-D.
Array whose diagonal is to be filled, it gets modified in-place.
val : scalar
Value to be written on the diagonal, its type must be compatible with that of the array a.

## See Also:

```
diag_indices,diag_indices_from
```


## Notes

New in version 1.4.0. This functionality can be obtained via diag_indices, but internally this version uses a much faster implementation that never constructs the indices and uses simple slicing.

## Examples

```
>>> a = np.zeros((3, 3), int)
>>> np.fill_diagonal(a, 5)
>>> a
array([[5, 0, 0],
    [0, 5, 0],
    [0, 0, 5]])
```

The same function can operate on a 4-D array:

```
>>> a = np.zeros((3, 3, 3, 3), int)
>>> np.fill_diagonal(a, 4)
```

We only show a few blocks for clarity:

```
>>> a[0, 0]
array([[4, 0, 0],
    [0, 0, 0],
    [0, 0, 0]])
```

```
>>> a[1, 1]
array([[0, 0, 0],
    [0, 4, 0],
    [0, 0, 0]])
>>> a[2, 2]
array([[0, 0, 0],
    [0, 0, 0],
    [0, 0, 4]])
```


### 3.3.4 Iterating over arrays

| nditer | Efficient multi-dimensional iterator object to iterate over arrays. |
| :--- | :--- |
| ndenumerate(arr) | Multidimensional index iterator. |
| ndindex(*args) | An N-dimensional iterator object to index arrays. |
| flatiter | Flat iterator object to iterate over arrays. |

class numpy. nditer
Efficient multi-dimensional iterator object to iterate over arrays.

## Parameters

op : ndarray or sequence of array_like
The array(s) to iterate over.
flags : sequence of str, optional
Flags to control the behavior of the iterator.

- "buffered" enables buffering when required.
- "c_index" causes a C-order index to be tracked.
- "f_index" causes a Fortran-order index to be tracked.
- "multi_index" causes a multi-index, or a tuple of indices with one per iteration dimension, to be tracked.
- "common_dtype" causes all the operands to be converted to a common data type, with copying or buffering as necessary
- "delay_bufalloc" delays allocation of the buffers until a reset() call is made. Allows "allocate" operands to be initialized before their values are copied into the buffers.
- "external_loop" causes the values given to be one-dimensional arrays with multiple values instead of zero-dimensional arrays.
- "grow_inner" allows the value array sizes to be made larger than the buffer size when both "buffered" and "external_loop" is used.
- "ranged" allows the iterator to be restricted to a sub-range of the iterindex values.
- "refs_ok" enables iteration of reference types, such as object arrays.
- "reduce_ok" enables iteration of "readwrite" operands which are broadcasted, also known as reduction operands.
- "zerosize_ok" allows itersize to be zero.
op_flags : list of list of str, optional
This is a list of flags for each operand. At minimum, one of "readonly", "readwrite", or "writeonly" must be specified.
- "readonly" indicates the operand will only be read from.
- "readwrite" indicates the operand will be read from and written to.
- "writeonly" indicates the operand will only be written to.
- "no_broadcast" prevents the operand from being broadcasted.
- "contig" forces the operand data to be contiguous.
- "aligned" forces the operand data to be aligned.
- "nbo" forces the operand data to be in native byte order.
- "copy" allows a temporary read-only copy if required.
- "updateifcopy" allows a temporary read-write copy if required.
- "allocate" causes the array to be allocated if it is None in the op parameter.
- "no_subtype" prevents an "allocate" operand from using a subtype.
op_dtypes : dtype or tuple of dtype(s), optional
The required data type(s) of the operands. If copying or buffering is enabled, the data will be converted to/from their original types.
order : \{ 'C', 'F', 'A', or 'K' \}, optional
Controls the iteration order. 'C' means $C$ order, ' $F$ ' means Fortran order, ' $A$ ' means ' $F$ ' order if all the arrays are Fortran contiguous, ' C ' order otherwise, and ' K ' means as close to the order the array elements appear in memory as possible. This also affects the element memory order of "allocate" operands, as they are allocated to be compatible with iteration order. Default is ' K '.
casting : \{ 'no', 'equiv', 'safe', 'same_kind', 'unsafe' \}, optional
Controls what kind of data casting may occur when making a copy or buffering. Setting this to 'unsafe' is not recommended, as it can adversely affect accumulations.
- 'no' means the data types should not be cast at all.
- 'equiv' means only byte-order changes are allowed.
- 'safe' means only casts which can preserve values are allowed.
- 'same_kind' means only safe casts or casts within a kind, like float64 to float32, are allowed.
- 'unsafe' means any data conversions may be done.
op_axes : list of list of ints, optional
If provided, is a list of ints or None for each operands. The list of axes for an operand is a mapping from the dimensions of the iterator to the dimensions of the operand. A value of -1 can be placed for entries, causing that dimension to be treated as "newaxis".
itershape : tuple of ints, optional
The desired shape of the iterator. This allows "allocate" operands with a dimension mapped by op_axes not corresponding to a dimension of a different operand to get a value not equal to 1 for that dimension.
buffersize : int, optional
When buffering is enabled, controls the size of the temporary buffers. Set to 0 for the default value.


## Notes

nditer supersedes flatiter. The iterator implementation behind nditer is also exposed by the Numpy C API.
The Python exposure supplies two iteration interfaces, one which follows the Python iterator protocol, and another which mirrors the C-style do-while pattern. The native Python approach is better in most cases, but if you need the iterator's coordinates or index, use the C-style pattern.

## Examples

Here is how we might write an iter_add function, using the Python iterator protocol:

```
def iter_add_py(x, y, out=None):
    addop = np.add
    it = np.nditer([x, y, out], [],
    [['readonly'], ['readonly'], ['writeonly','allocate']])
    for (a, b, c) in it
        addop(a, b, out=c)
    return it.operands[2]
```

Here is the same function, but following the C-style pattern:

```
def iter_add(x, y, out=None):
    addop = np.add
    it = np.nditer([x, y, out], [],
            [['readonly'], ['readonly'], ['writeonly','allocate']])
    while not it.finished:
        addop(it[0], it[1], out=it[2])
        it.iternext()
    return it.operands[2]
```

Here is an example outer product function:

```
def outer_it(x, y, out=None):
    mulop = np.multiply
    it = np.nditer([x, y, out], ['external_loop'],
            [['readonly'], ['readonly'], ['writeonly', 'allocate']],
            op_axes=[range(x.ndim) +[-1]*y.ndim,
                    [-1]*x.ndim+range(y.ndim),
                    None])
    for (a, b, c) in it:
        mulop(a, b, out=c)
    return it.operands[2]
>>> a = np.arange(2)+1
>>> b = np.arange (3) +1
>>> outer_it(a,b)
array([[1, 2, 3],
    [2, 4, 6]])
```

Here is an example function which operates like a "lambda" ufunc:

```
def luf(lamdaexpr, *args, **kwargs):
    "luf(lambdaexpr, op1, ..., opn, out=None, order='K', casting='safe', buffersize=0)"
    nargs = len(args)
```

```
    op = (kwargs.get('out',None),) + args
    it = np.nditer(op, ['buffered','external_loop'],
        [['writeonly','allocate','no_broadcast']] +
        [['readonly','nbo',' aligned']] *nargs,
    order=kwargs.get ('order','K'),
    casting=kwargs.get('casting','safe'),
    buffersize=kwargs.get('buffersize',0))
while not it.finished:
    it[0] = lamdaexpr(*it[1:])
    it.iternext()
return it.operands[0]
>>> a = np.arange(5)
>>> b = np.ones(5)
>>> luf(lambda i,j:i*i + j/2, a, b)
array([ 0.5, 1.5, 4.5, 9.5, 16.5])
```


## Attributes

```
dtypes
finished
has_delayed_bufalloc
has_index
has_multi_index
iterationneedsapi
iterindex
itersize
ndim(a) Return the number of dimensions of an array.
nop
operands
shape(a) Return the shape of an array.
```


## Methods

```
copy(a) Return an array copy of the given object.
debug_print
enable_external_loop
iternext
next
remove_axis
remove_multi_index
reset
```

numpy. copy (a)

Return an array copy of the given object.

## Parameters

a : array_like
Input data.

## Returns

arr : ndarray
Array interpretation of $a$.

## Notes

This is equivalent to

```
>>> np.array(a, copy=True)
```


## Examples

Create an array $x$, with a reference $y$ and a copy $z$ :

```
>>> x = np.array([1, 2, 3])
>>> y = x
>>> z = np.copy(x)
```

Note that, when we modify $x$, y changes, but not z:

```
>>> x[0] = 10
>>> x[0] == y[0]
True
>>> x[0] == z[0]
False
```

class numpy . ndenumerate (arr)
Multidimensional index iterator.
Return an iterator yielding pairs of array coordinates and values.

## Parameters

a : ndarray
Input array.

## See Also:

ndindex, flatiter

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> for index, x in np.ndenumerate(a):
... print index, x
(0, 0) 1
(0, 1) 2
(1, 0) 3
(1, 1) 4
```


## Methods

next
class numpy.ndindex (*args)
An N -dimensional iterator object to index arrays.
Given the shape of an array, an ndindex instance iterates over the N-dimensional index of the array. At each iteration a tuple of indices is returned, the last dimension is iterated over first.

## Parameters

'*args' : ints
The size of each dimension of the array.

## See Also:

```
ndenumerate, flatiter
```


## Examples

```
>>> for index in np.ndindex(3, 2, 1):
... print index
(0, 0, 0)
(0, 1, 0)
(1, 0, 0)
(1, 1, 0)
(2, 0, 0)
(2, 1, 0)
```

Methods
ndincr
next
class numpy.flatiter
Flat iterator object to iterate over arrays.
A flatiter iterator is returned by $x . f l a t$ for any array $x$. It allows iterating over the array as if it were a 1-D array, either in a for-loop or by calling its next method.

Iteration is done in C-contiguous style, with the last index varying the fastest. The iterator can also be indexed using basic slicing or advanced indexing.

## See Also:

```
ndarray.flat
```

Return a flat iterator over an array.

```
ndarray.flatten
```

Returns a flattened copy of an array.

## Notes

A flatiter iterator can not be constructed directly from Python code by calling the flatiter constructor.

## Examples

```
>>> x = np.arange (6).reshape (2, 3)
>>> fl = x.flat
>>> type(fl)
<type 'numpy.flatiter'>
>>> for item in fl:
... print item
0
1
2
3
4
5
>>> fl[2:4]
array([2, 3])
```


## Methods

copy(a) Return an array copy of the given object. next
numpy. copy (a)
Return an array copy of the given object.

## Parameters

a : array_like
Input data.

## Returns

arr : ndarray
Array interpretation of $a$.

## Notes

This is equivalent to

```
>>> np.array(a, copy=True)
```


## Examples

Create an array x , with a reference y and a copy z :

```
>>> x = np.array([1, 2, 3])
>>> y = x
>>> z = np.copy(x)
```

Note that, when we modify $x$, $y$ changes, but not $z$ :

```
>>> x[0] = 10
>>> x[0] == y[0]
True
>>> x[0] == z[0]
False
```


### 3.4 Data type routines

```
can_cast(from, totype) Returns True if cast between data types can occur according to the
promote_types(type1, Returns the data type with the smallest size and smallest scalar kind to which both
type2) type1 and type2 may be safely cast.
min_scalar_type(a) For scalar a, returns the data type with the smallest size and smallest scalar kind
    which can hold its value.
result_type(*arrays_andRdtupes)the type that results from applying the NumPy
common_type(*arrays) Return a scalar type which is common to the input arrays.
obj2sctype(rep[, Return the scalar dtype or NumPy equivalent of Python type of an object.
default])
```

numpy. can_cast (from, totype, casting = 'safe')
Returns True if cast between data types can occur according to the casting rule. If from is a scalar or array scalar, also returns True if the scalar value can be cast without overflow or truncation to an integer.

## Parameters

from : dtype, dtype specifier, scalar, or array
Data type, scalar, or array to cast from.
totype : dtype or dtype specifier
Data type to cast to.
casting : casting rule
May be any of 'no', 'equiv', 'safe', 'same_kind', or 'unsafe'.

## Returns

 out : boolTrue if cast can occur according to the casting rule.

## Examples

Basic examples

```
>>> np.can_cast(np.int32, np.int64)
True
>>> np.can_cast(np.float64, np.complex)
True
>>> np.can_cast(np.complex, np.float)
False
>>> np.can_cast('i8', 'f8')
True
>>> np.can_cast('i8', 'f4')
False
>>> np.can_cast('i4', 'S4')
True
```


## Casting scalars

```
>>> np.can_cast(100, 'il')
True
>>> np.can_cast(150, 'i1')
False
>>> np.can_cast(150, 'ul')
True
>>> np.can_cast(3.5e100, np.float32)
False
>>> np.can_cast(1000.0, np.float32)
True
```

Array scalar checks the value, array does not

```
>>> np.can_cast(np.array(1000.0), np.float32)
True
>>> np.can_cast(np.array([1000.0]), np.float32)
False
```

Using the casting rules

```
>>> np.can_cast('i8', 'i8', 'no')
True
>>> np.can_cast('<i8', '>i8', 'no')
False
>>> np.can_cast('<i8', '>i8', 'equiv')
True
>>> np.can_cast('<i4', '>i8', 'equiv')
False
```

```
>>> np.can_cast('<i4', '>i8', 'safe')
True
>>> np.can_cast('<i8', '>i4', 'safe')
False
>>> np.can_cast('<i8', '>i4', 'same_kind')
True
>>> np.can_cast('<i8', '>u4', 'same_kind')
False
>>> np.can_cast('<i8', '>u4', 'unsafe')
True
```

numpy.promote_types (type1, type2)

Returns the data type with the smallest size and smallest scalar kind to which both type 1 and type 2 may be safely cast. The returned data type is always in native byte order.

## Parameters

type 1: dtype or dtype specifier
First data type.
type2 : dtype or dtype specifier
Second data type.

## Returns

out : dtype
The promoted data type.

## See Also:

```
issctype, issubsctype, issubdtype, obj2sctype, sctype2char, maximum_sctype,
min_scalar_type
```


## Examples

```
>>> np.promote_types('f4', 'f8')
dtype('float64')
>>> np.promote_types('i8', 'f4')
dtype('float64')
>>> np.promote_types('>i8', '<c8')
dtype('complex128')
>>> np.promote_types('i1', 'S8')
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
TypeError: invalid type promotion
```

numpy.min_scalar_type (a)

For scalar a, returns the data type with the smallest size and smallest scalar kind which can hold its value. For non-scalar array a, returns the vector's dtype unmodified.

As a special case, floating point values are not demoted to integers, and complex values are not demoted to floats.

## Parameters

a : scalar or array_like

The value whose minimal data type is to be found.

## Returns

 out : dtypeThe minimal data type.

## See Also:

```
issctype, issubsctype, issubdtype, obj2sctype, sctype2char, maximum_sctype,
promote_types
```

Examples
>>> np.min_scalar_type(10)
dtype('uint8')
>>> np.min_scalar_type(-260)
dtype('int16')
>>> np.min_scalar_type(3.1)
dtype('float16')
>>> np.min_scalar_type(1e50)
dtype('float64')
>>> np.min_scalar_type(np.arange (4,dtype='f8'))
dtype('float64')
numpy.result_type (*arrays_and_dtypes)
Returns the type that results from applying the NumPy type promotion rules to the arguments.
Type promotion in NumPy works similarly to the rules in languages like C++, with some slight differences. When both scalars and arrays are used, the array's type takes precedence and the actual value of the scalar is taken into account.

For example, calculating $3 *$ a, where a is an array of 32 -bit floats, intuitively should result in a 32 -bit float output. If the 3 is a 32 -bit integer, the NumPy rules indicate it can't convert losslessly into a 32-bit float, so a 64-bit float should be the result type. By examining the value of the constant, ' 3 ', we see that it fits in an 8 -bit integer, which can be cast losslessly into the 32-bit float.

## Parameters

arrays_and_dtypes : list of arrays and dtypes
The operands of some operation whose result type is needed.

## Returns <br> out : dtype

The result type.

## Examples

```
>>> np.result_type(3, np.arange(7, dtype='i1'))
dtype('int8')
>>> np.result_type('i4', 'c8')
dtype(' complex128')
>>> np.result_type(3.0, -2)
dtype('float64')
```


## numpy. common_type (*arrays)

Return a scalar type which is common to the input arrays.
The return type will always be an inexact (i.e. floating point) scalar type, even if all the arrays are integer arrays. If one of the inputs is an integer array, the minimum precision type that is returned is a 64-bit floating point dtype.

All input arrays can be safely cast to the returned dtype without loss of information.

## Parameters

array1, array2, ... : ndarrays
Input arrays.

## Returns

out : data type code
Data type code.

## See Also:

dtype, mintypecode
Examples

```
>>> np.common_type(np.arange(2, dtype=np.float32))
<type 'numpy.float32'>
>>> np.common_type(np.arange(2, dtype=np.float32), np.arange(2))
<type 'numpy.float64'>
>>> np.common_type(np.arange(4), np.array([45, 6.j]), np.array([45.0]))
<type 'numpy.complex128'>
```

numpy.obj2sctype (rep, default=None)

Return the scalar dtype or NumPy equivalent of Python type of an object.

## Parameters

rep : any
The object of which the type is returned.
default : any, optional
If given, this is returned for objects whose types can not be determined. If not given, None is returned for those objects.

## Returns

dtype : dtype or Python type
The data type of rep.

## See Also:

sctype2char, issctype, issubsctype, issubdtype, maximum_sctype

## Examples

```
>>> np.obj2sctype(np.int32)
<type 'numpy.int32'>
>>> np.obj2sctype(np.array([1., 2.]))
<type 'numpy.float64'>
>>> np.obj2sctype(np.array([1.j]))
<type 'numpy.complex128'>
```

```
>>> np.obj2sctype(dict)
<type 'numpy.object_'>
>>> np.obj2sctype('string')
<type 'numpy.string_'>
>>> np.obj2sctype(1, default=list)
<type 'list'>
```


### 3.4.1 Creating data types

| dtype <br> format_parser(formats, names, titles[, ...]) | Create a data type object. <br> Class to convert formats, names, titles description to a dtype. |
| :--- | :--- |

class numpy. dtype
Create a data type object.
A numpy array is homogeneous, and contains elements described by a dtype object. A dtype object can be constructed from different combinations of fundamental numeric types.

## Parameters

obj :
Object to be converted to a data type object.
align : bool, optional
Add padding to the fields to match what a C compiler would output for a similar Cstruct. Can be True only if obj is a dictionary or a comma-separated string.
copy : bool, optional
Make a new copy of the data-type object. If False, the result may just be a reference to a built-in data-type object.

## Examples

Using array-scalar type:

```
>>> np.dtype(np.int16)
dtype('int16')
```

Record, one field name 'f1', containing int16:

```
>>> np.dtype([('f1', np.int16)])
dtype([('f1', '<i2')])
```

Record, one field named ' f 1 ', in itself containing a record with one field:

```
>>> np.dtype([('f1', [('f1', np.int16)])])
dtype([('f1', [('f1', '<i2')])])
```

Record, two fields: the first field contains an unsigned int, the second an int32:

```
>>> np.dtype([('f1', np.uint), ('f2', np.int32)])
dtype([('f1', '<u4'), ('f2', '<i4')])
```

Using array-protocol type strings:

```
>>> np.dtype([('a','f8'),('b','S10')])
dtype([('a', '<f8'), ('b', '|S10')])
```

Using comma-separated field formats. The shape is $(2,3)$ :

```
>>> np.dtype("i4, (2,3)f8")
dtype([('f0', '<i4'), ('f1', '<f8', (2, 3))])
```

Using tuples. int is a fixed type, 3 the field's shape. void is a flexible type, here of size 10 :

```
>>> np.dtype([('hello',(np.int,3)),('world',np.void,10)])
dtype([('hello', '<i4', 3), ('world', '|V10')])
```

Subdivide int 16 into 2 int 8 's, called $x$ and $y .0$ and 1 are the offsets in bytes:

```
>>> np.dtype((np.int16, {'x':(np.int8,0), 'y':(np.int8,1)}))
dtype(('<i2', [('x', '|i1'), ('y', '|i1')]))
```

Using dictionaries. Two fields named 'gender' and 'age':

```
>>> np.dtype({'names':['gender','age'], 'formats':['S1',np.uint8]})
dtype([('gender', '|S1'), ('age', '|u1')])
```

Offsets in bytes, here 0 and 25:

```
>>> np.dtype({'surname':('S25',0),'age':(np.uint8,25)})
dtype([('surname', '|S25'), ('age', '|u1')])
```


## Methods

```
newbyteorder
```

class numpy.format_parser (formats, names, titles, aligned=False, byteorder=None)
Class to convert formats, names, titles description to a dtype.
After constructing the format_parser object, the dtype attribute is the converted data-type: dtype = format_parser(formats, names, titles).dtype

## Parameters

formats : str or list of str
The format description, either specified as a string with comma-separated format descriptions in the form ' $\mathrm{f} 8, \mathrm{i} 4, \mathrm{a} 5^{\prime}$, or a list of format description strings in the form ['f8', 'i4', 'a5'].
names : str or list/tuple of str
The field names, either specified as a comma-separated string in the form ' coll, col2, col3', or as a list or tuple of strings in the form [' coll', ' col2', ${ }^{\prime} \mathrm{col} 3^{\prime}$ ]. An empty list can be used, in that case default field names (' f 0 ', ' f 1 ', ...) are used.
titles: sequence
Sequence of title strings. An empty list can be used to leave titles out.
aligned : bool, optional
If True, align the fields by padding as the C-compiler would. Default is False.
byteorder : str, optional
If specified, all the fields will be changed to the provided byte-order. Otherwise, the default byte-order is used. For all available string specifiers, see dtype.newbyteorder.

## See Also:

```
dtype,typename, sctype2char
```

Examples

```
>>> np.format_parser(['f8', 'i4', 'a5'], ['col1', 'col2', 'col3'],
... ['T1', 'T2', 'T3']).dtype
dtype([(('T1', 'col1'), '<f8'), (('T2', 'col2'), '<i4'),
    (('T3', 'Col3'), '|S5')])
```

names and/or titles can be empty lists. If titles is an empty list, titles will simply not appear. If names is empty, default field names will be used.

```
>>> np.format_parser(['f8', 'i4', 'a5'], ['col1', 'col2', 'col3'],
... []).dtype
dtype([('col1', '<f8'), ('col2', '<i4'), ('col3', '|S5')])
>>> np.format_parser(['f8', 'i4', 'a5'], [], []).dtype
dtype([('f0', '<f8'), ('f1', '<i4'), ('f2', '|S5')])
```

Attributes

| dtype | dtype | The converted data-type. |
| :--- | :--- | :--- |

### 3.4.2 Data type information

| finfo | Machine limits for floating point types. |
| :--- | :--- |
| in $f \circ($ type $)$ | Machine limits for integer types. |
| MachAr([float_conv, int_conv, ...]) | Diagnosing machine parameters. |

class numpy.finfo
Machine limits for floating point types.

## Parameters

dtype : float, dtype, or instance
Kind of floating point data-type about which to get information.

## See Also:

MachAr
The implementation of the tests that produce this information.
iinfo
The equivalent for integer data types.

## Notes

For developers of NumPy: do not instantiate this at the module level. The initial calculation of these parameters is expensive and negatively impacts import times. These objects are cached, so calling finfo() repeatedly inside your functions is not a problem.

## Attributes

class numpy.iinfo (type)
Machine limits for integer types.

## Parameters

type : integer type, dtype, or instance

The kind of integer data type to get information about.

## See Also:

## finfo

The equivalent for floating point data types.

## Examples

With types:

```
>>> ii16 = np.iinfo(np.int16)
>>> ii16.min
-32768
>>> ii16.max
32767
>>> ii32 = np.iinfo(np.int32)
>>> ii32.min
-2147483648
>>> ii32.max
2147483647
```

With instances:

```
>>> ii32 = np.iinfo(np.int32(10))
>>> ii32.min
-2147483648
>>> ii32.max
2147483647
```


## Attributes

| $\min (\mathrm{a}[$, axis, out $])$ | Return the minimum of an array or minimum along an axis. |
| :--- | :--- |
| $\max (\mathrm{a}[$, axis, out $])$ | Return the maximum of an array or maximum along an axis. |

class numpy. MachAr (float_conv=<type 'float'>, int_conv=<type 'int'>, float_to_float=<type 'float'>, float_to_str $=<$ function $<l a m b d a>$ at $0 x 20067 f 0>$, title $=$ 'Python floating point number')
Diagnosing machine parameters.

## Parameters

float_conv : function, optional
Function that converts an integer or integer array to a float or float array. Default is float.
int_conv : function, optional
Function that converts a float or float array to an integer or integer array. Default is int.
float_to_float : function, optional
Function that converts a float array to float. Default is float. Note that this does not seem to do anything useful in the current implementation.
float_to_str : function, optional
Function that converts a single float to a string. Default is lambda v:' $\% 24.16 \mathrm{e}^{\prime}$ \% V.
title : str, optional
Title that is printed in the string representation of MachAr.

## See Also:

```
finfo
    Machine limits for floating point types.
iinfo
    Machine limits for integer types.
```


## References

[R1]

## Attributes

| ibeta | int | Radix in which numbers are represented. |
| :---: | :---: | :---: |
| it | int | Number of base-ibeta digits in the floating point mantissa M. |
| machep | int | Exponent of the smallest (most negative) power of ibeta that, added to 1.0 , gives something different from 1.0 |
| eps | float | Floating-point number beta**machep (floating point precision) |
| negep | int | Exponent of the smallest power of ibeta that, substracted from 1.0, gives something different from 1.0. |
| epsneg | float | Floating-point number beta**negep. |
| iexp | int | Number of bits in the exponent (including its sign and bias). |
| minexp | int | Smallest (most negative) power of ibeta consistent with there being no leading zeros in the mantissa. |
| xmin | float | Floating point number beta**minexp (the smallest [in magnitude] usable floating value). |
| maxexp | int | Smallest (positive) power of ibeta that causes overflow. |
| xmax | float | (1-epsneg) * beta**maxexp (the largest [in magnitude] usable floating value). |
| irnd | int | In range (6), information on what kind of rounding is done in addition, and on how underflow is handled. |
| ngrd | int | Number of 'guard digits' used when truncating the product of two mantissas to fit the representation. |
| epsilon | float | Same as eps. |
| tiny | float | Same as xmin. |
| huge | float | Same as xmax. |
| preci- | float | - int (-log10 (eps)) |
| sion resolution | float | - 10** (-precision) |

### 3.4.3 Data type testing

```
issctype(rep)
issubdtype(arg1, arg2)
issubsctype(arg1, arg2)
issubclass_(arg1, arg2)
find_common_type(array_types,
scalar_types)
numpy.issctype (rep)
Determines whether the given object represents a scalar data-type.
```


## Parameters

```
rep : any
```

If rep is an instance of a scalar dtype, True is returned. If not, False is returned.

## Returns

 out : boolBoolean result of check whether rep is a scalar dtype.

## See Also:

issubsctype, issubdtype, obj2sctype, sctype 2 char

## Examples

```
>>> np.issctype(np.int32)
True
>>> np.issctype(list)
False
>>> np.issctype(1.1)
False
```

Strings are also a scalar type:

```
>>> np.issctype(np.dtype('str'))
```

True
numpy.issubdtype (arg1, arg2)
Returns True if first argument is a typecode lower/equal in type hierarchy.

## Parameters

$\arg 1, \arg 2$ : dtype_like dtype or string representing a typecode.
Returns
out : bool

## See Also:

issubsctype, issubclass_
numpy.core.numerictypes
Overview of numpy type hierarchy.

## Examples

```
>>> np.issubdtype('S1', str)
True
>>> np.issubdtype(np.float64, np.float32)
False
```

numpy.issubsctype (arg1, arg2)
Determine if the first argument is a subclass of the second argument.

## Parameters

arg1, arg2 : dtype or dtype specifier
Data-types.

## Returns

out : bool
The result.

## See Also:

```
issctype, issubdtype, obj2sctype
```

Examples

```
>>> np.issubsctype('S8', str)
True
>>> np.issubsctype(np.array([1]), np.int)
True
>>> np.issubsctype(np.array([1]), np.float)
False
```

numpy.issubclass_(arg1, arg2)
Determine if a class is a subclass of a second class.
issubclass_ is equivalent to the Python built-in issubclass, except that it returns False instead of raising a TypeError is one of the arguments is not a class.

## Parameters

$\arg 1$ : class
Input class. True is returned if $\arg 1$ is a subclass of $\arg 2$.
arg2 : class or tuple of classes.
Input class. If a tuple of classes, True is returned if $\arg 1$ is a subclass of any of the tuple elements.

## Returns

out : bool
Whether $\arg 1$ is a subclass of $\arg 2$ or not.

## See Also:

```
issubsctype, issubdtype, issctype
```


## Examples

```
>>> np.issubclass_(np.int32, np.int)
True
>>> np.issubclass_(np.int32, np.float)
False
```

numpy.find_common_type (array_types, scalar_types)

Determine common type following standard coercion rules.

## Parameters

array_types : sequence
A list of dtypes or dtype convertible objects representing arrays.
scalar_types : sequence
A list of dtypes or dtype convertible objects representing scalars.

## Returns

datatype : dtype
The common data type, which is the maximum of array_types ignoring scalar_types, unless the maximum of scalar_types is of a different kind (dtype.kind). If the kind is not understood, then None is returned.

## See Also:

```
dtype, common_type, can_cast, mintypecode
```


## Examples

```
>>> np.find_common_type([], [np.int64, np.float32, np.complex])
dtype('complex128')
>>> np.find_common_type([np.int64, np.float32], [])
dtype('float64')
```

The standard casting rules ensure that a scalar cannot up-cast an array unless the scalar is of a fundamentally different kind of data (i.e. under a different hierarchy in the data type hierarchy) then the array:

```
>>> np.find_common_type([np.float32], [np.int64, np.float64])
dtype('float32')
```

Complex is of a different type, so it up-casts the float in the array_types argument:

```
>>> np.find_common_type([np.float32], [np.complex])
dtype('complex128')
```

Type specifier strings are convertible to dtypes and can therefore be used instead of dtypes:

```
>>> np.find_common_type(['f4', 'f4', 'i4'], ['c8'])
dtype('complex128')
```


### 3.4.4 Miscellaneous

| typename(char) | Return a description for the given data type code. |
| :--- | :--- |
| sctype2char(sctype) | Return the string representation of a scalar dtype. |
| mintypecode(typechars[, typeset, | Return the character for the minimum-size type to which given types can |
| default]) | be safely cast. |

numpy.typename (char)
Return a description for the given data type code.

## Parameters

char : str
Data type code.

## Returns

out : str
Description of the input data type code.

## See Also:

dtype, typecodes

## Examples

```
>>> typechars = ['S1', '?', 'B', 'D', 'G', 'E', 'I', 'H', 'L', 'O', 'Q',
... 'S', 'U', 'V', 'b', 'd', 'g', 'f', 'i', 'h', 'l', 'g']
>>> for typechar in typechars:
... print typechar, ' : ', np.typename(typechar)
...
S1 : character
? : bool
```

```
unsigned char
: complex double precision
: complex long double precision
: complex single precision
: unsigned integer
unsigned short
: unsigned long integer
: object
: unsigned long long integer
string
unicode
void
signed char
double precision
: long precision
single precision
integer
short
long integer
: long long integer
```

numpy.sctype2char (sctype)

Return the string representation of a scalar dtype.

## Parameters

sctype : scalar dtype or object
If a scalar dtype, the corresponding string character is returned. If an object, sctype2char tries to infer its scalar type and then return the corresponding string character.

## Returns

## typechar : str

The string character corresponding to the scalar type.

## Raises

## ValueError :

If sctype is an object for which the type can not be inferred.

## See Also:

```
obj2sctype, issctype, issubsctype, mintypecode
```


## Examples

```
>>> for sctype in [np.int32, np.float, np.complex, np.string_, np.ndarray]:
... print np.sctype2char(sctype)
l
d
D
S
O
>>> x = np.array([1., 2-1.j])
>>> np.sctype2char(x)
'D'
>>> np.sctype2char(list)
'O'
```

numpy .mintypecode (typechars, typeset='GDFgdf', default='d')
Return the character for the minimum-size type to which given types can be safely cast.
The returned type character must represent the smallest size dtype such that an array of the returned type can handle the data from an array of all types in typechars (or if typechars is an array, then its dtype.char).

## Parameters

typechars : list of str or array_like
If a list of strings, each string should represent a dtype. If array_like, the character representation of the array dtype is used.
typeset : str or list of str, optional
The set of characters that the returned character is chosen from. The default set is 'GDFgdf'.
default : str, optional
The default character, this is returned if none of the characters in typechars matches a character in typeset.

## Returns

typechar: str
The character representing the minimum-size type that was found.

## See Also:

dtype, sctype2char, maximum_sctype
Examples

```
>>> np.mintypecode(['d', 'f', 'S'])
'd'
>>> x = np.array([1.1, 2-3.j])
>>> np.mintypecode(x)
'D'
>>> np.mintypecode('abceh', default='G')
'G'
```


### 3.5 Input and output

### 3.5.1 NPZ files

```
load(file[, mmap_mode]) Load a pickled, .npy, or . npz binary file.
save(file, arr) Save an array to a binary file in NumPy . npy format.
savez(file, *args, **kwds) Save several arrays into a single file in uncompressed . npz format.
```

numpy. load (file, mmap_mode=None)

Load a pickled, . npy, or . npz binary file.

## Parameters

file : file-like object or string
The file to read. It must support seek () and read () methods. If the filename extension is.$g \mathrm{z}$, the file is first decompressed.
mmap_mode: \{None, 'r+', 'r', 'w+', 'c'\}, optional :

If not None, then memory-map the file, using the given mode (see numpy .memmap). The mode has no effect for pickled or zipped files. A memory-mapped array is stored on disk, and not directly loaded into memory. However, it can be accessed and sliced like any ndarray. Memory mapping is especially useful for accessing small fragments of large files without reading the entire file into memory.

## Returns

result : array, tuple, dict, etc.
Data stored in the file.

## Raises

IOError :
If the input file does not exist or cannot be read.

## See Also:

```
save, savez, loadtxt
```

memmap
Create a memory-map to an array stored in a file on disk.

## Notes

-If the file contains pickle data, then whatever is stored in the pickle is returned.
-If the file is a . npy file, then an array is returned.
-If the file is a . npz file, then a dictionary-like object is returned, containing \{filename: array\} key-value pairs, one for each file in the archive.

## Examples

Store data to disk, and load it again:

```
>>> np.save('/tmp/123', np.array([[1, 2, 3], [4, 5, 6]]))
>>> np.load('/tmp/123.npy')
array([[1, 2, 3],
    [4, 5, 6]])
```

Mem-map the stored array, and then access the second row directly from disk:

```
>>> X = np.load('/tmp/123.npy', mmap_mode='r')
>>> X[1, :]
memmap([4, 5, 6])
numpy . save (file, arr)
```

Save an array to a binary file in NumPy . npy format.

## Parameters

file : file or str
File or filename to which the data is saved. If file is a file-object, then the filename is unchanged. If file is a string, a . npy extension will be appended to the file name if it does not already have one.
arr : array_like
Array data to be saved.

## See Also:

## savez

Save several arrays into a . npz archive

```
savetxt,load
```


## Notes

For a description of the . npy format, see format.

## Examples

```
>>> from tempfile import TemporaryFile
>>> outfile = TemporaryFile()
>>> x = np.arange(10)
>>> np.save(outfile, x)
>>> outfile.seek(0) # Only needed here to simulate closing & reopening file
>>> np.load(outfile)
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

numpy.savez (file, *args, **kwds)
Save several arrays into a single file in uncompressed .npz format.
If arguments are passed in with no keywords, the corresponding variable names, in the .npz file, are 'arr_0', 'arr_1', etc. If keyword arguments are given, the corresponding variable names, in the .npz file will match the keyword names.

## Parameters

file : str or file
Either the file name (string) or an open file (file-like object) where the data will be saved. If file is a string, the . npz extension will be appended to the file name if it is not already there.
*args : Arguments, optional
Arrays to save to the file. Since it is not possible for Python to know the names of the arrays outside savez, the arrays will be saved with names "arr_0", "arr_1", and so on. These arguments can be any expression.
**kwds : Keyword arguments, optional
Arrays to save to the file. Arrays will be saved in the file with the keyword names.

## Returns

None :

## See Also:

## numpy.savez_compressed

Save several arrays into a compressed .npz file format

## Notes

The .npz file format is a zipped archive of files named after the variables they contain. The archive is not compressed and each file in the archive contains one variable in . npy format. For a description of the .npy format, see format.

When opening the saved . npz file with load a NpzFile object is returned. This is a dictionary-like object which can be queried for its list of arrays (with the .files attribute), and for the arrays themselves.

## Examples

```
>>> from tempfile import TemporaryFile
>>> outfile = TemporaryFile()
>>> x = np.arange(10)
>>> y = np.sin(x)
```

Using savez with *args, the arrays are saved with default names.

```
>>> np.savez(outfile, x, y)
>>> outfile.seek(0) # Only needed here to simulate closing & reopening file
>>> npzfile = np.load(outfile)
>>> npzfile.files
['arr_1', 'arr_0']
>>> npzfile['arr_0']
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

Using savez with **kwds, the arrays are saved with the keyword names.

```
>>> outfile = TemporaryFile()
>>> np.savez(outfile, x=x, y=y)
>>> outfile.seek(0)
>>> npzfile = np.load(outfile)
>>> npzfile.files
['y', 'x']
>>> npzfile['x']
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```


### 3.5.2 Text files

loadtxt(fname[, dtype, comments, delimiter, Load data from a text file.
...])
savetxt(fname, $X[, f m t$, delimiter, newline]) Save an array to a text file.
genfromtxt(fname[, dtype, comments, ...]) Load data from a text file, with missing values handled as
specified.
fromregex(file, regexp, dtype) Construct an array from a text file, using regular expression
parsing.
fromstring(string[, dtype, count, sep]) A new 1-D array initialized from raw binary or text data in a
string.
ndarray.tofile(fid[, sep, format]) Write array to a file as text or binary (default).
ndarray.tolist() Return the array as a (possibly nested) list.

```
numpy.loadtxt (fname, dtype=<type 'float'>, comments='#', delimiter=None, converters=None,
                        skiprows=0, usecols=None, unpack=False, ndmin=0)
```

    Load data from a text file.
    Each row in the text file must have the same number of values.

## Parameters

fname : file or str
File, filename, or generator to read. If the filename extension is.$g z$ or . $b z 2$, the file is first decompressed. Note that generators should return byte strings for Python 3 k .
dtype : data-type, optional
Data-type of the resulting array; default: float. If this is a record data-type, the resulting array will be 1-dimensional, and each row will be interpreted as an element of the array.

In this case, the number of columns used must match the number of fields in the datatype.
comments : str, optional
The character used to indicate the start of a comment; default: '\#'.
delimiter : str, optional
The string used to separate values. By default, this is any whitespace.
converters : dict, optional
A dictionary mapping column number to a function that will convert that column to a float. E.g., if column 0 is a date string: converters $=\{0$ : datestr2num . Converters can also be used to provide a default value for missing data (but see also genfromtxt): converters $=\{3:$ lambda $s:$ float(s.strip() or 0) $\}$. Default: None.
skiprows : int, optional
Skip the first skiprows lines; default: 0.
usecols : sequence, optional
Which columns to read, with 0 being the first. For example, usecols $=(1,4,5)$ will extract the 2nd, 5th and 6th columns. The default, None, results in all columns being read.
unpack : bool, optional
If True, the returned array is transposed, so that arguments may be unpacked using x , $y, z=$ loadtxt (...). When used with a record data-type, arrays are returned for each field. Default is False.
ndmin : int, optional
The returned array must have at least ndmin dimensions. Legal values: 0 (default), 1 or 2. .. versionadded:: 1.6.0

## Returns

out : ndarray
Data read from the text file.

## See Also:

```
load,fromstring, fromregex
```

genfromtxt
Load data with missing values handled as specified.
scipy.io.loadmat
reads MATLAB data files

## Notes

This function aims to be a fast reader for simply formatted files. The genfromtxt function provides more sophisticated handling of, e.g., lines with missing values.

## Examples

```
>>> from StringIO import StringIO # StringIO behaves like a file object
>>> c = StringIO("0 1\n2 3")
>>> np.loadtxt(c)
```

```
array([[ 0., 1.],
    [ 2., 3.]])
>>> d = StringIO("M 21 72\nF 35 58")
>>> np.loadtxt(d, dtype={'names': ('gender', 'age', 'weight'),
... 'formats': ('S1', 'i4', 'f4')})
array([('M', 21, 72.0), ('F', 35, 58.0)],
    dtype=[('gender', '|S1'), ('age', '<i4'), ('weight', '<f4')])
>>> c = StringIO("1,0,2\n3,0,4")
>>> x, y = np.loadtxt(c, delimiter=',', usecols=(0, 2), unpack=True)
>>> x
array([ 1., 3.])
>>> y
array([ 2., 4.])
numpy.savetxt (fname, X, fmt='%.18e', delimiter=' ', newline= '\n')
```

Save an array to a text file.

## Parameters

fname : filename or file handle
If the filename ends in.$g z$, the file is automatically saved in compressed gzip format. loadtxt understands gzipped files transparently.
$\mathbf{X}$ : array_like
Data to be saved to a text file.
fmt : str or sequence of strs
A single format ( $\% 10.5 \mathrm{f})$, a sequence of formats, or a multi-format string, e.g. 'Iteration $\% \mathrm{~d}-\% 10.5 \mathrm{f}$ ', in which case delimiter is ignored.
delimiter: str
Character separating columns.
newline : str
New in version 1.5.0. Character separating lines.

## See Also:

save
Save an array to a binary file in NumPy . npy format
savez
Save several arrays into a . npz compressed archive

## Notes

Further explanation of the $f m t$ parameter (\% [flag]width[.precision]specifier):
flags:

- : left justify
+ : Forces to preceed result with + or.-
0 : Left pad the number with zeros instead of space (see width).
width:
Minimum number of characters to be printed. The value is not truncated if it has more characters.


## precision:

- For integer specifiers (eg. $d, i, \circ, x$ ), the minimum number of digits.
- For $e, E$ and $f$ specifiers, the number of digits to print after the decimal point.
- For $g$ and $G$, the maximum number of significant digits.
- For $s$, the maximum number of characters.


## specifiers:

c: character
d or i : signed decimal integer
e or $E$ : scientific notation with e or $E$.
f: decimal floating point
$g, G$ : use the shorter of $e, E$ or $f$
$\bigcirc$ : signed octal
$s$ : string of characters
$u$ : unsigned decimal integer
$x, X$ : unsigned hexadecimal integer
This explanation of fmt is not complete, for an exhaustive specification see [R218].

## References

[R218]

## Examples

```
>>> x = y = z = np.arange(0.0,5.0,1.0)
>>> np.savetxt('test.out', x, delimiter=',') # X is an array
>>> np.savetxt('test.out', (x,y,z)) # x,y,z equal sized 1D arrays
>>> np.savetxt('test.out', x, fmt='%1.4e') # use exponential notation
```

numpy.genfromtxt (fname, dtype=<type 'float'>, comments='\#', delimiter=None, skiprows=0, skip_header $=0$, skip_footer $=0$, converters $=$ None, missing $=$ '', missing_values $=$ None, filling_values=None, usecols=None, names=None, excludelist=None, deletechars=None, replace_space='_,' autostrip=False, case_sensitive=True, defaultfmt='f\%i', unpack=None, usemask=False, loose=True, invalid_raise=True)
Load data from a text file, with missing values handled as specified.
Each line past the first skip_header lines is split at the delimiter character, and characters following the comments character are discarded.

## Parameters

fname : file or str
File, filename, or generator to read. If the filename extension is $g z$ or bz2, the file is first decompressed. Note that generators must return byte strings in Python 3k.
dtype : dtype, optional
Data type of the resulting array. If None, the dtypes will be determined by the contents of each column, individually.
comments : str, optional

The character used to indicate the start of a comment. All the characters occurring on a line after a comment are discarded
delimiter : str, int, or sequence, optional
The string used to separate values. By default, any consecutive whitespaces act as delimiter. An integer or sequence of integers can also be provided as width(s) of each field.
skip_header : int, optional
The numbers of lines to skip at the beginning of the file.
skip_footer : int, optional
The numbers of lines to skip at the end of the file
converters : variable, optional
The set of functions that convert the data of a column to a value. The converters can also be used to provide a default value for missing data: converters $=\{3: \quad$ lambda s: float (s or 0 ) \}.
missing_values : variable, optional
The set of strings corresponding to missing data.
filling_values : variable, optional
The set of values to be used as default when the data are missing.
usecols : sequence, optional
Which columns to read, with 0 being the first. For example, usecols $=(1,4$, 5 ) will extract the 2 nd, 5 th and 6 th columns.
names : \{None, True, str, sequence \}, optional
If names is True, the field names are read from the first valid line after the first skip_header lines. If names is a sequence or a single-string of comma-separated names, the names will be used to define the field names in a structured dtype. If names is None, the names of the dtype fields will be used, if any.
excludelist : sequence, optional
A list of names to exclude. This list is appended to the default list ['return','file','print']. Excluded names are appended an underscore: for example, file would become file_.
deletechars: str, optional
A string combining invalid characters that must be deleted from the names.
defaultfmt : str, optional
A format used to define default field names, such as " $\mathrm{f} \% \mathrm{i}$ " or "f_\%02i".
autostrip : bool, optional
Whether to automatically strip white spaces from the variables.
replace_space : char, optional
Character(s) used in replacement of white spaces in the variables names. By default, use a '_,
case_sensitive : \{True, False, 'upper', 'lower'\}, optional

If True, field names are case sensitive. If False or 'upper', field names are converted to upper case. If 'lower', field names are converted to lower case.
unpack : bool, optional
If True, the returned array is transposed, so that arguments may be unpacked using x , y, $z=$ loadtxt (...)
usemask : bool, optional
If True, return a masked array. If False, return a regular array.
invalid_raise : bool, optional
If True, an exception is raised if an inconsistency is detected in the number of columns. If False, a warning is emitted and the offending lines are skipped.

## Returns

out : ndarray
Data read from the text file. If usemask is True, this is a masked array.

## See Also:

numpy.loadtxt
equivalent function when no data is missing.

## Notes

-When spaces are used as delimiters, or when no delimiter has been given as input, there should not be any missing data between two fields.
-When the variables are named (either by a flexible dtype or with names, there must not be any header in the file (else a ValueError exception is raised).

- Individual values are not stripped of spaces by default. When using a custom converter, make sure the function does remove spaces.


## Examples

```
>>> from StringIO import StringIO
>>> import numpy as np
```

Comma delimited file with mixed dtype

```
>>> s = StringIO("1,1.3,abcde")
>>> data = np.genfromtxt(s, dtype=[('myint','i8'),('myfloat','f8'),
... ('mystring','S5')], delimiter=",")
>>> data
array((1, 1.3, 'abcde'),
    dtype=[('myint', '<i8'), ('myfloat', '<f8'), ('mystring', '|S5')])
```

Using dtype $=$ None

```
>>> s.seek(0) # needed for StringIO example only
>>> data = np.genfromtxt(s, dtype=None,
... names = ['myint','myfloat','mystring'], delimiter=",")
>>> data
array((1, 1.3, 'abcde'),
    dtype=[('myint', '<i8'), ('myfloat', '<f8'), ('mystring', '|S5')])
```

Specifying dtype and names

```
>>> s.seek(0)
>>> data = np.genfromtxt(s, dtype="i8,f8,S5",
... names=['myint','myfloat','mystring'], delimiter=",")
>>> data
array((1, 1.3, 'abcde'),
    dtype=[('myint', '<i8'), ('myfloat', '<f8'), ('mystring', '|S5')])
```

An example with fixed-width columns

```
>>> s = StringIO("11.3abcde")
>>> data = np.genfromtxt(s, dtype=None, names=['intvar','fltvar','strvar'],
... delimiter=[1,3,5])
>>> data
array((1, 1.3, 'abcde'),
    dtype=[('intvar', '<i8'), ('fltvar', '<f8'), ('strvar', '|S5')])
```

numpy.fromregex (file, regexp, dtype)
Construct an array from a text file, using regular expression parsing.
The returned array is always a structured array, and is constructed from all matches of the regular expression in the file. Groups in the regular expression are converted to fields of the structured array.

## Parameters

file : str or file
File name or file object to read.
regexp : str or regexp
Regular expression used to parse the file. Groups in the regular expression correspond to fields in the dtype.
dtype: dtype or list of dtypes
Dtype for the structured array.

## Returns

output : ndarray
The output array, containing the part of the content of file that was matched by regexp. output is always a structured array.

## Raises

## TypeError :

When dtype is not a valid dtype for a structured array.

## See Also:

```
fromstring, loadtxt
```


## Notes

Dtypes for structured arrays can be specified in several forms, but all forms specify at least the data type and field name. For details see doc.structured_arrays.

## Examples

```
>>> f = open('test.dat', 'w')
>>> f.write("1312 foo\n1534 bar\n444 qux")
>>> f.close()
```

```
>>> regexp = r"(\d+)\s+(...)" # match [digits, whitespace, anything]
>>> output = np.fromregex('test.dat', regexp,
... [('num', np.int64), ('key', 'S3')])
>>> output
array([(1312L, 'foo'), (1534L, 'bar'), (444L, 'qux')],
    dtype=[('num', '<i8'), ('key', '|S3')])
>>> output['num']
array([1312, 1534, 444], dtype=int64)
numpy.fromstring (string, dtype=float, count=-1, sep='')
```

A new 1-D array initialized from raw binary or text data in a string.

## Parameters

string : str
A string containing the data.
dtype : data-type, optional
The data type of the array; default: float. For binary input data, the data must be in exactly this format.
count : int, optional
Read this number of dtype elements from the data. If this is negative (the default), the count will be determined from the length of the data.
sep : str, optional
If not provided or, equivalently, the empty string, the data will be interpreted as binary data; otherwise, as ASCII text with decimal numbers. Also in this latter case, this argument is interpreted as the string separating numbers in the data; extra whitespace between elements is also ignored.

## Returns

 arr : ndarrayThe constructed array.

## Raises

## ValueError :

If the string is not the correct size to satisfy the requested dtype and count.

## See Also:

```
frombuffer,fromfile,fromiter
```


## Examples

```
>>> np.fromstring('\x01\x02', dtype=np.uint8)
array([1, 2], dtype=uint8)
>>> np.fromstring('1 2', dtype=int, sep=' ')
array([1, 2])
>>> np.fromstring('1, 2', dtype=int, sep=',')
array([1, 2])
>>> np.fromstring('\x01\x02\x03\x04\x05', dtype=np.uint8, count=3)
array([1, 2, 3], dtype=uint8)
```

ndarray.tofile (fid, sep="", format="\%s")

Write array to a file as text or binary (default).

Data is always written in ' $C$ ' order, independent of the order of $a$. The data produced by this method can be recovered using the function fromfile().

## Parameters

fid : file or str
An open file object, or a string containing a filename.
sep : str
Separator between array items for text output. If "" (empty), a binary file is written, equivalent to file.write(a.tostring()).
format : str
Format string for text file output. Each entry in the array is formatted to text by first converting it to the closest Python type, and then using "format" \% item.

## Notes

This is a convenience function for quick storage of array data. Information on endianness and precision is lost, so this method is not a good choice for files intended to archive data or transport data between machines with different endianness. Some of these problems can be overcome by outputting the data as text files, at the expense of speed and file size.
ndarray.tolist()
Return the array as a (possibly nested) list.
Return a copy of the array data as a (nested) Python list. Data items are converted to the nearest compatible Python type.

## Parameters

none :

## Returns

$\mathbf{y}$ : list
The possibly nested list of array elements.

## Notes

The array may be recreated, $a=n p . \operatorname{array}(a$. tolist()).

## Examples

```
>>> a = np.array([1, 2])
>>> a.tolist()
[1, 2]
>>> a = np.array([[1, 2], [3, 4]])
>>> list(a)
[array([1, 2]), array([3, 4])]
>>> a.tolist()
[[1, 2], [3, 4]]
```


### 3.5.3 String formatting

```
array_repr(arr[, max_line_width, precision, ...]) Return the string representation of an array.
array_str(a[,max_line_width, precision, ...]) Return a string representation of the data in an array.
numpy.array_repr (arr,max_line_width=None,precision=None, suppress_small=None)
```

Return the string representation of an array.

## Parameters

arr : ndarray
Input array.
max_line_width : int, optional
The maximum number of columns the string should span. Newline characters split the string appropriately after array elements.
precision : int, optional
Floating point precision. Default is the current printing precision (usually 8), which can be altered using set_printoptions.
suppress_small : bool, optional
Represent very small numbers as zero, default is False. Very small is defined by precision, if the precision is 8 then numbers smaller than $5 \mathrm{e}-9$ are represented as zero.

## Returns

string : str
The string representation of an array.

## See Also:

```
array_str,array2string, set_printoptions
```


## Examples

```
>>> np.array_repr(np.array([1,2]))
'array([1, 2])'
>>> np.array_repr(np.ma.array([0.]))
'MaskedArray([ 0.])'
>>> np.array_repr(np.array([], np.int32))
'array([], dtype=int32)'
>>> x = np.array([1e-6, 4e-7, 2, 3])
>>> np.array_repr(x, precision=6, suppress_small=True)
'array([ 0.000001, 0. , 2. , 3. ])'
```

numpy.array_str (a, max_line_width=None, precision=None, suppress_small=None)
Return a string representation of the data in an array.
The data in the array is returned as a single string. This function is similar to array_repr, the difference being that array_repr also returns information on the kind of array and its data type.

## Parameters

a : ndarray
Input array.
max_line_width : int, optional
Inserts newlines if text is longer than max_line_width. The default is, indirectly, 75.
precision : int, optional
Floating point precision. Default is the current printing precision (usually 8), which can be altered using set_printoptions.
suppress_small : bool, optional

Represent numbers "very close" to zero as zero; default is False. Very close is defined by precision: if the precision is 8 , e.g., numbers smaller (in absolute value) than $5 \mathrm{e}-9$ are represented as zero.

## See Also:

array2string, array_repr, set_printoptions

## Examples

```
>>> np.array_str(np.arange(3))
```

${ }^{\prime}\left[\begin{array}{lll}0 & 1 & 2\end{array}\right]^{\prime}$

### 3.5.4 Memory mapping files

## memmap Create a memory-map to an array stored in a binary file on disk.

class numpy . memmap
Create a memory-map to an array stored in a binary file on disk.
Memory-mapped files are used for accessing small segments of large files on disk, without reading the entire file into memory. Numpy's memmap's are array-like objects. This differs from Python's mmap module, which uses file-like objects.

## Parameters

filename : str or file-like object
The file name or file object to be used as the array data buffer.
dtype : data-type, optional
The data-type used to interpret the file contents. Default is uint8.
mode : \{ 'r+', 'r', 'w+', 'c'\}, optional
The file is opened in this mode:

| ' $r$ ' | Open existing file for reading only. |
| :--- | :--- |
| ' $\mathrm{r}+$ | Open existing file for reading and writing. |
| ' $\mathrm{w}+$ ' | Create or overwrite existing file for reading and writing. |
| ' $c$ ' | Copy-on-write: assignments affect data in memory, but changes are not saved <br> to disk. The file on disk is read-only. |

Default is ' $\mathrm{r}+$ '.
offset : int, optional
In the file, array data starts at this offset. Since offset is measured in bytes, it should be a multiple of the byte-size of dtype. Requires shape=None. The default is 0 .
shape : tuple, optional
The desired shape of the array. By default, the returned array will be 1-D with the number of elements determined by file size and data-type.
order : \{ 'C', 'F' $\}$, optional
Specify the order of the ndarray memory layout: C (row-major) or Fortran (columnmajor). This only has an effect if the shape is greater than 1-D. The default order is ' C '.

## Notes

The memmap object can be used anywhere an ndarray is accepted. Given a memmap $f p$, isinstance (fp, numpy.ndarray) returns True.

Memory-mapped arrays use the Python memory-map object which (prior to Python 2.5) does not allow files to be larger than a certain size depending on the platform. This size is always $<2 \mathrm{~GB}$ even on 64 -bit systems.

## Examples

```
>>> data = np.arange(12, dtype='float32')
>>> data.resize((3,4))
```

This example uses a temporary file so that doctest doesn't write files to your directory. You would use a 'normal' filename.

```
>>> from tempfile import mkdtemp
>>> import os.path as path
>>> filename = path.join(mkdtemp(), 'newfile.dat')
```

Create a memmap with dtype and shape that matches our data:

```
>>> fp = np.memmap(filename, dtype='float 32', mode='w+', shape=(3,4))
>>> fp
memmap([[ 0., 0., 0., 0.],
    [ 0., 0., 0., 0.],
    [ 0., 0., 0., 0.]], dtype=float 32)
```

Write data to memmap array:

```
>>> fp[:] = data[:]
>>> fp
memmap([[[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.]], dtype=float32)
>>> fp.filename == path.abspath(filename)
True
```

Deletion flushes memory changes to disk before removing the object:

```
>>> del fp
```

Load the memmap and verify data was stored:

```
>>> newfp = np.memmap(filename, dtype='float32', mode='r', shape=(3,4))
>>> newfp
memmap([[[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.]], dtype=float32)
```

Read-only memmap:

```
>>> fpr = np.memmap(filename, dtype='float 32', mode='r', shape=(3,4))
>>> fpr.flags.writeable
False
```

Copy-on-write memmap:

```
>>> fpc = np.memmap(filename, dtype='float 32', mode=' c', shape=(3,4))
>>> fpc.flags.writeable
True
```

It's possible to assign to copy-on-write array, but values are only written into the memory copy of the array, and not written to disk:

```
>>> fpc
memmap([[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.]], dtype=float32)
>>> fpc[0,:] = 0
>>> fpc
memmap([[[ 0., 0., 0., 0.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.]], dtype=float32)
```

File on disk is unchanged:

```
>>> fpr
memmap([[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.]], dtype=float32)
```

Offset into a memmap:

```
>>> fpo = np.memmap(filename, dtype='float32', mode='r', offset=16)
>>> fpo
memmap([ 4., 5., 6., 7., 8., 9., 10., 11.], dtype=float32)
```


## Attributes

| filename <br> offset <br> mode | str <br> int | Path to the mapped file. <br> str |
| :--- | :--- | :--- |
| Offset position in the file. |  |  |
| File mode. |  |  |

## Methods

### 3.5.5 Text formatting options

```
set_printoptions([precision, threshold,...]) Set printing options.
get_printoptions() Return the current print options.
set_string_function(f[, repr]) Set a Python function to be used when pretty printing arrays.
```

numpy.set_printoptions (precision=None, threshold=None, edgeitems=None, linewidth=None, suppress $=$ None, nanstr $=$ None, infstr $=$ None )
Set printing options.
These options determine the way floating point numbers, arrays and other NumPy objects are displayed.

## Parameters

precision : int, optional
Number of digits of precision for floating point output (default 8).
threshold : int, optional
Total number of array elements which trigger summarization rather than full repr (default 1000).
edgeitems : int, optional
Number of array items in summary at beginning and end of each dimension (default 3).
linewidth : int, optional
The number of characters per line for the purpose of inserting line breaks (default 75). suppress : bool, optional

Whether or not suppress printing of small floating point values using scientific notation (default False).

```
nanstr : str, optional
```

String representation of floating point not-a-number (default nan).
infstr : str, optional
String representation of floating point infinity (default inf).

## See Also:

```
get_printoptions,set_string_function
```


## Examples

Floating point precision can be set:

```
>>> np.set_printoptions(precision=4)
>>> print np.array([1.123456789])
[ 1.1235]
```

Long arrays can be summarised:

```
>>> np.set_printoptions(threshold=5)
>>> print np.arange(10)
[0}012\mp@code{2.., 7 8 9]
```

Small results can be suppressed:

```
>>> eps = np.finfo(float).eps
>>> x = np.arange(4.)
>>> x**2 - (x + eps)**2
array([ -4.9304e-32, -4.4409e-16, 0.0000e+00, 0.0000e+00])
>>> np.set_printoptions(suppress=True)
>>> x**2 - (x + eps)**2
array([-0., -0., 0., 0.])
```

To put back the default options, you can use:

```
>>> np.set_printoptions(edgeitems=3,infstr=' Inf',
... linewidth=75, nanstr='NaN', precision=8,
... suppress=False, threshold=1000)
```

numpy.get_printoptions()

Return the current print options.

## Returns

print_opts : dict
Dictionary of current print options with keys

- precision : int
- threshold : int
- edgeitems : int
- linewidth : int
- suppress : bool
- nanstr : str
- infstr : str

For a full description of these options, see set_printoptions.

## See Also:

```
set_printoptions, set_string_function
```

numpy.set_string_function ( $f$, repr=True)

Set a Python function to be used when pretty printing arrays.

## Parameters

f: function or None
Function to be used to pretty print arrays. The function should expect a single array argument and return a string of the representation of the array. If None, the function is reset to the default NumPy function to print arrays.
repr : bool, optional
If True (default), the function for pretty printing (__repr__) is set, if False the function that returns the default string representation (__str__) is set.

## See Also:

set_printoptions, get_printoptions

## Examples

```
>>> def pprint(arr):
... return 'HA! - What are you going to do now?'
...
>>> np.set_string_function(pprint)
>>> a = np.arange(10)
>>> a
HA! - What are you going to do now?
>>> print a
[0}[\begin{array}{lllllllllll}{1}&{2}&{3}&{4}&{5}&{6}&{7}&{8}&{9}\end{array}
```

We can reset the function to the default:

```
>>> np.set_string_function(None)
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

repr affects either pretty printing or normal string representation. Note that $\qquad$ repr $\qquad$ is still affected by setting __st r__ because the width of each array element in the returned string becomes equal to the length of the result of $\qquad$ () .

```
>>> x = np.arange(4)
>>> np.set_string_function(lambda x:'random', repr=False)
>>> x.__str__()
'random'
>>> x.__repr__()
'array([ 0, 1, 2, 3])'
```


### 3.5.6 Base-n representations

binary_repr(num[, width]) Return the binary representation of the input number as a string.
base_repr(number[, base, padding]) Return a string representation of a number in the given base system.
numpy.binary_repr (num, width=None)
Return the binary representation of the input number as a string.
For negative numbers, if width is not given, a minus sign is added to the front. If width is given, the two's complement of the number is returned, with respect to that width.

In a two's-complement system negative numbers are represented by the two's complement of the absolute value. This is the most common method of representing signed integers on computers [R16]. A N-bit two'scomplement system can represent every integer in the range $-2^{N-1}$ to $+2^{N-1}-1$.

## Parameters

num : int
Only an integer decimal number can be used.
width : int, optional
The length of the returned string if num is positive, the length of the two's complement if num is negative.

## Returns

 bin : strBinary representation of num or two's complement of num.

## See Also:

base_repr
Return a string representation of a number in the given base system.

## Notes

binary_repr is equivalent to using base_repr with base 2 , but about 25 x faster.

## References

[R16]

## Examples

```
>>> np.binary_repr(3)
'11'
>>> np.binary_repr(-3)
'-11'
>>> np.binary_repr(3, width=4)
'0011'
```

The two's complement is returned when the input number is negative and width is specified:

```
>>> np.binary_repr(-3, width=4)
'1101'
```

numpy.base_repr (number, base $=2$, padding=0)
Return a string representation of a number in the given base system.

## Parameters

number : int

The value to convert. Only positive values are handled.
base : int, optional
Convert number to the base number system. The valid range is $2-36$, the default value is 2 .
padding : int, optional
Number of zeros padded on the left. Default is 0 (no padding).

## Returns

out : str
String representation of number in base system.

## See Also:

binary_repr
Faster version of base_repr for base 2.

## Examples

```
>>> np.base_repr(5)
'101'
>>> np.base_repr(6, 5)
'11'
>>> np.base_repr(7, base=5, padding=3)
'00012'
>>> np.base_repr(10, base=16)
'A'
>>> np.base_repr(32, base=16)
'20'
```


### 3.5.7 Data sources

DataSource([destpath]) A generic data source file (file, http, ftp, ...).
class numpy.DataSource (destpath='.')
A generic data source file (file, http, ftp, ...).
DataSources can be local files or remote files/URLs. The files may also be compressed or uncompressed. DataSource hides some of the low-level details of downloading the file, allowing you to simply pass in a valid file path (or URL) and obtain a file object.

## Parameters

destpath : str or None, optional
Path to the directory where the source file gets downloaded to for use. If destpath is None, a temporary directory will be created. The default path is the current directory.

## Notes

URLs require a scheme string (http:/ /) to be used, without it they will fail:

```
>>> repos = DataSource()
>>> repos.exists('www.google.com/index.html')
False
>>> repos.exists('http://www.google.com/index.html')
True
```

Temporary directories are deleted when the DataSource is deleted.

## Examples

```
>>> ds = DataSource('/home/guido')
>>> urlname = 'http://www.google.com/index.html'
>>> gfile = ds.open('http://www.google.com/index.html') # remote file
>>> ds.abspath(urlname)
'/home/guido/www.google.com/site/index.html'
>>> ds = DataSource(None) # use with temporary file
>>> ds.open('/home/guido/foobar.txt')
<open file '/home/guido.foobar.txt', mode 'r' at 0x91d4430>
>>> ds.abspath('/home/guido/foobar.txt')
'/tmp/tmpy4pgsP/home/guido/foobar.txt'
```


## Methods

```
abspath
exists
open
```


### 3.6 Discrete Fourier Transform (numpy.fft)

### 3.6.1 Standard FFTs

| fft(a[, n, axis]) | Compute the one-dimensional discrete Fourier Transform. |
| :---: | :---: |
| ifft(a[, n, axis]) | Compute the one-dimensional inverse discrete Fourier Transform. |
| fft2(a[, s, axes]) | Compute the 2-dimensional discrete Fourier Transform |
| ifft2(a[, s, axes]) | Compute the 2-dimensional inverse discrete Fourier Transform. |
| fftn(a[, s, axes]) | Compute the N -dimensional discrete Fourier Transform. |
| ifftn(a[, s, axes]) | Compute the N -dimensional inverse discrete Fourier Transform. |

Compute the one-dimensional discrete Fourier Transform.
This function computes the one-dimensional $n$-point discrete Fourier Transform (DFT) with the efficient Fast Fourier Transform (FFT) algorithm [CT].

## Parameters

a : array_like
Input array, can be complex.
$\mathbf{n}$ : int, optional
Length of the transformed axis of the output. If $n$ is smaller than the length of the input, the input is cropped. If it is larger, the input is padded with zeros. If $n$ is not given, the length of the input (along the axis specified by axis) is used.
axis : int, optional
Axis over which to compute the FFT. If not given, the last axis is used.

## Returns

out : complex ndarray

The truncated or zero-padded input, transformed along the axis indicated by axis, or the last one if axis is not specified.

## Raises

## IndexError :

if axes is larger than the last axis of $a$.

## See Also:

numpy.fft
for definition of the DFT and conventions used.

```
ifft
```

The inverse of $f f t$.

```
fft2
```

The two-dimensional FFT.

```
fftn
```

The $n$-dimensional FFT.
rfftn
The $n$-dimensional FFT of real input.

## fftfreq

Frequency bins for given FFT parameters.

## Notes

FFT (Fast Fourier Transform) refers to a way the discrete Fourier Transform (DFT) can be calculated efficiently, by using symmetries in the calculated terms. The symmetry is highest when $n$ is a power of 2 , and the transform is therefore most efficient for these sizes.

The DFT is defined, with the conventions used in this implementation, in the documentation for the numpy.fft module.

## References

## [CT]

## Examples

```
>>> np.fft.fft(np.exp(2j * np.pi * np.arange(8) / 8))
array([ -3.44505240e-16 +1.14383329e-17j,
    8.00000000e+00-5.71092652e-15j,
    2.33482938e-16 +1.22460635e-16j,
    1.64863782e-15 +1.77635684e-15j,
    9.95839695e-17 +2.33482938e-16j,
    0.00000000e+00 +1.66837030e-15j,
    1.14383329e-17 +1.22460635e-16j,
    -1.64863782e-15 +1.77635684e-15j])
>>> import matplotlib.pyplot as plt
>>> t = np.arange(256)
>>> sp = np.fft.fft(np.sin(t))
>>> freq = np.fft.fftfreq(t.shape[-1])
>>> plt.plot(freq, sp.real, freq, sp.imag)
[<matplotlib.lines.Line2D object at 0x...>, <matplotlib.lines.Line2D object at 0x...>]
>>> plt.show()
```

In this example, real input has an FFT which is Hermitian, i.e., symmetric in the real part and anti-symmetric in the imaginary part, as described in the numpy.fft documentation.

## numpy.fft.ifft ( $a, n=$ None, axis=-1)

Compute the one-dimensional inverse discrete Fourier Transform.
This function computes the inverse of the one-dimensional $n$-point discrete Fourier transform computed by fft. In other words, ifft (fft (a)) == a to within numerical accuracy. For a general description of the algorithm and definitions, see numpy.fft.

The input should be ordered in the same way as is returned by fft, i.e., a [0] should contain the zero frequency term, a [1:n/2+1] should contain the positive-frequency terms, and a[n/2+1:] should contain the negative-frequency terms, in order of decreasingly negative frequency. See numpy. fft for details.

## Parameters

a : array_like
Input array, can be complex.
n : int, optional
Length of the transformed axis of the output. If $n$ is smaller than the length of the input, the input is cropped. If it is larger, the input is padded with zeros. If $n$ is not given, the length of the input (along the axis specified by axis) is used. See notes about padding issues.
axis : int, optional
Axis over which to compute the inverse DFT. If not given, the last axis is used.

## Returns

out : complex ndarray
The truncated or zero-padded input, transformed along the axis indicated by axis, or the last one if axis is not specified.

## Raises

## IndexError :

If axes is larger than the last axis of $a$.

## See Also:

numpy.fft
An introduction, with definitions and general explanations.
fft
The one-dimensional (forward) FFT, of which ifft is the inverse
ifft2
The two-dimensional inverse FFT.
ifftn
The n-dimensional inverse FFT.

## Notes

If the input parameter $n$ is larger than the size of the input, the input is padded by appending zeros at the end. Even though this is the common approach, it might lead to surprising results. If a different padding is desired, it must be performed before calling ifft.

## Examples

```
>>> np.fft.ifft([0, 4, 0, 0])
array([ 1.+0.j, 0.+1.j, -1.+0.j, 0.-1.j])
```

Create and plot a band-limited signal with random phases:

```
>>> import matplotlib.pyplot as plt
>>> t = np.arange(400)
>>> n = np.zeros((400,), dtype=complex)
>>> n[40:60] = np.exp(1j*np.random.uniform(0, 2*np.pi, (20,)))
>>> s = np.fft.ifft(n)
>>> plt.plot(t, s.real, 'b-', t, s.imag, 'r--'')
[<matplotlib.lines.Line2D object at 0x...>, <matplotlib.lines.Line2D object at 0x...>]
>>> plt.legend(('real', 'imaginary'))
<matplotlib.legend.Legend object at 0x...>
>>> plt.show()
```


numpy.fft.fft2 ( $a$, $s=$ None, axes=(-2, -1 ) )
Compute the 2-dimensional discrete Fourier Transform
This function computes the $n$-dimensional discrete Fourier Transform over any axes in an $M$-dimensional array by means of the Fast Fourier Transform (FFT). By default, the transform is computed over the last two axes of the input array, i.e., a 2-dimensional FFT.

## Parameters

a : array_like
Input array, can be complex
$\mathbf{s}$ : sequence of ints, optional
Shape (length of each transformed axis) of the output ( $s[0]$ refers to axis $0, s[1]$ to axis 1 , etc.). This corresponds to $n$ for $f f t(x, n)$. Along each axis, if the given shape is smaller than that of the input, the input is cropped. If it is larger, the input is padded with zeros. if $s$ is not given, the shape of the input (along the axes specified by axes) is used.
axes : sequence of ints, optional
Axes over which to compute the FFT. If not given, the last two axes are used. A repeated
index in axes means the transform over that axis is performed multiple times. A oneelement sequence means that a one-dimensional FFT is performed.

## Returns

out : complex ndarray
The truncated or zero-padded input, transformed along the axes indicated by axes, or the last two axes if axes is not given.

## Raises

ValueError :
If $s$ and axes have different length, or axes not given and len (s) $\quad!=2$.

## IndexError :

If an element of axes is larger than than the number of axes of $a$.

## See Also:

numpy.fft
Overall view of discrete Fourier transforms, with definitions and conventions used.

## ifft2

The inverse two-dimensional FFT.
fft
The one-dimensional FFT.
fftn
The $n$-dimensional FFT.

```
fftshift
```

Shifts zero-frequency terms to the center of the array. For two-dimensional input, swaps first and third quadrants, and second and fourth quadrants.

## Notes

$f f t 2$ is just $f f t n$ with a different default for axes.
The output, analogously to $f f t$, contains the term for zero frequency in the low-order corner of the transformed axes, the positive frequency terms in the first half of these axes, the term for the Nyquist frequency in the middle of the axes and the negative frequency terms in the second half of the axes, in order of decreasingly negative frequency.

See fftn for details and a plotting example, and numpy.fft for definitions and conventions used.

## Examples

```
>>> a = np.mgrid[:5, :5][0]
>>> np.fft.fft2(a)
array([[ 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
    [ 5.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
    [ 10.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
    [ 15.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
    [ 20.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j]])
```

numpy.fft.ifft2 ( $a, s=$ None, axes $=(-2,-1)$ )
Compute the 2-dimensional inverse discrete Fourier Transform.
This function computes the inverse of the 2-dimensional discrete Fourier Transform over any number of axes in an M-dimensional array by means of the Fast Fourier Transform (FFT). In other words, ifft2 (fft2 (a))
$==$ a to within numerical accuracy. By default, the inverse transform is computed over the last two axes of the input array.
The input, analogously to ifft, should be ordered in the same way as is returned by $f f t 2$, i.e. it should have the term for zero frequency in the low-order corner of the two axes, the positive frequency terms in the first half of these axes, the term for the Nyquist frequency in the middle of the axes and the negative frequency terms in the second half of both axes, in order of decreasingly negative frequency.

## Parameters

a : array_like
Input array, can be complex.
s: sequence of ints, optional
Shape (length of each axis) of the output (s [0] refers to axis $0, \mathrm{~s}[1]$ to axis 1, etc.). This corresponds to $n$ for ifft $(x, n)$. Along each axis, if the given shape is smaller than that of the input, the input is cropped. If it is larger, the input is padded with zeros. if $s$ is not given, the shape of the input (along the axes specified by axes) is used. See notes for issue on ifft zero padding.
axes : sequence of ints, optional
Axes over which to compute the FFT. If not given, the last two axes are used. A repeated index in axes means the transform over that axis is performed multiple times. A oneelement sequence means that a one-dimensional FFT is performed.

## Returns

out : complex ndarray
The truncated or zero-padded input, transformed along the axes indicated by axes, or the last two axes if axes is not given.

## Raises

ValueError :
If $s$ and axes have different length, or axes not given and len (s) $\quad!=2$.

## IndexError :

If an element of axes is larger than than the number of axes of $a$.

## See Also:

numpy.fft
Overall view of discrete Fourier transforms, with definitions and conventions used.

## fft2

The forward 2-dimensional FFT, of which ifft2 is the inverse.

```
ifftn
```

The inverse of the $n$-dimensional FFT.
fft
The one-dimensional FFT.
ifft
The one-dimensional inverse FFT.

## Notes

ifft2 is just ifftn with a different default for axes.
See ifftn for details and a plotting example, and numpy.fft for definition and conventions used.

Zero-padding, analogously with ifft, is performed by appending zeros to the input along the specified dimension. Although this is the common approach, it might lead to surprising results. If another form of zero padding is desired, it must be performed before ifft 2 is called.

Examples

```
>>> a = 4 * np.eye(4)
>>> np.fft.ifft2(a)
array([[ 1.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j, 1.+0.j],
    [ 0.+0.j, 0.+0.j, 1.+0.j, 0.+0.j],
    [ 0.+0.j, 1.+0.j, 0.+0.j, 0.+0.j]])
```

numpy.fft.fftn ( $a, s=$ None, axes=None)
Compute the N -dimensional discrete Fourier Transform.
This function computes the $N$-dimensional discrete Fourier Transform over any number of axes in an $M$ dimensional array by means of the Fast Fourier Transform (FFT).

## Parameters

a : array_like
Input array, can be complex.
s: sequence of ints, optional
Shape (length of each transformed axis) of the output ( $s[0]$ refers to axis $0, s[1]$ to axis 1 , etc.). This corresponds to $n$ for $f f t(x, n)$. Along any axis, if the given shape is smaller than that of the input, the input is cropped. If it is larger, the input is padded with zeros. if $s$ is not given, the shape of the input (along the axes specified by axes) is used.
axes : sequence of ints, optional
Axes over which to compute the FFT. If not given, the last len (s) axes are used, or all axes if $s$ is also not specified. Repeated indices in axes means that the transform over that axis is performed multiple times.

## Returns

out : complex ndarray
The truncated or zero-padded input, transformed along the axes indicated by axes, or by a combination of $s$ and $a$, as explained in the parameters section above.

## Raises

ValueError :
If $s$ and axes have different length.

## IndexError :

If an element of axes is larger than than the number of axes of $a$.

## See Also:

numpy.fft
Overall view of discrete Fourier transforms, with definitions and conventions used.
ifftn
The inverse of $f f t n$, the inverse $n$-dimensional FFT.
fft
The one-dimensional FFT, with definitions and conventions used.

```
rfftn
```

The $n$-dimensional FFT of real input.

## fft2

The two-dimensional FFT.

```
fftshift
```

Shifts zero-frequency terms to centre of array

## Notes

The output, analogously to $f f t$, contains the term for zero frequency in the low-order corner of all axes, the positive frequency terms in the first half of all axes, the term for the Nyquist frequency in the middle of all axes and the negative frequency terms in the second half of all axes, in order of decreasingly negative frequency.

See numpy.fft for details, definitions and conventions used.

## Examples

```
>>> a = np.mgrid[:3, :3, :3][0]
>>> np.fft.fftn(a, axes=(1, 2))
array([[[ 0.+0.j, 0.+0.j, 0.+0.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j]],
    [[ 9.+0.j, 0.+0.j, 0.+0.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j]],
    [[ 18.+0.j, 0.+0.j, 0.+0.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j]]])
>>> np.fft.fftn(a, (2, 2), axes=(0, 1))
array([[[ 2.+0.j, 2.+0.j, 2.+0.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j]],
    [[-2.+0.j, -2.+0.j, -2.+0.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j]]])
>>> import matplotlib.pyplot as plt
>>> [X, Y] = np.meshgrid(2 * np.pi * np.arange(200) / 12,
... 2 * np.pi * np.arange(200) / 34)
>>> S = np.sin(X) + np.cos(Y) + np.random.uniform(0, 1, X.shape)
>>> FS = np.fft.fftn(S)
>>> plt.imshow(np.log(np.abs(np.fft.fftshift(FS))**2))
<matplotlib.image.AxesImage object at 0x...>
>>> plt.show()
```


numpy.fft.ifftn ( $a, s=$ None, axes=None)
Compute the N -dimensional inverse discrete Fourier Transform.
This function computes the inverse of the N -dimensional discrete Fourier Transform over any number of axes in an M-dimensional array by means of the Fast Fourier Transform (FFT). In other words, ifftn (fftn (a)) $==a$ to within numerical accuracy. For a description of the definitions and conventions used, see numpy.fft.

The input, analogously to ifft, should be ordered in the same way as is returned by fftn, i.e. it should have the term for zero frequency in all axes in the low-order corner, the positive frequency terms in the first half of all axes, the term for the Nyquist frequency in the middle of all axes and the negative frequency terms in the second half of all axes, in order of decreasingly negative frequency.

## Parameters

a : array_like
Input array, can be complex.
$\mathbf{s}$ : sequence of ints, optional
Shape (length of each transformed axis) of the output (s [0] refers to axis $0, \mathrm{~s}[1]$ to axis 1 , etc.). This corresponds to $n$ for ifft ( $x, n$ ). Along any axis, if the given shape is smaller than that of the input, the input is cropped. If it is larger, the input is padded with zeros. if $s$ is not given, the shape of the input (along the axes specified by axes) is used. See notes for issue on ifft zero padding.
axes : sequence of ints, optional
Axes over which to compute the IFFT. If not given, the last len (s) axes are used, or all axes if $s$ is also not specified. Repeated indices in axes means that the inverse transform over that axis is performed multiple times.

## Returns

out : complex ndarray
The truncated or zero-padded input, transformed along the axes indicated by axes, or by a combination of $s$ or $a$, as explained in the parameters section above.

## Raises

ValueError :
If $s$ and axes have different length.

## IndexError :

If an element of axes is larger than than the number of axes of $a$.

## See Also:

numpy.fft
Overall view of discrete Fourier transforms, with definitions and conventions used.
fftn
The forward $n$-dimensional FFT, of which ifftn is the inverse.
ifft
The one-dimensional inverse FFT.
ifft2
The two-dimensional inverse FFT.

```
ifftshift
```

Undoes fftshift, shifts zero-frequency terms to beginning of array.

## Notes

See numpy.fft for definitions and conventions used.
Zero-padding, analogously with ifft, is performed by appending zeros to the input along the specified dimension. Although this is the common approach, it might lead to surprising results. If another form of zero padding is desired, it must be performed before ifftn is called.

## Examples

```
>>> a = np.eye(4)
>>> np.fft.ifftn(np.fft.fftn(a, axes=(0,)), axes=(1,))
array([[ 1.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
    [ 0.+0.j, 1.+0.j, 0.+0.j, 0.+0.j],
    [ 0.+0.j, 0.+0.j, 1.+0.j, 0.+0.j],
    [0.+0.j, 0.+0.j, 0.+0.j, 1.+0.j]])
```

Create and plot an image with band-limited frequency content:

```
>>> import matplotlib.pyplot as plt
>>> n = np.zeros((200,200), dtype=complex)
>>> n[60:80, 20:40] = np.exp(1j*np.random.uniform(0, 2*np.pi, (20, 20)))
>>> im = np.fft.ifftn(n).real
>>> plt.imshow(im)
<matplotlib.image.AxesImage object at 0x...>
>>> plt.show()
```



### 3.6.2 Real FFTs

$$
\begin{array}{ll}
\operatorname{rfft}(\mathrm{a}[, \mathrm{n}, \mathrm{axis}]) & \text { Compute the one-dimensional discrete Fourier Transform for real input. } \\
\text { irfft }(\mathrm{a}[, \mathrm{n}, \mathrm{axis}]) & \text { Compute the inverse of the } \mathrm{n} \text {-point DFT for real input. } \\
\mathrm{rfft2}(\mathrm{a}[, \mathrm{~s}, \mathrm{axes}]) & \text { Compute the 2-dimensional FFT of a real array. } \\
\text { irfft2(a[,s, axes] }) & \text { Compute the 2-dimensional inverse FFT of a real array. } \\
\operatorname{rfftn}(\mathrm{a}[, \mathrm{~s}, \mathrm{axes}]) & \text { Compute the N-dimensional discrete Fourier Transform for real input. } \\
\text { irfftn(a[,s, axes] }) & \text { Compute the inverse of the N-dimensional FFT of real input. } \\
\hline
\end{array}
$$

numpy.fft.rfft ( $a, n=$ None, axis=-1)
Compute the one-dimensional discrete Fourier Transform for real input.
This function computes the one-dimensional $n$-point discrete Fourier Transform (DFT) of a real-valued array by means of an efficient algorithm called the Fast Fourier Transform (FFT).

## Parameters

a : array_like

## Input array

$\mathbf{n}$ : int, optional
Number of points along transformation axis in the input to use. If $n$ is smaller than the length of the input, the input is cropped. If it is larger, the input is padded with zeros. If $n$ is not given, the length of the input (along the axis specified by axis) is used.
axis : int, optional
Axis over which to compute the FFT. If not given, the last axis is used.

## Returns

out : complex ndarray
The truncated or zero-padded input, transformed along the axis indicated by axis, or the last one if axis is not specified. The length of the transformed axis is $n / 2+1$.

## Raises

IndexError :
If axis is larger than the last axis of $a$.

## See Also:

```
numpy.fft
```

For definition of the DFT and conventions used.

```
irfft
```

The inverse of $r f f t$.
fft
The one-dimensional FFT of general (complex) input.

```
fftn
```

The $n$-dimensional FFT.

```
rfftn
```

The $n$-dimensional FFT of real input.

## Notes

When the DFT is computed for purely real input, the output is Hermite-symmetric, i.e. the negative frequency terms are just the complex conjugates of the corresponding positive-frequency terms, and the negative-frequency terms are therefore redundant. This function does not compute the negative frequency terms, and the length of the transformed axis of the output is therefore $n / 2+1$.
When $A=r f f t(a), A[0]$ contains the zero-frequency term, which must be purely real due to the Hermite symmetry.

If $n$ is even, A [ -1 ] contains the term for frequencies $n / 2$ and $-n / 2$, and must also be purely real. If $n$ is odd, $A[-1]$ contains the term for frequency $A[(n-1) / 2]$, and is complex in the general case.
If the input $a$ contains an imaginary part, it is silently discarded.

## Examples

```
>>> np.fft.fft([0, 1, 0, 0])
array([ 1.+0.j, 0.-1.j, -1.+0.j, 0.+1.j])
>>> np.fft.rfft([0, 1, 0, 0])
array([ 1.+0.j, 0.-1.j, -1.+0.j])
```

Notice how the final element of the $f f t$ output is the complex conjugate of the second element, for real input. For $r f f t$, this symmetry is exploited to compute only the non-negative frequency terms.
numpy.fft.irfft ( $a, n=$ None, axis=- 1 )
Compute the inverse of the n -point DFT for real input.
This function computes the inverse of the one-dimensional $n$-point discrete Fourier Transform of real input computed by rfft. In other words, $\operatorname{irfft}(\operatorname{rfft}(a), \operatorname{len}(a))==a$ to within numerical accuracy. (See Notes below for why len (a) is necessary here.)
The input is expected to be in the form returned by $r f f t$, i.e. the real zero-frequency term followed by the complex positive frequency terms in order of increasing frequency. Since the discrete Fourier Transform of real input is Hermite-symmetric, the negative frequency terms are taken to be the complex conjugates of the corresponding positive frequency terms.

## Parameters

a: array_like
The input array.
$\mathbf{n}$ : int, optional

Length of the transformed axis of the output. For $n$ output points, $n / 2+1$ input points are necessary. If the input is longer than this, it is cropped. If it is shorter than this, it is padded with zeros. If $n$ is not given, it is determined from the length of the input (along the axis specified by axis).
axis : int, optional
Axis over which to compute the inverse FFT.

## Returns

out : ndarray
The truncated or zero-padded input, transformed along the axis indicated by axis, or the last one if axis is not specified. The length of the transformed axis is $n$, or, if $n$ is not given, $2 *(m-1)$ where $m$ is the length of the transformed axis of the input. To get an odd number of output points, $n$ must be specified.

## Raises

## IndexError :

If axis is larger than the last axis of $a$.

## See Also:

numpy.fft
For definition of the DFT and conventions used.

```
rfft
```

The one-dimensional FFT of real input, of which irfft is inverse.
fft
The one-dimensional FFT.

## irfft2

The inverse of the two-dimensional FFT of real input.
irfftn
The inverse of the $n$-dimensional FFT of real input.

## Notes

Returns the real valued $n$-point inverse discrete Fourier transform of $a$, where $a$ contains the non-negative frequency terms of a Hermite-symmetric sequence. $n$ is the length of the result, not the input.
If you specify an $n$ such that $a$ must be zero-padded or truncated, the extra/removed values will be added/removed at high frequencies. One can thus resample a series to $m$ points via Fourier interpolation by: a_resamp $=\operatorname{irfft}(r f f t(a), m)$.

## Examples

```
>>> np.fft.ifft([1, -1j, -1, 1j])
array([ 0.+0.j, 1.+0.j, 0.+0.j, 0.+0.j])
>>> np.fft.irfft([1, -1j, -1])
array([ 0., 1., 0., 0.])
```

Notice how the last term in the input to the ordinary ifft is the complex conjugate of the second term, and the output has zero imaginary part everywhere. When calling irfft, the negative frequencies are not specified, and the output array is purely real.
numpy.fft. $\mathbf{r f f t} \mathbf{2}(a, s=$ None, axes=( $-2,-1))$
Compute the 2-dimensional FFT of a real array.

## Parameters

$\mathbf{a}$ : array
Input array, taken to be real.
$\mathbf{s}$ : sequence of ints, optional
Shape of the FFT.
axes: sequence of ints, optional
Axes over which to compute the FFT.

## Returns

out : ndarray
The result of the real 2-D FFT.

## See Also:

rfftn
Compute the N -dimensional discrete Fourier Transform for real input.

## Notes

This is really just $r f f t n$ with different default behavior. For more details see $r f f t n$.
numpy.fft.irfft2 ( $a, s=$ None, axes=( $-2,-1$ ) )
Compute the 2-dimensional inverse FFT of a real array.

## Parameters

a : array_like
The input array
$\mathbf{s}$ : sequence of ints, optional
Shape of the inverse FFT.
axes: sequence of ints, optional
The axes over which to compute the inverse fft. Default is the last two axes.

## Returns

out : ndarray
The result of the inverse real 2-D FFT.

## See Also:

irfftn
Compute the inverse of the N -dimensional FFT of real input.

## Notes

This is really irfftn with different defaults. For more details see irfftn.
numpy.fft.rfftn ( $a, s=$ None, axes=None)
Compute the N -dimensional discrete Fourier Transform for real input.
This function computes the N-dimensional discrete Fourier Transform over any number of axes in an Mdimensional real array by means of the Fast Fourier Transform (FFT). By default, all axes are transformed, with the real transform performed over the last axis, while the remaining transforms are complex.

## Parameters

a : array_like
Input array, taken to be real.
s: sequence of ints, optional
Shape (length along each transformed axis) to use from the input. ( $\mathrm{s}[0]$ refers to axis $0, s[1]$ to axis 1 , etc.). The final element of $s$ corresponds to $n$ for $r f f t(x, n)$, while for the remaining axes, it corresponds to $n$ for $\mathrm{fft}(\mathrm{x}, \mathrm{n})$. Along any axis, if the given shape is smaller than that of the input, the input is cropped. If it is larger, the input is padded with zeros. if $s$ is not given, the shape of the input (along the axes specified by axes) is used.
axes : sequence of ints, optional
Axes over which to compute the FFT. If not given, the last len (s) axes are used, or all axes if $s$ is also not specified.

## Returns

out : complex ndarray
The truncated or zero-padded input, transformed along the axes indicated by axes, or by a combination of $s$ and $a$, as explained in the parameters section above. The length of the last axis transformed will be $s[-1] / / 2+1$, while the remaining transformed axes will have lengths according to $s$, or unchanged from the input.

## Raises

## ValueError :

If $s$ and axes have different length.

## IndexError :

If an element of axes is larger than than the number of axes of $a$.

```
See Also:
irfftn
    The inverse of rfftn, i.e. the inverse of the n-dimensional FFT of real input.
fft
    The one-dimensional FFT, with definitions and conventions used.
rfft
    The one-dimensional FFT of real input.
fftn
    The n-dimensional FFT.
rfft2
    The two-dimensional FFT of real input.
```


## Notes

The transform for real input is performed over the last transformation axis, as by $r f f$, then the transform over the remaining axes is performed as by fft . The order of the output is as for $r f f t$ for the final transformation axis, and as for fft for the remaining transformation axes.
See $f f t$ for details, definitions and conventions used.

## Examples

```
>>> a = np.ones((2, 2, 2))
>>> np.fft.rfftn(a)
array([[[ 8.+0.j, 0.+0.j],
    [ 0.+0.j, 0.+0.j]],
    [[ 0.+0.j, 0.+0.j],
    [ 0.+0.j, 0.+0.j]]])
>>> np.fft.rfftn(a, axes=(2, 0))
array([[[ 4.+0.j, 0.+0.j],
    [ 4.+0.j, 0.+0.j]],
    [[ 0.+0.j, 0.+0.j],
    [ 0.+0.j, 0.+0.j]]])
```

numpy.fft.irfftn ( $a, s=$ None, axes=None)

Compute the inverse of the N -dimensional FFT of real input.
This function computes the inverse of the N-dimensional discrete Fourier Transform for real input over any number of axes in an M-dimensional array by means of the Fast Fourier Transform (FFT). In other words, irfftn (rfftn(a), a.shape) == a to within numerical accuracy. (The a.shape is necessary like len (a) is for irfft, and for the same reason.)

The input should be ordered in the same way as is returned by $r f f t n$, i.e. as for $i r f f t$ for the final transformation axis, and as for ifftn along all the other axes.

## Parameters

a : array_like
Input array.
$\mathbf{s}$ : sequence of ints, optional
Shape (length of each transformed axis) of the output ( $\mathrm{s}[0]$ refers to axis $0, \mathrm{~s}$ [1] to axis 1 , etc.). $s$ is also the number of input points used along this axis, except for the last axis, where $s[-1] / / 2+1$ points of the input are used. Along any axis, if the shape indicated by $s$ is smaller than that of the input, the input is cropped. If it is larger, the input is padded with zeros. If $s$ is not given, the shape of the input (along the axes specified by axes) is used.
axes : sequence of ints, optional
Axes over which to compute the inverse FFT. If not given, the last $\operatorname{len}(s)$ axes are used, or all axes if $s$ is also not specified. Repeated indices in axes means that the inverse transform over that axis is performed multiple times.

## Returns

out : ndarray
The truncated or zero-padded input, transformed along the axes indicated by axes, or by a combination of $s$ or $a$, as explained in the parameters section above. The length of each transformed axis is as given by the corresponding element of $s$, or the length of the input in every axis except for the last one if $s$ is not given. In the final transformed axis the length of the output when $s$ is not given is $2 \star(m-1)$ where $m$ is the length of the final transformed axis of the input. To get an odd number of output points in the final axis, $s$ must be specified.

## Raises

## ValueError :

If $s$ and axes have different length.

## IndexError :

If an element of axes is larger than than the number of axes of $a$.

## See Also:

rfftn
The forward n-dimensional FFT of real input, of which ifftn is the inverse.
fft
The one-dimensional FFT, with definitions and conventions used.
irfft
The inverse of the one-dimensional FFT of real input.
irfft2
The inverse of the two-dimensional FFT of real input.

## Notes

See fft for definitions and conventions used.
See rfft for definitions and conventions used for real input.

## Examples

```
>>> a = np.zeros((3, 2, 2))
>>> a[0, 0, 0] = 3 * 2 * 2
>>> np.fft.irfftn(a)
array([[[ 1., 1.],
    [ 1., 1.]],
    [[ 1., 1.],
    [ 1., 1.]],
    [[ 1., 1.],
    [ 1., 1.]]])
```


### 3.6.3 Hermitian FFTs

hfft(a[, n, axis]) Compute the FFT of a signal whose spectrum has Hermitian symmetry. ihfft(a[, n, axis]) Compute the inverse FFT of a signal whose spectrum has Hermitian symmetry.
numpy.fft. $\mathrm{hfft}(a, n=$ None, axis=- 1 )
Compute the FFT of a signal whose spectrum has Hermitian symmetry.

## Parameters

a : array_like
The input array.
n : int, optional
The length of the FFT.
axis : int, optional
The axis over which to compute the FFT, assuming Hermitian symmetry of the spectrum. Default is the last axis.

## Returns

out : ndarray
The transformed input.

## See Also:

rfft
Compute the one-dimensional FFT for real input.
ihfft
The inverse of $h f f t$.

## Notes

$h f f t / i h f f t$ are a pair analogous to $r f f t / i r f f t$, but for the opposite case: here the signal is real in the frequency domain and has Hermite symmetry in the time domain. So here it's hfft for which you must supply the length of the result if it is to be odd: ihfft (hfft(a), len(a)) == a, within numerical accuracy.

## Examples

```
>>> signal = np.array([[1, 1.j], [-1.j, 2]])
>>> np.conj(signal.T) - signal # check Hermitian symmetry
array([[ 0.-0.j, 0.+0.j],
    [ 0.+0.j, 0.-0.j]])
>>> freq_spectrum = np.fft.hfft(signal)
>>> freq_spectrum
array([[ 1., 1.],
    [ 2., -2.]])
```

numpy.fft.ihfft ( $a, n=$ None, axis=- 1 )

Compute the inverse FFT of a signal whose spectrum has Hermitian symmetry.

## Parameters

a: array_like
Input array.
$\mathbf{n}$ : int, optional
Length of the inverse FFT.
axis : int, optional
Axis over which to compute the inverse FFT, assuming Hermitian symmetry of the spectrum. Default is the last axis.

## Returns

out : ndarray
The transformed input.

## See Also:

```
hfft,irfft
```


## Notes

$h f f t / i h f f t$ are a pair analogous to $r f f t / i r f f t$, but for the opposite case: here the signal is real in the frequency domain and has Hermite symmetry in the time domain. So here it's hfft for which you must supply the length of the result if it is to be odd: ihfft (hfft(a), len(a)) ==a, within numerical accuracy.

### 3.6.4 Helper routines

```
fftfreq(n[,d]) Return the Discrete Fourier Transform sample frequencies.
fftshift(x[,axes]) Shift the zero-frequency component to the center of the spectrum.
ifftshift(x[,axes]) The inverse of fftshift.
numpy.fft.fftfreq( }n,d=1.0
```

Return the Discrete Fourier Transform sample frequencies.
The returned float array contains the frequency bins in cycles/unit (with zero at the start) given a window length $n$ and a sample spacing $d$ :

```
f = [0, 1, ..., n/2-1, -n/2, ..., -1] / (d*n) if n is even
f = [0, 1, ..., (n-1)/2, -(n-1)/2, ..., -1] / (d*n) if n is odd
```


## Parameters

$\mathbf{n}$ : int
Window length.
d : scalar
Sample spacing.

## Returns

out : ndarray
The array of length $n$, containing the sample frequencies.

## Examples

```
>>> signal = np.array([-2, 8, 6, 4, 1, 0, 3, 5], dtype=float)
>>> fourier = np.fft.fft(signal)
>>> n = signal.size
>>> timestep = 0.1
>>> freq = np.fft.fftfreq(n, d=timestep)
>>> freq
array([ 0. , 1.25, 2.5 , 3.75, -5. , -3.75, -2.5 , -1.25])
```

numpy.fft.fftshift ( $x$, axes=None)
Shift the zero-frequency component to the center of the spectrum.
This function swaps half-spaces for all axes listed (defaults to all). Note that $\mathrm{y}[0]$ is the Nyquist component only if len ( $x$ ) is even.

## Parameters

$\mathbf{x}$ : array_like
Input array.
axes : int or shape tuple, optional
Axes over which to shift. Default is None, which shifts all axes.

## Returns

$\mathbf{y}$ : ndarray
The shifted array.

## See Also:

ifftshift
The inverse of fftshift.

## Examples

```
>>> freqs = np.fft.fftfreq(10, 0.1)
>>> freqs
array([ 0., 1., 2., 3., 4., -5., -4., -3., -2., -1.])
>>> np.fft.fftshift(freqs)
array([-5., -4., -3., -2., -1., 0., 1., 2., 3., 4.])
```

Shift the zero-frequency component only along the second axis:

```
>>> freqs = np.fft.fftfreq(9, d=1./9).reshape(3, 3)
>>> freqs
array([[ 0., 1., 2.],
    [ 3., 4., -4.],
    [-3., -2., -1.]])
>>> np.fft.fftshift(freqs, axes=(1,))
array([[ 2., 0., 1.],
    [-4., 3., 4.],
    [-1., -3., -2.]])
```

numpy.fft.ifftshift ( $x$, axes=None)

The inverse of fftshift.

## Parameters

$\mathbf{x}$ : array_like
Input array.
axes : int or shape tuple, optional
Axes over which to calculate. Defaults to None, which shifts all axes.

## Returns

$\mathbf{y}$ : ndarray
The shifted array.

## See Also:

```
fftshift
```

Shift zero-frequency component to the center of the spectrum.

## Examples

```
>>> freqs = np.fft.fftfreq(9, d=1./9).reshape(3, 3)
>>> freqs
array([[ 0., 1., 2.],
    [ 3., 4., -4.],
    [-3., -2., -1.]])
>>> np.fft.ifftshift(np.fft.fftshift(freqs))
array([[ 0., 1., 2.],
    [ 3., 4., -4.],
    [-3., -2., -1.]])
```


### 3.6.5 Background information

Fourier analysis is fundamentally a method for expressing a function as a sum of periodic components, and for recovering the signal from those components. When both the function and its Fourier transform are replaced with discretized counterparts, it is called the discrete Fourier transform (DFT). The DFT has become a mainstay of numerical computing in part because of a very fast algorithm for computing it, called the Fast Fourier Transform (FFT), which was
known to Gauss (1805) and was brought to light in its current form by Cooley and Tukey [CT]. Press et al. [NR] provide an accessible introduction to Fourier analysis and its applications.
Because the discrete Fourier transform separates its input into components that contribute at discrete frequencies, it has a great number of applications in digital signal processing, e.g., for filtering, and in this context the discretized input to the transform is customarily referred to as a signal, which exists in the time domain. The output is called a spectrum or transform and exists in the frequency domain.

There are many ways to define the DFT, varying in the sign of the exponent, normalization, etc. In this implementation, the DFT is defined as

$$
A_{k}=\sum_{m=0}^{n-1} a_{m} \exp \left\{-2 \pi i \frac{m k}{n}\right\} \quad k=0, \ldots, n-1
$$

The DFT is in general defined for complex inputs and outputs, and a single-frequency component at linear frequency $f$ is represented by a complex exponential $a_{m}=\exp \{2 \pi i f m \Delta t\}$, where $\Delta t$ is the sampling interval.

The values in the result follow so-called "standard" order: If $A=f f t(a, n)$, then $A[0]$ contains the zerofrequency term (the mean of the signal), which is always purely real for real inputs. Then $A[1: n / 2]$ contains the positive-frequency terms, and $A[n / 2+1:]$ contains the negative-frequency terms, in order of decreasingly negative frequency. For an even number of input points, A [ $n / 2$ ] represents both positive and negative Nyquist frequency, and is also purely real for real input. For an odd number of input points, $A[(n-1) / 2]$ contains the largest positive frequency, while $A[(n+1) / 2]$ contains the largest negative frequency. The routine np.fft.fftfreq (A) returns an array giving the frequencies of corresponding elements in the output. The routine np.fft.fftshift (A) shifts transforms and their frequencies to put the zero-frequency components in the middle, and np.fft.ifftshift (A) undoes that shift.

When the input $a$ is a time-domain signal and $A=f f t(a), n p . a b s(A)$ is its amplitude spectrum and np.abs (A) $* * 2$ is its power spectrum. The phase spectrum is obtained by np.angle (A).

The inverse DFT is defined as

$$
a_{m}=\frac{1}{n} \sum_{k=0}^{n-1} A_{k} \exp \left\{2 \pi i \frac{m k}{n}\right\} \quad n=0, \ldots, n-1
$$

It differs from the forward transform by the sign of the exponential argument and the normalization by $1 / n$.

## Real and Hermitian transforms

When the input is purely real, its transform is Hermitian, i.e., the component at frequency $f_{k}$ is the complex conjugate of the component at frequency $-f_{k}$, which means that for real inputs there is no information in the negative frequency components that is not already available from the positive frequency components. The family of $r f f t$ functions is designed to operate on real inputs, and exploits this symmetry by computing only the positive frequency components, up to and including the Nyquist frequency. Thus, $n$ input points produce $n / 2+1$ complex output points. The inverses of this family assumes the same symmetry of its input, and for an output of $n$ points uses $n / 2+1$ input points.

Correspondingly, when the spectrum is purely real, the signal is Hermitian. The hfft family of functions exploits this symmetry by using $n / 2+1$ complex points in the input (time) domain for $n$ real points in the frequency domain.

In higher dimensions, FFTs are used, e.g., for image analysis and filtering. The computational efficiency of the FFT means that it can also be a faster way to compute large convolutions, using the property that a convolution in the time domain is equivalent to a point-by-point multiplication in the frequency domain.

In two dimensions, the DFT is defined as

$$
A_{k l}=\sum_{m=0}^{M-1} \sum_{n=0}^{N-1} a_{m n} \exp \left\{-2 \pi i\left(\frac{m k}{M}+\frac{n l}{N}\right)\right\} \quad k=0, \ldots, N-1 ; \quad l=0, \ldots, M-1
$$

which extends in the obvious way to higher dimensions, and the inverses in higher dimensions also extend in the same way.

## References

## Examples

For examples, see the various functions.

### 3.7 Linear algebra (numpy.linalg)

### 3.7.1 Matrix and vector products

| $\operatorname{dot}(\mathrm{a}, \mathrm{b}[$, out $])$ | Dot product of two arrays. |
| :--- | :--- |
| $\operatorname{vdot}$ | Return the dot product of two vectors. |
| inner $(\mathrm{a}, \mathrm{b})$ | Inner product of two arrays. |
| outer $(\mathrm{a}, \mathrm{b})$ | Compute the outer product of two vectors. |
| tensordot $(\mathrm{a}, \mathrm{b}[$, axes $])$ | Compute tensor dot product along specified axes for arrays >= 1-D. |
| einsum(subscripts, *operands[, out, dtype, ...]) | Evaluates the Einstein summation convention on the operands. |
| linalg.matrix_power(M, n) | Raise a square matrix to the (integer) power $n$. |
| kron $(\mathrm{a}, \mathrm{b})$ | Kronecker product of two arrays. |

numpy . dot ( $a, b$, out=None)
Dot product of two arrays.
For 2-D arrays it is equivalent to matrix multiplication, and for 1-D arrays to inner product of vectors (without complex conjugation). For N dimensions it is a sum product over the last axis of $a$ and the second-to-last of $b$ :

```
dot(a, b)[i,j,k,m] = sum(a[i,j,:] * b[k,:,m])
```


## Parameters

a : array_like
First argument.
b: array_like
Second argument.
out : ndarray, optional
Output argument. This must have the exact kind that would be returned if it was not used. In particular, it must have the right type, must be C-contiguous, and its dtype must be the dtype that would be returned for $\operatorname{dot}(a, b)$. This is a performance feature. Therefore, if these conditions are not met, an exception is raised, instead of attempting to be flexible.

## Returns

output : ndarray

Returns the dot product of $a$ and $b$. If $a$ and $b$ are both scalars or both 1-D arrays then a scalar is returned; otherwise an array is returned. If out is given, then it is returned.

## Raises

## ValueError :

If the last dimension of $a$ is not the same size as the second-to-last dimension of $b$.

```
See Also:
vdot
    Complex-conjugating dot product.
tensordot
```

Sum products over arbitrary axes.

```
einsum
```

    Einstein summation convention.
    
## Examples

```
>>> np.dot(3, 4)
12
```

Neither argument is complex-conjugated:

```
>>> np.dot([2j, 3j], [2j, 3j])
(-13+0j)
```

For 2-D arrays it's the matrix product:

```
>>> a = [[1, 0], [0, 1]]
>>> b = [[4, 1], [2, 2]]
>>> np.dot(a, b)
array([[4, 1],
    [2, 2]])
>>> a = np.arange ( }3*4*5*6).reshape((3,4,5,6)
>>> b = np.arange( }3*4*5*6)[::-1].reshape((5,4,6,3)
>>> np.dot(a, b)[2,3,2,1,2,2]
499128
>>> sum(a[2,3,2,:] * b[1,2,:,2])
499128
```

numpy.vdot ()
Return the dot product of two vectors.
The $\operatorname{vdot}(a, b)$ function handles complex numbers differently than $\operatorname{dot}(a, b)$. If the first argument is complex the complex conjugate of the first argument is used for the calculation of the dot product.

Note that vdot handles multidimensional arrays differently than dot: it does not perform a matrix product, but flattens input arguments to 1-D vectors first. Consequently, it should only be used for vectors.

## Parameters

a : array_like
If $a$ is complex the complex conjugate is taken before calculation of the dot product.
b : array_like
Second argument to the dot product.

## Returns

output : ndarray
Dot product of $a$ and $b$. Can be an int, float, or complex depending on the types of $a$ and $b$.

## See Also:

dot
Return the dot product without using the complex conjugate of the first argument.
Examples

```
>>> a = np.array([1+2j,3+4j])
>>> b = np.array([5+6j,7+8j])
>>> np.vdot(a, b)
(70-8j)
>>> np.vdot(b, a)
(70+8j)
```

Note that higher-dimensional arrays are flattened!

```
>>> a = np.array([[1, 4], [5, 6]])
>>> b = np.array([[4, 1], [2, 2]])
>>> np.vdot(a, b)
30
>>> np.vdot (b, a)
30
>>> 1*4 + 4*1 + 5*2 + 6*2
30
```

numpy.inner $(a, b)$

Inner product of two arrays.
Ordinary inner product of vectors for 1-D arrays (without complex conjugation), in higher dimensions a sum product over the last axes.

## Parameters

$\mathbf{a}, \mathbf{b}:$ array_like
If $a$ and $b$ are nonscalar, their last dimensions of must match.

## Returns

out : ndarray
out.shape $=$ a.shape $[:-1]+$ b.shape $[:-1]$

## Raises

## ValueError :

If the last dimension of $a$ and $b$ has different size.

## See Also:

```
    tensordot
```

        Sum products over arbitrary axes.
    dot
    Generalised matrix product, using second last dimension of $b$.
einsum
Einstein summation convention.

## Notes

For vectors (1-D arrays) it computes the ordinary inner-product:

```
np.inner(a, b) = sum(a[:]*b[:])
```

More generally, if $\operatorname{ndim}(a)=r>0$ and $\operatorname{ndim}(b)=s>0$ :

```
np.inner(a, b) = np.tensordot(a, b, axes=(-1,-1))
```

or explicitly:

```
np.inner(a, b)[i0,...,ir-1,j0,...,js-1]
    = sum(a[i0,...,ir-1,:]*b[j0,...,js-1,:])
```

In addition $a$ or $b$ may be scalars, in which case:

```
np.inner (a,b) = a*b
```


## Examples

Ordinary inner product for vectors:

```
>>> a = np.array([1,2,3])
>>> b = np.array([0,1,0])
>>> np.inner(a, b)
2
```

A multidimensional example:

```
>>> a = np.arange(24).reshape((2,3,4))
>>> b = np.arange(4)
>>> np.inner(a, b)
array([[ 14, 38, 62],
    [ 86, 110, 134]])
```

An example where $b$ is a scalar:

```
>>> np.inner(np.eye(2), 7)
array([[ 7., 0.],
    [ 0., 7.]])
```

numpy . outer ( $a, b$ )

Compute the outer product of two vectors.
Given two vectors, $a=[a 0, a 1, \ldots, a M]$ and $b=[b 0, b 1, \ldots, b N]$, the outer product [R52] is:

```
[[a0*b0 a0*bb1 ... a0*bN ]
    [a1*b0
    [ ...
    [aM*b0 aM*bN ]]
```


## Parameters

a, b: array_like, shape (M,), (N,)
First and second input vectors. Inputs are flattened if they are not already 1-dimensional.

## Returns

out : ndarray, shape ( $\mathrm{M}, \mathrm{N}$ )

```
out[i, j] = a[i] * b[j]
```


## See Also:

```
inner, einsum
```


## References

[R52]

## Examples

Make a (very coarse) grid for computing a Mandelbrot set:

```
>>> rl = np.outer(np.ones((5,)), np.linspace(-2, 2, 5))
>>> rl
array([[-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.]])
>>> im = np.outer(1j*np.linspace(2, -2, 5), np.ones((5,)))
>>> im
array([[ 0.+2.j, 0.+2.j, 0.+2.j, 0.+2.j, 0.+2.j],
    [ 0.+1.j, 0.+1.j, 0.+1.j, 0.+1.j, 0.+1.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
    [ 0.-1.j, 0.-1.j, 0.-1.j, 0.-1.j, 0.-1.j],
    [0.-2.j, 0.-2.j, 0.-2.j, 0.-2.j, 0.-2.j]])
>>> grid = rl + im
>>> grid
array([[-2.+2.j, -1.+2.j, 0.+2.j, 1.+2.j, 2.+2.j],
    [-2.+1.j, -1.+1.j, 0.+1.j, 1.+1.j, 2.+1.j],
    [-2.+0.j, -1.+0.j, 0.+0.j, 1.+0.j, 2.+0.j],
    [-2.-1.j, -1.-1.j, 0.-1.j, 1.-1.j, 2.-1.j],
    [-2.-2.j, -1.-2.j, 0.-2.j, 1.-2.j, 2.-2.j]])
```

An example using a "vector" of letters:

```
>>> x = np.array(['a', 'b', 'c'], dtype=object)
>>> np.outer(x, [1, 2, 3])
array([[a, aa, aaa],
    [b, b.b, b.b.b],
    [c, cc, ccc]], dtype=object)
```

numpy.tensordot ( $a, b$, axes=2)
Compute tensor dot product along specified axes for arrays $>=1-\mathrm{D}$.
Given two tensors (arrays of dimension greater than or equal to one), a and b, and an array_like object containing two array_like objects, (a_axes, b_axes), sum the products of a's and b's elements (components) over the axes specified by a_axes and b_axes. The third argument can be a single non-negative integer_like scalar, N ; if it is such, then the last N dimensions of $a$ and the first N dimensions of b are summed over.

## Parameters

$$
\mathbf{a}, \mathbf{b}: \text { array_like, len(shape) }>=1
$$

Tensors to "dot".
axes: variable type

## * integer_like scalar :

Number of axes to sum over (applies to both arrays); or

* array_like, shape $=(2$,$) , both elements array_like :$

Axes to be summed over, first sequence applying to $a$, second to $b$.

## See Also:

```
dot, einsum
```


## Notes

When there is more than one axis to sum over - and they are not the last (first) axes of a (b) - the argument axes should consist of two sequences of the same length, with the first axis to sum over given first in both sequences, the second axis second, and so forth.

## Examples

A "traditional" example:

```
>>> a = np.arange(60.).reshape(3,4,5)
>>> b = np.arange(24.).reshape (4,3,2)
>>> c = np.tensordot(a,b, axes=([1,0],[0,1]))
>>> c.shape
    (5, 2)
>>> c
array([[ 4400., 4730.],
    [ 4532., 4874.],
    [ 4664., 5018.],
    [ 4796., 5162.],
    [ 4928., 5306.]])
>>> # A slower but equivalent way of computing the same...
>>> d = np.zeros((5,2))
>>> for i in range(5):
... for j in range(2):
... for k in range(3):
... for }n\mathrm{ in range(4):
... d[i,j] += a[k,n,i] * b[n,k,j]
>>> C == d
array([[ True, True],
    [ True, True],
    [ True, True],
    [ True, True],
    [ True, True]], dtype=bool)
```

An extended example taking advantage of the overloading of + and $*$ :

```
>>> a = np.array(range(1, 9))
>>> a.shape = (2, 2, 2)
>>> A = np.array(('a', 'b', 'c', 'd'), dtype=object)
>>> A.shape = (2, 2)
>>> a; A
array([[[1, 2],
            [3, 4]],
            [[5, 6],
            [7, 8]]])
array([[a, b],
            [c, d]], dtype=object)
>>> np.tensordot(a, A) # third argument default is 2
array([abbcccdddd, aaaaab.b.b.bcccccccdddddddd], dtype=object)
>>> np.tensordot(a, A, 1)
array([[[acc, bdd],
```

```
    [aaacccc, bbbodddd]],
    [[aaaaacccccc, bbbbbdddddd],
    [aaaaaaacccccccc, b.bbbbbbbdddddddd]]], dtype=object)
>>> np.tensordot(a, A, 0) # "Left for reader" (result too long to incl.)
array([[[[[a, b],
            [c, d]],
>>> np.tensordot(a, A, (0, 1))
array([[[abbb.b.b, cddddd],
    [aa.b.b.b.b, ccdddddd]],
    [[aaabbb.bbbb, cccddddddd],
            [aaaabb.b.b.bb, ccccdddddddd]]], dtype=object)
>>> np.tensordot(a, A, (2, 1))
array([[[abb, cdd],
    [aaabbbb, cccdddd]],
    [[aaaaab.b.b.b, cccccdddddd],
        [aaaaaaabbbbbbbb, cccccccdddddddd]]], dtype=object)
>>> np.tensordot(a, A, ((0, 1), (0, 1)))
array([abbbcccccddddddd, aabbbbccccccdddddddd], dtype=object)
>>> np.tensordot(a, A, ((2, 1), (1, 0)))
array([acccbbdddd, aaaaacccccccbbbbbbdddddddd], dtype=object)
numpy. einsum (subscripts, *operands,out=None, dtype=None,order='K', casting='safe')
Evaluates the Einstein summation convention on the operands.
```

Using the Einstein summation convention, many common multi-dimensional array operations can be represented in a simple fashion. This function provides a way compute such summations. The best way to understand this function is to try the examples below, which show how many common NumPy functions can be implemented as calls to einsum.

## Parameters <br> subscripts : str

Specifies the subscripts for summation.
operands : list of array_like
These are the arrays for the operation.
out : ndarray, optional
If provided, the calculation is done into this array.
dtype : data-type, optional
If provided, forces the calculation to use the data type specified. Note that you may have to also give a more liberal casting parameter to allow the conversions.
order : \{ 'C', ' F ', ' A ', or ' K '\}, optional
Controls the memory layout of the output. 'C' means it should be C contiguous. ' F ' means it should be Fortran contiguous, ' $A$ ' means it should be ' $F$ ' if the inputs are all ' F ', ' C ' otherwise. ' K ' means it should be as close to the layout as the inputs as is possible, including arbitrarily permuted axes. Default is ' K '.
casting : \{'no’, 'equiv', ‘safe', 'same_kind', 'unsafe'\}, optional

Controls what kind of data casting may occur. Setting this to 'unsafe' is not recommended, as it can adversely affect accumulations.

- 'no' means the data types should not be cast at all.
- 'equiv' means only byte-order changes are allowed.
- 'safe' means only casts which can preserve values are allowed.
- 'unsafe' means any data conversions may be done.
- 'same_kind' means only safe casts or casts within a kind, like float64 to float32, are allowed.


## Returns

output : ndarray
The calculation based on the Einstein summation convention.

## See Also:

dot, inner, outer, tensordot

## Notes

The subscripts string is a comma-separated list of subscript labels, where each label refers to a dimension of the corresponding operand. Repeated subscripts labels in one operand take the diagonal. For example, np.einsum('ii', a) is equivalent to np.trace (a).
Whenever a label is repeated, it is summed, so np.einsum('i,i', $a, b)$ is equivalent to $n p$.inner $(a, b)$. If a label appears only once, it is not summed, so np.einsum('i', a) produces a view of a with no changes.

The order of labels in the output is by default alphabetical. This means that np.einsum ('ij', a) doesn't affect a 2D array, while np.einsum ('ji', a) takes its transpose.

The output can be controlled by specifying output subscript labels as well. This specifies the label order, and allows summing to be disallowed or forced when desired. The call np.einsum('i->', a) is like np.sum (a, axis=-1), and np.einsum('ii->i', a) is like np.diag(a). The difference is that einsum does not allow broadcasting by default.
To enable and control broadcasting, use an ellipsis. Default NumPy-style broadcasting is done by adding an ellipsis to the left of each term, like np.einsum(' ...ii->...i', a). To take the trace along the first and last axes, you can do np.einsum('i...i', a), or to do a matrix-matrix product with the left-most indices instead of rightmost, you can do np.einsum ('ij..., jk...->ik...', a, b).

When there is only one operand, no axes are summed, and no output parameter is provided, a view into the operand is returned instead of a new array. Thus, taking the diagonal as np.einsum ('ii->i', a) produces a view.

An alternative way to provide the subscripts and operands is as einsum (op0, sublist0, op1, sublist1, ..., [sublistout]). The examples below have corresponding einsum calls with the two parameter methods.

## Examples

```
>>> a = np.arange(25).reshape(5,5)
>>> b = np.arange(5)
>>> c = np.arange (6).reshape (2,3)
>>> np.einsum('ii', a)
60
>>> np.einsum(a, [0,0])
```

```
60
>>> np.trace(a)
60
>>> np.einsum('ii->i', a)
array([ 0, 6, 12, 18, 24])
>>> np.einsum(a, [0,0], [0])
array([ 0, 6, 12, 18, 24])
>>> np.diag(a)
array([ 0, 6, 12, 18, 24])
>>> np.einsum('ij,j', a, b)
array([ 30, 80, 130, 180, 230])
>>> np.einsum(a, [0,1], b, [1])
array([ 30, 80, 130, 180, 230])
>>> np.dot(a, b)
array([ 30, 80, 130, 180, 230])
>>> np.einsum('ji', c)
array([[0, 3],
    [1, 4],
    [2, 5]])
>>> np.einsum(c, [1,0])
array([[0, 3],
    [1, 4],
    [2, 5]])
>>> C.T
array([[0, 3],
    [1, 4],
    [2, 5]])
>>> np.einsum('..., ...', 3, c)
array([[ 0, 3, 6],
    [ 9, 12, 15]])
>>> np.einsum(3, [Ellipsis], c, [Ellipsis])
array([[ 0, 3, 6],
    [ 9, 12, 15]])
>>> np.multiply(3, c)
array([[ 0, 3, 6],
    [ 9, 12, 15]])
>>> np.einsum('i,i', b, b)
30
>>> np.einsum(b, [0], b, [0])
30
>>> np.inner (b,b)
30
>>> np.einsum('i,j', np.arange(2)+1, b)
array([[0, 1, 2, 3, 4],
    [0, 2, 4, 6, 8]])
>>> np.einsum(np.arange(2)+1, [0], b, [1])
array([[0, 1, 2, 3, 4],
    [0, 2, 4, 6, 8]])
>>> np.outer(np.arange (2)+1, b)
array([[0, 1, 2, 3, 4],
    [0, 2, 4, 6, 8]])
```

```
>>> np.einsum('i...->...', a)
array([50, 55, 60, 65, 70])
>>> np.einsum(a, [0,Ellipsis], [Ellipsis])
array([50, 55, 60, 65, 70])
>>> np.sum(a, axis=0)
array([50, 55, 60, 65, 70])
>>> a = np.arange(60.).reshape (3,4,5)
>>> b = np.arange(24.).reshape(4,3,2)
>>> np.einsum('ijk,jil->kl', a, b)
array([[ 4400., 4730.],
    [ 4532., 4874.],
    [ 4664., 5018.],
    [ 4796., 5162.],
    [ 4928., 5306.]])
>>> np.einsum(a, [0,1,2], b, [1,0,3], [2,3])
array([[ 4400., 4730.],
    [ 4532., 4874.],
    [ 4664., 5018.],
    [ 4796., 5162.],
    [ 4928., 5306.]])
>>> np.tensordot(a,b, axes=([1,0],[0,1]))
array([[ 4400., 4730.],
    [ 4532., 4874.],
    [ 4664., 5018.],
    [ 4796., 5162.],
    [4928., 5306.]])
```

numpy.linalg.matrix_power ( $M, n$ )
Raise a square matrix to the (integer) power $n$.
For positive integers $n$, the power is computed by repeated matrix squarings and matrix multiplications. If $n==$ 0 , the identity matrix of the same shape as $M$ is returned. If $n<0$, the inverse is computed and then raised to the abs ( n ).

## Parameters

$\mathbf{M}$ : ndarray or matrix object
Matrix to be "powered." Must be square, i.e. M. shape $==(m, m)$, with $m$ a positive integer.
n : int
The exponent can be any integer or long integer, positive, negative, or zero.

## Returns

$\mathbf{M}^{* *} \mathbf{n}$ : ndarray or matrix object
The return value is the same shape and type as $M$; if the exponent is positive or zero then the type of the elements is the same as those of $M$. If the exponent is negative the elements are floating-point.

## Raises

## LinAlgError :

If the matrix is not numerically invertible.

## See Also:

matrix
Provides an equivalent function as the exponentiation operator $(* *, \operatorname{not} \wedge)$.

## Examples

```
>>> from numpy import linalg as LA
>>> i = np.array([[0, 1], [-1, 0]]) # matrix equiv. of the imaginary unit
>>> LA.matrix_power(i, 3) # should = -i
array([[ 0, -1],
    [ 1, 0]])
>>> LA.matrix_power(np.matrix(i), 3) # matrix arg returns matrix
matrix([[ 0, -1],
    [ 1, 0]])
>>> LA.matrix_power(i, 0)
array([[1, 0],
    [0, 1]])
>>> LA.matrix_power(i, -3) # should = I/(-i) = i, but w/ f.p. elements
array([[ 0., 1.],
    [-1., 0.]])
```

Somewhat more sophisticated example

```
>>> q = np.zeros((4, 4))
>>> q[0:2, 0:2] = -i
>>> q[2:4, 2:4] = i
>>> q # one of the three quarternion units not equal to I
array([[ 0., -1., 0., 0.],
    [ 1., 0., 0., 0.],
    [ 0., 0., 0., 1.],
    [ 0., 0., -1., 0.]])
>>> LA.matrix_power(q, 2) # = -np.eye(4)
array([[-1., 0., 0., 0.],
    [ 0., -1., 0., 0.],
    [ 0., 0., -1., 0.],
    [ 0., 0., 0., -1.]])
```

numpy. kron ( $a, b$ )
Kronecker product of two arrays.
Computes the Kronecker product, a composite array made of blocks of the second array scaled by the first.

## Parameters

$\mathbf{a}, \mathbf{b}$ : array_like

## Returns

out : ndarray

## See Also:

outer
The outer product

## Notes

The function assumes that the number of dimenensions of $a$ and $b$ are the same, if necessary prepending the smallest with ones. If a.shape $=(r 0, r 1, \ldots, r N)$ and b.shape $=(s 0, s l, \ldots, s N)$, the Kronecker product has shape $\left(r 0 *_{S} 0, r l{ }^{*} S l, \ldots, r N^{*} S N\right)$. The elements are products of elements from $a$ and $b$, organized explicitly by:

$$
\operatorname{kron}(a, b)[k 0, k 1, \ldots, k N]=a[i 0, i 1, \ldots, i N] * b[j 0, j 1, \ldots, j N]
$$

where:

```
kt = it * st + jt, t = 0,\ldots,N
```

In the common 2-D case $(\mathrm{N}=1)$, the block structure can be visualized:

```
[[ a[0,0]*b, a[0,1]*b, ... , a[0,-1]*b ],
    [ ... ... ],
    [a[-1,0]*b, a[-1,1]*b, ... , a[-1,-1]*b ]]
```


## Examples

```
>>> np.kron([1,10,100], [5,6,7])
array([ 5, 6, 7, 50, 60, 70, 500, 600, 700])
>>> np.kron([5,6,7], [1,10,100])
array([ 5, 50, 500, 6, 60, 600, 7, 70, 700])
>>> np.kron(np.eye(2), np.ones((2,2)))
array([[ 1., 1., 0., 0.],
    [ 1., 1., 0., 0.],
    [ 0., 0., 1., 1.],
    [ 0., 0., 1., 1.]])
>>> a = np.arange(100).reshape((2,5,2,5))
>>> b = np.arange(24).reshape( (2,3,4))
>>> c = np.kron(a,b)
>>> c.shape
(2, 10, 6, 20)
>>> I = (1,3,0,2)
>>> J = (0,2,1)
>> J1 = (0,) + J # extend to ndim=4
>>> S1 = (1,) + b.shape
>>> K = tuple(np.array(I) * np.array(S1) + np.array(J1))
>>> c[K] == a[I]*b[J]
True
```


### 3.7.2 Decompositions

| linalg.cholesky(a) | Cholesky decomposition. |
| :--- | :--- |
| linalg.qr(a[, mode]) | Compute the qr factorization of a matrix. |
| linalg.svd(a[, full_matrices, compute_uv]) | Singular Value Decomposition. |

numpy.linalg.cholesky (a)

Cholesky decomposition.
Return the Cholesky decomposition, $L * L . H$, of the square matrix $a$, where $L$ is lower-triangular and. H is the conjugate transpose operator (which is the ordinary transpose if $a$ is real-valued). $a$ must be Hermitian (symmetric if real-valued) and positive-definite. Only $L$ is actually returned.

## Parameters

a : array_like, shape (M, M)
Hermitian (symmetric if all elements are real), positive-definite input matrix.

## Returns

$\mathbf{L}$ : ndarray, or matrix object if $a$ is, shape (M, M)
Lower-triangular Cholesky factor of a.

## Raises

## LinAlgError :

If the decomposition fails, for example, if $a$ is not positive-definite.

## Notes

The Cholesky decomposition is often used as a fast way of solving

$$
A \mathbf{x}=\mathbf{b}
$$

(when $A$ is both Hermitian/symmetric and positive-definite).
First, we solve for $\mathbf{y}$ in

$$
L \mathbf{y}=\mathbf{b}
$$

and then for $\mathbf{x}$ in

$$
L \cdot H \mathbf{x}=\mathbf{y} .
$$

## Examples

```
>>> A = np.array([[1,-2j],[2j,5]])
>>> A
array([[ 1.+0.j, 0.-2.j],
    [ 0.+2.j, 5.+0.j]])
>>> L = np.linalg.cholesky(A)
>>> L
array([[ 1.+0.j, 0.+0.j],
    [ 0.+2.j, 1.+0.j]])
>>> np.dot(L, L.T.conj()) # verify that L * L.H = A
array([[ 1.+0.j, 0.-2.j],
    [ 0.+2.j, 5.+0.j]])
>>> A = [[1,-2j],[2j,5]] # what happens if A is only array_like?
>>> np.linalg.cholesky(A) # an ndarray object is returned
array([[ 1.+0.j, 0.+0.j],
    [ 0.+2.j, 1.+0.j]])
>>> # But a matrix object is returned if A is a matrix object
>>> LA.cholesky(np.matrix(A))
matrix([[ 1.+0.j, 0.+0.j],
    [ 0.+2.j, 1.+0.j]])
```

numpy.linalg.qr (a, mode='full')

Compute the qr factorization of a matrix.
Factor the matrix $a$ as $q r$, where $q$ is orthonormal and $r$ is upper-triangular.

## Parameters

a : array_like
Matrix to be factored, of shape ( $\mathrm{M}, \mathrm{N}$ ).
mode : \{'full', 'r', 'economic'\}, optional
Specifies the values to be returned. 'full' is the default. Economic mode is slightly faster then ' $r$ ' mode if only $r$ is needed.

## Returns

$\mathbf{q}$ : ndarray of float or complex, optional
The orthonormal matrix, of shape (M, K). Only returned if mode=' full'.
$\mathbf{r}$ : ndarray of float or complex, optional
The upper-triangular matrix, of shape $(K, N)$ with $K=\min (M, N)$. Only returned when mode=' full' or mode=' r'.
a2 : ndarray of float or complex, optional
Array of shape ( $M, N$ ), only returned when mode='economic'. The diagonal and the upper triangle of $a 2$ contains $r$, while the rest of the matrix is undefined.

## Raises

## LinAlgError :

If factoring fails.

## Notes

This is an interface to the LAPACK routines dgeqrf, zgeqrf, dorgqr, and zungqr.
For more information on the qr factorization, see for example: http://en.wikipedia.org/wiki/QR_factorization
Subclasses of ndarray are preserved, so if $a$ is of type matrix, all the return values will be matrices too.

## Examples

```
>>> a = np.random.randn(9, 6)
>>> q, r = np.linalg.qr(a)
>>> np.allclose(a, np.dot(q, r)) # a does equal qr
True
>>> r2 = np.linalg.qr(a, mode='r')
>>> r3 = np.linalg.qr(a, mode='economic')
>>> np.allclose(r, r2) # mode='r' returns the same r as mode='full'
True
>>> # But only triu parts are guaranteed equal when mode='economic'
>>> np.allclose(r, np.triu(r3[:6,:6], k=0))
True
```

Example illustrating a common use of $q r$ : solving of least squares problems
What are the least-squares-best $m$ and $y 0$ in $y=y 0+m x$ for the following data: $\{(0,1),(1,0),(1,2),(2,1)\}$. (Graph the points and you'll see that it should be $\mathrm{y} 0=0, \mathrm{~m}=1$.) The answer is provided by solving the over-determined matrix equation $A x=b$, where:

```
A = array([[0, 1], [1, 1], [1, 1], [2, 1]])
x = array([[y0], [m]])
b = array([[1], [0], [2], [1]])
```

If $\mathrm{A}=\mathrm{qr}$ such that q is orthonormal (which is always possible via Gram-Schmidt), then $\mathrm{x}=\operatorname{inv}(\mathrm{r}) *$ (q.T) * b. (In numpy practice, however, we simply use lstsq.)

```
>>> A = np.array([[0, 1], [1, 1], [1, 1], [2, 1]])
>>> A
array([[0, 1],
    [1, 1],
    [1, 1],
    [2, 1]])
>>> b = np.array([1, 0, 2, 1])
>>> q, r = LA.qr(A)
>>> p = np.dot(q.T, b)
>>> np.dot(LA.inv(r), p)
array([ 1.1e-16, 1.0e+00])
```

```
numpy.linalg.svd (a,full_matrices=1, compute_uv=1)
```

Singular Value Decomposition.
Factors the matrix $a$ as u $\quad \mathrm{np} . \operatorname{diag}(\mathrm{s}) \quad * \mathrm{v}$, where $u$ and $v$ are unitary and $s$ is a 1-d array of $a$ 's singular values.

## Parameters

a : array_like
A real or complex matrix of shape $(M, N)$.
full_matrices : bool, optional
If True (default), $u$ and $v$ have the shapes $(M, M)$ and $(N, N)$, respectively. Otherwise, the shapes are $(M, K)$ and $(K, N)$, respectively, where $K=\min (M, N)$.
compute_uv : bool, optional
Whether or not to compute $u$ and $v$ in addition to $s$. True by default.

## Returns

$\mathbf{u}$ : ndarray
Unitary matrix. The shape of $u$ is $(M, M)$ or $(M, K)$ depending on value of full_matrices.
s: ndarray
The singular values, sorted so that $s[i]>=s[i+1] . s$ is a 1-d array of length $\min (M, N)$.
$\mathbf{v}$ : ndarray
Unitary matrix of shape $(N, N)$ or $(K, N)$, depending on full_matrices.

## Raises

## LinAlgError :

If SVD computation does not converge.

## Notes

The SVD is commonly written as $\mathrm{a}=\mathrm{U} \mathrm{S} V . \mathrm{H}$. The $v$ returned by this function is $\mathrm{V} . \mathrm{H}$ and $\mathrm{u}=\mathrm{U}$.
If $U$ is a unitary matrix, it means that it satisfies $U . H=\operatorname{inv}(U)$.
The rows of $v$ are the eigenvectors of $\mathrm{a} . \mathrm{H}$ a. The columns of $u$ are the eigenvectors of $\mathrm{a} a$. H. For row i in $v$ and column $i$ in $u$, the corresponding eigenvalue is $s[i] * * 2$.

If $a$ is a matrix object (as opposed to an ndarray), then so are all the return values.

## Examples

```
>>> a = np.random.randn(9, 6) + 1j*np.random.randn (9, 6)
```

Reconstruction based on full SVD:

```
>>> U, s, V = np.linalg.svd(a, full_matrices=True)
>>> U.shape, V.shape, s.shape
((9, 6), (6, 6), (6,))
>>> S = np.zeros((9, 6), dtype=complex)
>>> S[:6, :6] = np.diag(s)
>>> np.allclose(a, np.dot(U, np.dot(S, V)))
True
```

Reconstruction based on reduced SVD:

```
>>> U, s, V = np.linalg.svd(a, full_matrices=False)
>>> U.shape, V.shape, s.shape
((9, 6), (6, 6), (6,))
>>> S = np.diag(s)
>>> np.allclose(a, np.dot(U, np.dot(S, V)))
True
```


### 3.7.3 Matrix eigenvalues

| linalg.eig(a) | Compute the eigenvalues and right eigenvectors of a square array. |
| :--- | :--- |
| linalg.eigh(a[, UPLO]) | Return the eigenvalues and eigenvectors of a Hermitian or symmetric matrix. |
| linalg.eigvals(a) | Compute the eigenvalues of a general matrix. |
| linalg.eigvalsh(a[, UPLO]) | Compute the eigenvalues of a Hermitian or real symmetric matrix. |

numpy.linalg.eig (a)

Compute the eigenvalues and right eigenvectors of a square array.

## Parameters

a : array_like, shape (M, M)
A square array of real or complex elements.

## Returns

$\mathbf{w}$ : ndarray, shape (M,)
The eigenvalues, each repeated according to its multiplicity. The eigenvalues are not necessarily ordered, nor are they necessarily real for real arrays (though for real arrays complex-valued eigenvalues should occur in conjugate pairs).
$\mathbf{v}$ : ndarray, shape (M, M)
The normalized (unit "length") eigenvectors, such that the column $v[:, i]$ is the eigenvector corresponding to the eigenvalue w [i].

## Raises

## LinAlgError :

If the eigenvalue computation does not converge.

## See Also:

eigvalsh
eigenvalues of a symmetric or Hermitian (conjugate symmetric) array.
eigvals
eigenvalues of a non-symmetric array.

## Notes

This is a simple interface to the LAPACK routines dgeev and zgeev which compute the eigenvalues and eigenvectors of, respectively, general real- and complex-valued square arrays.

The number $w$ is an eigenvalue of $a$ if there exists a vector $v$ such that $\operatorname{dot}(\mathrm{a}, \mathrm{v})=\mathrm{w} * \mathrm{v}$. Thus, the arrays $a, w$, and $v$ satisfy the equations $\operatorname{dot}(\mathrm{a}[\mathrm{i},:], \mathrm{v}[\mathrm{i}])=\mathrm{w}[\mathrm{i}] * \mathrm{v}[:, \mathrm{i}]$ for $i \in\{0, \ldots, M-1\}$.

The array $v$ of eigenvectors may not be of maximum rank, that is, some of the columns may be linearly dependent, although round-off error may obscure that fact. If the eigenvalues are all different, then theoretically the eigenvectors are linearly independent. Likewise, the (complex-valued) matrix of eigenvectors $v$ is unitary if the
matrix $a$ is normal, i.e., if $\operatorname{dot}(\mathrm{a}, \mathrm{a} . \mathrm{H})=\operatorname{dot}(\mathrm{a} . \mathrm{H}, \mathrm{a})$, where $a . H$ denotes the conjugate transpose of $a$.

Finally, it is emphasized that $v$ consists of the right (as in right-hand side) eigenvectors of $a$. A vector $y$ satisfying $\operatorname{dot}(\mathrm{Y} . \mathrm{T}, \mathrm{a})=\mathrm{z} * \mathrm{Y} . \mathrm{T}$ for some number $z$ is called a left eigenvector of $a$, and, in general, the left and right eigenvectors of a matrix are not necessarily the (perhaps conjugate) transposes of each other.

## References

G. Strang, Linear Algebra and Its Applications, 2nd Ed., Orlando, FL, Academic Press, Inc., 1980, Various pp.

## Examples

```
>>> from numpy import linalg as LA
```

(Almost) trivial example with real e-values and e-vectors.

```
>>> w, v = LA.eig(np.diag((1, 2, 3)))
>>> W; V
array([ 1., 2., 3.])
array([[ 1., 0., 0.],
    [ 0., 1., 0.],
    [ 0., 0., 1.]])
```

Real matrix possessing complex e-values and e-vectors; note that the e-values are complex conjugates of each other.

```
>>> w, v = LA.eig(np.array([[1, -1], [1, 1]]))
>>> w; v
array([ 1. + 1.j, 1. - 1.j])
array([[ 0.70710678+0.j , 0.70710678+0.j ],
    [ 0.00000000-0.70710678j, 0.000000000+0.70710678j]])
```

Complex-valued matrix with real e-values (but complex-valued e-vectors); note that a.conj(). $\mathrm{T}=\mathrm{a}$, i.e., a is Hermitian.

```
>>> a = np.array([[1, 1j], [-1j, 1]])
>>> w, v = LA.eig(a)
>>> w; v
array([ 2.00000000e+00+0.j, 5.98651912e-36+0.j]) # i.e., {2, 0}
array([[ 0.00000000+0.70710678j, 0.70710678+0.j ],
    [0.70710678+0.j , 0.000000000+0.70710678j]])
```

Be careful about round-off error!

```
>>> a = np.array([[1 + 1e-9, 0], [0, 1 - 1e-9]])
>>> # Theor. e-values are 1 +/- le-9
>>> w, v = LA.eig(a)
>>> w; v
array([ 1., 1.])
array([[ 1., 0.],
    [ 0., 1.]])
```

numpy.linalg.eigh ( $a, U P L O=$ ' $L$ ')

Return the eigenvalues and eigenvectors of a Hermitian or symmetric matrix.
Returns two objects, a 1-D array containing the eigenvalues of $a$, and a 2-D square array or matrix (depending on the input type) of the corresponding eigenvectors (in columns).

## Parameters

a : array_like, shape (M, M)

A complex Hermitian or real symmetric matrix.
UPLO : \{'L', 'U'\}, optional
Specifies whether the calculation is done with the lower triangular part of $a$ (' L ', default) or the upper triangular part ('U').

## Returns

w : ndarray, shape ( M, )
The eigenvalues, not necessarily ordered.
$\mathbf{v}$ : ndarray, or matrix object if $a$ is, shape (M, M)
The column $\mathrm{v}[:, \mathrm{i}]$ is the normalized eigenvector corresponding to the eigenvalue w[i].

## Raises

## LinAlgError :

If the eigenvalue computation does not converge.

## See Also:

```
eigvalsh
    eigenvalues of symmetric or Hermitian arrays.
eig
    eigenvalues and right eigenvectors for non-symmetric arrays.
eigvals
    eigenvalues of non-symmetric arrays.
```


## Notes

This is a simple interface to the LAPACK routines dsyevd and zheevd, which compute the eigenvalues and eigenvectors of real symmetric and complex Hermitian arrays, respectively.

The eigenvalues of real symmetric or complex Hermitian matrices are always real. [R37] The array $v$ of (column) eigenvectors is unitary and $a, w$, and $v$ satisfy the equations $\operatorname{dot}(a, \mathrm{v}[:, ~ i])=\mathrm{w}[\mathrm{i}] \quad * \mathrm{v}[:, \mathrm{i}]$.

## References

## [R37]

## Examples

```
>>> from numpy import linalg as LA
>>> a = np.array([[1, -2j], [2j, 5]])
>>> a
array([[ 1.+0.j, 0.-2.j],
    [ 0.+2.j, 5.+0.j]])
>>> w, v = LA.eigh(a)
>>> w; v
array([ 0.17157288, 5.82842712])
array([[-0.92387953+0.j , -0.38268343+0.j ],
    [ 0.00000000+0.38268343j, 0.000000000-0.92387953j]])
>>> np.dot(a, v[:, 0]) - w[0] * v[:, 0] # verify lst e-val/vec pair
array([2.77555756e-17 + 0.j, 0. + 1.38777878e-16j])
>>> np.dot(a, v[:, 1]) - w[1] * v[:, 1] # verify 2nd e-val/vec pair
array([ 0.+0.j, 0.+0.j])
```

```
>>> A = np.matrix(a) # what happens if input is a matrix object
>>> A
matrix([[ 1.+0.j, 0.-2.j],
    [ 0.+2.j, 5.+0.j]])
>>> w, v = LA.eigh(A)
>>> w; v
array([ 0.17157288, 5.82842712])
matrix([[-0.92387953+0.j , -0.38268343+0.j ],
    [ 0.00000000+0.38268343j, 0.00000000-0..92387953j]])
```

numpy.linalg.eigvals (a)

Compute the eigenvalues of a general matrix.
Main difference between eigvals and eig: the eigenvectors aren't returned.

## Parameters

a : array_like, shape (M, M)
A complex- or real-valued matrix whose eigenvalues will be computed.

## Returns

w : ndarray, shape (M,)
The eigenvalues, each repeated according to its multiplicity. They are not necessarily ordered, nor are they necessarily real for real matrices.

## Raises

## LinAlgError :

If the eigenvalue computation does not converge.

## See Also:

eig
eigenvalues and right eigenvectors of general arrays
eigvalsh
eigenvalues of symmetric or Hermitian arrays.
eigh
eigenvalues and eigenvectors of symmetric/Hermitian arrays.

## Notes

This is a simple interface to the LAPACK routines dgeev and zgeev that sets those routines' flags to return only the eigenvalues of general real and complex arrays, respectively.

## Examples

Illustration, using the fact that the eigenvalues of a diagonal matrix are its diagonal elements, that multiplying a matrix on the left by an orthogonal matrix, $Q$, and on the right by $Q . T$ (the transpose of $Q$ ), preserves the eigenvalues of the "middle" matrix. In other words, if $Q$ is orthogonal, then $Q \star A * Q . T$ has the same eigenvalues as A :

```
>>> from numpy import linalg as LA
>>> x = np.random.random()
>>> Q = np.array([[np.cos(x), -np.sin(x)], [np.sin(x), np.cos(x)]])
>>> LA.norm(Q[0, :]), LA.norm(Q[1, :]), np.dot(Q[0, :],Q[1, :])
(1.0, 1.0, 0.0)
```

Now multiply a diagonal matrix by Q on one side and by $\mathrm{Q} . \mathrm{T}$ on the other:

```
>>> D = np.diag((-1,1))
>>> LA.eigvals(D)
array([-1., 1.])
>>> A = np.dot(Q, D)
>>> A = np.dot(A, Q.T)
>>> LA.eigvals(A)
array([ 1., -1.])
numpy.linalg.eigvalsh(a,UPLO='L')
```

Compute the eigenvalues of a Hermitian or real symmetric matrix.
Main difference from eigh: the eigenvectors are not computed.

## Parameters

a : array_like, shape (M, M)
A complex- or real-valued matrix whose eigenvalues are to be computed.
UPLO : \{'L', 'U'\}, optional
Specifies whether the calculation is done with the lower triangular part of $a$ (' L ', default) or the upper triangular part ('U').

## Returns

$\mathbf{w}$ : ndarray, shape (M,)
The eigenvalues, not necessarily ordered, each repeated according to its multiplicity.

## Raises

## LinAlgError :

If the eigenvalue computation does not converge.

## See Also:

## eigh

eigenvalues and eigenvectors of symmetric/Hermitian arrays.
eigvals
eigenvalues of general real or complex arrays.
eig
eigenvalues and right eigenvectors of general real or complex arrays.

## Notes

This is a simple interface to the LAPACK routines dsyevd and zheevd that sets those routines' flags to return only the eigenvalues of real symmetric and complex Hermitian arrays, respectively.

## Examples

```
>>> from numpy import linalg as LA
>>> a = np.array([[1, -2j], [2j, 5]])
>>> LA.eigvalsh(a)
array([ 0.17157288+0.j, 5.82842712+0.j])
```


### 3.7.4 Norms and other numbers

| linalg. norm(x[, ord $])$ | Matrix or vector norm. |
| :--- | :--- |
| linalg. $\operatorname{cond}(\mathrm{x}[, \mathrm{p}])$ | Compute the condition number of a matrix. |
| linalg. det(a) | Compute the determinant of an array. |
| linalg.slogdet(a) | Compute the sign and (natural) logarithm of the determinant of an array. |
| trace(a[, offset, axis1, axis2, dtype, out $])$ | Return the sum along diagonals of the array. |

numpy.linalg.norm ( $x$, ord=None)
Matrix or vector norm.
This function is able to return one of seven different matrix norms, or one of an infinite number of vector norms (described below), depending on the value of the ord parameter.

## Parameters

$\mathbf{x}$ : array_like, shape $(\mathrm{M}$,$) or (\mathrm{M}, \mathrm{N})$
Input array.
ord : \{non-zero int, inf, -inf, 'fro' \}, optional
Order of the norm (see table under Notes). inf means numpy's inf object.

## Returns

$\mathbf{n}$ : float
Norm of the matrix or vector.

## Notes

For values of ord $<=0$, the result is, strictly speaking, not a mathematical 'norm', but it may still be useful for various numerical purposes.
The following norms can be calculated:

| ord | norm for matrices | norm for vectors |
| :---: | :---: | :---: |
| None | Frobenius norm | 2-norm |
| 'fro' | Frobenius norm | - |
| inf | $\max (\operatorname{sum}(\operatorname{abs}(\mathrm{x}), \mathrm{axis}=1))$ | $\max (\mathrm{abs}(\mathrm{x})$ ) |
| -inf | $\min (\operatorname{sum}(\operatorname{abs}(x)$, axis $=1))$ | $\min (\operatorname{abs}(\mathrm{x})$ ) |
| 0 | - | sum(x ! = 0) |
| 1 | $\max (\operatorname{sum}(\operatorname{abs}(\mathrm{x}), \mathrm{axis}=0))$ | as below |
| -1 | $\min (\operatorname{sum}(\operatorname{abs}(\mathrm{x}), \mathrm{axis}=0))$ | as below |
| 2 | 2-norm (largest sing. value) | as below |
| -2 | smallest singular value | as below |
| other | - | $\operatorname{sum}\left(\operatorname{abs}(\mathrm{x})^{* *}\right.$ ord) ${ }^{* *}$ (1./ord) |

The Frobenius norm is given by [R38]:

$$
\|A\|_{F}=\left[\sum_{i, j} a b s\left(a_{i, j}\right)^{2}\right]^{1 / 2}
$$

## References

[R38]

## Examples

```
>>> from numpy import linalg as LA
>>> a = np.arange(9) - 4
>>> a
array([-4, -3, -2, -1, 0, 1, 2, 3, 4])
```

```
>>> b = a.reshape((3, 3))
>>> b
array([[-4, -3, -2],
    [-1, 0, 1],
    [ 2, 3, 4]])
```

>>> LA.norm(a)
7.745966692414834
>>> LA.norm(b)
7.745966692414834
>>> LA.norm(b, 'fro')
7.745966692414834
>>> LA.norm(a, np.inf)
4
>>> LA.norm(b, np.inf)
9
>>> LA.norm(a, -np.inf)
0
>>> LA.norm(b, -np.inf)
2
>>> LA. norm (a, 1)
20
>>> LA.norm (b, 1)
7
>>> LA. norm(a, -1)
-4.6566128774142013e-010
>>> LA.norm(b, -1)
6
>>> LA. norm (a, 2)
7.745966692414834
>>> LA.norm (b, 2)
7.3484692283495345
>>> LA. norm(a, -2)
nan
>>> LA. norm(b, -2)
1.8570331885190563e-016
>>> LA. norm (a, 3)
5.8480354764257312
>>> LA. norm(a, -3)
nan
numpy.linalg.cond ( $x, p=$ None)
Compute the condition number of a matrix.
This function is capable of returning the condition number using one of seven different norms, depending on the value of $p$ (see Parameters below).

## Parameters

$\mathbf{x}$ : array_like, shape $(\mathrm{M}, \mathrm{N})$
The matrix whose condition number is sought.
$\mathbf{p}:\{$ None, 1, $-1,2,-2$, inf, -inf, 'fro' $\}$, optional
Order of the norm:

| p | norm for matrices |
| :--- | :--- |
| None | 2-norm, computed directly using the SVD |
| 'fro' | Frobenius norm |
| $\inf$ | $\max (\operatorname{sum}(\operatorname{abs}(\mathrm{x})$, axis=1)) |
| -inf | $\min (\operatorname{sum}(\operatorname{abs}(\mathrm{x})$, axis=1)) |
| 1 | $\max (\operatorname{sum}(\operatorname{abs}(\mathrm{x})$, axis=0)) |
| -1 | $\min (\operatorname{sum}(\operatorname{abs}(\mathrm{x})$, axis=0)) |
| 2 | 2-norm (largest sing. value) |
| -2 | smallest singular value |

inf means the numpy.inf object, and the Frobenius norm is the root-of-sum-of-squares norm.

## Returns

$\mathbf{c}:\{$ float, inf $\}$
The condition number of the matrix. May be infinite.

## See Also:

numpy.linalg.linalg.norm

## Notes

The condition number of $x$ is defined as the norm of $x$ times the norm of the inverse of $x$ [R36]; the norm can be the usual L2-norm (root-of-sum-of-squares) or one of a number of other matrix norms.

## References

[R36]

## Examples

```
>>> from numpy import linalg as LA
>>> a no.array([[1, 0, -1], [0, 1, 0], [1, 0, 1]])
>>> a
array([[ 1, 0, -1],
    [ 0, 1, 0],
    [ 1, 0, 1]])
>>> LA.cond(a)
1.4142135623730951
>>> LA.cond(a, 'fro')
3.1622776601683795
>>> LA.cond(a, np.inf)
2.0
>>> LA.cond(a, -np.inf)
1.0
>>> LA.cond(a, 1)
2.0
>>> LA.cond(a, -1)
1.0
>>> LA.cond(a, 2)
1.4142135623730951
>>> LA.cond(a, -2)
0.70710678118654746
>>> min(LA.svd(a, compute_uv=0)) *min(LA.svd(LA.inv(a), compute_uv=0))
0.70710678118654746
```

numpy.linalg. $\operatorname{det}(a)$

Compute the determinant of an array.

## Parameters

$\mathbf{a}$ : array_like, shape ( $\mathrm{M}, \mathrm{M}$ )
Input array.

## Returns

det : ndarray
Determinant of $a$.

## See Also:

slogdet
Another way to representing the determinant, more suitable for large matrices where underflow/overflow may occur.

## Notes

The determinant is computed via LU factorization using the LAPACK routine z/dgetrf.

## Examples

The determinant of a 2-D array $[[\mathrm{a}, \mathrm{b}],[\mathrm{c}, \mathrm{d}]]$ is $\mathrm{ad}-\mathrm{bc}$ :

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.linalg.det(a)
-2.0
```

numpy.linalg.slogdet (a)
Compute the sign and (natural) logarithm of the determinant of an array.
If an array has a very small or very large determinant, than a call to det may overflow or underflow. This routine is more robust against such issues, because it computes the logarithm of the determinant rather than the determinant itself.

## Parameters

a: array_like
Input array, has to be a square 2-D array.

## Returns

sign : float or complex
A number representing the sign of the determinant. For a real matrix, this is 1,0 , or -1 . For a complex matrix, this is a complex number with absolute value 1 (i.e., it is on the unit circle), or else 0 .

## logdet : float

The natural $\log$ of the absolute value of the determinant.
If the determinant is zero, then 'sign' will be 0 and 'logdet' will be :
-Inf. In all cases, the determinant is equal to "sign * np.exp(logdet)". :

## See Also:

det

## Notes

The determinant is computed via LU factorization using the LAPACK routine z/dgetrf. New in version 1.6.0..

## Examples

The determinant of a 2-D array [ [a, b], [c, d] ] is ad - bc:

```
>>> a = np.array([[1, 2], [3, 4]])
>>> (sign, logdet) = np.linalg.slogdet(a)
>>> (sign, logdet)
(-1, 0.69314718055994529)
>>> sign * np.exp(logdet)
-2.0
```

This routine succeeds where ordinary det does not:

```
>>> np.linalg.det(np.eye(500) * 0.1)
0.0
>>> np.linalg.slogdet(np.eye(500) * 0.1)
(1, -1151.2925464970228)
```

numpy.trace ( $a$, offset $=0$, axis $1=0$, axis $2=1$, dtype $=$ None, out $=$ None )
Return the sum along diagonals of the array.
If $a$ is 2-D, the sum along its diagonal with the given offset is returned, i.e., the sum of elements a[i,i+offset] for all i.

If $a$ has more than two dimensions, then the axes specified by axis 1 and axis 2 are used to determine the 2-D sub-arrays whose traces are returned. The shape of the resulting array is the same as that of $a$ with axisl and axis2 removed.

## Parameters

a : array_like
Input array, from which the diagonals are taken.
offset : int, optional
Offset of the diagonal from the main diagonal. Can be both positive and negative. Defaults to 0 .
axis1, axis2 : int, optional
Axes to be used as the first and second axis of the 2-D sub-arrays from which the diagonals should be taken. Defaults are the first two axes of $a$.
dtype : dtype, optional
Determines the data-type of the returned array and of the accumulator where the elements are summed. If dtype has the value None and $a$ is of integer type of precision less than the default integer precision, then the default integer precision is used. Otherwise, the precision is the same as that of $a$.
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

sum_along_diagonals : ndarray
If $a$ is 2-D, the sum along the diagonal is returned. If $a$ has larger dimensions, then an array of sums along diagonals is returned.

## See Also:

diag, diagonal, diagflat

## Examples

```
>>> np.trace(np.eye(3))
3.0
>>> a = np.arange(8).reshape((2,2,2))
>>> np.trace(a)
array([6, 8])
>>> a = np.arange(24).reshape((2,2,2,3))
>>> np.trace(a).shape
(2, 3)
```


### 3.7.5 Solving equations and inverting matrices

| linalg.solve( $\mathrm{a}, \mathrm{b})$ | Solve a linear matrix equation, or system of linear scalar equations. |
| :--- | :--- |
| linalg.tensorsolve(a, $\mathrm{b}[$, axes $])$ | Solve the tensor equation $\mathrm{x}=\mathrm{b}$ for x. |
| linalg.lstsq(a, $\mathrm{b}[$, rcond $])$ | Return the least-squares solution to a linear matrix equation. |
| linalg.inv(a) | Compute the (multiplicative) inverse of a matrix. |
| linalg.pinv(a[, rcond $])$ | Compute the (Moore-Penrose) pseudo-inverse of a matrix. |
| linalg.tensorinv(a[,ind]) | Compute the 'inverse' of an N-dimensional array. |

numpy.linalg.solve ( $a, b$ )
Solve a linear matrix equation, or system of linear scalar equations.
Computes the "exact" solution, $x$, of the well-determined, i.e., full rank, linear matrix equation $a x=b$.

## Parameters

a : array_like, shape (M, M)
Coefficient matrix.
b : array_like, shape (M,) or (M, N)
Ordinate or "dependent variable" values.

## Returns

$\mathbf{x}$ : ndarray, shape $(\mathrm{M}$, ) or $(\mathrm{M}, \mathrm{N})$ depending on b
Solution to the system $\mathrm{ax}=\mathrm{b}$

## Raises

LinAlgError :
If $a$ is singular or not square.

## Notes

solve is a wrapper for the LAPACK routines dgesv and zgesv, the former being used if $a$ is real-valued, the latter if it is complex-valued. The solution to the system of linear equations is computed using an LU decomposition [R40] with partial pivoting and row interchanges.
$a$ must be square and of full-rank, i.e., all rows (or, equivalently, columns) must be linearly independent; if either is not true, use $l s t s q$ for the least-squares best "solution" of the system/equation.

## References

[R40]

## Examples

Solve the system of equations $3 * x 0+x 1=9$ and $x 0+2 * x 1=8$ :

```
>>> a = np.array([[3,1], [1,2]])
>>> b = np.array([9,8])
>>> x = np.linalg.solve(a, b)
>>> x
array([ 2., 3.])
```

Check that the solution is correct:

```
>>> (np.dot(a, x) == b).all()
```

True
numpy.linalg.tensorsolve ( $a, b$, axes=None)

Solve the tensor equation $\mathrm{x}=\mathrm{b}$ for x .
It is assumed that all indices of $x$ are summed over in the product, together with the rightmost indices of $a$, as is done in, for example, tensordot ( $a, x$, $a x e s=l e n(b . s h a p e)$ ).

## Parameters

a : array_like
Coefficient tensor, of shape b. shape $+\mathrm{Q} . Q$, a tuple, equals the shape of that sub-tensor of $a$ consisting of the appropriate number of its rightmost indices, and must be such that
$\operatorname{prod}(Q)==\operatorname{prod}(\mathrm{b}$. shape) (in which sense $a$ is said to be 'square').
b : array_like
Right-hand tensor, which can be of any shape.
axes : tuple of ints, optional
Axes in $a$ to reorder to the right, before inversion. If None (default), no reordering is done.

## Returns

$\mathbf{x}$ : ndarray, shape Q

## Raises

## LinAlgError :

If $a$ is singular or not 'square' (in the above sense).

## See Also:

```
tensordot, tensorinv, einsum
```


## Examples

```
>>> a = np.eye (2* 3*4)
>>> a.shape = (2*3, 4, 2, 3, 4)
>>> b = np.random.randn ( 2* 3, 4)
>>> x = np.linalg.tensorsolve(a, b)
>>> x.shape
(2, 3, 4)
>>> np.allclose(np.tensordot(a, x, axes=3), b)
True
```

numpy.linalg.lstsq $(a, b, r$ cond $=-1)$

Return the least-squares solution to a linear matrix equation.

Solves the equation $a x=b$ by computing a vector $x$ that minimizes the Euclidean 2-norm \| $b-a x \|^{\wedge} 2$. The equation may be under-, well-, or over- determined (i.e., the number of linearly independent rows of $a$ can be less than, equal to, or greater than its number of linearly independent columns). If $a$ is square and of full rank, then $x$ (but for round-off error) is the "exact" solution of the equation.

## Parameters

$\mathbf{a}$ : array_like, shape $(\mathrm{M}, \mathrm{N})$
"Coefficient" matrix.
b : array_like, shape (M,) or (M, K)
Ordinate or "dependent variable" values. If $b$ is two-dimensional, the least-squares solution is calculated for each of the $K$ columns of $b$.
rcond : float, optional
Cut-off ratio for small singular values of $a$. Singular values are set to zero if they are smaller than rcond times the largest singular value of $a$.

## Returns

$\mathbf{x}$ : ndarray, shape $(\mathrm{N}$,$) or (\mathrm{N}, \mathrm{K})$
Least-squares solution. The shape of $x$ depends on the shape of $b$.
residues : ndarray, shape (), (1,), or (K,)
Sums of residues; squared Euclidean 2-norm for each column in b $-a * x$. If the rank of $a$ is $<\mathrm{N}$ or $>\mathrm{M}$, this is an empty array. If $b$ is 1 -dimensional, this is a (1,) shape array. Otherwise the shape is (K,).
rank: int
Rank of matrix $a$.
$\mathbf{s}:$ ndarray, shape $(\min (M, N)$,
Singular values of $a$.

## Raises

## LinAlgError :

If computation does not converge.

## Notes

If $b$ is a matrix, then all array results are returned as matrices.

## Examples

Fit a line, $y=m x+c$, through some noisy data-points:

```
>>> x = np.array([0, 1, 2, 3])
>>>y=np.array([-1, 0.2,0.9, 2.1])
```

By examining the coefficients, we see that the line should have a gradient of roughly 1 and cut the $y$-axis at, more or less, -1 .

We can rewrite the line equation as $y=A p$, where $\left.A=\left[\begin{array}{ll}\mathrm{x} & 1\end{array}\right]\right]$ and $\mathrm{p}=[[\mathrm{m}]$, [c]]. Now use lstsq to solve for $p$ :

```
>>> A = np.vstack([x, np.ones(len(x))]).T
>>> A
array([[ 0., 1.],
    [ 1., 1.],
```

```
    [ 2., 1.],
    [ 3., 1.]])
>>> m, c = np.linalg.lstsq(A, y)[0]
>>> print m, C
1.0-0.95
```

Plot the data along with the fitted line:

```
>>> import matplotlib.pyplot as plt
>>> plt.plot(x, y, 'o', label='Original data', markersize=10)
>>> plt.plot(x, m*x + c, 'r', label='Fitted line')
>>> plt.legend()
>>> plt.show()
```


numpy.linalg.inv (a)
Compute the (multiplicative) inverse of a matrix.
Given a square matrix $a$, return the matrix ainv satisfying $\operatorname{dot}(a, \operatorname{ainv})=\operatorname{dot}(\operatorname{ainv}, a)=$ eye (a.shape[0]).

## Parameters

a : array_like, shape (M, M)
Matrix to be inverted.

## Returns

ainv : ndarray or matrix, shape ( $\mathrm{M}, \mathrm{M}$ )
(Multiplicative) inverse of the matrix $a$.

## Raises

## LinAlgError :

If $a$ is singular or not square.

## Examples

```
>>> from numpy import linalg as LA
>>> a = np.array([[1., 2.], [3., 4.]])
```

```
>>> ainv = LA.inv(a)
>>> np.allclose(np.dot(a, ainv), np.eye(2))
True
>>> np.allclose(np.dot(ainv, a), np.eye(2))
True
```

If a is a matrix object, then the return value is a matrix as well:

```
>>> ainv = LA.inv(np.matrix(a))
>>> ainv
matrix([[-2., 1. ],
    [ 1.5, -0.5]])
```

numpy.linalg.pinv ( $a$, rcond=1.00000000000000001e-15)
Compute the (Moore-Penrose) pseudo-inverse of a matrix.
Calculate the generalized inverse of a matrix using its singular-value decomposition (SVD) and including all large singular values.

## Parameters

a : array_like, shape (M, N)
Matrix to be pseudo-inverted.
rcond : float
Cutoff for small singular values. Singular values smaller (in modulus) than rcond * largest_singular_value (again, in modulus) are set to zero.

## Returns

B : ndarray, shape ( $\mathrm{N}, \mathrm{M}$ )
The pseudo-inverse of $a$. If $a$ is a matrix instance, then so is $B$.

## Raises <br> LinAlgError :

If the SVD computation does not converge.

## Notes

The pseudo-inverse of a matrix A, denoted $A^{+}$, is defined as: "the matrix that 'solves' [the least-squares problem] $A x=b, "$ i.e., if $\bar{x}$ is said solution, then $A^{+}$is that matrix such that $\bar{x}=A^{+} b$.

It can be shown that if $Q_{1} \Sigma Q_{2}^{T}=A$ is the singular value decomposition of A , then $A^{+}=Q_{2} \Sigma^{+} Q_{1}^{T}$, where $Q_{1,2}$ are orthogonal matrices, $\Sigma$ is a diagonal matrix consisting of A's so-called singular values, (followed, typically, by zeros), and then $\Sigma^{+}$is simply the diagonal matrix consisting of the reciprocals of A's singular values (again, followed by zeros). [R39]

## References

[R39]

## Examples

The following example checks that $a * a+* a==a$ and $a+* a * a+==a+$ :

```
>>> a = np.random.randn(9, 6)
>>> B = np.linalg.pinv(a)
>>> np.allclose(a, np.dot(a, np.dot(B, a)))
True
>>> np.allclose(B, np.dot(B, np.dot(a, B)))
True
```

```
numpy.linalg.tensorinv ( \(a\), ind=2)
```

Compute the 'inverse' of an N -dimensional array.
The result is an inverse for $a$ relative to the tensordot operation tensordot (a, b, ind), i. e., up to floating-point accuracy, tensordot (tensorinv(a), a, ind) is the "identity" tensor for the tensordot operation.

## Parameters

a : array_like
Tensor to 'invert'. Its shape must be 'square', i. e., prod(a.shape [:ind]) == prod(a.shape[ind:]).
ind : int, optional
Number of first indices that are involved in the inverse sum. Must be a positive integer, default is 2 .

## Returns

b : ndarray
$a^{\text {'s }}$ tensordot inverse, shape a.shape [:ind] + a.shape [ind:].

## Raises

## LinAlgError :

If $a$ is singular or not 'square' (in the above sense).

## See Also:

tensordot, tensorsolve

## Examples

```
>>> a = np.eye(4*6)
>>> a.shape = (4, 6, 8, 3)
>>> ainv = np.linalg.tensorinv(a, ind=2)
>>> ainv.shape
    (8, 3, 4, 6)
>>> b = np.random.randn(4, 6)
>>> np.allclose(np.tensordot(ainv, b), np.linalg.tensorsolve(a, b))
True
>>> a = np.eye(4*6)
>>> a.shape = (24, 8, 3)
>>> ainv = np.linalg.tensorinv(a, ind=1)
>>> ainv.shape
    (8, 3, 24)
    >>> b = np.random.randn(24)
    >>> np.allclose(np.tensordot(ainv, b, 1), np.linalg.tensorsolve(a, b))
    True
```


### 3.7.6 Exceptions

## linalg.LinAlgError Generic Python-exception-derived object raised by linalg functions.

exception numpy.linalg.LinAlgError
Generic Python-exception-derived object raised by linalg functions.
General purpose exception class, derived from Python's exception.Exception class, programmatically raised in linalg functions when a Linear Algebra-related condition would prevent further correct execution of the function.

## Parameters

None :

## Examples

```
>>> from numpy import linalg as LA
>>> LA.inv(np.zeros((2,2)))
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
    File "...linalg.py", line 350,
        in inv return wrap(solve(a, identity(a.shape[0], dtype=a.dtype)))
    File "...linalg.py", line 249,
        in solve
        raise LinAlgError, 'Singular matrix'
numpy.linalg.linalg.LinAlgError: Singular matrix
```


### 3.8 Random sampling (numpy . random)

### 3.8.1 Simple random data

| rand(d0, d1, dn) | Random values in a given shape. |
| :--- | :--- |
| randn(d1) | Return a sample (or samples) from the "standard normal" distribution. |
| randint(low[, high, size]) | Return random integers from low (inclusive) to high (exclusive). |
| random_integers(low[, high, size]) | Return random integers between low and high, inclusive. |
| random_sample([size]) | Return random floats in the half-open interval [0.0, 1.0). |
| bytes(length) | Return random bytes. |

[^3]Random values in a given shape.
Create an array of the given shape and propagate it with random samples from a uniform distribution over [0, 1).

## Parameters

d0, d1, ..., dn : int
Shape of the output.

## Returns

out : ndarray, shape (d0, d1, ..., dn)
Random values.
See Also:
random

## Notes

This is a convenience function. If you want an interface that takes a shape-tuple as the first argument, refer to random.

## Examples

```
>>> np.random.rand(3,2)
array([[ 0.14022471, 0.96360618], #random
    [ 0.37601032, 0.25528411], #random
    [ 0.49313049, 0.94909878]]) #random
```

numpy. random. $\boldsymbol{r a n d n}([d l, \ldots, d n])$
Return a sample (or samples) from the "standard normal" distribution.
If positive, int_like or int-convertible arguments are provided, randn generates an array of shape ( d 1 , . . . , dn ), filled with random floats sampled from a univariate "normal" (Gaussian) distribution of mean 0 and variance 1 (if any of the $d_{i}$ are floats, they are first converted to integers by truncation). A single float randomly sampled from the distribution is returned if no argument is provided.

This is a convenience function. If you want an interface that takes a tuple as the first argument, use numpy.random.standard_normal instead.

## Parameters

d1, ..., dn : $n$ ints, optional
The dimensions of the returned array, should be all positive.

## Returns

$\mathbf{Z}$ : ndarray or float
A (d1, . . ., dn) -shaped array of floating-point samples from the standard normal distribution, or a single such float if no parameters were supplied.

## See Also:

random.standard_normal
Similar, but takes a tuple as its argument.

## Notes

For random samples from $N\left(\mu, \sigma^{2}\right)$, use:
sigma * np.random.randn(...) + mu

## Examples

```
>>> np.random.randn()
2.1923875335537315 #random
```

Two-by-four array of samples from $\mathrm{N}(3,6.25)$ :

```
>>> 2.5 * np.random.randn (2, 4) + 3
array([[-4.49401501, 4.00950034, -1.81814867, 7.29718677], #random
    [ 0.39924804, 4.68456316, 4.99394529, 4.84057254]]) #random
```

numpy. random. randint (low, high=None, size=None)
Return random integers from low (inclusive) to high (exclusive).
Return random integers from the "discrete uniform" distribution in the "half-open" interval [low, high). If high is None (the default), then results are from [0,low).

## Parameters

low : int
Lowest (signed) integer to be drawn from the distribution (unless high=None, in which case this parameter is the highest such integer).
high : int, optional
If provided, one above the largest (signed) integer to be drawn from the distribution (see above for behavior if high=None).
size : int or tuple of ints, optional
Output shape. Default is None, in which case a single int is returned.

## Returns

out : int or ndarray of ints size-shaped array of random integers from the appropriate distribution, or a single such random int if size not provided.

## See Also:

random.random_integers
similar to randint, only for the closed interval [low, high], and 1 is the lowest value if high is omitted. In particular, this other one is the one to use to generate uniformly distributed discrete non-integers.

## Examples

```
>>> np.random.randint(2, size=10)
array([1, 0, 0, 0, 1, 1, 0, 0, 1, 0])
>>> np.random.randint(1, size=10)
array([0, 0, 0, 0, 0, 0, 0, 0, 0, 0])
```

Generate a $2 \times 4$ array of ints between 0 and 4, inclusive:

```
>>> np.random.randint(5, size=(2, 4))
array([[4, 0, 2, 1],
    [3, 2, 2, 0]])
```

numpy.random.random_integers (low, high=None, size=None)
Return random integers between low and high, inclusive.
Return random integers from the "discrete uniform" distribution in the closed interval [low, high]. If high is None (the default), then results are from [1,low].

## Parameters

low : int
Lowest (signed) integer to be drawn from the distribution (unless high=None, in which case this parameter is the highest such integer).
high : int, optional
If provided, the largest (signed) integer to be drawn from the distribution (see above for behavior if high=None).
size : int or tuple of ints, optional
Output shape. Default is None, in which case a single int is returned.

## Returns

out : int or ndarray of ints
size-shaped array of random integers from the appropriate distribution, or a single such random int if size not provided.

## See Also:

random.randint
Similar to random_integers, only for the half-open interval [low, high), and 0 is the lowest value if high is omitted.

## Notes

To sample from N evenly spaced floating-point numbers between $a$ and $b$, use:

```
a + (b - a) * (np.random.random_integers(N) - 1) / (N - 1.)
```


## Examples

```
>>> np.random.random_integers(5)
4
>>> type(np.random.random_integers(5))
<type 'int'>
>>> np.random.random_integers(5, size=(3.,2.))
array([[5, 4],
    [3, 3],
    [4, 5]])
```

Choose five random numbers from the set of five evenly-spaced numbers between 0 and 2.5, inclusive (i.e., from the set $0,5 / 8,10 / 8,15 / 8,20 / 8)$ :

```
>>> 2.5 * (np.random.random_integers(5, size=(5,)) - 1) / 4.
array([ 0.625, 1.25,0.625, 0.625, 2.5 ] )
```

Roll two six sided dice 1000 times and sum the results:

```
>>> d1 = np.random.random_integers(1, 6, 1000)
>>> d2 = np.random.random_integers(1, 6, 1000)
>>> dsums = d1 + d2
```

Display results as a histogram:

```
>>> import matplotlib.pyplot as plt
>>> count, bins, ignored = plt.hist(dsums, 11, normed=True)
>>> plt.show()
```


numpy.random.random_sample (size=None)
Return random floats in the half-open interval [0.0, 1.0).
Results are from the "continuous uniform" distribution over the stated interval. To sample Unif $[a, b), b>a$ multiply the output of random_sample by $(b-a)$ and add $a$ :

```
(b - a) * random_sample() + a
```


## Parameters

size : int or tuple of ints, optional
Defines the shape of the returned array of random floats. If None (the default), returns a single float.

## Returns

out : float or ndarray of floats
Array of random floats of shape size (unless size=None, in which case a single float is returned).

## Examples

```
>>> np.random.random_sample()
0.47108547995356098
>>> type(np.random.random_sample())
<type 'float'>
>>> np.random.random_sample((5,))
array([ 0.30220482, 0.86820401, 0.1654503 , 0.11659149, 0.54323428])
```

Three-by-two array of random numbers from $[-5,0)$ :

```
>>> 5 * np.random.random_sample((3, 2)) - 5
array([[-3.99149989, -0.52338984],
    [-2.99091858, -0.79479508],
    [-1.23204345, -1.75224494]])
```

numpy.random.bytes (length)
Return random bytes.

## Parameters

length : int
Number of random bytes.

## Returns

out : str
String of length length.

## Examples

```
>>> np.random.bytes(10)
' eh\x85\x022SZ\xbf\xa4' #random
```


### 3.8.2 Permutations

shuffle(x) Modify a sequence in-place by shuffling its contents.
permutation(x) Randomly permute a sequence, or return a permuted range.
numpy.random.shuffle ( $x$ )
Modify a sequence in-place by shuffling its contents.

## Parameters

$\mathbf{x}$ : array_like
The array or list to be shuffled.

## Returns

None :

## Examples

```
>>> arr = np.arange(10)
>>> np.random.shuffle(arr)
>>> arr
[1 [4 5
```

This function only shuffles the array along the first index of a multi-dimensional array:

```
>>> arr = np.arange(9).reshape((3, 3))
>>> np.random.shuffle(arr)
>>> arr
array([[3, 4, 5],
    [6, 7, 8],
    [0, 1, 2]])
```

numpy.random.permutation ( $x$ )

Randomly permute a sequence, or return a permuted range.
If $x$ is a multi-dimensional array, it is only shuffled along its first index.

## Parameters

$\mathbf{x}$ : int or array_like
If $x$ is an integer, randomly permute $n p$. arange ( $x$ ). If $x$ is an array, make a copy and shuffle the elements randomly.

## Returns

out : ndarray
Permuted sequence or array range.

## Examples

```
>>> np.random.permutation(10)
array([1, 7, 4, 3, 0, 9, 2, 5, 8, 6])
>>> np.random.permutation([1, 4, 9, 12, 15])
array([15, 1, 9, 4, 12])
>>> arr = np.arange(9).reshape((3, 3))
>>> np.random.permutation(arr)
array([[6, 7, 8],
    [0, 1, 2],
    [3, 4, 5]])
```


### 3.8.3 Distributions

| beta(a, | size]) | The | Beta | distribution | over binomial | $[0,1] .$ distribution. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| binomial(n, p[, | size]) | Draw | samples | from a |  |  |
| chisquare(df[, | size]) | Draw | samples | from a | chi-square | distribution. |
| mtrand.dirichlet(alpha[, | size]) | Draw | samples | from the | Dirichlet | distribution. |
| exponential([scale, | size]) | Exponential |  | distribution. |  |  |
| f(dfnum, dfden[, | size]) | Draw | samples | from a | F | distribution. |
| gamma(shape[, scale, | size]) | Draw | samples | from a | Gamma | distribution. |
| geometric(p[, | size]) | Draw | samples | from the | geometric | distribution. |
| gumbel([loc, scale, | size]) | Gumbel |  | distribution. |  |  |
|  |  |  |  |  |  | Continued on |

Table 3.1 - continued from previous page

| ]) | Draw samples from a Hypergeometric distribution. |
| :---: | :---: |
| laplace([loc, scale, size]) | Draw samples from the Laplace or double exponential distribution |
| logistic([loc, scale, size]) | Draw samples from a Logistic distribution. |
| lognormal ([mean, sigma, size]) | Return samples drawn from a log-normal distribution. |
| logseries(p[, size]) | Draw samples from a Logarithmic Series distributio |
| multinomial(n, pvals[, size]) | Draw samples from a multinomial distribution. |
| multivariate_normal(mean) | Draw random samples from a multivariate normal distribution. |
| negative_binomial(n, p[, siz | Draw samples from a negative_binomial distributio |
| noncentral_chisquare(df, nonc[, size]) | Draw samples from a noncentral chi-square distributio |
| noncentral_f(dfnum, dfden, nonc[, size]) | Draw samples from the noncentral F distributio |
| normal ([loc, scale, size]) | Draw random samples from a normal (Gaussian) distributir |
| pareto(a[, size]) | Draw samples from a Pareto II or Lomax distribution with specified shap |
| poisson([lam, size]) | Draw samples from a Poisson distribution |
| power(a[, size]) | Draws samples in [0, 1] from a power distribution with positive exp |
| rayleigh([scale, size]) | Draw samples from a Rayleigh distribution. |
| standard_cauchy([size]) | Standard Cauchy distribution with mode |
| standard_exponential([size]) | Draw samples from the standard exponential distribution |
| standard_gamma(shape[, size]) | Draw samples from a Standard Gamma distributio |
| standard_normal([size]) | Returns samples from a Standard Normal distribution (mean=0, stde |
| standard_t(df[, size]) | Standard Student's t distribution with df degrees of freedom. |
| left, mode, right[, size]) | Draw samples from the triangular distribution |
| uniform([low, high, size]) | Draw samples from a uniform distribution. |
| vonmises(mu, kappa[, size]) | Draw samples from a von Mises distribu |
| wald(mean, scale[, size]) | Draw samples from a Wald, or Inverse Gaussian, distribut |
| weibull(a[, size]) | Weibull |
| zipf(a[, size]) | Draw samples from a ${ }^{\text {a }}$ (ipf distribution. |

numpy.random.beta ( $a, b$, size $=$ None )
The Beta distribution over [0, 1].
The Beta distribution is a special case of the Dirichlet distribution, and is related to the Gamma distribution. It has the probability distribution function

$$
f(x ; a, b)=\frac{1}{B(\alpha, \beta)} x^{\alpha-1}(1-x)^{\beta-1}
$$

where the normalisation, B , is the beta function,

$$
B(\alpha, \beta)=\int_{0}^{1} t^{\alpha-1}(1-t)^{\beta-1} d t
$$

It is often seen in Bayesian inference and order statistics.

## Parameters

a : float
Alpha, non-negative.
b : float
Beta, non-negative.
size : tuple of ints, optional
The number of samples to draw. The ouput is packed according to the size given.

## Returns

out : ndarray
Array of the given shape, containing values drawn from a Beta distribution.
numpy.random.binomial ( $n, p$, size $=$ None )
Draw samples from a binomial distribution.
Samples are drawn from a Binomial distribution with specified parameters, $n$ trials and $p$ probability of success where n an integer $>0$ and p is in the interval [0,1]. (n may be input as a float, but it is truncated to an integer in use)

## Parameters

$\mathbf{n}$ : float (but truncated to an integer)
parameter, $>0$.
p: float
parameter, $>=0$ and $<=1$.
size : \{tuple, int $\}$
Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn.

## Returns

samples : \{ndarray, scalar\}
where the values are all integers in $[0, \mathrm{n}]$.
See Also:
scipy.stats.distributions.binom
probability density function, distribution or cumulative density function, etc.

## Notes

The probability density for the Binomial distribution is

$$
P(N)=\binom{n}{N} p^{N}(1-p)^{n-N}
$$

where $n$ is the number of trials, $p$ is the probability of success, and $N$ is the number of successes.
When estimating the standard error of a proportion in a population by using a random sample, the normal distribution works well unless the product $\mathrm{p} * \mathrm{n}<=5$, where $\mathrm{p}=$ population proportion estimate, and $\mathrm{n}=$ number of samples, in which case the binomial distribution is used instead. For example, a sample of 15 people shows 4 who are left handed, and 11 who are right handed. Then $\mathrm{p}=4 / 15=27 \% .0 .27 * 15=4$, so the binomial distribution should be used in this case.

## References

[R58], [R59], [R60], [R61], [R62]

## Examples

Draw samples from the distribution:

```
>>> n, p = 10, .5 # number of trials, probability of each trial
>>> s = np.random.binomial(n, p, 1000)
# result of flipping a coin 10 times, tested 1000 times.
```

A real world example. A company drills 9 wild-cat oil exploration wells, each with an estimated probability of success of 0.1 . All nine wells fail. What is the probability of that happening?
Let's do 20,000 trials of the model, and count the number that generate zero positive results.

```
>>> sum(np.random.binomial(9,0.1,20000)==0)/20000.
answer = 0.38885, or 38%.
```

numpy.random. chisquare ( $d f$, size $=$ None )
Draw samples from a chi-square distribution.
When $d f$ independent random variables, each with standard normal distributions (mean 0 , variance 1 ), are squared and summed, the resulting distribution is chi-square (see Notes). This distribution is often used in hypothesis testing.

## Parameters

df: int
Number of degrees of freedom.
size : tuple of ints, int, optional
Size of the returned array. By default, a scalar is returned.

## Returns

output : ndarray
Samples drawn from the distribution, packed in a size-shaped array.

## Raises

ValueError :
When $d f<=0$ or when an inappropriate size (e.g. size=-1) is given.

## Notes

The variable obtained by summing the squares of $d f$ independent, standard normally distributed random variables:

$$
Q=\sum_{i=0}^{\mathrm{df}} X_{i}^{2}
$$

is chi-square distributed, denoted

$$
Q \sim \chi_{k}^{2}
$$

The probability density function of the chi-squared distribution is

$$
p(x)=\frac{(1 / 2)^{k / 2}}{\Gamma(k / 2)} x^{k / 2-1} e^{-x / 2}
$$

where $\Gamma$ is the gamma function,

$$
\Gamma(x)=\int_{0}^{-\infty} t^{x-1} e^{-t} d t
$$

## References

NIST/SEMATECH e-Handbook of Statistical Methods

## Examples

```
>>> np.random.chisquare (2,4)
array([ 1.89920014, 9.00867716, 3.13710533, 5.62318272])
```

numpy.random.mtrand.dirichlet (alpha, size=None)
Draw samples from the Dirichlet distribution.
Draw size samples of dimension k from a Dirichlet distribution. A Dirichlet-distributed random variable can be seen as a multivariate generalization of a Beta distribution. Dirichlet pdf is the conjugate prior of a multinomial in Bayesian inference.

## Parameters

alpha : array
Parameter of the distribution ( $k$ dimension for sample of dimension $k$ ).
size : array
Number of samples to draw.

## Returns

samples: ndarray,
The drawn samples, of shape (alpha.ndim, size).

## Notes

$$
X \approx \prod_{i=1}^{k} x_{i}^{\alpha_{i}-1}
$$

Uses the following property for computation: for each dimension, draw a random sample y_i from a standard gamma generator of shape alpha_i, then $X=\frac{1}{\sum_{i=1}^{k} y_{i}}\left(y_{1}, \ldots, y_{n}\right)$ is Dirichlet distributed.

## References

[R193], [R194]

## Examples

Taking an example cited in Wikipedia, this distribution can be used if one wanted to cut strings (each of initial length 1.0) into K pieces with different lengths, where each piece had, on average, a designated average length, but allowing some variation in the relative sizes of the pieces.

```
>>> s = np.random.dirichlet((10, 5, 3), 20).transpose()
>>> plt.barh(range(20), s[0])
>>> plt.barh(range(20), s[1], left=s[0], color=' g')
>>> plt.barh(range(20), s[2], left=s[0]+s[1], color='r')
>>> plt.title("Lengths of Strings")
numpy.random.exponential (scale=1.0, size=None)
Exponential distribution.
```

Its probability density function is

$$
f\left(x ; \frac{1}{\beta}\right)=\frac{1}{\beta} \exp \left(-\frac{x}{\beta}\right),
$$

for $\mathrm{x}>0$ and 0 elsewhere. $\beta$ is the scale parameter, which is the inverse of the rate parameter $\lambda=1 / \beta$. The rate parameter is an alternative, widely used parameterization of the exponential distribution [R65].

The exponential distribution is a continuous analogue of the geometric distribution. It describes many common situations, such as the size of raindrops measured over many rainstorms [R63], or the time between page requests to Wikipedia [R64].

## Parameters

scale : float
The scale parameter, $\beta=1 / \lambda$.
size : tuple of ints
Number of samples to draw. The output is shaped according to size.

## References

[R63], [R64], [R65]
numpy. random. $\mathbf{f}$ (dfnum, dfden, size=None)
Draw samples from a F distribution.
Samples are drawn from an F distribution with specified parameters, dfnum (degrees of freedom in numerator) and $d f d e n$ (degrees of freedom in denominator), where both parameters should be greater than zero.

The random variate of the F distribution (also known as the Fisher distribution) is a continuous probability distribution that arises in ANOVA tests, and is the ratio of two chi-square variates.

## Parameters

dfnum : float
Degrees of freedom in numerator. Should be greater than zero.
dfden : float
Degrees of freedom in denominator. Should be greater than zero.
size : \{tuple, int \}, optional
Output shape. If the given shape is, e.g., ( $\mathrm{m}, \mathrm{n}, \mathrm{k}$ ), then $\mathrm{m} * \mathrm{n} * \mathrm{k}$ samples are drawn. By default only one sample is returned.

## Returns

samples: \{ndarray, scalar\}
Samples from the Fisher distribution.

## See Also:

scipy.stats.distributions.f
probability density function, distribution or cumulative density function, etc.

## Notes

The F statistic is used to compare in-group variances to between-group variances. Calculating the distribution depends on the sampling, and so it is a function of the respective degrees of freedom in the problem. The variable dfnum is the number of samples minus one, the between-groups degrees of freedom, while dfden is the within-groups degrees of freedom, the sum of the number of samples in each group minus the number of groups.

## References

[R66], [R67]

## Examples

An example from Glantz[1], pp 47-40. Two groups, children of diabetics ( 25 people) and children from people without diabetes ( 25 controls). Fasting blood glucose was measured, case group had a mean value of 86.1, controls had a mean value of 82.2. Standard deviations were 2.09 and 2.49 respectively. Are these data consistent with the null hypothesis that the parents diabetic status does not affect their children's blood glucose levels? Calculating the F statistic from the data gives a value of 36.01 .
Draw samples from the distribution:

```
>>> dfnum = 1. # between group degrees of freedom
>>> dfden = 48. # within groups degrees of freedom
>>> s = np.random.f(dfnum, dfden, 1000)
```

The lower bound for the top $1 \%$ of the samples is :

```
>>> sort(s) [-10]
7.61988120985
```

So there is about a $1 \%$ chance that the F statistic will exceed 7.62 , the measured value is 36 , so the null hypothesis is rejected at the $1 \%$ level.

```
numpy.random.gamma (shape, scale=1.0, size=None)
```

Draw samples from a Gamma distribution.
Samples are drawn from a Gamma distribution with specified parameters, shape (sometimes designated " k ") and scale (sometimes designated "theta"), where both parameters are $>0$.

## Parameters

shape : scalar >0

The shape of the gamma distribution.
scale : scalar $>0$, optional
The scale of the gamma distribution. Default is equal to 1 .
size : shape_tuple, optional
Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn.

## Returns

out : ndarray, float
Returns one sample unless size parameter is specified.

## See Also:

scipy.stats.distributions.gamma
probability density function, distribution or cumulative density function, etc.

## Notes

The probability density for the Gamma distribution is

$$
p(x)=x^{k-1} \frac{e^{-x / \theta}}{\theta^{k} \Gamma(k)},
$$

where $k$ is the shape and $\theta$ the scale, and $\Gamma$ is the Gamma function.
The Gamma distribution is often used to model the times to failure of electronic components, and arises naturally in processes for which the waiting times between Poisson distributed events are relevant.

## References

[R68], [R69]

## Examples

Draw samples from the distribution:

```
>>> shape, scale = 2., 2. # mean and dispersion
>>>}s=np.random.gamma(shape, scale, 1000
```

Display the histogram of the samples, along with the probability density function:

```
>>> import matplotlib.pyplot as plt
>>> import scipy.special as sps
>>> count, bins, ignored = plt.hist(s, 50, normed=True)
>>> y = bins**(shape-1)*(np.exp(-bins/scale) /
... (sps.gamma(shape)*scale**shape))
>>> plt.plot(bins, y, linewidth=2, color='r')
>>> plt.show()
```


numpy.random.geometric ( $p$, size=None)
Draw samples from the geometric distribution.
Bernoulli trials are experiments with one of two outcomes: success or failure (an example of such an experiment is flipping a coin). The geometric distribution models the number of trials that must be run in order to achieve success. It is therefore supported on the positive integers, $k=1$, 2 , ....

The probability mass function of the geometric distribution is

$$
f(k)=(1-p)^{k-1} p
$$

where $p$ is the probability of success of an individual trial.

## Parameters

p : float
The probability of success of an individual trial.
size : tuple of ints
Number of values to draw from the distribution. The output is shaped according to size.

## Returns

out : ndarray
Samples from the geometric distribution, shaped according to size.

## Examples

Draw ten thousand values from the geometric distribution, with the probability of an individual success equal to 0.35 :

```
>>> z = np.random.geometric(p=0.35, size=10000)
```

How many trials succeeded after a single run?

```
>>> (z == 1).sum() / 10000.
0.348899999999999999 #random
```

numpy. random.gumbel (loc=0.0, scale $=1.0$, size $=$ None $)$

Gumbel distribution.
Draw samples from a Gumbel distribution with specified location and scale. For more information on the Gumbel distribution, see Notes and References below.

## Parameters

loc: float
The location of the mode of the distribution.
scale : float
The scale parameter of the distribution.
size : tuple of ints
Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn.

## Returns

out : ndarray
The samples

## See Also:

scipy.stats.gumbel_l, scipy.stats.gumbel_r
scipy.stats.genextreme
probability density function, distribution, or cumulative density function, etc. for each of the above
weibull

## Notes

The Gumbel (or Smallest Extreme Value (SEV) or the Smallest Extreme Value Type I) distribution is one of a class of Generalized Extreme Value (GEV) distributions used in modeling extreme value problems. The Gumbel is a special case of the Extreme Value Type I distribution for maximums from distributions with "exponentiallike" tails.

The probability density for the Gumbel distribution is

$$
p(x)=\frac{e^{-(x-\mu) / \beta}}{\beta} e^{-e^{-(x-\mu) / \beta}},
$$

where $\mu$ is the mode, a location parameter, and $\beta$ is the scale parameter.
The Gumbel (named for German mathematician Emil Julius Gumbel) was used very early in the hydrology literature, for modeling the occurrence of flood events. It is also used for modeling maximum wind speed and rainfall rates. It is a "fat-tailed" distribution - the probability of an event in the tail of the distribution is larger than if one used a Gaussian, hence the surprisingly frequent occurrence of 100-year floods. Floods were initially modeled as a Gaussian process, which underestimated the frequency of extreme events.

It is one of a class of extreme value distributions, the Generalized Extreme Value (GEV) distributions, which also includes the Weibull and Frechet.
The function has a mean of $\mu+0.57721 \beta$ and a variance of $\frac{\pi^{2}}{6} \beta^{2}$.

## References

Gumbel, E. J., Statistics of Extremes, New York: Columbia University Press, 1958.
Reiss, R.-D. and Thomas, M., Statistical Analysis of Extreme Values from Insurance, Finance, Hydrology and Other Fields, Basel: Birkhauser Verlag, 2001.

## Examples

Draw samples from the distribution:

```
>>> mu, beta = 0, 0.1 # location and scale
>>> s=np.random.gumbel(mu, beta, 1000)
```

Display the histogram of the samples, along with the probability density function:

```
>>> import matplotlib.pyplot as plt
>>> count, bins, ignored = plt.hist(s, 30, normed=True)
>>> plt.plot(bins, (1/beta) *np.exp(-(bins - mu)/beta)
... * np.exp( -np.exp( - (bins - mu) /beta) ),
... linewidth=2, color='r')
>>> plt.show()
```



Show how an extreme value distribution can arise from a Gaussian process and compare to a Gaussian:

```
>>> means = []
>>> maxima = []
>>> for i in range(0,1000) :
... a = np.random.normal(mu, beta, 1000)
... means.append (a.mean())
... maxima.append(a.max())
>>> count, bins, ignored = plt.hist(maxima, 30, normed=True)
>>> beta = np.std(maxima)*np.pi/np.sqrt(6)
>>> mu = np.mean(maxima) - 0.57721*beta
>>> plt.plot(bins, (1/beta)*np.exp(-(bins - mu)/beta)
... * np.exp(-np.exp(-(bins - mu)/beta)),
... linewidth=2, color='r')
>>> plt.plot(bins, 1/(beta * np.sqrt(2 * np.pi))
... * np.exp(-(bins - mu)**2 / (2 * beta**2)),
... linewidth=2, color=' g')
>>> plt.show()
```


numpy.random. hypergeometric (ngood, nbad, nsample, size=None)
Draw samples from a Hypergeometric distribution.
Samples are drawn from a Hypergeometric distribution with specified parameters, ngood (ways to make a good selection), nbad (ways to make a bad selection), and nsample = number of items sampled, which is less than or equal to the sum ngood + nbad.

## Parameters

ngood : float (but truncated to an integer)
parameter, $>0$.
nbad : float
parameter, $>=0$.
nsample : float
parameter, $>0$ and $<=$ ngood+nbad
size : \{tuple, int \}

Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn.

## Returns

samples: \{ndarray, scalar\}
where the values are all integers in $[0, n]$.

## See Also:

## scipy.stats.distributions.hypergeom

probability density function, distribution or cumulative density function, etc.

## Notes

The probability density for the Hypergeometric distribution is

$$
P(x)=\frac{\binom{m}{n}\binom{N-m}{n-x}}{\binom{N}{n}}
$$

where $0 \leq x \leq m$ and $n+m-N \leq x \leq n$
for $\mathrm{P}(\mathrm{x})$ the probability of x successes, $\mathrm{n}=$ ngood, $\mathrm{m}=\mathrm{nbad}$, and $\mathrm{N}=$ number of samples.
Consider an urn with black and white marbles in it, ngood of them black and nbad are white. If you draw nsample balls without replacement, then the Hypergeometric distribution describes the distribution of black balls in the drawn sample.

Note that this distribution is very similar to the Binomial distribution, except that in this case, samples are drawn without replacement, whereas in the Binomial case samples are drawn with replacement (or the sample space is infinite). As the sample space becomes large, this distribution approaches the Binomial.

## References

[R70], [R71], [R72]

## Examples

Draw samples from the distribution:

```
>>> ngood, nbad, nsamp = 100, 2, 10
# number of good, number of bad, and number of samples
>>> s = np.random.hypergeometric(ngood, nbad, nsamp, 1000)
>>> hist(s)
# note that it is very unlikely to grab both bad items
```

Suppose you have an urn with 15 white and 15 black marbles. If you pull 15 marbles at random, how likely is it that 12 or more of them are one color?

```
>>> s = np.random.hypergeometric(15, 15, 15, 100000)
```

>>> $\operatorname{sum}(s>=12) / 100000 .+\operatorname{sum}(s<=3) / 100000$.
\# answer $=0.003 \ldots$ pretty unlikely!
numpy.random.laplace (loc=0.0, scale $=1.0$, size $=$ None $)$
Draw samples from the Laplace or double exponential distribution with specified location (or mean) and scale (decay).

The Laplace distribution is similar to the Gaussian/normal distribution, but is sharper at the peak and has fatter tails. It represents the difference between two independent, identically distributed exponential random variables.

## Parameters

loc : float
The position, $\mu$, of the distribution peak.
scale : float
$\lambda$, the exponential decay.

## Notes

It has the probability density function

$$
f(x ; \mu, \lambda)=\frac{1}{2 \lambda} \exp \left(-\frac{|x-\mu|}{\lambda}\right)
$$

The first law of Laplace, from 1774, states that the frequency of an error can be expressed as an exponential function of the absolute magnitude of the error, which leads to the Laplace distribution. For many problems in Economics and Health sciences, this distribution seems to model the data better than the standard Gaussian distribution

## References

[R73], [R74], [R75], [R76]

## Examples

Draw samples from the distribution

```
>>> loc, scale = 0., 1.
>>> s = np.random.laplace(loc, scale, 1000)
```

Display the histogram of the samples, along with the probability density function:

```
>>> import matplotlib.pyplot as plt
>>> count, bins, ignored = plt.hist(s, 30, normed=True)
>>> x = np.arange(-8., 8., .01)
>>> pdf = np.exp(-abs(x-loc/scale))/(2.*scale)
>>> plt.plot(x, pdf)
```

Plot Gaussian for comparison:

```
>>> g = (1/(scale * np.sqrt(2 * np.pi)) *
... np.exp( - (x - loc)**2 / (2 * scale**2) ))
>>> plt.plot(x,g)
```


numpy.random.logistic (loc=0.0, scale $=1.0$, size $=$ None $)$
Draw samples from a Logistic distribution.
Samples are drawn from a Logistic distribution with specified parameters, loc (location or mean, also median), and scale ( $>0$ ).

## Parameters

loc : float
scale : float $>0$.
size : \{tuple, int \}
Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn.

## Returns

samples: \{ndarray, scalar\}
where the values are all integers in $[0, n]$.

## See Also:

## scipy.stats.distributions.logistic

probability density function, distribution or cumulative density function, etc.

## Notes

The probability density for the Logistic distribution is

$$
P(x)=P(x)=\frac{e^{-(x-\mu) / s}}{s\left(1+e^{-(x-\mu) / s}\right)^{2}},
$$

where $\mu=$ location and $s=$ scale.
The Logistic distribution is used in Extreme Value problems where it can act as a mixture of Gumbel distributions, in Epidemiology, and by the World Chess Federation (FIDE) where it is used in the Elo ranking system, assuming the performance of each player is a logistically distributed random variable.

## References

[R77], [R78], [R79]

## Examples

Draw samples from the distribution:

```
>>> loc, scale = 10, 1
>>> s = np.random.logistic(loc, scale, 10000)
>>> count, bins, ignored = plt.hist(s, bins=50)
```

\# plot against distribution

```
>>> def logist(x, loc, scale):
... return exp((loc-x)/scale)/(scale*(1+exp((loc-x)/scale))**2)
>>> plt.plot(bins, logist(bins, loc, scale)*count.max()/\
... logist(bins, loc, scale).max())
>>> plt.show()
```

numpy.random.lognormal ( mean $=0.0$, sigma $=1.0$, size $=$ None )
Return samples drawn from a log-normal distribution.
Draw samples from a log-normal distribution with specified mean, standard deviation, and shape. Note that the mean and standard deviation are not the values for the distribution itself, but of the underlying normal distribution it is derived from.

## Parameters

## mean : float

Mean value of the underlying normal distribution

$$
\text { sigma : float, }>0 \text {. }
$$

Standard deviation of the underlying normal distribution
size : tuple of ints
Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn.

## See Also:

## scipy.stats.lognorm

probability density function, distribution, cumulative density function, etc.

## Notes

A variable $x$ has a $\log$-normal distribution if $\log (x)$ is normally distributed.
The probability density function for the log-normal distribution is

$$
p(x)=\frac{1}{\sigma x \sqrt{2 \pi}} e^{\left(-\frac{(\ln (x)-\mu)^{2}}{2 \sigma^{2}}\right)}
$$

where $\mu$ is the mean and $\sigma$ is the standard deviation of the normally distributed logarithm of the variable.
A log-normal distribution results if a random variable is the product of a large number of independent, identically-distributed variables in the same way that a normal distribution results if the variable is the sum of a large number of independent, identically-distributed variables (see the last example). It is one of the so-called "fat-tailed" distributions.

The log-normal distribution is commonly used to model the lifespan of units with fatigue-stress failure modes. Since this includes most mechanical systems, the log-normal distribution has widespread application.

It is also commonly used to model oil field sizes, species abundance, and latent periods of infectious diseases.

## References

[R80], [R81], [R82]

## Examples

Draw samples from the distribution:

```
>>> mu, sigma = 3., 1. # mean and standard deviation
>>> s = np.random.lognormal(mu, sigma, 1000)
```

Display the histogram of the samples, along with the probability density function:

```
>>> import matplotlib.pyplot as plt
>>> count, bins, ignored = plt.hist(s, 100, normed=True, align='mid')
>>> x = np.linspace(min(bins), max(bins), 10000)
>>> pdf = (np.exp(-(np.log(x) - mu)**2 / (2 * sigma**2))
... / (x * sigma * np.sqrt(2 * np.pi)))
>>> plt.plot(x, pdf, linewidth=2, color='r')
>>> plt.axis('tight')
>>> plt.show()
```



Demonstrate that taking the products of random samples from a uniform distribution can be fit well by a lognormal probability density function.

```
>>> # Generate a thousand samples: each is the product of 100 random
>>> # values, drawn from a normal distribution.
>>> b = []
>>> for i in range(1000):
... a = 10. + np.random.random(100)
... b.append(np.product (a))
```

```
>>> b = np.array(b) / np.min(b) # scale values to be positive
>>> count, bins, ignored = plt.hist(b, 100, normed=True, align='center')
>>> sigma = np.std(np.log(b))
>>> mu = np.mean(np.log(b))
>>> x = np.linspace(min(bins), max(bins), 10000)
>>> pdf = (np.exp(-(np.log(x) - mu)**2 / (2 * sigma**2))
... / (x * sigma * np.sqrt(2 * np.pi)))
>>> plt.plot(x, pdf, color='r', linewidth=2)
>>> plt.show()
```


numpy.random.logseries ( $p$, size $=$ None)
Draw samples from a Logarithmic Series distribution.
Samples are drawn from a Log Series distribution with specified parameter, p (probability, $0<\mathrm{p}<1$ ).

## Parameters

loc: float
scale : float $>0$.
size : \{tuple, int $\}$
Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn.

## Returns

samples: \{ndarray, scalar \}
where the values are all integers in $[0, \mathrm{n}]$.

## See Also:

scipy.stats.distributions.logser
probability density function, distribution or cumulative density function, etc.

## Notes

The probability density for the Log Series distribution is

$$
P(k)=\frac{-p^{k}}{k \ln (1-p)},
$$

where $\mathrm{p}=$ probability.
The Log Series distribution is frequently used to represent species richness and occurrence, first proposed by Fisher, Corbet, and Williams in 1943 [2]. It may also be used to model the numbers of occupants seen in cars [3].

## References

[R83], [R84], [R85], [R86]

## Examples

Draw samples from the distribution:

```
>>> a = . 6
>>> s = np.random.logseries(a, 10000)
>>> count, bins, ignored = plt.hist(s)
```

\# plot against distribution

```
>>> def logseries(k, p):
... return -p**k/(k*log(1-p))
>>> plt.plot(bins, logseries(bins, a)*count.max()/
            logseries(bins, a).max(), 'r')
>>> plt.show()
```

numpy.random.multinomial ( $n, p v a l s$, size $=$ None $)$
Draw samples from a multinomial distribution.
The multinomial distribution is a multivariate generalisation of the binomial distribution. Take an experiment with one of p possible outcomes. An example of such an experiment is throwing a dice, where the outcome can be 1 through 6 . Each sample drawn from the distribution represents $n$ such experiments. Its values, X_i = [ X_0, X_1, ..., X_p], represent the number of times the outcome was i.

## Parameters

n : int
Number of experiments.
pvals : sequence of floats, length p
Probabilities of each of the $p$ different outcomes. These should sum to 1 (however, the last element is always assumed to account for the remaining probability, as long as sum(pvals[:-1]) <= 1).
size : tuple of ints
Given a size of $(M, N, K)$, then $M * N * K$ samples are drawn, and the output shape becomes ( $M, N, K, p$ ), since each sample has shape ( $p$, ).

## Examples

Throw a dice 20 times:

```
>>> np.random.multinomial(20, [1/6.]*6, size=1)
array([[4, 1, 7, 5, 2, 1]])
```

It landed 4 times on 1 , once on 2 , etc.
Now, throw the dice 20 times, and 20 times again:

```
>>> np.random.multinomial(20, [1/6.]*6, size=2)
array([[3, 4, 3, 3, 4, 3],
    [2, 4, 3, 4, 0, 7]])
```

For the first run, we threw 3 times 1 , 4 times 2 , etc. For the second, we threw 2 times 1,4 times 2 , etc.
A loaded dice is more likely to land on number 6:

```
>>> np.random.multinomial(100, [1/7.]*5)
array([13, 16, 13, 16, 42])
```

numpy.random.multivariate_normal (mean, cov[, size])
Draw random samples from a multivariate normal distribution.
The multivariate normal, multinormal or Gaussian distribution is a generalization of the one-dimensional normal distribution to higher dimensions. Such a distribution is specified by its mean and covariance matrix. These parameters are analogous to the mean (average or "center") and variance (standard deviation, or "width," squared) of the one-dimensional normal distribution.

## Parameters

mean : 1-D array_like, of length N
Mean of the N -dimensional distribution.
cov : 2-D array_like, of shape ( $\mathrm{N}, \mathrm{N}$ )
Covariance matrix of the distribution. Must be symmetric and positive semi-definite for "physically meaningful" results.
size : tuple of ints, optional
Given a shape of, for example, $(m, n, k), m * n * k$ samples are generated, and packed in an $m$-by- $n$-by- $k$ arrangement. Because each sample is $N$-dimensional, the output shape is $(m, n, k, N)$. If no shape is specified, a single ( $N-D$ ) sample is returned.

## Returns

out : ndarray
The drawn samples, of shape size, if that was provided. If not, the shape is ( N, ).
In other words, each entry out [i,j, .., : ] is an N -dimensional value drawn from the distribution.

## Notes

The mean is a coordinate in N -dimensional space, which represents the location where samples are most likely to be generated. This is analogous to the peak of the bell curve for the one-dimensional or univariate normal distribution.

Covariance indicates the level to which two variables vary together. From the multivariate normal distribution, we draw N -dimensional samples, $X=\left[x_{1}, x_{2}, \ldots x_{N}\right]$. The covariance matrix element $C_{i j}$ is the covariance of $x_{i}$ and $x_{j}$. The element $C_{i i}$ is the variance of $x_{i}$ (i.e. its "spread").
Instead of specifying the full covariance matrix, popular approximations include:
-Spherical covariance ( $\operatorname{cov}$ is a multiple of the identity matrix)
-Diagonal covariance ( $\operatorname{cov}$ has non-negative elements, and only on the diagonal)
This geometrical property can be seen in two dimensions by plotting generated data-points:

```
>>> mean = [0,0]
>>> cov = [[1,0],[0,100]] # diagonal covariance, points lie on x or y-axis
>>> import matplotlib.pyplot as plt
>>> x,y = np.random.multivariate_normal(mean,cov,5000).T
>>> plt.plot(x,y,'x'); plt.axis('equal'); plt.show()
```

Note that the covariance matrix must be non-negative definite.

## References

Papoulis, A., Probability, Random Variables, and Stochastic Processes, 3rd ed., New York: McGraw-Hill, 1991.
Duda, R. O., Hart, P. E., and Stork, D. G., Pattern Classification, 2nd ed., New York: Wiley, 2001.

## Examples

```
>>> mean = (1,2)
>>> cov = [[1,0],[1,0]]
>>> x = np.random.multivariate_normal(mean,cov, (3,3))
>>> x.shape
(3, 3, 2)
```

The following is probably true, given that 0.6 is roughly twice the standard deviation:

```
>>> print list( (x[0,0,:] - mean) < 0.6 )
[True, True]
```

numpy.random.negative_binomial ( $n, p$, size $=$ None $)$
Draw samples from a negative_binomial distribution.
Samples are drawn from a negative_Binomial distribution with specified parameters, $n$ trials and $p$ probability of success where $n$ is an integer $>0$ and $p$ is in the interval $[0,1]$.

## Parameters

$\mathbf{n}$ : int
Parameter, $>0$.
$\mathbf{p}$ : float
Parameter, $>=0$ and $<=1$.
size : int or tuple of ints
Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn.

## Returns

samples : int or ndarray of ints
Drawn samples.

## Notes

The probability density for the Negative Binomial distribution is

$$
P(N ; n, p)=\binom{N+n-1}{n-1} p^{n}(1-p)^{N}
$$

where $n-1$ is the number of successes, $p$ is the probability of success, and $N+n-1$ is the number of trials.
The negative binomial distribution gives the probability of $\mathrm{n}-1$ successes and N failures in $\mathrm{N}+\mathrm{n}-1$ trials, and success on the $(\mathrm{N}+\mathrm{n})$ th trial.

If one throws a die repeatedly until the third time a " 1 " appears, then the probability distribution of the number of non-" 1 "s that appear before the third " 1 " is a negative binomial distribution.

## References

[R195], [R196]

## Examples

Draw samples from the distribution:
A real world example. A company drills wild-cat oil exploration wells, each with an estimated probability of success of 0.1 . What is the probability of having one success for each successive well, that is what is the probability of a single success after drilling 5 wells, after 6 wells, etc.?

```
>>> s = np.random.negative_binomial(1, 0.1, 100000)
>>> for i in range(1, 11):
... probability = sum(s<i) / 100000.
... print i, "wells drilled, probability of one success =", probability
```

numpy.random.noncentral_chisquare ( $d f$, nonc, size=None)
Draw samples from a noncentral chi-square distribution.
The noncentral $\chi^{2}$ distribution is a generalisation of the $\chi^{2}$ distribution.

## Parameters

df : int
Degrees of freedom, should be $>=1$.
nonc : float
Non-centrality, should be $>0$.
size : int or tuple of ints
Shape of the output.

## Notes

The probability density function for the noncentral Chi-square distribution is

$$
P(x ; d f, n o n c)=\sum_{i=0}^{\infty} \frac{e^{-n o n c / 2}(n o n c / 2)^{i}}{i!} P_{Y_{d f+2 i}}(x),
$$

where $Y_{q}$ is the Chi-square with q degrees of freedom.
In Delhi (2007), it is noted that the noncentral chi-square is useful in bombing and coverage problems, the probability of killing the point target given by the noncentral chi-squared distribution.

## References

[R197], [R198]

## Examples

Draw values from the distribution and plot the histogram

```
>>> import matplotlib.pyplot as plt
>>> values = plt.hist(np.random.noncentral_chisquare(3, 20, 100000),
... bins=200, normed=True)
>>> plt.show()
```



Draw values from a noncentral chisquare with very small noncentrality, and compare to a chisquare.

```
>>> plt.figure()
>>> values = plt.hist(np.random.noncentral_chisquare(3, .0000001, 100000),
... bins=np.arange(0., 25, .1), normed=True)
>>> values2 = plt.hist(np.random.chisquare(3, 100000),
... bins=np.arange(0., 25, .1), normed=True)
>>> plt.plot(values[1][0:-1], values[0]-values2[0], 'ob')
>>> plt.show()
```



Demonstrate how large values of non-centrality lead to a more symmetric distribution.

```
>>> plt.figure()
>>> values = plt.hist(np.random.noncentral_chisquare(3, 20, 100000),
... bins=200, normed=True)
>>> plt.show()
```


numpy.random.noncentral_f (dfnum, dfden, nonc, size=None)
Draw samples from the noncentral F distribution.
Samples are drawn from an F distribution with specified parameters, dfnum (degrees of freedom in numerator) and dfden (degrees of freedom in denominator), where both parameters $>1$. nonc is the non-centrality parameter.

## Parameters

dfnum : int
Parameter, should be $>1$.
dfden : int
Parameter, should be $>1$.
nonc : float
Parameter, should be $>=0$.
size : int or tuple of ints
Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn.

## Returns

samples : scalar or ndarray
Drawn samples.

## Notes

When calculating the power of an experiment (power = probability of rejecting the null hypothesis when a specific alternative is true) the non-central F statistic becomes important. When the null hypothesis is true, the F statistic follows a central F distribution. When the null hypothesis is not true, then it follows a non-central F statistic.

## References

Weisstein, Eric W. "Noncentral F-Distribution." From MathWorld-A Wolfram Web Resource. http://mathworld.wolfram.com/NoncentralF-Distribution.html
Wikipedia, "Noncentral F distribution", http://en.wikipedia.org/wiki/Noncentral_F-distribution

## Examples

In a study, testing for a specific alternative to the null hypothesis requires use of the Noncentral F distribution. We need to calculate the area in the tail of the distribution that exceeds the value of the F distribution for the null hypothesis. We'll plot the two probability distributions for comparison.

```
>>> dfnum = 3 # between group deg of freedom
>>> dfden = 20 # within groups degrees of freedom
>>> nonc = 3.0
>>> nc_vals = np.random.noncentral_f(dfnum, dfden, nonc, 1000000)
>>> NF = np.histogram(nc_vals, bins=50, normed=True)
>>> c_vals = np.random.f(dfnum, dfden, 1000000)
>>> F = np.histogram(c_vals, bins=50, normed=True)
>>> plt.plot(F[1][1:], F[0])
>>> plt.plot(NF[1][1:], NF[0])
>>> plt.show()
numpy.random.normal (loc=0.0, scale=1.0, size=None)
```

Draw random samples from a normal (Gaussian) distribution.
The probability density function of the normal distribution, first derived by De Moivre and 200 years later by both Gauss and Laplace independently [R200], is often called the bell curve because of its characteristic shape (see the example below).

The normal distributions occurs often in nature. For example, it describes the commonly occurring distribution of samples influenced by a large number of tiny, random disturbances, each with its own unique distribution [R200].

## Parameters

loc : float
Mean ("centre") of the distribution.
scale : float
Standard deviation (spread or "width") of the distribution.
size : tuple of ints
Output shape. If the given shape is, e.g., ( $m, n, k$ ), then $m * n * k$ samples are drawn.

## See Also:

## scipy.stats.distributions.norm

probability density function, distribution or cumulative density function, etc.

## Notes

The probability density for the Gaussian distribution is

$$
p(x)=\frac{1}{\sqrt{2 \pi \sigma^{2}}} e^{-\frac{(x-\mu)^{2}}{2 \sigma^{2}}}
$$

where $\mu$ is the mean and $\sigma$ the standard deviation. The square of the standard deviation, $\sigma^{2}$, is called the variance.

The function has its peak at the mean, and its "spread" increases with the standard deviation (the function reaches 0.607 times its maximum at $x+\sigma$ and $x-\sigma[\mathrm{R} 200]$ ). This implies that numpy. random. normal is more likely to return samples lying close to the mean, rather than those far away.

## References

[R199], [R200]

## Examples

Draw samples from the distribution:

```
>>> mu, sigma = 0, 0.1 # mean and standard deviation
>>> s = np.random.normal(mu, sigma, 1000)
```

Verify the mean and the variance:

```
>>> abs(mu - np.mean(s)) < 0.01
True
>>> abs(sigma - np.std(s, ddof=1)) < 0.01
True
```

Display the histogram of the samples, along with the probability density function:

```
>>> import matplotlib.pyplot as plt
>>> count, bins, ignored = plt.hist(s, 30, normed=True)
>>> plt.plot(bins, l/(sigma * np.sqrt(2 * np.pi)) *
... np.exp( - (bins - mu)**2 / (2 * sigma**2) ),
... linewidth=2, color='r')
>>> plt.show()
```


numpy.random.pareto ( $a$, size $=$ None )
Draw samples from a Pareto II or Lomax distribution with specified shape.
The Lomax or Pareto II distribution is a shifted Pareto distribution. The classical Pareto distribution can be obtained from the Lomax distribution by adding the location parameter m , see below. The smallest value of
the Lomax distribution is zero while for the classical Pareto distribution it is m , where the standard Pareto distribution has location $\mathrm{m}=1$. Lomax can also be considered as a simplified version of the Generalized Pareto distribution (available in SciPy), with the scale set to one and the location set to zero.

The Pareto distribution must be greater than zero, and is unbounded above. It is also known as the " $80-20$ rule". In this distribution, 80 percent of the weights are in the lowest 20 percent of the range, while the other 20 percent fill the remaining 80 percent of the range.

## Parameters

$$
\text { shape : float, > } 0 \text {. }
$$

Shape of the distribution.
size : tuple of ints
Output shape. If the given shape is, e.g., ( $m, n, k$ ), then $m * n * k$ samples are drawn.

## See Also:

scipy.stats.distributions.lomax.pdf
probability density function, distribution or cumulative density function, etc.

## scipy.stats.distributions.genpareto.pdf

probability density function, distribution or cumulative density function, etc.

## Notes

The probability density for the Pareto distribution is

$$
p(x)=\frac{a m^{a}}{x^{a+1}}
$$

where $a$ is the shape and $m$ the location
The Pareto distribution, named after the Italian economist Vilfredo Pareto, is a power law probability distribution useful in many real world problems. Outside the field of economics it is generally referred to as the Bradford distribution. Pareto developed the distribution to describe the distribution of wealth in an economy. It has also found use in insurance, web page access statistics, oil field sizes, and many other problems, including the download frequency for projects in Sourceforge [1]. It is one of the so-called "fat-tailed" distributions.

## References

[R201], [R202], [R203], [R204]

## Examples

Draw samples from the distribution:

```
>>> a, m=3., 1. # shape and mode
>>>}s=np.random.pareto(a, 1000) + 
```

Display the histogram of the samples, along with the probability density function:

```
>>> import matplotlib.pyplot as plt
>>> count, bins, ignored = plt.hist(s, 100, normed=True, align='center')
>>> fit = a*m**a/bins**(a+1)
>>> plt.plot(bins, max(count)*fit/max(fit),linewidth=2, color='r')
>>> plt.show()
```


numpy.random.poisson (lam=1.0, size=None)
Draw samples from a Poisson distribution.
The Poisson distribution is the limit of the Binomial distribution for large N .

## Parameters

lam : float
Expectation of interval, should be $>=0$.
size : int or tuple of ints, optional
Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn.

## Notes

The Poisson distribution

$$
f(k ; \lambda)=\frac{\lambda^{k} e^{-\lambda}}{k!}
$$

For events with an expected separation $\lambda$ the Poisson distribution $f(k ; \lambda)$ describes the probability of $k$ events occurring within the observed interval $\lambda$.

Because the output is limited to the range of the C long type, a ValueError is raised when lam is within 10 sigma of the maximum representable value.

## References

[R205], [R206]

## Examples

Draw samples from the distribution:

```
>>> import numpy as np
>>> s = np.random.poisson(5, 10000)
```

Display histogram of the sample:

```
>>> import matplotlib.pyplot as plt
>>> count, bins, ignored = plt.hist(s, 14, normed=True)
>>> plt.show()
```


numpy.random. power ( $a$, size=None )
Draws samples in [0, 1] from a power distribution with positive exponent a-1.
Also known as the power function distribution.

## Parameters

$\mathbf{a}$ : float
parameter, $>0$
size : tuple of ints
Output shape. If the given shape is, e.g., ( $m, n, k$ ), then $m * n * k$ samples are drawn.

## Returns

samples: \{ndarray, scalar \}
The returned samples lie in $[0,1]$.

## Raises

ValueError :
If $\mathrm{a}<1$.

## Notes

The probability density function is

$$
P(x ; a)=a x^{a-1}, 0 \leq x \leq 1, a>0 .
$$

The power function distribution is just the inverse of the Pareto distribution. It may also be seen as a special case of the Beta distribution.

It is used, for example, in modeling the over-reporting of insurance claims.

## References

[R207], [R208]

## Examples

Draw samples from the distribution:

```
>>> a = 5. # shape
>>> samples = 1000
>>> s = np.random.power(a, samples)
```

Display the histogram of the samples, along with the probability density function:

```
>>> import matplotlib.pyplot as plt
```

$\ggg$ count, bins, ignored = plt.hist(s, bins=30)
$\ggg x=n p . l i n s p a c e(0,1,100)$
$\ggg y=a * x * *(a-1$.
>>> normed_y = samples*np.diff(bins) [0]*y
>>> plt.plot(x, normed_y)
>>> plt.show()


Compare the power function distribution to the inverse of the Pareto.

```
>>> from scipy import stats
>>> rvs = np.random.power(5, 1000000)
>>> rvsp = np.random.pareto(5, 1000000)
>>> xx = np.linspace(0,1,100)
>>> powpdf = stats.powerlaw.pdf(xx,5)
>>> plt.figure()
>>> plt.hist(rvs, bins=50, normed=True)
>>> plt.plot(xx,powpdf,'r-')
>>> plt.title('np.random.power(5)')
>>> plt.figure()
>>> plt.hist(1./(1.+rvsp), bins=50, normed=True)
>>> plt.plot(xx,powpdf,'r-')
>>> plt.title('inverse of 1 + np.random.pareto(5)')
```

```
>>> plt.figure()
>>> plt.hist(1./(1.+rvsp), bins=50, normed=True)
>>> plt.plot(xx,powpdf,'r-')
>>> plt.title('inverse of stats.pareto(5)')
```




numpy.random.rayleigh (scale $=1.0$, size $=$ None $)$
Draw samples from a Rayleigh distribution.
The $\chi$ and Weibull distributions are generalizations of the Rayleigh.

## Parameters

 scale : scalarScale, also equals the mode. Should be $>=0$. size : int or tuple of ints, optional

Shape of the output. Default is None, in which case a single value is returned.

## Notes

The probability density function for the Rayleigh distribution is

$$
P(x ; \text { scale })=\frac{x}{s c a l e^{2}} e^{\frac{-x^{2}}{2 \cdot s c a l e^{2}}}
$$

The Rayleigh distribution arises if the wind speed and wind direction are both gaussian variables, then the vector wind velocity forms a Rayleigh distribution. The Rayleigh distribution is used to model the expected output from wind turbines.

## References

## ..[1] Brighton Webs Ltd., Rayleigh Distribution,

http://www.brighton-webs.co.uk/distributions/rayleigh.asp
..[2] Wikipedia, "Rayleigh distribution"
http://en.wikipedia.org/wiki/Rayleigh_distribution

## Examples

Draw values from the distribution and plot the histogram

```
>>> values = hist(np.random.rayleigh(3, 100000), bins=200, normed=True)
```

Wave heights tend to follow a Rayleigh distribution. If the mean wave height is 1 meter, what fraction of waves are likely to be larger than 3 meters?

```
>>> meanvalue = 1
>>> modevalue = np.sqrt(2 / np.pi) * meanvalue
>>> s = np.random.rayleigh(modevalue, 1000000)
```

The percentage of waves larger than 3 meters is:

```
>>> 100.*sum(s>3)/1000000.
0.0873000000000000003
```

numpy.random.standard_cauchy (size=None)

Standard Cauchy distribution with mode $=0$.
Also known as the Lorentz distribution.

## Parameters

size : int or tuple of ints
Shape of the output.

## Returns

samples : ndarray or scalar
The drawn samples.

## Notes

The probability density function for the full Cauchy distribution is

$$
P\left(x ; x_{0}, \gamma\right)=\frac{1}{\pi \gamma\left[1+\left(\frac{x-x_{0}}{\gamma}\right)^{2}\right]}
$$

and the Standard Cauchy distribution just sets $x_{0}=0$ and $\gamma=1$
The Cauchy distribution arises in the solution to the driven harmonic oscillator problem, and also describes spectral line broadening. It also describes the distribution of values at which a line tilted at a random angle will cut the x axis.

When studying hypothesis tests that assume normality, seeing how the tests perform on data from a Cauchy distribution is a good indicator of their sensitivity to a heavy-tailed distribution, since the Cauchy looks very much like a Gaussian distribution, but with heavier tails.

## References

..[1] NIST/SEMATECH e-Handbook of Statistical Methods, "Cauchy
Distribution", http://www.itl.nist.gov/div898/handbook/eda/section3/eda3663.htm
..[2] Weisstein, Eric W. "Cauchy Distribution." From MathWorld-A
Wolfram Web Resource. http://mathworld.wolfram.com/CauchyDistribution.html
..[3] Wikipedia, "Cauchy distribution"
http://en.wikipedia.org/wiki/Cauchy_distribution

## Examples

Draw samples and plot the distribution:

```
>>> s = np.random.standard_cauchy(1000000)
>>> s = s[(s>-25) & (s<25)] # truncate distribution so it plots well
>>> plt.hist(s, bins=100)
>>> plt.show()
```

numpy.random.standard_exponential (size=None)

Draw samples from the standard exponential distribution.
standard_exponential is identical to the exponential distribution with a scale parameter of 1 .

## Parameters

size : int or tuple of ints
Shape of the output.

## Returns

out : float or ndarray
Drawn samples.

## Examples

Output a $3 \times 8000$ array:
>>> n = np.random.standard_exponential((3, 8000))
numpy.random.standard_gamma (shape, size=None)
Draw samples from a Standard Gamma distribution.
Samples are drawn from a Gamma distribution with specified parameters, shape (sometimes designated "k") and scale $=1$.

## Parameters

shape : float
Parameter, should be $>0$.
size : int or tuple of ints
Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn.

## Returns

samples : ndarray or scalar
The drawn samples.
See Also:
scipy.stats.distributions.gamma
probability density function, distribution or cumulative density function, etc.

## Notes

The probability density for the Gamma distribution is

$$
p(x)=x^{k-1} \frac{e^{-x / \theta}}{\theta^{k} \Gamma(k)}
$$

where $k$ is the shape and $\theta$ the scale, and $\Gamma$ is the Gamma function.
The Gamma distribution is often used to model the times to failure of electronic components, and arises naturally in processes for which the waiting times between Poisson distributed events are relevant.

## References

[R210], [R211]

## Examples

Draw samples from the distribution:

```
>>> shape, scale = 2., 1. # mean and width
>>> s = np.random.standard_gamma(shape, 1000000)
```

Display the histogram of the samples, along with the probability density function:

```
>>> import matplotlib.pyplot as plt
>>> import scipy.special as sps
>>> count, bins, ignored = plt.hist(s, 50, normed=True)
>>> y = bins**(shape-1) * ((np.exp(-bins/scale))/ \
... (sps.gamma(shape) * scale**shape))
>>> plt.plot(bins, y, linewidth=2, color='r')
>>> plt.show()
```


numpy.random.standard_normal (size=None)
Returns samples from a Standard Normal distribution (mean=0, stdev=1).

## Parameters

size : int or tuple of ints, optional
Output shape. Default is None, in which case a single value is returned.

## Returns

out : float or ndarray
Drawn samples.

## Examples

```
>>> s = np.random.standard_normal(8000)
>>> s
array([ 0.6888893 , 0.78096262, -0.89086505, ..., 0.49876311, #random
    -0.38672696, -0.4685006 ]) #random
>>> s.shape
```

```
(8000,)
>>> s = np.random.standard_normal(size=(3, 4, 2))
>>> s.shape
(3, 4, 2)
```

numpy.random.standard_t (df, size=None)

Standard Student's $t$ distribution with df degrees of freedom.
A special case of the hyperbolic distribution. As $d f$ gets large, the result resembles that of the standard normal distribution (standard_normal).

## Parameters

df : int
Degrees of freedom, should be $>0$.
size : int or tuple of ints, optional
Output shape. Default is None, in which case a single value is returned.

## Returns

samples : ndarray or scalar
Drawn samples.

## Notes

The probability density function for the $t$ distribution is

$$
P(x, d f)=\frac{\Gamma\left(\frac{d f+1}{2}\right)}{\sqrt{\pi d f} \Gamma\left(\frac{d f}{2}\right)}\left(1+\frac{x^{2}}{d f}\right)^{-(d f+1) / 2}
$$

The $t$ test is based on an assumption that the data come from a Normal distribution. The $t$ test provides a way to test whether the sample mean (that is the mean calculated from the data) is a good estimate of the true mean.
The derivation of the t-distribution was forst published in 1908 by William Gisset while working for the Guinness Brewery in Dublin. Due to proprietary issues, he had to publish under a pseudonym, and so he used the name Student.

## References

[R212], [R213]

## Examples

From Dalgaard page 83 [R212], suppose the daily energy intake for 11 women in Kj is:

```
>>> intake = np.array([5260., 5470, 5640, 6180, 6390, 6515, 6805, 7515, \
... 7515, 8230, 8770])
```

Does their energy intake deviate systematically from the recommended value of 7725 kJ ?
We have 10 degrees of freedom, so is the sample mean within $95 \%$ of the recommended value?

```
>>> s = np.random.standard_t(10, size=100000)
>>> np.mean(intake)
6753.636363636364
>>> intake.std(ddof=1)
1142.1232221373727
```

Calculate the $t$ statistic, setting the ddof parameter to the unbiased value so the divisor in the standard deviation will be degrees of freedom, $\mathrm{N}-1$.

```
>>> t = (np.mean(intake)-7725)/(intake.std(ddof=1)/np.sqrt(len(intake)))
>>> import matplotlib.pyplot as plt
>>> h = plt.hist(s, bins=100, normed=True)
```

For a one-sided t -test, how far out in the distribution does the t statistic appear?

```
>>> >>> np.sum(s<t) / float(len(s))
0.0090699999999999999 #random
```

So the p-value is about 0.009 , which says the null hypothesis has a probability of about $99 \%$ of being true.

```
numpy.random.triangular(left, mode, right, size=None)
```

Draw samples from the triangular distribution.
The triangular distribution is a continuous probability distribution with lower limit left, peak at mode, and upper limit right. Unlike the other distributions, these parameters directly define the shape of the pdf.

## Parameters

left : scalar
Lower limit.
mode : scalar
The value where the peak of the distribution occurs. The value should fulfill the condition left <= mode <= right.
right : scalar
Upper limit, should be larger than left.
size : int or tuple of ints, optional
Output shape. Default is None, in which case a single value is returned.

## Returns

samples : ndarray or scalar
The returned samples all lie in the interval [left, right].

## Notes

The probability density function for the Triangular distribution is

$$
P(x ; l, m, r)= \begin{cases}\frac{2(x-l)}{(r-l)(m-l)} & \text { for } l \leq x \leq m \\ \frac{2(m-x)}{(r-l)(r-m)} & \text { for } m \leq x \leq r \\ 0 & \text { otherwise }\end{cases}
$$

The triangular distribution is often used in ill-defined problems where the underlying distribution is not known, but some knowledge of the limits and mode exists. Often it is used in simulations.

## References

..[1] Wikipedia, "Triangular distribution"
http://en.wikipedia.org/wiki/Triangular_distribution

## Examples

Draw values from the distribution and plot the histogram:

```
>>> import matplotlib.pyplot as plt
>>> h = plt.hist(np.random.triangular(-3, 0, 8, 100000), bins=200,
... normed=True)
>>> plt.show()
```


numpy. random.uniform (low=0.0, high=1.0, size=1)
Draw samples from a uniform distribution.
Samples are uniformly distributed over the half-open interval [low, high) (includes low, but excludes high). In other words, any value within the given interval is equally likely to be drawn by uniform.

## Parameters

low : float, optional
Lower boundary of the output interval. All values generated will be greater than or equal to low. The default value is 0 .
high : float
Upper boundary of the output interval. All values generated will be less than high. The default value is 1.0 .
size : int or tuple of ints, optional
Shape of output. If the given size is, for example, ( $\mathrm{m}, \mathrm{n}, \mathrm{k}$ ), $\mathrm{m} * \mathrm{n} * \mathrm{k}$ samples are generated. If no shape is specified, a single sample is returned.

## Returns

out : ndarray
Drawn samples, with shape size.

## See Also:

randint
Discrete uniform distribution, yielding integers.

## random_integers

Discrete uniform distribution over the closed interval [low, high].
random_sample
Floats uniformly distributed over [0, 1).
random
Alias for random_sample.
rand
Convenience function that accepts dimensions as input, e.g., rand $(2,2)$ would generate a 2-by-2 array of floats, uniformly distributed over [0, 1).

## Notes

The probability density function of the uniform distribution is

$$
p(x)=\frac{1}{b-a}
$$

anywhere within the interval [a, b), and zero elsewhere.

## Examples

Draw samples from the distribution:

```
>>> s = np.random.uniform(-1,0,1000)
```

All values are within the given interval:

```
>>> np.all(s >= -1)
True
>>> np.all(s < 0)
True
```

Display the histogram of the samples, along with the probability density function:

```
>>> import matplotlib.pyplot as plt
>>> count, bins, ignored = plt.hist(s, 15, normed=True)
>>> plt.plot(bins, np.ones_like(bins), linewidth=2, color='r')
>>> plt.show()
```


numpy.random.vonmises ( $m u$, kappa, size=None)
Draw samples from a von Mises distribution.
Samples are drawn from a von Mises distribution with specified mode (mu) and dispersion (kappa), on the interval [-pi, pi].

The von Mises distribution (also known as the circular normal distribution) is a continuous probability distribution on the unit circle. It may be thought of as the circular analogue of the normal distribution.

## Parameters

mu : float
Mode ("center") of the distribution.
kappa : float
Dispersion of the distribution, has to be $>=0$.
size : int or tuple of int
Output shape. If the given shape is, e.g., ( $m, n, k$ ), then $m * n * k$ samples are drawn.

## Returns

samples : scalar or ndarray
The returned samples, which are in the interval [-pi, pi].

## See Also:

scipy.stats.distributions.vonmises
probability density function, distribution, or cumulative density function, etc.

## Notes

The probability density for the von Mises distribution is

$$
p(x)=\frac{e^{\kappa \cos (x-\mu)}}{2 \pi I_{0}(\kappa)}
$$

where $\mu$ is the mode and $\kappa$ the dispersion, and $I_{0}(\kappa)$ is the modified Bessel function of order 0 .
The von Mises is named for Richard Edler von Mises, who was born in Austria-Hungary, in what is now the Ukraine. He fled to the United States in 1939 and became a professor at Harvard. He worked in probability theory, aerodynamics, fluid mechanics, and philosophy of science.

## References

Abramowitz, M. and Stegun, I. A. (ed.), Handbook of Mathematical Functions, New York: Dover, 1965.
von Mises, R., Mathematical Theory of Probability and Statistics, New York: Academic Press, 1964.

## Examples

Draw samples from the distribution:

```
>> mu, kappa = 0.0, 4.0 # mean and dispersion
>>>}s=np.random.vonmises(mu, kappa, 1000
```

Display the histogram of the samples, along with the probability density function:

```
>>> import matplotlib.pyplot as plt
>>> import scipy.special as sps
>>> count, bins, ignored = plt.hist(s, 50, normed=True)
>>> x = np.arange(-np.pi, np.pi, 2*np.pi/50.)
>>> y = -np.exp(kappa*np.cos(x-mu))/(2*np.pi*sps.jn(0,kappa))
>>> plt.plot(x, y/max(y), linewidth=2, color='r')
>>> plt.show()
```


numpy.random.wald (mean, scale, size=None)
Draw samples from a Wald, or Inverse Gaussian, distribution.
As the scale approaches infinity, the distribution becomes more like a Gaussian.
Some references claim that the Wald is an Inverse Gaussian with mean=1, but this is by no means universal.
The Inverse Gaussian distribution was first studied in relationship to Brownian motion. In 1956 M.C.K. Tweedie used the name Inverse Gaussian because there is an inverse relationship between the time to cover a unit distance and distance covered in unit time.

## Parameters

mean : scalar
Distribution mean, should be $>0$.
scale : scalar
Scale parameter, should be $>=0$.
size : int or tuple of ints, optional
Output shape. Default is None, in which case a single value is returned.

## Returns

samples : ndarray or scalar
Drawn sample, all greater than zero.

## Notes

The probability density function for the Wald distribution is

$$
P(x ; \text { mean }, \text { scale })=\sqrt{\frac{s c a l e}{2 \pi x^{3}}} e^{\frac{-s c a l e(x-m e a n)^{2}}{2 \cdot m_{e a n}{ }^{2} x}}
$$

As noted above the Inverse Gaussian distribution first arise from attempts to model Brownian Motion. It is also a competitor to the Weibull for use in reliability modeling and modeling stock returns and interest rate processes.

## References

## ..[1] Brighton Webs Ltd., Wald Distribution,

http://www.brighton-webs.co.uk/distributions/wald.asp
..[2] Chhikara, Raj S., and Folks, J. Leroy, "The Inverse Gaussian
Distribution: Theory : Methodology, and Applications", CRC Press, 1988.
..[3] Wikipedia, "Wald distribution"
http://en.wikipedia.org/wiki/Wald_distribution

## Examples

Draw values from the distribution and plot the histogram:

```
>>> import matplotlib.pyplot as plt
>>> h = plt.hist(np.random.wald(3, 2, 100000), bins=200, normed=True)
>>> plt.show()
```


numpy.random.weibull (a, size=None)
Weibull distribution.
Draw samples from a 1-parameter Weibull distribution with the given shape parameter $a$.

$$
X=(-\ln (U))^{1 / a}
$$

Here, $U$ is drawn from the uniform distribution over $(0,1]$.
The more common 2-parameter Weibull, including a scale parameter $\lambda$ is just $X=\lambda(-\ln (U))^{1 / a}$.

## Parameters

a : float
Shape of the distribution.
size : tuple of ints
Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn.

## See Also:

scipy.stats.distributions. weibull
probability density function, distribution or cumulative density function, etc.
gumbel, scipy.stats.distributions.genextreme

## Notes

The Weibull (or Type III asymptotic extreme value distribution for smallest values, SEV Type III, or RosinRammler distribution) is one of a class of Generalized Extreme Value (GEV) distributions used in modeling extreme value problems. This class includes the Gumbel and Frechet distributions.

The probability density for the Weibull distribution is

$$
p(x)=\frac{a}{\lambda}\left(\frac{x}{\lambda}\right)^{a-1} e^{-(x / \lambda)^{a}},
$$

where $a$ is the shape and $\lambda$ the scale.
The function has its peak (the mode) at $\lambda\left(\frac{a-1}{a}\right)^{1 / a}$.
When $\mathrm{a}=1$, the Weibull distribution reduces to the exponential distribution.

## References

[R214], [R215], [R216]

## Examples

Draw samples from the distribution:

```
>>> a = 5. # shape
>>> s = np.random.weibull(a, 1000)
```

Display the histogram of the samples, along with the probability density function:

```
>>> import matplotlib.pyplot as plt
>>> x = np.arange(1,100.)/50.
>>> def weib(x,n,a):
... return (a/n)* (x/n)**(a-1) * np.exp (- (x/n)**a)
>>> count, bins, ignored = plt.hist(np.random.weibull(5.,1000))
>>> x = np.arange(1,100.)/50.
>>> scale = count.max()/weib(x, 1., 5.).max()
>>> plt.plot(x, weib(x, 1., 5.)*scale)
>>> plt.show()
```


numpy.random. $\mathbf{z i p f}$ ( $a$, size $=$ None )
Draw samples from a Zipf distribution.
Samples are drawn from a Zipf distribution with specified parameter $a>1$.
The Zipf distribution (also known as the zeta distribution) is a continuous probability distribution that satisfies Zipf's law: the frequency of an item is inversely proportional to its rank in a frequency table.

## Parameters

a : float $>1$
Distribution parameter.
size : int or tuple of int, optional
Output shape. If the given shape is, e.g., $(m, n, k)$, then $m * n * k$ samples are drawn; a single integer is equivalent in its result to providing a mono-tuple, i.e., a 1-D array of length size is returned. The default is None, in which case a single scalar is returned.

## Returns

samples : scalar or ndarray
The returned samples are greater than or equal to one.

## See Also:

scipy.stats.distributions.zipf
probability density function, distribution, or cumulative density function, etc.

## Notes

The probability density for the Zipf distribution is

$$
p(x)=\frac{x^{-a}}{\zeta(a)}
$$

where $\zeta$ is the Riemann Zeta function.
It is named for the American linguist George Kingsley Zipf, who noted that the frequency of any word in a sample of a language is inversely proportional to its rank in the frequency table.

## References

Zipf, G. K., Selected Studies of the Principle of Relative Frequency in Language, Cambridge, MA: Harvard Univ. Press, 1932.

## Examples

Draw samples from the distribution:

```
>>> a = 2. # parameter
>>> s = np.random.zipf(a, 1000)
```

Display the histogram of the samples, along with the probability density function:

```
>>> import matplotlib.pyplot as plt
>>> import scipy.special as sps
Truncate s values at 50 so plot is interesting
>>> count, bins, ignored = plt.hist(s[s<50], 50, normed=True)
>>> x = np.arange(1., 50.)
>>> y = x**(-a)/sps.zetac(a)
>>> plt.plot(x, y/max(y), linewidth=2, color='r')
>>> plt.show()
```



### 3.8.4 Random generator

| mtrand. RandomState | Container for the Mersenne Twister pseudo-random number generator. |
| :--- | :--- |
| seed([seed]) | Seed the generator. |
| get_state () | Return a tuple representing the internal state of the generator. |
| set_state(state) | Set the internal state of the generator from a tuple. |

class numpy.random.mtrand.RandomState
Container for the Mersenne Twister pseudo-random number generator.
RandomState exposes a number of methods for generating random numbers drawn from a variety of probability distributions. In addition to the distribution-specific arguments, each method takes a keyword argument size that defaults to None. If size is None, then a single value is generated and returned. If size is an integer, then a 1-D array filled with generated values is returned. If size is a tuple, then an array with that shape is filled and returned.

## Parameters

seed : int or array_like, optional
Random seed initializing the pseudo-random number generator. Can be an integer, an array (or other sequence) of integers of any length, or None (the default). If seed is None, then RandomState will try to read data from / dev/urandom (or the Windows analogue) if available or seed from the clock otherwise.

## Notes

The Python stdlib module "random" also contains a Mersenne Twister pseudo-random number generator with a number of methods that are similar to the ones available in RandomState. RandomState, besides being NumPyaware, has the advantage that it provides a much larger number of probability distributions to choose from.

## Methods



Table 3.2 - continued from previous page

numpy.random.mtrand.dirichlet (alpha, size=None)
Draw samples from the Dirichlet distribution.
Draw size samples of dimension k from a Dirichlet distribution. A Dirichlet-distributed random variable can be seen as a multivariate generalization of a Beta distribution. Dirichlet pdf is the conjugate prior of a multinomial in Bayesian inference.

## Parameters

alpha: array
Parameter of the distribution ( $k$ dimension for sample of dimension $k$ ).
size : array
Number of samples to draw.

## Returns

samples : ndarray,
The drawn samples, of shape (alpha.ndim, size).

## Notes

$$
X \approx \prod_{i=1}^{k} x_{i}^{\alpha_{i}-1}
$$

Uses the following property for computation: for each dimension, draw a random sample y_i from a standard gamma generator of shape alpha_i, then $X=\frac{1}{\sum_{i=1}^{k} y_{i}}\left(y_{1}, \ldots, y_{n}\right)$ is Dirichlet distributed.

## References

[R193], [R194]

## Examples

Taking an example cited in Wikipedia, this distribution can be used if one wanted to cut strings (each of initial length 1.0) into K pieces with different lengths, where each piece had, on average, a designated average length, but allowing some variation in the relative sizes of the pieces.

```
>>> s = np.random.dirichlet((10, 5, 3), 20).transpose()
>>> plt.barh(range(20), s[0])
>>> plt.barh(range(20), s[1], left=s[0], color='g')
>>> plt.barh(range(20), s[2], left=s[0]+s[1], color='r')
>>> plt.title("Lengths of Strings")
```

numpy. random. seed (seed=None)
Seed the generator.
This method is called when RandomState is initialized. It can be called again to re-seed the generator. For details, see RandomState.

## Parameters

seed : int or array_like, optional
Seed for RandomState.

## See Also:

RandomState
numpy.random.get_state()
Return a tuple representing the internal state of the generator.
For more details, see set_state.

## Returns

out : tuple(str, ndarray of 624 uints, int, int, float)

The returned tuple has the following items:

1. the string 'MT19937'.
2. a 1-D array of 624 unsigned integer keys.
3. an integer pos.
4. an integer has_gauss.
5. a float cached_gaussian.

## See Also:

```
set_state
```


## Notes

set_state and get_state are not needed to work with any of the random distributions in NumPy. If the internal state is manually altered, the user should know exactly what he/she is doing.

```
numpy.random.set_state (state)
```

Set the internal state of the generator from a tuple.
For use if one has reason to manually (re-)set the internal state of the "Mersenne Twister"[R209] pseudo-random number generating algorithm.

## Parameters

state : tuple(str, ndarray of 624 uints, int, int, float)
The state tuple has the following items:

1. the string 'MT19937', specifying the Mersenne Twister algorithm.
2. a 1-D array of 624 unsigned integers keys.
3. an integer pos.
4. an integer has_gauss.
5. a float cached_gaussian.

## Returns

out : None
Returns 'None' on success.

## See Also:

get_state

## Notes

set_state and get_state are not needed to work with any of the random distributions in NumPy. If the internal state is manually altered, the user should know exactly what he/she is doing.

For backwards compatibility, the form (str, array of 624 uints, int) is also accepted although it is missing some information about the cached Gaussian value: state $=$ ('MT19937', keys, pos).

## References

[R209]

### 3.9 Sorting, searching, and counting

### 3.9.1 Sorting

```
sort(a[, axis, kind, order]) Return a sorted copy of an array.
lexsort(keys[,axis]) Perform an indirect sort using a sequence of keys.
argsort(a[, axis, kind, order]) Returns the indices that would sort an array.
ndarray.sort([axis, kind, order]) Sort an array, in-place.
msort(a) Return a copy of an array sorted along the first axis.
sort_complex(a) Sort a complex array using the real part first, then the imaginary part.
numpy.sort (a, axis=-1, kind='quicksort', order=None)
    Return a sorted copy of an array.
```


## Parameters

```
a: array_like
Array to be sorted.
axis : int or None, optional
Axis along which to sort. If None, the array is flattened before sorting. The default is -1 , which sorts along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort'\}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
```

When $a$ is a structured array, this argument specifies which fields to compare first, second, and so on. This list does not need to include all of the fields.

## Returns

sorted_array : ndarray
Array of the same type and shape as $a$.

## See Also:

ndarray.sort
Method to sort an array in-place.
argsort
Indirect sort.
lexsort
Indirect stable sort on multiple keys.
searchsorted
Find elements in a sorted array.

## Notes

The various sorting algorithms are characterized by their average speed, worst case performance, work space size, and whether they are stable. A stable sort keeps items with the same key in the same relative order. The three available algorithms have the following properties:

| kind | speed | worst case | work space | stable |
| :--- | :--- | :--- | :--- | :--- |
| 'quicksort' | 1 | $\mathrm{O}\left(\mathrm{n}^{\wedge} 2\right)$ | 0 | no |
| 'mergesort' | 2 | $\mathrm{O}\left(\mathrm{n}^{*} \log (\mathrm{n})\right)$ | $\sim \mathrm{n} / 2$ | yes |
| 'heapsort' | 3 | $\mathrm{O}(\mathrm{n} * \log (\mathrm{n}))$ | 0 | no |

All the sort algorithms make temporary copies of the data when sorting along any but the last axis. Consequently, sorting along the last axis is faster and uses less space than sorting along any other axis.

The sort order for complex numbers is lexicographic. If both the real and imaginary parts are non-nan then the order is determined by the real parts except when they are equal, in which case the order is determined by the imaginary parts.

Previous to numpy 1.4.0 sorting real and complex arrays containing nan values led to undefined behaviour. In numpy versions $>=1.4 .0$ nan values are sorted to the end. The extended sort order is:
-Real: [R, nan]
-Complex: [ $\mathrm{R}+\mathrm{Rj}, \mathrm{R}+$ nanj, nan +Rj , nan + nanj]
where R is a non-nan real value. Complex values with the same nan placements are sorted according to the non-nan part if it exists. Non-nan values are sorted as before.

## Examples

```
>>> a = np.array([[1,4],[3,1]])
>>> np.sort(a) # sort along the last axis
array([[1, 4],
    [1, 3]])
>>> np.sort(a, axis=None) # sort the flattened array
array([1, 1, 3, 4])
>>> np.sort(a, axis=0) # sort along the first axis
array([[1, 1],
    [3, 4]])
```

Use the order keyword to specify a field to use when sorting a structured array:

```
>>> dtype = [('name', 'S10'), ('height', float), ('age', int)]
>>> values = [('Arthur', 1.8, 41), ('Lancelot', 1.9, 38),
... ('Galahad', 1.7, 38)]
>>> a = np.array(values, dtype=dtype) # create a structured array
>>> np.sort(a, order='height')
array([('Galahad', 1.7, 38), ('Arthur', 1.8, 41),
    ('Lancelot', 1.89999999999999999, 38)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

Sort by age, then height if ages are equal:

```
>>> np.sort(a, order=['age', 'height'])
array([('Galahad', 1.7, 38), ('Lancelot', 1.89999999999999999, 38),
    ('Arthur', 1.8, 41)],
    dtype=[('name', '|S10'), ('height', '<f8'), ('age', '<i4')])
```

numpy. lexsort (keys, axis=-1)
Perform an indirect sort using a sequence of keys.
Given multiple sorting keys, which can be interpreted as columns in a spreadsheet, lexsort returns an array of integer indices that describes the sort order by multiple columns. The last key in the sequence is used for the primary sort order, the second-to-last key for the secondary sort order, and so on. The keys argument must be a sequence of objects that can be converted to arrays of the same shape. If a 2 D array is provided for the keys argument, it's rows are interpreted as the sorting keys and sorting is according to the last row, second last row etc.

## Parameters

keys : ( $\mathrm{k}, \mathrm{N}$ ) array or tuple containing $\mathrm{k}(\mathrm{N}$, )-shaped sequences
The $k$ different "columns" to be sorted. The last column (or row if keys is a 2D array) is the primary sort key.
axis : int, optional
Axis to be indirectly sorted. By default, sort over the last axis.

## Returns

indices : ( N, ) ndarray of ints
Array of indices that sort the keys along the specified axis.

## See Also:

```
argsort
```

Indirect sort.
ndarray.sort
In-place sort.
sort
Return a sorted copy of an array.

## Examples

Sort names: first by surname, then by name.

```
>>> surnames = ('Hertz', 'Galilei', 'Hertz')
>>> first_names = ('Heinrich', 'Galileo', 'Gustav')
>>> ind = np.lexsort((first_names, surnames))
>>> ind
array([1, 2, 0])
>>> [surnames[i] + ", " + first_names[i] for i in ind]
['Galilei, Galileo', 'Hertz, Gustav', 'Hertz, Heinrich']
```

Sort two columns of numbers:

```
>>> a = [1,5,1,4,3,4,4] # First column
>>> b = [9,4,0,4,0,2,1] # Second column
>>> ind = np.lexsort((b,a)) # Sort by a, then by b
>>> print ind
[2 0 4 6 5 3 1]
>>> [(a[i],b[i]) for i in ind]
[(1, 0), (1, 9), (3, 0), (4, 1), (4, 2), (4, 4), (5, 4)]
```

Note that sorting is first according to the elements of a. Secondary sorting is according to the elements of b .
A normal argsort would have yielded:

```
>>> [(a[i],b[i]) for i in np.argsort(a)]
[(1, 9), (1, 0), (3, 0), (4, 4), (4, 2), (4, 1), (5, 4)]
```

Structured arrays are sorted lexically by argsort:

```
>>> x = np.array([(1,9), (5,4), (1,0), (4,4), (3,0), (4,2), (4,1)],
... dtype=np.dtype([('x', int), ('y', int)]))
```

```
>>> np.argsort(x) # or np.argsort(x, order=('x', 'y'))
array ([2, 0, 4, 6, 5, 3, 1])
```

numpy.argsort ( $a$, axis=-1, kind='quicksort', order=None)
Returns the indices that would sort an array.
Perform an indirect sort along the given axis using the algorithm specified by the kind keyword. It returns an array of indices of the same shape as $a$ that index data along the given axis in sorted order.

## Parameters

a : array_like
Array to sort.
axis : int or None, optional
Axis along which to sort. The default is -1 (the last axis). If None, the flattened array is used.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## Returns

index_array : ndarray, int
Array of indices that sort $a$ along the specified axis. In other words, a [index_array] yields a sorted $a$.

## See Also:

sort
Describes sorting algorithms used.
lexsort
Indirect stable sort with multiple keys.
ndarray.sort
Inplace sort.

## Notes

See sort for notes on the different sorting algorithms.
As of NumPy 1.4.0 argsort works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

One dimensional array:

```
>>> x = np.array([3, 1, 2])
>>> np.argsort(x)
array([1, 2, 0])
```

Two-dimensional array:

```
>>> x = np.array([[0, 3], [2, 2]])
>>> x
array([[0, 3],
    [2, 2]])
>>> np.argsort(x, axis=0)
array([[0, 1],
    [1, 0]])
>>> np.argsort(x, axis=1)
array([[0, 1],
    [0, 1]])
```

Sorting with keys:

```
>>> x = np.array([(1, 0), (0, 1)], dtype=[('x', '<i4'), ('y', '<i4')])
>>> x
array([(1, 0), (0, 1)],
    dtype=[('x', '<i4'), ('y', '<i4')])
>>> np.argsort(x, order=('x','y'))
array([1, 0])
>>> np.argsort(x, order=('y',' ('))
array([0, 1])
ndarray.sort (axis=-1, kind='quicksort', order=None)
```

    Sort an array, in-place.
    
## Parameters

axis : int, optional
Axis along which to sort. Default is -1 , which means sort along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## See Also:

numpy.sort
Return a sorted copy of an array.
argsort
Indirect sort.
lexsort
Indirect stable sort on multiple keys.
searchsorted
Find elements in sorted array.

## Notes

See sort for notes on the different sorting algorithms.

## Examples

```
>>> a = np.array([[1,4], [3,1]])
>>> a.sort(axis=1)
>>> a
array([[1, 4],
    [1, 3]])
>>> a.sort(axis=0)
>>> a
array([[1, 3],
    [1, 4]])
```

Use the order keyword to specify a field to use when sorting a structured array:

```
>>> a = np.array([('a', 2), ('c', 1)], dtype=[('x', 'S1'), ('y', int)])
>>> a.sort(order='y')
>>> a
array([('c', 1), ('a', 2)],
    dtype=[('x', '|S1'), ('y', '<i4')])
```

numpy.msort (a)

Return a copy of an array sorted along the first axis.

## Parameters

a : array_like
Array to be sorted.

## Returns

 sorted_array : ndarrayArray of the same type and shape as $a$.

## See Also:

sort

## Notes

np.msort (a) is equivalent to np. sort (a, axis=0).
numpy. sort_complex (a)
Sort a complex array using the real part first, then the imaginary part.

## Parameters

a : array_like
Input array

## Returns

out : complex ndarray
Always returns a sorted complex array.
Examples

```
>>> np.sort_complex([5, 3, 6, 2, 1])
array([ 1.+0.j, 2.+0.j, 3.+0.j, 5.+0.j, 6.+0.j])
>>> np.sort_complex([1 + 2j, 2 - 1j, 3 - 2j, 3 - 3j, 3 + 5j])
array([ 1.+2.j, 2.-1.j, 3.-3.j, 3.-2.j, 3.+5.j])
```


### 3.9.2 Searching

| $\operatorname{argmax}(\mathrm{a}, \mathrm{axis}])$ | Indices of the maximum values along an axis. |
| :---: | :---: |
| nanargmax(a[, axis]) | Return indices of the maximum values over an axis, ignoring NaNs. |
| $\operatorname{argmin}\left(\mathrm{a}\right.$, axis] ${ }^{\text {a }}$ | Return the indices of the minimum values along an axis. |
| nanargmin(a[, axis]) | Return indices of the minimum values over an axis, ignoring NaNs. |
| argwhere(a) | Find the indices of array elements that are non-zero, grouped by element. |
| nonzero(a) | Return the indices of the elements that are non-zero. |
| flatnonzero(a) | Return indices that are non-zero in the flattened version of a. |
| where(condition, x ) | Return elements, either from $x$ or $y$, depending on condition. |
| searchsorted(a, v[, side]) | Find indices where elements should be inserted to maintain order. |
| extract(condition, arr) | Return the elements of an array that satisfy some condition. |
| numpy . argmax ( $a$, axis=None) |  |
| Indices of the maximum values along an axis. |  |
| Parameters |  |
| a : array_like |  |
| Input array. |  |
| axis : int, option |  |

By default, the index is into the flattened array, otherwise along the specified axis.

## Returns

index_array : ndarray of ints
Array of indices into the array. It has the same shape as a.shape with the dimension along axis removed.

## See Also:

```
ndarray.argmax, argmin
```

amax
The maximum value along a given axis.
unravel_index
Convert a flat index into an index tuple.

## Notes

In case of multiple occurrences of the maximum values, the indices corresponding to the first occurrence are returned.

## Examples

```
>>> a = np.arange (6).reshape (2,3)
>>> a
array([[0, 1, 2],
    [3, 4, 5]])
>>> np.argmax(a)
5
>>> np.argmax(a, axis=0)
array([1, 1, 1])
>>> np.argmax(a, axis=1)
array([2, 2])
>>> b = np.arange(6)
>>> b[1] = 5
```

```
>>> b
array([0, 5, 2, 3, 4, 5])
>>> np.argmax(b) # Only the first occurrence is returned.
1
```

numpy . nanargmax (a, axis=None)

Return indices of the maximum values over an axis, ignoring NaNs.

## Parameters

a : array_like
Input data.
axis : int, optional
Axis along which to operate. By default flattened input is used.

## Returns

index_array : ndarray
An array of indices or a single index value.

## See Also:

argmax, nanargmin

## Examples

```
>>> a = np.array([[np.nan, 4], [2, 3]])
>>> np.argmax(a)
0
>>> np.nanargmax(a)
1
>>> np.nanargmax(a, axis=0)
array([1, 0])
>>> np.nanargmax(a, axis=1)
array([1, 1])
```

numpy. argmin (a, axis=None)

Return the indices of the minimum values along an axis.
See Also:
argmax
Similar function. Please refer to numpy . argmax for detailed documentation.
numpy . nanargmin (a, axis=None)
Return indices of the minimum values over an axis, ignoring NaNs.

## Parameters

a : array_like
Input data.
axis : int, optional
Axis along which to operate. By default flattened input is used.

## Returns

index_array : ndarray
An array of indices or a single index value.

## See Also:

```
argmin, nanargmax
```


## Examples

```
>>> a = np.array([[np.nan, 4], [2, 3]])
>>> np.argmin(a)
0
>>> np.nanargmin(a)
2
>>> np.nanargmin(a, axis=0)
array([1, 1])
>>> np.nanargmin(a, axis=1)
array([1, 0])
```

numpy. argwhere (a)
Find the indices of array elements that are non-zero, grouped by element.

## Parameters

a : array_like
Input data.

## Returns

index_array : ndarray
Indices of elements that are non-zero. Indices are grouped by element.

## See Also:

```
where, nonzero
```


## Notes

np. argwhere (a) is the same as np.transpose (np.nonzero (a)).
The output of argwhere is not suitable for indexing arrays. For this purpose use where (a) instead.

## Examples

```
>>> x = np.arange (6).reshape (2,3)
>>> x
array([[0, 1, 2],
    [3, 4, 5]])
>>> np.argwhere(x>1)
array([[0, 2],
    [1, 0],
    [1, 1],
    [1, 2]])
```

numpy. nonzero (a)

Return the indices of the elements that are non-zero.
Returns a tuple of arrays, one for each dimension of $a$, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

```
a[nonzero(a)]
```

To group the indices by element, rather than dimension, use:

```
transpose(nonzero(a))
```

The result of this is always a 2-D array, with a row for each non-zero element.

## Parameters

a : array_like
Input array.

## Returns

tuple_of_arrays : tuple
Indices of elements that are non-zero.

## See Also:

## flatnonzero

Return indices that are non-zero in the flattened version of the input array.

```
ndarray.nonzero
```

Equivalent ndarray method.

```
count_nonzero
```

Counts the number of non-zero elements in the input array.

## Examples

```
>>> x = np.eye(3)
>>> x
array([[ 1., 0., 0.],
    [ 0., 1., 0.],
    [ 0., 0., 1.]])
>>> np.nonzero(x)
(array([0, 1, 2]), array([0, 1, 2]))
>>> x[np.nonzero(x)]
array([ 1., 1., 1.])
>>> np.transpose(np.nonzero(x))
array([[0, 0],
    [1, 1],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , np.nonzero( $a>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a = np.array([[1,2,3],[4,5,6],[7, 8,9]])
>>> a > 3
array([[False, False, False],
    [ True, True, True],
    [ True, True, True]], dtype=bool)
>>> np.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the boolean array can also be called.

```
>>> (a > 3).nonzero()
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

numpy.flatnonzero (a)

Return indices that are non-zero in the flattened version of a.
This is equivalent to a.ravel().nonzero()[0].

## Parameters

a : ndarray
Input array.

## Returns

res: ndarray
Output array, containing the indices of the elements of a.ravel() that are non-zero.

## See Also:

```
nonzero
```

Return the indices of the non-zero elements of the input array.
ravel
Return a 1-D array containing the elements of the input array.

## Examples

```
>>> x = np.arange (-2, 3)
>>> x
array([-2, -1, 0, 1, 2])
>>> np.flatnonzero(x)
array([0, 1, 3, 4])
```

Use the indices of the non-zero elements as an index array to extract these elements:

```
>>> x.ravel()[np.flatnonzero(x)]
array([-2, -1, 1, 2])
```

numpy . where (condition $[, x, y]$ )
Return elements, either from $x$ or $y$, depending on condition.
If only condition is given, return condition. nonzero().

## Parameters

condition : array_like, bool
When True, yield $x$, otherwise yield $y$.
$\mathbf{x , ~ y}$ : array_like, optional
Values from which to choose. $x$ and $y$ need to have the same shape as condition.

## Returns

out : ndarray or tuple of ndarrays
If both $x$ and $y$ are specified, the output array contains elements of $x$ where condition is True, and elements from $y$ elsewhere.

If only condition is given, return the tuple condition. nonzero(), the indices where condition is True.

See Also:
nonzero, choose

## Notes

If $x$ and $y$ are given and input arrays are 1-D, where is equivalent to:
[xv if c else yv for (c, xv, yv) in zip(condition, $x, y)$ ]

## Examples

```
>>> np.where([[True, False], [True, True]],
... [[1, 2], [3, 4]],
... [[9, 8], [7, 6]])
array([[1, 8],
[3, 4]])
>>> np.where([[0, 1], [1, 0]])
(array([0, 1]), array([1, 0]))
>>> x = np.arange(9.).reshape(3, 3)
>>> np.where( x > 5 )
(array([2, 2, 2]), array([0, 1, 2]))
>> x[np.where( x > 3.0 )] # Note: result is ID.
array([ 4., 5., 6., 7., 8.])
>>> np.where(x < 5, x, -1) # Note: broadcasting.
array([[ 0., 1., 2.],
    [ 3., 4., -1.],
    [-1., -1., -1.]])
```

numpy. searchsorted ( $a, v$, side $=$ 'left')

Find indices where elements should be inserted to maintain order.
Find the indices into a sorted array $a$ such that, if the corresponding elements in $v$ were inserted before the indices, the order of $a$ would be preserved.

## Parameters

a: 1-D array_like
Input array, sorted in ascending order.
v: array_like
Values to insert into $a$.
side : \{ 'left', 'right' \}, optional
If 'left', the index of the first suitable location found is given. If 'right', return the last such index. If there is no suitable index, return either 0 or N (where N is the length of a).

## Returns

indices : array of ints
Array of insertion points with the same shape as $v$.

## See Also:

sort
Return a sorted copy of an array.
histogram
Produce histogram from 1-D data.

## Notes

Binary search is used to find the required insertion points.
As of Numpy 1.4.0 searchsorted works with real/complex arrays containing nan values. The enhanced sort order is documented in sort.

## Examples

```
>>> np.searchsorted([1,2,3,4,5], 3)
2
>>> np.searchsorted([1,2,3,4,5], 3, side='right')
3
>>> np.searchsorted([1,2,3,4,5], [-10, 10, 2, 3])
array([0, 5, 1, 2])
```

numpy .extract (condition, arr)
Return the elements of an array that satisfy some condition.
This is equivalent to np.compress(ravel(condition), ravel(arr)). If condition is boolean np.extract is equivalent to arr [condition].

## Parameters <br> condition : array_like

An array whose nonzero or True entries indicate the elements of arr to extract. arr : array_like

Input array of the same size as condition.

## See Also:

```
take, put,putmask, compress
```


## Examples

```
>>> arr = np.arange(12).reshape((3, 4))
>>> arr
array([[ 0, 1, 2, 3],
    [ 4, 5, 6, 7],
    [ 8, 9, 10, 11]])
>>> condition = np.mod(arr, 3)==0
>>> condition
array([[ True, False, False, True],
    [False, False, True, False],
    [False, True, False, False]], dtype=bool)
>>> np.extract(condition, arr)
array([0, 3, 6, 9])
```

If condition is boolean:

```
>>> arr[condition]
array([0, 3, 6, 9])
```


### 3.9.3 Counting

count_nonzero(a) Counts the number of non-zero values in the array a.
numpy.count_nonzero (a)
Counts the number of non-zero values in the array a.

## Parameters

a : array_like
The array for which to count non-zeros.

## Returns

count : int
Number of non-zero values in the array.

## See Also:

```
nonzero
```

Return the coordinates of all the non-zero values.

## Examples

```
>>> np.count_nonzero(np.eye(4))
```

4
>>> np.count_nonzero([[0,1,7,0,0],[3,0,0,2,19] ])
5

### 3.10 Logic functions

### 3.10.1 Truth value testing

```
    all(a[, axis, out]) Test whether all array elements along a given axis evaluate to True.
any(a[,axis,out]) Test whether any array element along a given axis evaluates to True.
numpy.all (a, axis=None, out=None)
Test whether all array elements along a given axis evaluate to True.
```


## Parameters

```
a : array_like
Input array or object that can be converted to an array.
axis : int, optional
```

Axis along which a logical AND is performed. The default (axis = None) is to perform a logical AND over a flattened input array. axis may be negative, in which case it counts from the last to the first axis.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output and its type is preserved (e.g., if dtype (out) is float, the result will consist of 0.0 's and 1.0 's). See doc.ufuncs (Section "Output arguments") for more details.

## Returns

all : ndarray, bool
A new boolean or array is returned unless out is specified, in which case a reference to out is returned.

## See Also:

ndarray.all
equivalent method
any
Test whether any element along a given axis evaluates to True.

## Notes

Not a Number (NaN), positive infinity and negative infinity evaluate to True because these are not equal to zero.

## Examples

```
>>> np.all([[True,False],[True,True]])
False
>>> np.all([[True,False],[True,True]], axis=0)
array([ True, False], dtype=bool)
>>> np.all([-1, 4, 5])
True
>>> np.all([1.0, np.nan])
True
>>> o=np.array([False])
>>> z=np.all([-1, 4, 5], out=0)
>>> id(z), id(0), z
(28293632, 28293632, array([ True], dtype=bool))
```

numpy . any ( $a$, axis=None, out=None)
Test whether any array element along a given axis evaluates to True.
Returns single boolean unless axis is not None

## Parameters

a : array_like
Input array or object that can be converted to an array.
axis : int, optional
Axis along which a logical OR is performed. The default (axis $=$ None) is to perform a logical OR over a flattened input array. axis may be negative, in which case it counts from the last to the first axis.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output and its type is preserved (e.g., if it is of type float, then it will remain so, returning 1.0 for True and 0.0 for False, regardless of the type of $a$ ). See doc.ufuncs (Section "Output arguments") for details.

## Returns

> any : bool or ndarray

A new boolean or ndarray is returned unless out is specified, in which case a reference to out is returned.

## See Also:

```
ndarray.any
```

    equivalent method
    all

Test whether all elements along a given axis evaluate to True.

## Notes

Not a Number (NaN), positive infinity and negative infinity evaluate to True because these are not equal to zero.

## Examples

```
>>> np.any([[True, False], [True, True]])
True
>>> np.any([[True, False], [False, False]], axis=0)
array([ True, False], dtype=bool)
>>> np.any([-1, 0, 5])
True
>>> np.any(np.nan)
True
>>> o=np.array([False])
>>> z=np.any([-1, 4, 5], out=0)
>>> z, O
(array([ True], dtype=bool), array([ True], dtype=bool))
>>> # Check now that z is a reference to o
>>> z is o
True
>>> id(z), id(o) # identity of z and o
(191614240, 191614240)
```


### 3.10.2 Array contents

| isfinite() | Test element-wise for finite-ness (not infinity or not Not a Number). |
| :--- | :--- |
| isinf () | Test element-wise for positive or negative infinity. |
| isnan () | Test element-wise for Not a Number (NaN), return result as a bool array. |
| isneginf $(\mathrm{x}[, \mathrm{y}])$ | Test element-wise for negative infinity, return result as bool array. |
| isposinf $(\mathrm{x}[, \mathrm{y}])$ | Test element-wise for positive infinity, return result as bool array. |
| numpy.isfinite $(x[$, out $])$ |  |

Test element-wise for finite-ness (not infinity or not Not a Number).
The result is returned as a boolean array.

## Parameters

$\mathbf{x}$ : array_like
Input values.
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output. See doc.ufuncs.

## Returns

y : ndarray, bool
For scalar input, the result is a new boolean with value True if the input is finite; otherwise the value is False (input is either positive infinity, negative infinity or Not a Number).

For array input, the result is a boolean array with the same dimensions as the input and the values are True if the corresponding element of the input is finite; otherwise the values are False (element is either positive infinity, negative infinity or Not a Number).

## See Also:

isinf, isneginf, isposinf, isnan

## Notes

Not a Number, positive infinity and negative infinity are considered to be non-finite.
Numpy uses the IEEE Standard for Binary Floating-Point for Arithmetic (IEEE 754). This means that Not a Number is not equivalent to infinity. Also that positive infinity is not equivalent to negative infinity. But infinity is equivalent to positive infinity. Errors result if the second argument is also supplied when $x$ is a scalar input, or if first and second arguments have different shapes.

## Examples

```
>>> np.isfinite(1)
True
>>> np.isfinite(0)
True
>>> np.isfinite(np.nan)
False
>>> np.isfinite(np.inf)
False
>>> np.isfinite(np.NINF)
False
>>> np.isfinite([np.log(-1.),1.,np.log(0)])
array([False, True, False], dtype=bool)
>>> x = np.array([-np.inf, 0., np.inf])
>>> y = np.array([2, 2, 2])
>>> np.isfinite(x, y)
array([0, 1, 0])
>>> y
array([0, 1, 0])
```

numpy.isinf ( $x[$, out $]$ )
Test element-wise for positive or negative infinity.
Return a bool-type array, the same shape as $x$, True where $\mathrm{x}==+/$-inf, False everywhere else.

## Parameters

$\mathbf{x}$ : array_like
Input values
out : array_like, optional
An array with the same shape as $x$ to store the result.

## Returns

$\mathbf{y}$ : bool (scalar) or bool-type ndarray
For scalar input, the result is a new boolean with value True if the input is positive or negative infinity; otherwise the value is False.
For array input, the result is a boolean array with the same shape as the input and the values are True where the corresponding element of the input is positive or negative infinity; elsewhere the values are False. If a second argument was supplied the result is stored there. If the type of that array is a numeric type the result is represented as zeros and ones, if the type is boolean then as False and True, respectively. The return value $y$ is then a reference to that array.

## See Also:

```
isneginf,isposinf,isnan,isfinite
```


## Notes

Numpy uses the IEEE Standard for Binary Floating-Point for Arithmetic (IEEE 754).
Errors result if the second argument is supplied when the first argument is a scalar, or if the first and second arguments have different shapes.

## Examples

```
>>> np.isinf(np.inf)
True
>>> np.isinf(np.nan)
False
>>> np.isinf(np.NINF)
True
>>> np.isinf([np.inf, -np.inf, 1.0, np.nan])
array([ True, True, False, False], dtype=bool)
>>> x = np.array([-np.inf, 0., np.inf])
>>> y = np.array([2, 2, 2])
>>> np.isinf(x, y)
array([1, 0, 1])
>>> y
array([1, 0, 1])
numpy.isnan(x[,out])
```

Test element-wise for Not a Number (NaN), return result as a bool array.

## Parameters

$\mathbf{x}$ : array_like
Input array.

## Returns

$\mathbf{y}:\{$ ndarray, bool $\}$
For scalar input, the result is a new boolean with value True if the input is NaN ; otherwise the value is False.

For array input, the result is a boolean array with the same dimensions as the input and the values are True if the corresponding element of the input is NaN ; otherwise the values are False.

## See Also:

```
isinf, isneginf, isposinf, isfinite
```


## Notes

Numpy uses the IEEE Standard for Binary Floating-Point for Arithmetic (IEEE 754). This means that Not a Number is not equivalent to infinity.

## Examples

```
>>> np.isnan(np.nan)
True
>>> np.isnan(np.inf)
False
>>> np.isnan([np.log(-1.),1.,np.log(0)])
array([ True, False, False], dtype=bool)
```


## numpy.isneginf ( $x, y=$ None)

Test element-wise for negative infinity, return result as bool array.

## Parameters

$\mathbf{x}$ : array_like
The input array.
$\mathbf{y}$ : array_like, optional
A boolean array with the same shape and type as $x$ to store the result.

## Returns

y : ndarray
A boolean array with the same dimensions as the input. If second argument is not supplied then a numpy boolean array is returned with values True where the corresponding element of the input is negative infinity and values False where the element of the input is not negative infinity.
If a second argument is supplied the result is stored there. If the type of that array is a numeric type the result is represented as zeros and ones, if the type is boolean then as False and True. The return value $y$ is then a reference to that array.

## See Also:

```
isinf,isposinf,isnan,isfinite
```


## Notes

Numpy uses the IEEE Standard for Binary Floating-Point for Arithmetic (IEEE 754).
Errors result if the second argument is also supplied when x is a scalar input, or if first and second arguments have different shapes.

## Examples

```
>>> np.isneginf(np.NINF)
array(True, dtype=bool)
>>> np.isneginf(np.inf)
array(False, dtype=bool)
>>> np.isneginf(np.PINF)
array(False, dtype=bool)
>>> np.isneginf([-np.inf, 0., np.inf])
array([ True, False, False], dtype=bool)
>>> x = np.array([-np.inf, 0., np.inf])
>>> y = np.array([2, 2, 2])
>>> np.isneginf(x, y)
array([1, 0, 0])
>>> y
array([1, 0, 0])
numpy.isposinf (x, y=None)
```

Test element-wise for positive infinity, return result as bool array.

## Parameters

$\mathbf{x}$ : array_like
The input array.
$\mathbf{y}$ : array_like, optional

A boolean array with the same shape as $x$ to store the result.

## Returns

$\mathbf{y}$ : ndarray
A boolean array with the same dimensions as the input. If second argument is not supplied then a boolean array is returned with values True where the corresponding element of the input is positive infinity and values False where the element of the input is not positive infinity.

If a second argument is supplied the result is stored there. If the type of that array is a numeric type the result is represented as zeros and ones, if the type is boolean then as False and True. The return value $y$ is then a reference to that array.

## See Also:

```
isinf,isneginf,isfinite, isnan
```


## Notes

Numpy uses the IEEE Standard for Binary Floating-Point for Arithmetic (IEEE 754).
Errors result if the second argument is also supplied when $x$ is a scalar input, or if first and second arguments have different shapes.

## Examples

```
>>> np.isposinf(np.PINF)
array(True, dtype=bool)
>>> np.isposinf(np.inf)
array(True, dtype=bool)
>>> np.isposinf(np.NINF)
array(False, dtype=bool)
>>> np.isposinf([-np.inf, 0., np.inf])
array([False, False, True], dtype=bool)
>>> x = np.array([-np.inf, 0., np.inf])
>>> y = np.array([2, 2, 2])
>>> np.isposinf(x, y)
array([0, 0, 1])
>>> y
array([0, 0, 1])
```


### 3.10.3 Array type testing

```
iscomplex(x) Returns a bool array, where True if input element is complex.
iscomplexobj(x) Return True if x is a complex type or an array of complex numbers.
isfortran(a) Returns True if array is arranged in Fortran-order in memory
isreal(x) Returns a bool array, where True if input element is real.
isrealobj(x) Return True if x is a not complex type or an array of complex numbers.
isscalar(num) Returns True if the type of num is a scalar type.
```


## numpy.iscomplex $(x)$

Returns a bool array, where True if input element is complex.
What is tested is whether the input has a non-zero imaginary part, not if the input type is complex.

## Parameters

$\mathbf{x}$ : array_like

Input array.

## Returns

out : ndarray of bools
Output array.

## See Also:

isreal
iscomplexobj
Return True if $x$ is a complex type or an array of complex numbers.

## Examples

```
>>> np.iscomplex([1+1j, 1+0j, 4.5, 3, 2, 2j])
array([ True, False, False, False, False, True], dtype=bool)
```

numpy.iscomplexobj $(x)$
Return True if x is a complex type or an array of complex numbers.
The type of the input is checked, not the value. So even if the input has an imaginary part equal to zero, iscomplexobj evaluates to True if the data type is complex.

## Parameters

## $\mathbf{x}$ : any

The input can be of any type and shape.

## Returns

$\mathbf{y}$ : bool
The return value, True if $x$ is of a complex type.

## See Also:

isrealobj, iscomplex

## Examples

```
>>> np.iscomplexobj(1)
False
>>> np.iscomplexobj(1+0j)
True
>>> np.iscomplexobj([3, 1+0j, True])
True
numpy.isfortran (a)
```

Returns True if array is arranged in Fortran-order in memory and dimension $>1$.
Parameters
a: ndarray
Input array.

## Examples

np.array allows to specify whether the array is written in C-contiguous order (last index varies the fastest), or FORTRAN-contiguous order in memory (first index varies the fastest).

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]], order='C')
>>> a
array([[1, 2, 3],
```

```
    [4, 5, 6]])
>>> np.isfortran(a)
False
>>> b = np.array([[1, 2, 3], [4, 5, 6]], order='FORTRAN')
>>> b
array([[1, 2, 3],
    [4, 5, 6]])
>>> np.isfortran(b)
True
```

The transpose of a C-ordered array is a FORTRAN-ordered array.

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]], order='C')
>>> a
array([[1, 2, 3],
    [4, 5, 6]])
>>> np.isfortran(a)
False
>>> b = a.T
>>> b
array([[1, 4],
    [2, 5],
    [3, 6]])
>>> np.isfortran(b)
True
```

1-D arrays always evaluate as False.

```
>>> np.isfortran(np.array([1, 2], order='FORTRAN'))
False
```

numpy.isreal ( $x$ )

Returns a bool array, where True if input element is real.
If element has complex type with zero complex part, the return value for that element is True.

## Parameters

$\mathbf{x}$ : array_like
Input array.

## Returns

out : ndarray, bool
Boolean array of same shape as $x$.

## See Also:

iscomplex
isrealobj
Return True if $x$ is not a complex type.

## Examples

```
>>> np.isreal([1+1j, 1+0j, 4.5, 3, 2, 2j])
array([False, True, True, True, True, False], dtype=bool)
numpy.isrealobj(x)
```

Return True if x is a not complex type or an array of complex numbers.

The type of the input is checked, not the value. So even if the input has an imaginary part equal to zero, isrealobj evaluates to False if the data type is complex.

## Parameters

$\mathbf{x}$ : any
The input can be of any type and shape.

## Returns

$\mathbf{y}$ : bool
The return value, False if $x$ is of a complex type.

## See Also:

```
iscomplexobj,isreal
```


## Examples

```
>>> np.isrealobj(1)
True
>>> np.isrealobj(1+0j)
False
>>> np.isrealobj([3, 1+0j, True])
False
```

numpy.isscalar (num)
Returns True if the type of num is a scalar type.

## Parameters

num : any
Input argument, can be of any type and shape.

## Returns

val : bool
True if num is a scalar type, False if it is not.

## Examples

```
>>> np.isscalar(3.1)
```

True
>>> np.isscalar([3.1])
False
>>> np.isscalar(False)
True

### 3.10.4 Logical operations

```
logical_and(x1) Compute the truth value of x1 AND x2 elementwise.
logical_or(x1) Compute the truth value of x1 OR x2 elementwise.
logical_not() Compute the truth value of NOT x elementwise.
logical_xor(x1) Compute the truth value of x1 XOR x2, element-wise.
numpy.logical_and (xl, x2[,out])
Compute the truth value of x 1 AND x 2 elementwise.
```

```
Parameters
```

Parameters
x1, x2 : array_like

```
            x1, x2 : array_like
```

Input arrays. $x 1$ and $x 2$ must be of the same shape.

## Returns

$\mathbf{y}:\{$ ndarray, bool $\}$
Boolean result with the same shape as $x 1$ and $x 2$ of the logical AND operation on corresponding elements of $x 1$ and $x 2$.

## See Also:

```
logical_or, logical_not,logical_xor, bitwise_and
```


## Examples

```
>>> np.logical_and(True, False)
False
>>> np.logical_and([True, False], [False, False])
array([False, False], dtype=bool)
>>> x = np.arange(5)
>>> np.logical_and(x>1, x<4)
array([False, False, True, True, False], dtype=bool)
```

numpy.logical_or ( $x 1, x 2[$, out $])$
Compute the truth value of x 1 OR x 2 elementwise.

## Parameters

$\mathbf{x 1}, \mathbf{x 2}$ : array_like
Logical OR is applied to the elements of $x 1$ and $x 2$. They have to be of the same shape.

## Returns

 $\mathbf{y}:\{$ ndarray, bool $\}$Boolean result with the same shape as $x 1$ and $x 2$ of the logical OR operation on elements of $x 1$ and $x 2$.

See Also:

```
logical_and, logical_not, logical_xor, bitwise_or
```


## Examples

```
>>> np.logical_or(True, False)
True
>>> np.logical_or([True, False], [False, False])
array([ True, False], dtype=bool)
>>> x = np.arange(5)
>>> np.logical_or(x < 1, x > 3)
array([ True, False, False, False, True], dtype=bool)
```

numpy.logical_not ( $x[$, out $]$ )
Compute the truth value of NOT x elementwise.

## Parameters

$\mathbf{x}$ : array_like
Logical NOT is applied to the elements of $x$.

## Returns

$\mathbf{y}$ : bool or ndarray of bool

Boolean result with the same shape as $x$ of the NOT operation on elements of $x$.

## See Also:

```
logical_and, logical_or, logical_xor
```


## Examples

```
>>> np.logical_not(3)
False
>>> np.logical_not([True, False, 0, 1])
array([False, True, True, False], dtype=bool)
>>> x = np.arange(5)
>>> np.logical_not (x<3)
array([False, False, False, True, True], dtype=bool)
numpy.logical_xor ( \(x 1, x 2[\), out \(]\) )
Compute the truth value of x 1 XOR x 2 , element-wise.
```


## Parameters

$\mathbf{x 1}, \mathbf{x 2}$ : array_like
Logical XOR is applied to the elements of $x 1$ and $x 2$. They must be broadcastable to the same shape.

## Returns

$\mathbf{y}$ : bool or ndarray of bool
Boolean result of the logical XOR operation applied to the elements of $x 1$ and $x 2$; the shape is determined by whether or not broadcasting of one or both arrays was required.

## See Also:

```
logical_and, logical_or, logical_not,bitwise_xor
```


## Examples

```
>>> np.logical_xor(True, False)
True
>>> np.logical_xor([True, True, False, False], [True, False, True, False])
array([False, True, True, False], dtype=bool)
>>> x = np.arange(5)
>>> np.logical_xor(x < 1, x > 3)
array([ True, False, False, False, True], dtype=bool)
```

Simple example showing support of broadcasting

```
>>> np.logical_xor(0, np.eye(2))
array([[ True, False],
    [False, True]], dtype=bool)
```


### 3.10.5 Comparison

| allclose $(a, b[$, rtol, atol] $)$ | Returns True if two arrays are element-wise equal within a tolerance. |
| :--- | :--- |
| array_equal(a1, a2) | True if two arrays have the same shape and elements, False otherwise. |
| array_equiv(a1, a2) | Returns True if input arrays are shape consistent and all elements equal. |

numpy.allclose ( $a, b$, rtol $=1.0000000000000001 e-05$, atol $=1 e-08$ )
Returns True if two arrays are element-wise equal within a tolerance.
The tolerance values are positive, typically very small numbers. The relative difference ( $\mathrm{rtol} \mathrm{*}^{*} \mathrm{abs}(b)$ ) and the absolute difference atol are added together to compare against the absolute difference between $a$ and $b$.

## Parameters

$$
\mathbf{a}, \mathbf{b} \text { : array_like }
$$

Input arrays to compare.
rtol : float
The relative tolerance parameter (see Notes).
atol : float
The absolute tolerance parameter (see Notes).

## Returns

y: bool
Returns True if the two arrays are equal within the given tolerance; False otherwise. If either array contains NaN , then False is returned.

## See Also:

all, any, alltrue, sometrue

## Notes

If the following equation is element-wise True, then allclose returns True.
absolute $(a-b)<=($ atol + rtol $* \operatorname{absolute}(b))$
The above equation is not symmetric in $a$ and $b$, so that $\operatorname{allclose}(a, b)$ might be different from $\operatorname{allclose}(b, a)$ in some rare cases.

## Examples

```
>>> np.allclose([1e10,1e-7], [1.00001e10,1e-8])
False
>>> np.allclose([1e10,1e-8], [1.00001e10,1e-9])
True
>>> np.allclose([1e10,1e-8], [1.0001e10,1e-9])
False
>>> np.allclose([1.0, np.nan], [1.0, np.nan])
False
```

numpy.array_equal (a1, a2)
True if two arrays have the same shape and elements, False otherwise.

## Parameters

a1, a2: array_like
Input arrays.

## Returns

b: bool
Returns True if the arrays are equal.

## See Also:

```
allclose
```

Returns True if two arrays are element-wise equal within a tolerance.

```
array_equiv
```

Returns True if input arrays are shape consistent and all elements equal.

## Examples

```
>>> np.array_equal([1, 2], [1, 2])
True
>>> np.array_equal(np.array([1, 2]), np.array([1, 2]))
True
>>> np.array_equal([1, 2], [1, 2, 3])
False
>>> np.array_equal([1, 2], [1, 4])
False
```

numpy.array_equiv (al, a2)

Returns True if input arrays are shape consistent and all elements equal.
Shape consistent means they are either the same shape, or one input array can be broadcasted to create the same shape as the other one.

## Parameters

a1, a2 : array_like
Input arrays.

## Returns

out : bool
True if equivalent, False otherwise.

## Examples

```
>>> np.array_equiv([1, 2], [1, 2])
True
>>> np.array_equiv([1, 2], [1, 3])
False
```

Showing the shape equivalence:

```
>>> np.array_equiv([1, 2], [[1, 2], [1, 2]])
True
>>> np.array_equiv([1, 2], [[1, 2, 1, 2], [1, 2, 1, 2]])
False
>>> np.array_equiv([1, 2], [[1, 2], [1, 3]])
False
```

| greater(x1) | Return the truth value of (x1>x2) element-wise. |
| :--- | :--- |
| greater_equal(x1) | Return the truth value of (x1>=x2) element-wise. |
| less(x1) | Return the truth value of (x1<x2) element-wise. |
| less_equal(x1) | Return the truth value of (x1=<x2) element-wise. |
| equal(x1) | Return $(x 1==x 2)$ element-wise. |
| not_equal(x1) | Return $(x 1!=x 2)$ element-wise. |

numpy.greater ( $x 1, x 2[$, out $]$ )
Return the truth value of ( $\mathrm{x} 1>\mathrm{x} 2$ ) element-wise.

## Parameters

$\mathbf{x 1}, \mathbf{x} 2$ : array_like

Input arrays. If $\times 1$. shape $!=x 2$. shape, they must be broadcastable to a common shape (which may be the shape of one or the other).

## Returns

 out : bool or ndarray of boolArray of bools, or a single bool if $x 1$ and $x 2$ are scalars.

## See Also:

```
greater_equal, less, less_equal, equal, not_equal
```


## Examples

```
>>> np.greater([4,2],[2,2])
array([ True, False], dtype=bool)
```

If the inputs are ndarrays, then np.greater is equivalent to ' $>$ '.

```
>>> a = np.array([4,2])
>>> b = np.array([2,2])
>>> a > b
array([ True, False], dtype=bool)
```

numpy.greater_equal ( $x 1, x 2[$, out $]$ )
Return the truth value of ( $\mathrm{x} 1>=\mathrm{x} 2$ ) element-wise.

## Parameters

$\mathbf{x 1}, \mathbf{x 2}$ : array_like
Input arrays. If x 1 . shape $!=\mathrm{x} 2$. shape, they must be broadcastable to a common shape (which may be the shape of one or the other).

## Returns

out : bool or ndarray of bool
Array of bools, or a single bool if $x 1$ and $x 2$ are scalars.

## See Also:

```
greater, less, less_equal, equal, not_equal
```


## Examples

```
>>> np.greater_equal([4, 2, 1], [2, 2, 2])
array([ True, True, False], dtype=bool)
```

numpy. less ( $x 1, x 2[$, out $]$ )
Return the truth value of ( $\mathrm{x} 1<\mathrm{x} 2$ ) element-wise.

## Parameters

$\mathbf{x 1}, \mathbf{x} 2$ : array_like
Input arrays. If $\times 1$. shape $!=x 2$. shape, they must be broadcastable to a common shape (which may be the shape of one or the other).

## Returns

out : bool or ndarray of bool
Array of bools, or a single bool if $x 1$ and $x 2$ are scalars.

## See Also:

greater, less_equal, greater_equal, equal, not_equal

## Examples

```
>>> np.less([1, 2], [2, 2])
array([ True, False], dtype=bool)
numpy.less_equal ( }x\mathrm{ l, x2[,out])
```

Return the truth value of ( $\mathrm{x} 1=<\mathrm{x} 2$ ) element-wise.

## Parameters <br> $\mathbf{x 1}, \mathbf{x} 2$ : array_like

Input arrays. If $\times 1$. shape $!=x 2$. shape, they must be broadcastable to a common shape (which may be the shape of one or the other).

## Returns

out : bool or ndarray of bool
Array of bools, or a single bool if $x 1$ and $x 2$ are scalars.

## See Also:

```
greater, less,greater_equal, equal, not_equal
```


## Examples

```
>>> np.less_equal([4, 2, 1], [2, 2, 2])
array([False, True, True], dtype=bool)
```

numpy.equal ( $x 1, x_{2}[$, out $]$ )

Return ( $\mathrm{x} 1==\mathrm{x} 2$ ) element-wise.

## Parameters

$\mathbf{x 1}, \mathbf{x 2}$ : array_like
Input arrays of the same shape.

## Returns

out : \{ndarray, bool\}
Output array of bools, or a single bool if x 1 and x 2 are scalars.

## See Also:

```
    not_equal,greater_equal, less_equal, greater, less
```


## Examples

```
>>> np.equal([0, 1, 3], np.arange(3))
array([ True, True, False], dtype=bool)
```

What is compared are values, not types. So an int (1) and an array of length one can evaluate as True:

```
>>> np.equal(1, np.ones(1))
array([ True], dtype=bool)
```

numpy.not_equal ( $x 1, x 2[$, out $]$ )
Return (x1 !=x2) element-wise.

## Parameters

$\mathbf{x 1}, \mathbf{x} 2$ : array_like
Input arrays.
out : ndarray, optional

A placeholder the same shape as $x l$ to store the result. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

not_equal : ndarray bool, scalar bool
For each element in $x 1, x 2$, return True if $x 1$ is not equal to $x 2$ and False otherwise.

## See Also:

```
equal,greater,greater_equal,less,less_equal
```


## Examples

```
>>> np.not_equal([1.,2.], [1., 3.])
array([False, True], dtype=bool)
>>> np.not_equal([1, 2], [[1, 3],[1, 4]])
array([[False, True],
    [False, True]], dtype=bool)
```


### 3.11 Binary operations

### 3.11.1 Elementwise bit operations

| bitwise_and(x1) | Compute the bit-wise AND of two arrays element-wise. |
| :--- | :--- |
| bitwise_or(x1) | Compute the bit-wise OR of two arrays element-wise. |
| bitwise_xor(x1) | Compute the bit-wise XOR of two arrays element-wise. |
| invert() | Compute bit-wise inversion, or bit-wise NOT, element-wise. |
| left_shift(x1) | Shift the bits of an integer to the left. |
| right_shift(x1) | Shift the bits of an integer to the right. |

numpy.bitwise_and ( $x 1, x 2[$, out $]$ )

Compute the bit-wise AND of two arrays element-wise.
Computes the bit-wise AND of the underlying binary representation of the integers in the input arrays. This ufunc implements the C/Python operator \& .

## Parameters

$\mathbf{x 1}, \mathbf{x 2}$ : array_like
Only integer types are handled (including booleans).

## Returns

out : array_like
Result.

## See Also:

logical_and, bitwise_or, bitwise_xor
binary_repr
Return the binary representation of the input number as a string.

## Examples

The number 13 is represented by 00001101 . Likewise, 17 is represented by 00010001 . The bit-wise AND of 13 and 17 is therefore 000000001 , or 1 :

```
>>> np.bitwise_and(13, 17)
1
>>> np.bitwise_and(14, 13)
12
>>> np.binary_repr(12)
'1100'
>>> np.bitwise_and([14,3], 13)
array([12, 1])
>>> np.bitwise_and([11,7], [4,25])
array([0, 1])
>>> np.bitwise_and(np.array([2,5,255]), np.array([3,14,16]))
array([ 2, 4, 16])
>>> np.bitwise_and([True, True], [False, True])
array([False, True], dtype=bool)
numpy.bitwise_or (xl, x2[,out])
Compute the bit-wise OR of two arrays element-wise.
```

Computes the bit-wise OR of the underlying binary representation of the integers in the input arrays. This ufunc implements the C/Python operator $\mid$.

## Parameters

$\mathbf{x 1}, \mathbf{x} 2$ : array_like
Only integer types are handled (including booleans).
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output. See doc.ufuncs.

## Returns

out : array_like
Result.

## See Also:

```
logical_or, bitwise_and, bitwise_xor
```

binary_repr
Return the binary representation of the input number as a string.

## Examples

The number 13 has the binaray representation 00001101 . Likewise, 16 is represented by 00010000 . The bit-wise OR of 13 and 16 is then 000111011 , or 29:

```
>>> np.bitwise_or(13, 16)
29
>>> np.binary_repr(29)
'11101'
>>> np.bitwise_or(32, 2)
34
>>> np.bitwise_or([33, 4], 1)
array([33, 5])
>>> np.bitwise_or([33, 4], [1, 2])
array([33, 6])
```

```
>>> np.bitwise_or(np.array([2, 5, 255]), np.array([4, 4, 4]))
array([ 6, 5, 255])
>>> np.array([2, 5, 255]) | np.array([4, 4, 4])
array([ 6, 5, 255])
>>> np.bitwise_or(np.array([2, 5, 255, 2147483647L], dtype=np.int32),
... np.array([4, 4, 4, 2147483647L], dtype=np.int32))
array([ 6, 5, 255, 2147483647])
>>> np.bitwise_or([True, True], [False, True])
array([ True, True], dtype=bool)
```

numpy.bitwise_xor $(x 1, x 2[$, out $])$
Compute the bit-wise XOR of two arrays element-wise.
Computes the bit-wise XOR of the underlying binary representation of the integers in the input arrays. This ufunc implements the C/Python operator ${ }^{\wedge}$.

## Parameters

 $\mathbf{x 1}, \mathbf{x} 2$ : array_likeOnly integer types are handled (including booleans).

## Returns

out : array_like
Result.

## See Also:

logical_xor, bitwise_and, bitwise_or
binary_repr
Return the binary representation of the input number as a string.

## Examples

The number 13 is represented by 00001101 . Likewise, 17 is represented by 00010001 . The bit-wise XOR of 13 and 17 is therefore 00011100 , or 28 :

```
>>> np.bitwise_xor(13, 17)
28
>>> np.binary_repr(28)
'11100'
>>> np.bitwise_xor(31, 5)
26
>>> np.bitwise_xor([31,3], 5)
array([26, 6])
>>> np.bitwise_xor([31,3], [5,6])
array([26, 5])
>>> np.bitwise_xor([True, True], [False, True])
array([ True, False], dtype=bool)
numpy.invert (x[,out])
```

Compute bit-wise inversion, or bit-wise NOT, element-wise.
Computes the bit-wise NOT of the underlying binary representation of the integers in the input arrays. This ufunc implements the C/Python operator ~.

For signed integer inputs, the two's complement is returned. In a two's-complement system negative numbers are represented by the two's complement of the absolute value. This is the most common method of representing
signed integers on computers [R31]. A N-bit two's-complement system can represent every integer in the range $-2^{N-1}$ to $+2^{N-1}-1$.

## Parameters

$\mathbf{x 1}$ : array_like
Only integer types are handled (including booleans).

## Returns

out : array_like
Result.

## See Also:

```
bitwise_and, bitwise_or, bitwise_xor, logical_not
```

binary_repr
Return the binary representation of the input number as a string.

## Notes

bitwise_not is an alias for invert:

```
>>> np.bitwise_not is np.invert
True
```


## References

[R31]

## Examples

We've seen that 13 is represented by 00001101 . The invert or bit-wise NOT of 13 is then:

```
>>> np.invert(np.array([13], dtype=uint8))
array([242], dtype=uint8)
>>> np.binary_repr(x, width=8)
'00001101'
>>> np.binary_repr(242, width=8)
'11110010'
```

The result depends on the bit-width:

```
>>> np.invert(np.array([13], dtype=uint16))
array([65522], dtype=uint16)
>>> np.binary_repr(x, width=16)
'0000000000001101'
>>> np.binary_repr(65522, width=16)
'1111111111110010'
```

When using signed integer types the result is the two's complement of the result for the unsigned type:

```
>>> np.invert(np.array([13], dtype=int8))
array([-14], dtype=int8)
>>> np.binary_repr(-14, width=8)
'11110010'
```

Booleans are accepted as well:

```
>>> np.invert(array([True, False]))
array([False, True], dtype=bool)
```

numpy.left_shift ( $x 1, x 2[$, out $]$ )
Shift the bits of an integer to the left.
Bits are shifted to the left by appending $x 20$ s at the right of $x 1$. Since the internal representation of numbers is in binary format, this operation is equivalent to multiplying $x l$ by $2 * * x 2$.

## Parameters

$\mathbf{x 1}$ : array_like of integer type
Input values.
$\mathbf{x 2}$ : array_like of integer type
Number of zeros to append to $x l$. Has to be non-negative.

## Returns

out : array of integer type
Return $x 1$ with bits shifted $x 2$ times to the left.

## See Also:

right_shift
Shift the bits of an integer to the right.
binary_repr
Return the binary representation of the input number as a string.

## Examples

```
        >>> np.binary_repr(5)
```

        '101'
        >>> np.left_shift(5, 2)
        20
        >>> np.binary_repr(20)
        '10100'
        >>> np.left_shift(5, [1,2,3])
        array([10, 20, 40])
    numpy.right_shift ( $x 1, x 2[$, out $]$ )

Shift the bits of an integer to the right.
Bits are shifted to the right by removing $x 2$ bits at the right of $x 1$. Since the internal representation of numbers is in binary format, this operation is equivalent to dividing $x l$ by $2 * * x 2$.

## Parameters

$\mathbf{x 1}$ : array_like, int
Input values.
$\mathbf{x 2}$ : array_like, int
Number of bits to remove at the right of $x l$.

## Returns

out : ndarray, int
Return $x 1$ with bits shifted $x 2$ times to the right.

## See Also:

left_shift
Shift the bits of an integer to the left.
binary_repr
Return the binary representation of the input number as a string.

## Examples

```
>>> np.binary_repr(10)
'1010'
>>> np.right_shift(10, 1)
5
>>> np.binary_repr(5)
'101'
>>> np.right_shift(10, [1,2,3])
array([5, 2, 1])
```


### 3.11.2 Bit packing

## packbits(myarray[, axis]) Packs the elements of a binary-valued array into bits in a uint8 array.

unpack.bits(myarray[, axis]) Unpacks elements of a uint8 array into a binary-valued output array.
numpy.packbits (myarray, axis=None)
Packs the elements of a binary-valued array into bits in a uint8 array.
The result is padded to full bytes by inserting zero bits at the end.

## Parameters

myarray : array_like
An integer type array whose elements should be packed to bits.
axis : int, optional
The dimension over which bit-packing is done. None implies packing the flattened array.

## Returns

packed : ndarray
Array of type uint8 whose elements represent bits corresponding to the logical ( 0 or nonzero) value of the input elements. The shape of packed has the same number of dimensions as the input (unless axis is None, in which case the output is 1-D).

## See Also:

```
    unpackbits
```

Unpacks elements of a uint8 array into a binary-valued output array.

## Examples

```
>>> a = np.array([[[1,0,1],
... [0,1,0]],
... [[1,1,0],
... [0,0,1]]])
>>> b = np.packbits(a, axis=-1)
>>> b
array([[[160],[64]],[[192],[32]]], dtype=uint8)
```

Note that in binary $160=10100000,64=01000000,192=11000000$, and $32=00100000$.

## numpy.unpackbits (myarray, axis=None)

Unpacks elements of a uint8 array into a binary-valued output array.
Each element of myarray represents a bit-field that should be unpacked into a binary-valued output array. The shape of the output array is either 1-D (if axis is None) or the same shape as the input array with unpacking done along the axis specified.

## Parameters

myarray : ndarray, uint8 type
Input array.
axis : int, optional
Unpacks along this axis.

## Returns

unpacked : ndarray, uint8 type
The elements are binary-valued (0 or 1 ).

## See Also:

## packbits

Packs the elements of a binary-valued array into bits in a uint8 array.

## Examples

```
>>> a = np.array([[2], [7], [23]], dtype=np.uint8)
>>> a
array([[ 2],
    [ 7],
    [23]], dtype=uint8)
>>> b = np.unpackbits(a, axis=1)
>>> b
array([[0, 0, 0, 0, 0, 0, 1, 0],
    [0, 0, 0, 0, 0, 1, 1, 1],
    [0, 0, 0, 1, 0, 1, 1, 1]], dtype=uint8)
```


### 3.11.3 Output formatting

binary_repr(num[, width]) Return the binary representation of the input number as a string.
numpy.binary_repr (num, width=None)
Return the binary representation of the input number as a string.
For negative numbers, if width is not given, a minus sign is added to the front. If width is given, the two's complement of the number is returned, with respect to that width.
In a two's-complement system negative numbers are represented by the two's complement of the absolute value. This is the most common method of representing signed integers on computers [R16]. A N-bit two'scomplement system can represent every integer in the range $-2^{N-1}$ to $+2^{N-1}-1$.

## Parameters

num : int
Only an integer decimal number can be used.
width : int, optional

The length of the returned string if num is positive, the length of the two's complement if num is negative.

## Returns

## bin : str

Binary representation of num or two's complement of num.

## See Also:

base_repr
Return a string representation of a number in the given base system.

## Notes

binary_repr is equivalent to using base_repr with base 2 , but about 25 x faster.

## References

[R16]

## Examples

```
>>> np.binary_repr(3)
'11'
>>> np.binary_repr(-3)
'-11'
>>> np.binary_repr(3, width=4)
'0011'
```

The two's complement is returned when the input number is negative and width is specified:
>>> np.binary_repr(-3, width=4)
'1101'

### 3.12 Statistics

### 3.12.1 Extremal values

amin(a[, axis, out]) Return the minimum of an array or minimum along an axis.
$\operatorname{amax}(\mathrm{a}[$, axis, out $]) \quad$ Return the maximum of an array or maximum along an axis.
nanmax(a[, axis]) Return the maximum of an array or maximum along an axis ignoring any NaNs.
nanmin(a[, axis]) Return the minimum of an array or minimum along an axis ignoring any NaNs.
$\mathrm{ptp}(\mathrm{a}[$, axis, out $]) \quad$ Range of values (maximum - minimum) along an axis.
numpy $\cdot \operatorname{amin}(a$, axis=None, out=None)
Return the minimum of an array or minimum along an axis.

## Parameters

a: array_like
Input data.
axis : int, optional
Axis along which to operate. By default a flattened input is used.
out : ndarray, optional

Alternative output array in which to place the result. Must be of the same shape and buffer length as the expected output. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

amin : ndarray
A new array or a scalar array with the result.

## See Also:

nanmin
nan values are ignored instead of being propagated

## fmin

same behavior as the C 99 fmin function
argmin
Return the indices of the minimum values.

```
amax, nanmax, fmax
```


## Notes

NaN values are propagated, that is if at least one item is nan, the corresponding min value will be nan as well. To ignore NaN values (matlab behavior), please use nanmin.

## Examples

```
>>> a = np.arange(4).reshape((2,2))
>>> a
array([[0, 1],
    [2, 3]])
>>> np.amin(a) # Minimum of the flattened array
0
>>> np.amin(a, axis=0) # Minima along the first axis
array([0, 1])
>>> np.amin(a, axis=1) # Minima along the second axis
array([0, 2])
>>> b = np.arange(5, dtype=np.float)
>>> b[2] = np.NaN
>>> np.amin(b)
nan
>>> np.nanmin(b)
0.0
```

numpy $\cdot \operatorname{amax}(a$, axis=None, out=None)

Return the maximum of an array or maximum along an axis.

## Parameters

a: array_like
Input data.
axis : int, optional
Axis along which to operate. By default flattened input is used.
out : ndarray, optional

Alternate output array in which to place the result. Must be of the same shape and buffer length as the expected output. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

amax : ndarray or scalar
Maximum of $a$. If axis is None, the result is a scalar value. If axis is given, the result is an array of dimension a. ndim -1 .

## See Also:

## nanmax

NaN values are ignored instead of being propagated.

## fmax

same behavior as the C99 fmax function.
argmax
indices of the maximum values.

## Notes

NaN values are propagated, that is if at least one item is NaN , the corresponding max value will be NaN as well. To ignore NaN values (MATLAB behavior), please use nanmax.

## Examples

```
>>> a = np.arange(4).reshape((2,2))
>>> a
array([[0, 1],
    [2, 3]])
    >>> np.amax(a)
    3
>>> np.amax(a, axis=0)
array([2, 3])
>>> np.amax(a, axis=1)
array([1, 3])
>>> b = np.arange(5, dtype=np.float)
>>> b[2] = np.NaN
>>> np.amax(b)
nan
>>> np.nanmax(b)
4.0
```

numpy . nanmax (a, axis=None)

Return the maximum of an array or maximum along an axis ignoring any NaNs .

## Parameters

a : array_like
Array containing numbers whose maximum is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the maximum is computed. The default is to compute the maximum of the flattened array.

## Returns

nanmax : ndarray

An array with the same shape as $a$, with the specified axis removed. If $a$ is a $0-\mathrm{d}$ array, or if axis is None, a ndarray scalar is returned. The the same dtype as $a$ is returned.

## See Also:

numpy. amax
Maximum across array including any Not a Numbers.
numpy. nanmin
Minimum across array ignoring any Not a Numbers.
isnan
Shows which elements are Not a Number (NaN).
isfinite
Shows which elements are not: Not a Number, positive and negative infinity

## Notes

Numpy uses the IEEE Standard for Binary Floating-Point for Arithmetic (IEEE 754). This means that Not a Number is not equivalent to infinity. Positive infinity is treated as a very large number and negative infinity is treated as a very small (i.e. negative) number.

If the input has a integer type the function is equivalent to np.max.

## Examples

```
>>> a = np.array([[1, 2], [3, np.nan]])
>>> np.nanmax(a)
3.0
>>> np.nanmax(a, axis=0)
array([ 3., 2.])
>>> np.nanmax(a, axis=1)
array([ 2., 3.])
```

When positive infinity and negative infinity are present:

```
>>> np.nanmax([1, 2, np.nan, np.NINF])
2.0
>>> np.nanmax([1, 2, np.nan, np.inf])
inf
```

numpy.nanmin (a, axis=None)
Return the minimum of an array or minimum along an axis ignoring any NaNs.

## Parameters

a : array_like
Array containing numbers whose minimum is desired.
axis : int, optional
Axis along which the minimum is computed.The default is to compute the minimum of the flattened array.

## Returns

nanmin : ndarray
A new array or a scalar array with the result.

## See Also:

numpy.amin
Minimum across array including any Not a Numbers.

```
numpy.nanmax
```

Maximum across array ignoring any Not a Numbers.

```
isnan
```

Shows which elements are Not a Number (NaN).

```
isfinite
```

Shows which elements are not: Not a Number, positive and negative infinity

## Notes

Numpy uses the IEEE Standard for Binary Floating-Point for Arithmetic (IEEE 754). This means that Not a Number is not equivalent to infinity. Positive infinity is treated as a very large number and negative infinity is treated as a very small (i.e. negative) number.

If the input has a integer type the function is equivalent to np.min.

## Examples

```
>>> a = np.array([[1, 2], [3, np.nan]])
>>> np.nanmin(a)
1.0
>>> np.nanmin(a, axis=0)
array([ 1., 2.])
>>> np.nanmin(a, axis=1)
array([ 1., 3.])
```

When positive infinity and negative infinity are present:

```
>>> np.nanmin([1, 2, np.nan, np.inf])
1.0
>>> np.nanmin([1, 2, np.nan, np.NINF])
-inf
```

numpy $\cdot$ ptp $(a$, axis=None, out=None $)$

Range of values (maximum - minimum) along an axis.
The name of the function comes from the acronym for 'peak to peak'.

## Parameters

a: array_like
Input values.
axis : int, optional
Axis along which to find the peaks. By default, flatten the array.
out : array_like
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output, but the type of the output values will be cast if necessary.

## Returns

ptp : ndarray
A new array holding the result, unless out was specified, in which case a reference to out is returned.

## Examples

```
>>> x = np.arange(4).reshape((2,2))
>>> x
array([[0, 1],
    [2, 3]])
>>> np.ptp(x, axis=0)
array([2, 2])
>>> np.ptp(x, axis=1)
array([1, 1])
```


### 3.12.2 Averages and variances

```
average(a[, axis, weights, returned]) Compute the weighted average along the specified axis.
mean(a[, axis, dtype, out]) Compute the arithmetic mean along the specified axis.
median(a[, axis, out, overwrite_input]) Compute the median along the specified axis.
std(a[, axis, dtype, out, ddof]) Compute the standard deviation along the specified axis.
var(a[, axis, dtype, out, ddof]) Compute the variance along the specified axis.
```

numpy . average ( $a$, axis=None, weights=None, returned $=$ False )
Compute the weighted average along the specified axis.

## Parameters

a : array_like
Array containing data to be averaged. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which to average $a$. If None, averaging is done over the flattened array.
weights : array_like, optional
An array of weights associated with the values in $a$. Each value in $a$ contributes to the average according to its associated weight. The weights array can either be 1-D (in which case its length must be the size of $a$ along the given axis) or of the same shape as $a$. If weights=None, then all data in $a$ are assumed to have a weight equal to one.
returned : bool, optional
Default is False. If True, the tuple (average, sum_of_weights) is returned, otherwise only the average is returned. If weights=None, sum_of_weights is equivalent to the number of elements over which the average is taken.

## Returns

average, [sum_of_weights] : \{array_type, double\}
Return the average along the specified axis. When returned is True, return a tuple with the average as the first element and the sum of the weights as the second element. The return type is Float if $a$ is of integer type, otherwise it is of the same type as $a$. sum_of_weights is of the same type as average.

## Raises

## ZeroDivisionError :

When all weights along axis are zero. See numpy.ma. average for a version robust to this type of error.

## TypeError :

When the length of 1D weights is not the same as the shape of $a$ along axis.

## See Also:

## mean

ma.average
average for masked arrays

## Examples

```
>>> data = range (1,5)
>>> data
[1, 2, 3, 4]
>>> np.average(data)
2.5
>>> np.average(range(1,11), weights=range(10,0,-1))
4.0
>>> data = np.arange(6).reshape( (3,2))
>>> data
array([[0, 1],
    [2, 3],
    [4, 5]])
>>> np.average(data, axis=1, weights=[1./4, 3./4])
array([ 0.75, 2.75, 4.75])
>>> np.average(data, weights=[1./4, 3./4])
Traceback (most recent call last):
TypeError: Axis must be specified when shapes of a and weights differ.
```

numpy . mean ( $a$, axis=None, dtype $=$ None, out $=$ None)
Compute the arithmetic mean along the specified axis.
Returns the average of the array elements. The average is taken over the flattened array by default, otherwise over the specified axis. float64 intermediate and return values are used for integer inputs.

## Parameters

a : array_like
Array containing numbers whose mean is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the means are computed. The default is to compute the mean of the flattened array.
dtype : data-type, optional
Type to use in computing the mean. For integer inputs, the default is float64; for floating point inputs, it is the same as the input dtype.
out : ndarray, optional
Alternate output array in which to place the result. The default is None; if provided, it must have the same shape as the expected output, but the type will be cast if necessary. See doc.ufuncs for details.

## Returns

m : ndarray, see dtype parameter above

If out=None, returns a new array containing the mean values, otherwise a reference to the output array is returned.

## See Also:

## average

Weighted average

## Notes

The arithmetic mean is the sum of the elements along the axis divided by the number of elements.
Note that for floating-point input, the mean is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-precision accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.mean(a)
2.5
>>> np.mean(a, axis=0)
array([ 2., 3.])
>>> np.mean(a, axis=1)
array([ 1.5, 3.5])
```

In single precision, mean can be inaccurate:

```
>>> a = np.zeros((2, 512*512), dtype=np.float32)
>>> a[0, :] = 1.0
>>> a[1, :] = 0.1
>>> np.mean(a)
0.546875
```

Computing the mean in float64 is more accurate:

```
>>> np.mean(a, dtype=np.float64)
0.55000000074505806
```

numpy.median (a, axis=None, out=None, overwrite_input=False)

Compute the median along the specified axis.
Returns the median of the array elements.

## Parameters

a : array_like
Input array or object that can be converted to an array.
axis: \{None, int \}, optional
Axis along which the medians are computed. The default (axis=None) is to compute the median along a flattened version of the array.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output, but the type (of the output) will be cast if necessary.
overwrite_input : \{False, True \}, optional
If True, then allow use of memory of input array (a) for calculations. The input array will be modified by the call to median. This will save memory when you do not need to
preserve the contents of the input array. Treat the input as undefined, but it will probably be fully or partially sorted. Default is False. Note that, if overwrite_input is True and the input is not already an ndarray, an error will be raised.

## Returns

median : ndarray
A new array holding the result (unless out is specified, in which case that array is returned instead). If the input contains integers, or floats of smaller precision than 64, then the output data-type is float64. Otherwise, the output data-type is the same as that of the input.

## See Also:

mean, percentile

## Notes

Given a vector V of length N , the median of V is the middle value of a sorted copy of V , V _sorted - i.e., V _sorted $[(\mathrm{N}-1) / 2]$, when N is odd. When N is even, it is the average of the two middle values of V_sorted.

## Examples

```
>>> a = np.array([[10, 7, 4], [3, 2, 1]])
>>> a
array([[10, 7, 4],
    [ 3, 2, 1]])
>>> np.median(a)
3.5
>>> np.median(a, axis=0)
array([ 6.5, 4.5, 2.5])
>>> np.median(a, axis=1)
array([ 7., 2.])
>>> m = np.median(a, axis=0)
>>> out = np.zeros_like(m)
>>> np.median(a, axis=0, out=m)
array([ 6.5, 4.5, 2.5])
>>> m
array([ 6.5, 4.5, 2.5])
>>> b = a.copy()
>>> np.median(b, axis=1, overwrite_input=True)
array([ 7., 2.])
>>> assert not np.all(a==b)
>>> b = a.copy()
>>> np.median(b, axis=None, overwrite_input=True)
3.5
>>> assert not np.all(a==b)
```

numpy. std ( $a$, axis=None, dtype=None, out=None, ddof=0)

Compute the standard deviation along the specified axis.
Returns the standard deviation, a measure of the spread of a distribution, of the array elements. The standard deviation is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Calculate the standard deviation of these values.
axis : int, optional

Axis along which the standard deviation is computed. The default is to compute the standard deviation of the flattened array.
dtype : dtype, optional
Type to use in computing the standard deviation. For arrays of integer type the default is float64, for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type (of the calculated values) will be cast if necessary.
ddof : int, optional
Means Delta Degrees of Freedom. The divisor used in calculations is N - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

standard_deviation : ndarray, see dtype parameter above.
If out is None, return a new array containing the standard deviation, otherwise return a reference to the output array.

## See Also:

```
var,mean
```

numpy.doc.ufuncs

Section "Output arguments"

## Notes

The standard deviation is the square root of the average of the squared deviations from the mean, i.e., std $=$ sqrt (mean (abs (x - x.mean()) **2)).

The average squared deviation is normally calculated as $x . \operatorname{sum}() / N$, where $N=$ len(x). If, however, $d d o f$ is specified, the divisor N - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of the infinite population. ddof $=0$ provides a maximum likelihood estimate of the variance for normally distributed variables. The standard deviation computed in this function is the square root of the estimated variance, so even with $d d o f=1$, it will not be an unbiased estimate of the standard deviation per se.
Note that, for complex numbers, std takes the absolute value before squaring, so that the result is always real and nonnegative.

For floating-point input, the std is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higheraccuracy accumulator using the dtype keyword can alleviate this issue.

```
Examples
>>> a = np.array([[1, 2], [3, 4]])
>>> np.std(a)
1.1180339887498949
>>> np.std(a, axis=0)
array([ 1., 1.])
>>> np.std(a, axis=1)
array([ 0.5, 0.5])
```

In single precision, $\operatorname{std}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.std(a)
0.45172946707416706
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.std(a, dtype=np.float64)
0.449999999925552653
```

numpy . var ( $a$, axis=None, dtype $=$ None, out $=$ None, , ddof=0)

Compute the variance along the specified axis.
Returns the variance of the array elements, a measure of the spread of a distribution. The variance is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Array containing numbers whose variance is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the variance is computed. The default is to compute the variance of the flattened array.
dtype : data-type, optional
Type to use in computing the variance. For arrays of integer type the default is float32; for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output, but the type is cast if necessary.
ddof : int, optional
"Delta Degrees of Freedom": the divisor used in the calculation is N - ddof, where N represents the number of elements. By default ddof is zero.

## Returns

variance : ndarray, see dtype parameter above
If out=None, returns a new array containing the variance; otherwise, a reference to the output array is returned.

## See Also:

std
Standard deviation
mean
Average
numpy.doc.ufuncs
Section "Output arguments"

## Notes

The variance is the average of the squared deviations from the mean, i.e., var $=$ mean (abs ( $x-$ x.mean()) **2).

The mean is normally calculated as $x . \operatorname{sum}() / N$, where $N=\operatorname{len}(x)$. If, however, $d$ dof is specified, the divisor $N$ - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of a hypothetical infinite population. ddof $=0$ provides a maximum likelihood estimate of the variance for normally distributed variables.

Note that for complex numbers, the absolute value is taken before squaring, so that the result is always real and nonnegative.

For floating-point input, the variance is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1,2],[3,4]])
>>> np.var(a)
1.25
>>> np.var(a,0)
array([ 1., 1.])
>>> np.var(a,1)
array([ 0.25, 0.25])
```

In single precision, $\operatorname{var}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.var(a)
0.20405951142311096
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.var(a, dtype=np.float64)
0.20249999932997387
>>> ((1-0.55)**2 + (0.1-0.55)**2)/2
0.20250000000000001
```


### 3.12.3 Correlating

| $\operatorname{corrcoef}(\mathrm{x}[, \mathrm{y}$, rowvar, bias, ddof $])$ | Return correlation coefficients. |
| :--- | :--- |
| $\operatorname{correlate}(\mathrm{a}, \mathrm{v}[$, mode, old_behavior $])$ | Cross-correlation of two 1-dimensional sequences. |
| $\operatorname{cov}(\mathrm{m}[, \mathrm{y}$, rowvar, bias, ddof $])$ | Estimate a covariance matrix, given data. |

numpy. corrcoef ( $x, y=$ None, rowvar $=1$, bias $=0$, ddof=None $)$
Return correlation coefficients.
Please refer to the documentation for $\operatorname{cov}$ for more detail. The relationship between the correlation coefficient matrix, $P$, and the covariance matrix, $C$, is

$$
P_{i j}=\frac{C_{i j}}{\sqrt{C_{i i} * C_{j j}}}
$$

The values of $P$ are between -1 and 1 , inclusive.

## Parameters

$\mathbf{x}$ : array_like
A 1-D or 2-D array containing multiple variables and observations. Each row of $m$ represents a variable, and each column a single observation of all those variables. Also see rowvar below.
$\mathbf{y}$ : array_like, optional
An additional set of variables and observations. $y$ has the same shape as $m$.
rowvar : int, optional
If rowvar is non-zero (default), then each row represents a variable, with observations in the columns. Otherwise, the relationship is transposed: each column represents a variable, while the rows contain observations.
bias : int, optional
Default normalization is by ( $\mathrm{N}-1$ ), where N is the number of observations (unbiased estimate). If bias is 1 , then normalization is by N. These values can be overridden by using the keyword ddof in numpy versions $>=1.5$.
ddof : \{None, int \}, optional
New in version 1.5. If not None normalization is by ( $N$ - ddof), where $N$ is the number of observations; this overrides the value implied by bias. The default value is None.

## Returns

out : ndarray
The correlation coefficient matrix of the variables.

## See Also:

cov
Covariance matrix
numpy.correlate ( $a, v$, mode='valid', old_behavior=False)
Cross-correlation of two 1-dimensional sequences.
This function computes the correlation as generally defined in signal processing texts:

```
z[k] = sum_n a[n] * conj(v[n+k])
```

with a and v sequences being zero-padded where necessary and conj being the conjugate.

## Parameters

$\mathbf{a , ~ v}$ : array_like
Input sequences.
mode : \{ 'valid', 'same', 'full'\}, optional
Refer to the convolve docstring. Note that the default is valid, unlike convolve, which uses full.
old_behavior : bool
If True, uses the old behavior from Numeric, (correlate $(a, v)==$ correlate $(v, a)$, and the conjugate is not taken for complex arrays). If False, uses the conventional signal processing definition (see note).

## See Also:

```
convolve
```

Discrete, linear convolution of two one-dimensional sequences.

## Examples

```
>>> np.correlate([1, 2, 3], [0, 1, 0.5])
array([ 3.5])
>>> np.correlate([1, 2, 3], [0, 1, 0.5], "same")
array([ 2. , 3.5, 3. ])
>>> np.correlate([1, 2, 3], [0, 1, 0.5], "full")
array([ 0.5, 2. , 3.5, 3. , 0. ])
```

numpy. cov $(m, y=$ None, rowvar $=1$, bias $=0, d d o f=$ None $)$
Estimate a covariance matrix, given data.
Covariance indicates the level to which two variables vary together. If we examine N -dimensional samples, $X=\left[x_{1}, x_{2}, \ldots x_{N}\right]^{T}$, then the covariance matrix element $C_{i j}$ is the covariance of $x_{i}$ and $x_{j}$. The element $C_{i i}$ is the variance of $x_{i}$.

## Parameters

m : array_like
A 1-D or 2-D array containing multiple variables and observations. Each row of $m$ represents a variable, and each column a single observation of all those variables. Also see rowvar below.
$\mathbf{y}$ : array_like, optional
An additional set of variables and observations. $y$ has the same form as that of $m$.
rowvar : int, optional
If rowvar is non-zero (default), then each row represents a variable, with observations in the columns. Otherwise, the relationship is transposed: each column represents a variable, while the rows contain observations.
bias : int, optional
Default normalization is by ( $\mathrm{N}-1$ ), where N is the number of observations given (unbiased estimate). If bias is 1 , then normalization is by $N$. These values can be overridden by using the keyword ddof in numpy versions $>=1.5$.
ddof : int, optional
New in version 1.5. If not None normalization is by ( N - ddof), where N is the number of observations; this overrides the value implied by bias. The default value is None.

## Returns

out : ndarray
The covariance matrix of the variables.

## See Also:

corrcoef
Normalized covariance matrix

## Examples

Consider two variables, $x_{0}$ and $x_{1}$, which correlate perfectly, but in opposite directions:

```
>>> x = np.array([[0, 2], [1, 1], [2, 0]]).T
>>> X
array([[0, 1, 2],
    [2, 1, 0]])
```

Note how $x_{0}$ increases while $x_{1}$ decreases. The covariance matrix shows this clearly:

```
>>> np.cov(x)
array([[ 1., -1.],
    [-1., 1.]])
```

Note that element $C_{0,1}$, which shows the correlation between $x_{0}$ and $x_{1}$, is negative.
Further, note how $x$ and $y$ are combined:

```
>>> x = [-2.1, -1, 4.3]
>>> y = [3, 1.1, 0.12]
>>> X = np.vstack((x,y))
>>> print np.cov(X)
[[ 11.71 -4.286 ]
    [ -4.286 2.14413333]]
>>> print np.cov(x, y)
[[ 11.71 -4.286 ]
    [ -4.286 2.14413333]]
>>> print np.cov(x)
11.71
```


### 3.12.4 Histograms

```
histogram(a[, bins, range, normed, weights, Compute the histogram of a set of data.
...])
histogram2d(x, y[, bins, range, normed, Compute the bi-dimensional histogram of two data samples.
weights])
histogramdd(sample[, bins, range, normed, Compute the multidimensional histogram of some data.
...])
bincount(x[, weights, minlength]) Count number of occurrences of each value in array of
non-negative ints.
digitize(x, bins)
```

Compute the histogram of a set of data.

Compute the bi-dimensional histogram of two data samples.
Compute the multidimensional histogram of some data.
Count number of occurrences of each value in array of non-negative ints.
Return the indices of the bins to which each value in input array belongs.

```
numpy. histogram ( \(a\), bins \(=10\), range \(=\) None, normed \(=\) False, weights \(=\) None, density=None )
Compute the histogram of a set of data.
```


## Parameters

```
a : array_like
Input data. The histogram is computed over the flattened array.
bins : int or sequence of scalars, optional
If bins is an int, it defines the number of equal-width bins in the given range (10, by default). If bins is a sequence, it defines the bin edges, including the rightmost edge, allowing for non-uniform bin widths.
range : (float, float), optional
```

The lower and upper range of the bins. If not provided, range is simply (a.min(), a.max ()). Values outside the range are ignored.
normed : bool, optional
This keyword is deprecated in Numpy 1.6 due to confusing/buggy behavior. It will be removed in Numpy 2.0. Use the density keyword instead. If False, the result will contain the number of samples in each bin. If True, the result is the value of the probability density function at the bin, normalized such that the integral over the range is 1 . Note that this latter behavior is known to be buggy with unequal bin widths; use density instead.
weights : array_like, optional
An array of weights, of the same shape as $a$. Each value in $a$ only contributes its associated weight towards the bin count (instead of 1). If normed is True, the weights are normalized, so that the integral of the density over the range remains 1
density : bool, optional
If False, the result will contain the number of samples in each bin. If True, the result is the value of the probability density function at the bin, normalized such that the integral over the range is 1 . Note that the sum of the histogram values will not be equal to 1 unless bins of unity width are chosen; it is not a probability mass function. Overrides the normed keyword if given.

## Returns

hist : array
The values of the histogram. See normed and weights for a description of the possible semantics.
bin_edges : array of dtype float
Return the bin edges (length (hist) +1 ).

## See Also:

```
histogramdd, bincount, searchsorted, digitize
```


## Notes

All but the last (righthand-most) bin is half-open. In other words, if bins is:

```
[1, 2, 3, 4]
```

then the first bin is [1, 2) (including 1, but excluding 2) and the second [2, 3). The last bin, however, is [3, 4], which includes 4.

## Examples

```
>>> np.histogram([1, 2, 1], bins=[0, 1, 2, 3])
(array([0, 2, 1]), array([0, 1, 2, 3]))
>>> np.histogram(np.arange(4), bins=np.arange(5), density=True)
(array([ 0.25, 0.25, 0.25, 0.25]), array([0, 1, 2, 3, 4]))
>>> np.histogram([[1, 2, 1], [1, 0, 1]], bins=[0,1,2,3])
(array([1, 4, 1]), array([0, 1, 2, 3]))
>>> a = np.arange(5)
>>> hist, bin_edges = np.histogram(a, density=True)
>>> hist
array([ 0.5, 0., 0.5, 0. , 0., 0.5,0., 0.5,0. 0.0.5])
```

```
>>> hist.sum()
```

2.4999999999999996
>>> np.sum(hist*np.diff(bin_edges))
1.0
numpy.histogram2d ( $x, y$, bins $=10$, range $=$ None, normed $=$ False, weights $=$ None $)$

Compute the bi-dimensional histogram of two data samples.

## Parameters

$\mathbf{x}$ : array_like, shape(N,)
A sequence of values to be histogrammed along the first dimension.
$\mathbf{y}$ : array_like, shape(M,)
A sequence of values to be histogrammed along the second dimension.
bins : int or [int, int] or array_like or [array, array], optional
The bin specification:

- If int, the number of bins for the two dimensions ( $n x=n y=b i n s$ ).
- If [int, int], the number of bins in each dimension ( $n x, n y=b i n s$ ).
- If array_like, the bin edges for the two dimensions (x_edges=y_edges=bins).
- If [array, array], the bin edges in each dimension (x_edges, y_edges = bins).
range : array_like, shape $(2,2)$, optional
The leftmost and rightmost edges of the bins along each dimension (if not specified explicitly in the bins parameters): [ [xmin, xmax], [ymin, ymax]]. All values outside of this range will be considered outliers and not tallied in the histogram.
normed : bool, optional
If False, returns the number of samples in each bin. If True, returns the bin density, i.e. the bin count divided by the bin area.
weights : array_like, shape( N ,), optional
An array of values w_i weighing each sample (x_i, y_i). Weights are normalized to 1 if normed is True. If normed is False, the values of the returned histogram are equal to the sum of the weights belonging to the samples falling into each bin.


## Returns

H : ndarray, shape(nx, ny)
The bi-dimensional histogram of samples $x$ and $y$. Values in $x$ are histogrammed along the first dimension and values in $y$ are histogrammed along the second dimension.
xedges : ndarray, shape( $n x$, )
The bin edges along the first dimension.
yedges : ndarray, shape(ny,)
The bin edges along the second dimension.

## See Also:

histogram
1D histogram

## histogramdd

Multidimensional histogram

## Notes

When normed is True, then the returned histogram is the sample density, defined such that:

$$
\sum_{i=0}^{n x-1} \sum_{j=0}^{n y-1} H_{i, j} \Delta x_{i} \Delta y_{j}=1
$$

where $H$ is the histogram array and $\Delta x_{i} \Delta y_{i}$ the area of bin $\{i, j\}$.
Please note that the histogram does not follow the Cartesian convention where $x$ values are on the abcissa and $y$ values on the ordinate axis. Rather, $x$ is histogrammed along the first dimension of the array (vertical), and $y$ along the second dimension of the array (horizontal). This ensures compatibility with histogramdd.

## Examples

```
>>> x, y = np.random.randn (2, 100)
>>> H, xedges, yedges = np.histogram2d(x, y, bins=(5, 8))
>>> H.shape, xedges.shape, yedges.shape
((5, 8), (6,), (9,))
```

We can now use the Matplotlib to visualize this 2-dimensional histogram:

```
>>> extent = [yedges[0], yedges[-1], xedges[-1], xedges[0]]
```

>>> import matplotlib.pyplot as plt
>>> plt.imshow(H, extent=extent, interpolation='nearest')
<matplotlib.image.AxesImage object at ...>
>>> plt.colorbar()
<matplotlib.colorbar.Colorbar instance at ...>
>>> plt.show()

numpy.histogramdd (sample, bins $=10$, range $=$ None, normed $=$ False, weights $=$ None )
Compute the multidimensional histogram of some data.

## Parameters

sample : array_like

The data to be histogrammed. It must be an (N,D) array or data that can be converted to such. The rows of the resulting array are the coordinates of points in a D dimensional polytope.
bins : sequence or int, optional
The bin specification:

- A sequence of arrays describing the bin edges along each dimension.
- The number of bins for each dimension (nx, ny, ... =bins)
- The number of bins for all dimensions ( $n x=n y=\ldots=b i n s$ ).
range : sequence, optional
A sequence of lower and upper bin edges to be used if the edges are not given explicitely in bins. Defaults to the minimum and maximum values along each dimension.
normed : bool, optional
If False, returns the number of samples in each bin. If True, returns the bin density, ie, the bin count divided by the bin hypervolume.
weights : array_like ( N ,), optional
An array of values $w_{-} i$ weighing each sample ( $x_{-} i, y_{-} i, z_{-} i, \ldots$ ). Weights are normalized to 1 if normed is True. If normed is False, the values of the returned histogram are equal to the sum of the weights belonging to the samples falling into each bin.


## Returns

H: ndarray
The multidimensional histogram of sample $x$. See normed and weights for the different possible semantics.
edges : list
A list of D arrays describing the bin edges for each dimension.

## See Also:

histogram
1-D histogram
histogram2d
2-D histogram

## Examples

```
>>> r = np.random.randn (100,3)
>>> H, edges = np.histogramdd(r, bins = (5, 8, 4))
>>> H.shape, edges[0].size, edges[1].size, edges[2].size
((5, 8, 4), 6, 9, 5)
```

numpy.bincount ( $x$, weights=None, minlength=None)
Count number of occurrences of each value in array of non-negative ints.
The number of bins (of size 1) is one larger than the largest value in $x$. If minlength is specified, there will be at least this number of bins in the output array (though it will be longer if necessary, depending on the contents of $x$ ). Each bin gives the number of occurrences of its index value in $x$. If weights is specified the input array is weighted by it, i.e. if a value $n$ is found at position $i$, out [ $n$ ] $+=$ weight [i] instead of out [ $n$ ] $+=1$.

## Parameters

$\mathbf{x}$ : array_like, 1 dimension, nonnegative ints
Input array.
weights : array_like, optional
Weights, array of the same shape as $x$.
minlength : int, optional
New in version 1.6.0. A minimum number of bins for the output array.

## Returns

out : ndarray of ints
The result of binning the input array. The length of out is equal to $n p$.amax $(x)+1$.

## Raises

ValueError :
If the input is not 1-dimensional, or contains elements with negative values, or if minlength is non-positive.

## TypeError :

If the type of the input is float or complex.

## See Also:

histogram, digitize, unique
Examples

```
>>> np.bincount(np.arange(5))
array([1, 1, 1, 1, 1])
>>> np.bincount(np.array([0, 1, 1, 3, 2, 1, 7]))
array([1, 3, 1, 1, 0, 0, 0, 1])
>>> x = np.array([0, 1, 1, 3, 2, 1, 7, 23])
>>> np.bincount(x).size == np.amax(x) +1
True
```

The input array needs to be of integer dtype, otherwise a TypeError is raised:

```
>>> np.bincount(np.arange(5, dtype=np.float))
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
TypeError: array cannot be safely cast to required type
```

A possible use of bincount is to perform sums over variable-size chunks of an array, using the weights keyword.

```
>>> w = np.array([0.3, 0.5, 0.2, 0.7, 1., -0.6]) # weights
>>> x = np.array([0, 1, 1, 2, 2, 2])
>>> np.bincount(x, weights=w)
array([ 0.3, 0.7, 1.1])
```

numpy.digitize ( $x$, bins)
Return the indices of the bins to which each value in input array belongs.
Each index i returned is such that bins[i-1] $<=x<$ bins[i] if bins is monotonically increasing, or bins[i-1] > $x>=$ bins[i] if bins is monotonically decreasing. If values in $x$ are beyond the bounds of bins, 0 or len (bins) is returned as appropriate.

## Parameters

$\mathbf{x}$ : array_like
Input array to be binned. It has to be 1-dimensional.
bins: array_like
Array of bins. It has to be 1-dimensional and monotonic.

## Returns

out : ndarray of ints
Output array of indices, of same shape as $x$.

## Raises

ValueError :
If the input is not 1-dimensional, or if bins is not monotonic.

## TypeError :

If the type of the input is complex.

## See Also:

bincount, histogram, unique

## Notes

If values in $x$ are such that they fall outside the bin range, attempting to index bins with the indices that digitize returns will result in an IndexError.

## Examples

```
>>> x = np.array([0.2, 6.4, 3.0, 1.6])
>>> bins = np.array([0.0, 1.0, 2.5, 4.0, 10.0])
>>> inds = np.digitize(x, bins)
>>> inds
array([1, 4, 3, 2])
>>> for n in range(x.size):
... print bins[inds[n]-1], "<=", x[n], "<", bins[inds[n]]
...
0.0<= 0.2< 1.0
4.0<= 6.4< 10.0
2.5<= 3.0<4.0
1.0<= 1.6< 2.5
```


### 3.13 Mathematical functions

### 3.13.1 Trigonometric functions

| $\sin ()$ | Trigonometric sine, element-wise. |
| :--- | :--- |
| $\cos ()$ | Cosine elementwise. |
| tan() | Compute tangent element-wise. |
| $\arcsin ()$ | Inverse sine, element-wise. |
| $\arccos ()$ | Trigonometric inverse cosine, element-wise. |
| arctan() | Trigonometric inverse tangent, element-wise. |
| hypot(x1) | Given the "legs" of a right triangle, return its hypotenuse. |
| arctan2(x1) | Element-wise arc tangent of x1/x2 choosing the quadrant correctly. |
| degrees() | Convert angles from radians to degrees. |
| radians() | Convert angles from degrees to radians. |
| unwrap(p[, discont, axis]) | Unwrap by changing deltas between values to 2*pi complement. |
| deg2rad() | Convert angles from degrees to radians. |
| rad2deg() | Convert angles from radians to degrees. |

numpy. $\boldsymbol{\operatorname { s i n }}(x[$, out $])$
Trigonometric sine, element-wise.

## Parameters

$\mathbf{x}$ : array_like
Angle, in radians ( $2 \pi$ rad equals 360 degrees).

## Returns

$$
\mathbf{y} \text { : array_like }
$$

The sine of each element of $x$.

## See Also:

```
    arcsin, sinh,cos
```


## Notes

The sine is one of the fundamental functions of trigonometry (the mathematical study of triangles). Consider a circle of radius 1 centered on the origin. A ray comes in from the $+x$ axis, makes an angle at the origin (measured counter-clockwise from that axis), and departs from the origin. The $y$ coordinate of the outgoing ray's intersection with the unit circle is the sine of that angle. It ranges from -1 for $x=3 \pi / 2$ to +1 for $\pi / 2$. The function has zeroes where the angle is a multiple of $\pi$. Sines of angles between $\pi$ and $2 \pi$ are negative. The numerous properties of the sine and related functions are included in any standard trigonometry text.

## Examples

Print sine of one angle:

```
>>> np.sin(np.pi/2.)
1.0
```

Print sines of an array of angles given in degrees:

```
>>> np.sin(np.array((0., 30., 45., 60., 90.)) * np.pi / 180.)
array([ 0. , 0.5 , 0.70710678, 0.8660254, 1. ])
```

Plot the sine function:

```
>>> import matplotlib.pylab as plt
>>> x = np.linspace(-np.pi, np.pi, 201)
>>> plt.plot(x, np.sin(x))
>>> plt.xlabel('Angle [rad]')
>>> plt.ylabel('sin(x)')
>>> plt.axis('tight')
>>> plt.show()
```


numpy. $\boldsymbol{\operatorname { c o s }}(x[$,out $])$
Cosine elementwise.

## Parameters

$\mathbf{x}$ : array_like
Input array in radians.
out : ndarray, optional
Output array of same shape as $x$.

## Returns

$\mathbf{y}$ : ndarray
The corresponding cosine values.

## Raises

ValueError: invalid return array shape :
if out is provided and out.shape $!=x$ shape (See Examples)

## Notes

If out is provided, the function writes the result into it, and returns a reference to out. (See Examples)

## References

M. Abramowitz and I. A. Stegun, Handbook of Mathematical Functions. New York, NY: Dover, 1972.

## Examples

```
>>> np.cos(np.array([0, np.pi/2, np.pi]))
array([ 1.00000000e+00, 6.12303177e-17, -1.00000000e+00])
>>>
>>> # Example of providing the optional output parameter
>>> out2 = np.cos([0.1], out1)
>>> out2 is out1
True
>>>
>>> # Example of ValueError due to provision of shape mis-matched 'out'
>>> np.cos(np.zeros((3,3)),np.zeros((2,2)))
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
ValueError: invalid return array shape
```

numpy.tan $(x[$,out $])$
Compute tangent element-wise.

Equivalent to np.sin(x)/np.cos(x) element-wise.

## Parameters

x : array_like
Input array.
out : ndarray, optional
Output array of same shape as $x$.

## Returns

$\mathbf{y}$ : ndarray
The corresponding tangent values.

## Raises

ValueError: invalid return array shape :
if out is provided and out.shape $!=x$.shape (See Examples)

## Notes

If out is provided, the function writes the result into it, and returns a reference to out. (See Examples)

## References

M. Abramowitz and I. A. Stegun, Handbook of Mathematical Functions. New York, NY: Dover, 1972.

## Examples

```
>>> from math import pi
>>> np.tan(np.array([-pi,pi/2,pi]))
array([ 1.22460635e-16, 1.63317787e+16, -1.22460635e-16])
>>>
>>> # Example of providing the optional output parameter illustrating
>>> # that what is returned is a reference to said parameter
>>> out2 = np.cos([0.1], out1)
>>> out2 is out1
True
>>>
>>> # Example of ValueError due to provision of shape mis-matched 'out'
>>> np.cos(np.zeros((3,3)),np.zeros((2,2)))
Traceback (most recent call last):
```

```
    File "<stdin>", line 1, in <module>
```

ValueError: invalid return array shape
numpy.arcsin ( $x[$, out $]$ )
Inverse sine, element-wise.

## Parameters

x: array_like
$y$-coordinate on the unit circle.
out : ndarray, optional
Array of the same shape as $x$, in which to store the results. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

angle : ndarray
The inverse sine of each element in $x$, in radians and in the closed interval $[-\mathrm{p} i / 2$, pi/2]. If $x$ is a scalar, a scalar is returned, otherwise an array.

## See Also:

sin, cos, arccos, tan, arctan, arctan2, emath. arcsin

## Notes

$\arcsin$ is a multivalued function: for each $x$ there are infinitely many numbers $z$ such that $\sin (z)=x$. The convention is to return the angle $z$ whose real part lies in [-pi/2, pi/2].

For real-valued input data types, arcsin always returns real output. For each value that cannot be expressed as a real number or infinity, it yields nan and sets the invalid floating point error flag.

For complex-valued input, arcsin is a complex analytic function that has, by convention, the branch cuts [-inf, $-1]$ and [1, inf] and is continuous from above on the former and from below on the latter.

The inverse sine is also known as $a \sin$ or $\sin ^{\wedge}\{-1\}$.

## References

Abramowitz, M. and Stegun, I. A., Handbook of Mathematical Functions, 10th printing, New York: Dover, 1964, pp. 79ff. http://www.math.sfu.ca/~cbm/aands/

## Examples

```
>>> np.arcsin(1) # pi/2
1.5707963267948966
>>> np.arcsin(-1) # -pi/2
-1.5707963267948966
>>> np.arcsin(0)
0.0
numpy. arccos ( \(x[\), out \(]\) )
```

Trigonometric inverse cosine, element-wise.
The inverse of $\cos$ so that, if $\mathrm{y}=\cos (\mathrm{x})$, then $\mathrm{x}=\arccos (\mathrm{y})$.

## Parameters

$\mathbf{x}$ : array_like
$x$-coordinate on the unit circle. For real arguments, the domain is $[-1,1]$.
out : ndarray, optional

Array of the same shape as $a$, to store results in. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

angle : ndarray
The angle of the ray intersecting the unit circle at the given $x$-coordinate in radians [ 0 , pi]. If $x$ is a scalar then a scalar is returned, otherwise an array of the same shape as $x$ is returned.

## See Also:

cos, arctan, arcsin, emath. arccos

## Notes

$\arccos$ is a multivalued function: for each $x$ there are infinitely many numbers $z$ such that $\cos (z)=x$. The convention is to return the angle $z$ whose real part lies in [0, pi].

For real-valued input data types, arccos always returns real output. For each value that cannot be expressed as a real number or infinity, it yields nan and sets the invalid floating point error flag.

For complex-valued input, arccos is a complex analytic function that has branch cuts [-inf, -1] and [1, inf] and is continuous from above on the former and from below on the latter.

The inverse $\cos$ is also known as $a \cos$ or $\cos ^{\wedge}-1$.

## References

M. Abramowitz and I.A. Stegun, "Handbook of Mathematical Functions", 10th printing, 1964, pp. 79. http://www.math.sfu.ca/~cbm/aands/

## Examples

We expect the arccos of 1 to be 0 , and of -1 to be pi:

```
>>> np.arccos([1, -1])
array([ 0. , 3.14159265])
```

Plot arccos:

```
>>> import matplotlib.pyplot as plt
>>> x = np.linspace(-1, 1, num=100)
>>> plt.plot(x, np.arccos(x))
>>> plt.axis('tight')
>>> plt.show()
```


numpy $\cdot \arctan (x[$, out $])$
Trigonometric inverse tangent, element-wise.
The inverse of tan, so that if $y=\tan (x)$ then $x=\arctan (y)$.

## Parameters

$\mathbf{x}$ : array_like
Input values. arctan is applied to each element of $x$.

## Returns

out : ndarray
Out has the same shape as $x$. Its real part is in [-pi/2, pi/2] (arctan(+/-inf) returns $+/-\mathrm{pi} / 2$ ). It is a scalar if $x$ is a scalar.

## See Also:

## arctan2

The "four quadrant" arctan of the angle formed by $(x, y)$ and the positive $x$-axis.
angle
Argument of complex values.

## Notes

$\arctan$ is a multi-valued function: for each $x$ there are infinitely many numbers $z$ such that $\tan (z)=x$. The convention is to return the angle $z$ whose real part lies in [- $\mathrm{pi} / 2, \mathrm{pi} / 2]$.
For real-valued input data types, arctan always returns real output. For each value that cannot be expressed as a real number or infinity, it yields nan and sets the invalid floating point error flag.

For complex-valued input, arctan is a complex analytic function that has $[1 j, i n f j]$ and $[-1 j$, $-i n f j]$ as branch cuts, and is continuous from the left on the former and from the right on the latter.
The inverse tangent is also known as atan or $\tan ^{\wedge}\{-1\}$.

## References

Abramowitz, M. and Stegun, I. A., Handbook of Mathematical Functions, 10th printing, New York: Dover, 1964, pp. 79. http://www.math.sfu.ca/~cbm/aands/

## Examples

We expect the arctan of 0 to be 0 , and of 1 to be pi/4:

```
>>> np.arctan([0, 1])
array([ 0. , 0.78539816])
>>> np.pi/4
0.78539816339744828
```

Plot arctan:
>>> import matplotlib.pyplot as plt
>>> x = np.linspace (-10, 10)
>>> plt.plot(x, np.arctan(x))
>>> plt.axis('tight')
>>> plt.show()

numpy . hypot ( $x 1, x_{2}[$, out $]$ )
Given the "legs" of a right triangle, return its hypotenuse.
Equivalent to sqrt $(x 1 * * 2+x 2 * * 2)$, element-wise. If $x l$ or $x 2$ is scalar_like (i.e., unambiguously castable to a scalar type), it is broadcast for use with each element of the other argument. (See Examples)

## Parameters

$\mathbf{x 1}, \mathbf{x 2}$ : array_like
Leg of the triangle(s).
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output. See doc.ufuncs.

## Returns

$\mathbf{z}$ : ndarray
The hypotenuse of the triangle(s).

## Examples

```
>>> np.hypot(3*np.ones((3, 3)), 4*np.ones((3, 3)))
array([[ 5., 5., 5.],
    [ 5., 5., 5.],
    [ 5., 5., 5.]])
```

Example showing broadcast of scalar_like argument:

```
>>> np.hypot(3*np.ones((3, 3)), [4])
array([[ 5., 5., 5.],
    [ 5., 5., 5.],
    [ 5., 5., 5.]])
```

numpy.arctan2 (x1, x2[,out])
Element-wise arc tangent of $\mathrm{x} 1 / \mathrm{x} 2$ choosing the quadrant correctly.
The quadrant (i.e., branch) is chosen so that $\arctan 2(x 1, x 2)$ is the signed angle in radians between the ray ending at the origin and passing through the point $(1,0)$, and the ray ending at the origin and passing through the point $(x 2, x 1)$. (Note the role reversal: the " $y$-coordinate" is the first function parameter, the " $x$-coordinate" is the second.) By IEEE convention, this function is defined for $x 2=+/-0$ and for either or both of $x 1$ and $x 2=$ +/-inf (see Notes for specific values).

This function is not defined for complex-valued arguments; for the so-called argument of complex values, use angle.

## Parameters

$\mathbf{x 1}$ : array_like, real-valued
$y$-coordinates.
$\mathbf{x 2}$ : array_like, real-valued
$x$-coordinates. $x 2$ must be broadcastable to match the shape of $x 1$ or vice versa.

## Returns

angle : ndarray
Array of angles in radians, in the range [-pi, pi].

## See Also:

arctan, tan, angle

## Notes

$\arctan 2$ is identical to the atan2 function of the underlying C library. The following special values are defined in the C standard: [R6]

| $\boldsymbol{x} \boldsymbol{1}$ | $\boldsymbol{x} 2$ | $\boldsymbol{a r c t a n} 2(\boldsymbol{x} \mathbf{1}, \boldsymbol{x} 2)$ |
| :--- | :--- | :--- |
| $+/-0$ | +0 | $+/-0$ |
| $+/-0$ | -0 | $+/-\mathrm{pi}$ |
| $>0$ | $+/-\mathrm{inf}$ | $+0 /+\mathrm{pi}$ |
| $<0$ | $+/-\mathrm{inf}$ | $-0 /-\mathrm{pi}$ |
| $+/-\mathrm{inf}$ | +inf | $+/-(\mathrm{pi} / 4)$ |
| +/-inf | - -inf | $+/-\left(3^{*} \mathrm{pi} / 4\right)$ |

Note that +0 and -0 are distinct floating point numbers, as are +inf and -inf.

## References

[R6]

## Examples

Consider four points in different quadrants:

```
>>> x = np.array([-1, +1, +1, -1])
>>> y = np.array([-1, -1, +1, +1])
>>> np.arctan2(y, x) * 180 / np.pi
array([-135., -45., 45., 135.])
```

Note the order of the parameters. arctan 2 is defined also when $x 2=0$ and at several other special points, obtaining values in the range $[-\mathrm{pi}, \mathrm{pi}]$ :

```
>>> np.arctan2([1., -1.], [0., 0.])
array([ 1.57079633, -1.57079633])
>>> np.arctan2([0., 0., np.inf], [+0., -0., np.inf])
array([ 0. , 3.14159265, 0.78539816])
numpy.degrees (x[,out])
```

Convert angles from radians to degrees.

## Parameters

## $\mathbf{x}$ : array_like

Input array in radians.
out : ndarray, optional
Output array of same shape as x .

## Returns

$\mathbf{y}$ : ndarray of floats
The corresponding degree values; if out was supplied this is a reference to it.

## See Also:

rad2deg
equivalent function

## Examples

Convert a radian array to degrees

```
>>> rad = np.arange(12.)*np.pi/6
>>> np.degrees(rad)
array([ 0., 30., 60., 90., 120., 150., 180., 210., 240.,
    270., 300., 330.])
>>> out = np.zeros((rad.shape))
>>> r = degrees(rad, out)
>>> np.all(r == out)
True
```

numpy . radians ( $x$ [, out $]$ )
Convert angles from degrees to radians.

## Parameters

$\mathbf{x}$ : array_like
Input array in degrees.
out : ndarray, optional

Output array of same shape as $x$.

## Returns

 y : ndarrayThe corresponding radian values.

## See Also:

deg2rad
equivalent function
Examples
Convert a degree array to radians

```
>>> deg = np.arange(12.) * 30.
>>> np.radians(deg)
array([ 0. , 0.52359878, 1.04719755, 1.57079633, 2.0943951,
    2.61799388, 3.14159265, 3.66519143, 4.1887902 , 4.71238898,
    5.23598776, 5.75958653])
>>> out = np.zeros((deg.shape))
>>> ret = np.radians(deg, out)
>>> ret is out
True
```

numpy . unwrap ( $p$, discont $=3.1415926535897931$, axis=-1)
Unwrap by changing deltas between values to $2 *$ pi complement.
Unwrap radian phase $p$ by changing absolute jumps greater than discont to their $2^{*}$ pi complement along the given axis.

## Parameters

p: array_like
Input array.
discont : float, optional
Maximum discontinuity between values, default is pi.
axis : int, optional
Axis along which unwrap will operate, default is the last axis.

## Returns

out : ndarray
Output array.

## See Also:

rad2deg, deg2rad

## Notes

If the discontinuity in $p$ is smaller than pi , but larger than discont, no unwrapping is done because taking the $2 *$ pi complement would only make the discontinuity larger.

## Examples

```
>>> phase = np.linspace(0, np.pi, num=5)
>>> phase[3:] += np.pi
>>> phase
array([ 0. , 0.78539816, 1.57079633, 5.49778714, 6.28318531])
>>> np.unwrap (phase)
array([ 0. , 0.78539816, 1.57079633, -0.78539816, 0. ])
```

numpy. deg $2 \operatorname{rad}(x[$, out $])$
Convert angles from degrees to radians.

## Parameters

 $\mathbf{x}$ : array_likeAngles in degrees.

## Returns

$$
\mathbf{y} \text { : ndarray }
$$

The corresponding angle in radians.

## See Also:

rad2deg
Convert angles from radians to degrees.
unwrap
Remove large jumps in angle by wrapping.

## Notes

New in version 1.3.0. deg $2 \operatorname{rad}(x)$ is $x$ * $p i / 180$.

## Examples

```
>>> np.deg2rad(180)
3.1415926535897931
```

numpy . rad2deg ( $x[$, out $]$ )
Convert angles from radians to degrees.

## Parameters

$\mathbf{x}$ : array_like
Angle in radians.
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output. See doc.ufuncs.

## Returns

y : ndarray
The corresponding angle in degrees.

## See Also:

deg2rad
Convert angles from degrees to radians.
unwrap
Remove large jumps in angle by wrapping.

## Notes

New in version 1.3.0. $\operatorname{rad} 2 \operatorname{deg}(x)$ is $180 * x / p i$.
Examples

```
>>> np.rad2deg(np.pi/2)
90.0
```


### 3.13.2 Hyperbolic functions

| $\sinh ()$ | Hyperbolic sine, element-wise. |
| :--- | :--- |
| $\cosh ()$ | Hyperbolic cosine, element-wise. |
| $\tanh ()$ | Compute hyperbolic tangent element-wise. |
| $\operatorname{arcsinh}()$ | Inverse hyperbolic sine elementwise. |
| $\operatorname{arccosh}()$ | Inverse hyperbolic cosine, elementwise. |
| $\operatorname{arctanh}()$ | Inverse hyperbolic tangent elementwise. |
| numpy. $\sinh (x[$, out $])$ |  |
| Hyperbolic sine, element-wise. |  |

Equivalent to $1 / 2 \star(n p \cdot \exp (x)-n p \cdot \exp (-x))$ or $-1 j * n p \cdot \sin (1 j * x)$.

## Parameters

$\mathbf{x}$ : array_like
Input array.
out : ndarray, optional
Output array of same shape as $x$.

## Returns

y : ndarray
The corresponding hyperbolic sine values.

## Raises

## ValueError: invalid return array shape :

if out is provided and out.shape $!=$ x.shape (See Examples)

## Notes

If out is provided, the function writes the result into it, and returns a reference to out. (See Examples)

## References

M. Abramowitz and I. A. Stegun, Handbook of Mathematical Functions. New York, NY: Dover, 1972, pg. 83.

## Examples

```
>>> np.sinh(0)
0.0
>>> np.sinh(np.pi*1j/2)
1j
>>> np.sinh(np.pi*1j) # (exact value is 0)
1.2246063538223773e-016j
>>> # Discrepancy due to vagaries of floating point arithmetic.
```

```
>>> # Example of providing the optional output parameter
>>> out2 = np.sinh([0.1], out1)
>>> out2 is out1
True
>>> # Example of ValueError due to provision of shape mis-matched 'out'
>>> np.sinh(np.zeros((3,3)),np.zeros((2,2)))
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
ValueError: invalid return array shape
```

numpy. $\cosh (x[, o u t])$
Hyperbolic cosine, element-wise.
Equivalent to $1 / 2$ * ( $n$. $\exp (x)+n p \cdot \exp (-x))$ and $n p \cdot \cos (1 j * x)$.

## Parameters

$\mathbf{x}$ : array_like
Input array.

## Returns

out : ndarray
Output array of same shape as $x$.

## Examples

```
>>> np.cosh(0)
1.0
```

The hyperbolic cosine describes the shape of a hanging cable:

```
>>> import matplotlib.pyplot as plt
>>> x = np.linspace(-4, 4, 1000)
>>> plt.plot(x, np.cosh(x))
>>> plt.show()
```


numpy. $\tanh (x[$, out $])$
Compute hyperbolic tangent element-wise.

Equivalent to $n p \cdot \sinh (x) / n p \cdot \cosh (x)$ or $-1 j * n p \cdot \tan (1 j * x)$.

## Parameters

$\mathbf{x}$ : array_like
Input array.
out : ndarray, optional
Output array of same shape as $x$.

## Returns

$\mathbf{y}$ : ndarray
The corresponding hyperbolic tangent values.

## Raises

## ValueError: invalid return array shape :

if out is provided and out.shape != x.shape (See Examples)

## Notes

If out is provided, the function writes the result into it, and returns a reference to out. (See Examples)

## References

[R222], [R223]

## Examples

```
>>> np.tanh((0, np.pi*1j, np.pi*1j/2))
array([ 0. +0.00000000e+00j, 0. -1.22460635e-16j, 0. +1.63317787e+16j])
>>> # Example of providing the optional output parameter illustrating
>>> # that what is returned is a reference to said parameter
>>> out2 = np.tanh([0.1], out1)
>>> out2 is out1
True
>>> # Example of ValueError due to provision of shape mis-matched 'out'
>>> np.tanh(np.zeros((3,3)),np.zeros((2, 2)))
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
ValueError: invalid return array shape
```

numpy.arcsinh (x[, out $]$ )
Inverse hyperbolic sine elementwise.

## Parameters

$\mathbf{x}$ : array_like
Input array.
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output. See doc.ufuncs.

## Returns

out : ndarray
Array of of the same shape as $x$.

## Notes

$\operatorname{arcsinh}$ is a multivalued function: for each $x$ there are infinitely many numbers $z$ such that $\sinh (z)=x$. The convention is to return the $z$ whose imaginary part lies in [-pi/2, pi/2].

For real-valued input data types, arcsinh always returns real output. For each value that cannot be expressed as a real number or infinity, it returns nan and sets the invalid floating point error flag.

For complex-valued input, $\arccos$ is a complex analytical function that has branch cuts [ $1 j$, infj] and [-1j, -infj] and is continuous from the right on the former and from the left on the latter.

The inverse hyperbolic sine is also known as $a \sinh$ or sinh ${ }^{\wedge}-1$.

## References

[R4], [R5]

## Examples

```
>>> np.arcsinh(np.array([np.e, 10.0]))
```

array ([ 1.72538256, 2.99822295])
numpy . arccosh (x[, out $]$ )
Inverse hyperbolic cosine, elementwise.

## Parameters

$\mathbf{x}$ : array_like
Input array.
out : ndarray, optional
Array of the same shape as $x$, to store results in. See doc.ufuncs (Section "Output arguments") for details.

## Returns

$\mathbf{y}$ : ndarray
Array of the same shape as $x$.

## See Also:

cosh, arcsinh, sinh, arctanh, tanh

## Notes

$\operatorname{arccosh}$ is a multivalued function: for each $x$ there are infinitely many numbers $z$ such that $\cosh (z)=x$. The convention is to return the $z$ whose imaginary part lies in [-pi, pi] and the real part in [0, inf].

For real-valued input data types, arccosh always returns real output. For each value that cannot be expressed as a real number or infinity, it yields nan and sets the invalid floating point error flag.

For complex-valued input, $\operatorname{arccosh}$ is a complex analytical function that has a branch cut [-inf, 1] and is continuous from above on it.

## References

[R2], [R3]

## Examples

```
>>> np.arccosh([np.e, 10.0])
array([ 1.65745445, 2.99322285])
```

```
>>> np.arccosh(1)
0.0
numpy.arctanh (x[,out])
```

    Inverse hyperbolic tangent elementwise.
    
## Parameters

$\mathbf{x}$ : array_like
Input array.

## Returns

out : ndarray
Array of the same shape as $x$.

## See Also:

```
emath.arctanh
```


## Notes

$\operatorname{arctanh}$ is a multivalued function: for each $x$ there are infinitely many numbers $z$ such that $\tanh (z)=x$. The convention is to return the $z$ whose imaginary part lies in [-pi/2, pi/2].

For real-valued input data types, arctanh always returns real output. For each value that cannot be expressed as a real number or infinity, it yields nan and sets the invalid floating point error flag.
For complex-valued input, arctanh is a complex analytical function that has branch cuts [-1, -inf] and [1, inf] and is continuous from above on the former and from below on the latter.

The inverse hyperbolic tangent is also known as atanh or tanh^-1.

## References

[R7], [R8]

## Examples

```
>>> np.arctanh([0, -0.5])
array([ 0. , -0.54930614])
```


### 3.13.3 Rounding

```
around(a[, decimals, out]) Evenly round to the given number of decimals.
round_(a[, decimals, out]) Round an array to the given number of decimals.
rint() Round elements of the array to the nearest integer.
fix(x[,y]) Round to nearest integer towards zero.
floor() Return the floor of the input, element-wise.
ceil() Return the ceiling of the input, element-wise.
trunc() Return the truncated value of the input, element-wise.
numpy . around (a, decimals=0, out=None)
Evenly round to the given number of decimals.
```


## Parameters

```
a : array_like
Input data.
decimals : int, optional
```

Number of decimal places to round to (default: 0). If decimals is negative, it specifies the number of positions to the left of the decimal point.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output, but the type of the output values will be cast if necessary. See doc.ufuncs (Section "Output arguments") for details.

## Returns

```
rounded_array : ndarray
```

An array of the same type as $a$, containing the rounded values. Unless out was specified, a new array is created. A reference to the result is returned.

The real and imaginary parts of complex numbers are rounded separately. The result of rounding a float is a float.

## See Also:

ndarray. round
equivalent method
ceil, fix, floor, rint, trunc

## Notes

For values exactly halfway between rounded decimal values, Numpy rounds to the nearest even value. Thus 1.5 and 2.5 round to $2.0,-0.5$ and 0.5 round to 0.0 , etc. Results may also be surprising due to the inexact representation of decimal fractions in the IEEE floating point standard [R9] and errors introduced when scaling by powers of ten.

## References

[R9], [R10]

## Examples

```
>>> np.around([0.37, 1.64])
array([ 0., 2.])
>>> np.around([0.37, 1.64], decimals=1)
array([ 0.4, 1.6])
>>> np.around([.5, 1.5, 2.5, 3.5, 4.5]) # rounds to nearest even value
array([ 0., 2., 2., 4., 4.])
>>> np.around([1,2,3,11], decimals=1) # ndarray of ints is returned
array([ 1, 2, 3, 11])
>>> np.around([1,2,3,11], decimals=-1)
array([ 0, 0, 0, 10])
```

numpy.round_( $a$, decimals $=0$, out=None)
Round an array to the given number of decimals.
Refer to around for full documentation.

## See Also:

around
equivalent function
numpy.rint ( $x[$, out $]$ )
Round elements of the array to the nearest integer.

## Parameters

x: array_like Input array.

## Returns

out : \{ndarray, scalar \}
Output array is same shape and type as $x$.

## See Also:

ceil,floor, trunc

## Examples

```
>>> a = np.array([-1.7, -1.5, -0.2, 0.2, 1.5, 1.7, 2.0])
>>> np.rint(a)
array([-2., -2., -0., 0., 2., 2., 2.])
```

numpy. $\mathbf{f i x}(x, y=$ None $)$
Round to nearest integer towards zero.
Round an array of floats element-wise to nearest integer towards zero. The rounded values are returned as floats.

## Parameters

$\mathbf{x}$ : array_like
An array of floats to be rounded
$\mathbf{y}$ : ndarray, optional
Output array

## Returns

out : ndarray of floats
The array of rounded numbers

## See Also:

trunc, floor, ceil
around
Round to given number of decimals

## Examples

```
>>> np.fix(3.14)
3.0
>>> np.fix(3)
3.0
>>> np.fix([2.1, 2.9, -2.1, -2.9])
array([ 2., 2., -2., -2.])
```

numpy.floor ( $x[$, out $]$ )
Return the floor of the input, element-wise.
The floor of the scalar $x$ is the largest integer $i$, such that $i<=x$. It is often denoted as $\lfloor x\rfloor$.

## Parameters

$\mathbf{x}$ : array_like
Input data.

## Returns

$\mathbf{y}:\{$ ndarray, scalar $\}$
The floor of each element in $x$.

## See Also:

ceil, trunc, rint

## Notes

Some spreadsheet programs calculate the "floor-towards-zero", in other words floor (-2.5) == -2 . NumPy, however, uses the a definition of floor such that floor $(-2.5)==-3$.

## Examples

```
>>> a = np.array([-1.7, -1.5, -0.2, 0.2, 1.5, 1.7, 2.0])
>>> np.floor(a)
array([-2., -2., -1., 0., 1., 1., 2.])
numpy.ceil (x[,out])
```

Return the ceiling of the input, element-wise.
The ceil of the scalar $x$ is the smallest integer $i$, such that $i>=x$. It is often denoted as $\lceil x\rceil$.

## Parameters

$\mathbf{x}:$ array_like
Input data.

## Returns

$\mathbf{y}:\{$ ndarray, scalar $\}$
The ceiling of each element in $x$, with float dtype.

## See Also:

floor, trunc, rint

## Examples

```
>>> a = np.array([-1.7, -1.5, -0.2, 0.2, 1.5, 1.7, 2.0])
>>> np.ceil(a)
array([-1., -1., -0., 1., 2., 2., 2.])
```

numpy.trunc ( $x[$, out $]$ )
Return the truncated value of the input, element-wise.
The truncated value of the scalar $x$ is the nearest integer $i$ which is closer to zero than $x$ is. In short, the fractional part of the signed number $x$ is discarded.

## Parameters

$\mathbf{x}$ : array_like
Input data.

## Returns

$\mathbf{y}:\{$ ndarray, scalar \}
The truncated value of each element in $x$.

## See Also:

```
ceil,floor,rint
```


## Notes

New in version 1.3.0.

## Examples

```
>>> a = np.array([-1.7, -1.5, -0.2, 0.2, 1.5, 1.7, 2.0])
>>> np.trunc(a)
array([-1., -1., -0., 0., 1., 1., 2.])
```


### 3.13.4 Sums, products, differences

| prod(a[, axis, dtype, out]) | Return the product of array elements over a given axis. |
| :---: | :---: |
| sum(a[, axis, dtype, out]) | Sum of array elements over a given axis. |
| nansum(a[, axis]) | Return the sum of array elements over a given axis treating |
| cumprod(a[, axis, dtype, out]) | Return the cumulative product of elements along a given axis. |
| cumsum(a[, axis, dtype, out]) | Return the cumulative sum of the elements along a given axis. |
| $\operatorname{diff}(\mathrm{a}$ [, n, axis]) | Calculate the n -th order discrete difference along given axis. |
| ediffid(ary[, to_end, to_begin]) | The differences between consecutive elements of an array. |
| gradient(f, *varargs) | Return the gradient of an N -dimensional array. |
| $\operatorname{cross}(\mathrm{a}, \mathrm{b}$ [, axisa, axisb, axisc, axis]) | Return the cross product of two (arrays of) vectors. |
| trapz(y[, x, dx, axis]) | Integrate along the given axis using the composite trapezoidal rule. |

numpy $\cdot \operatorname{prod}(a$, axis=None, dtype=None, out=None)
Return the product of array elements over a given axis.

## Parameters

a : array_like
Input data.
axis : int, optional
Axis over which the product is taken. By default, the product of all elements is calculated.
dtype : data-type, optional
The data-type of the returned array, as well as of the accumulator in which the elements are multiplied. By default, if $a$ is of integer type, dtype is the default platform integer. (Note: if the type of $a$ is unsigned, then so is dtype.) Otherwise, the dtype is the same as that of $a$.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output, but the type of the output values will be cast if necessary.

## Returns

product_along_axis : ndarray, see dtype parameter above.
An array shaped as $a$ but with the specified axis removed. Returns a reference to out if specified.

## See Also:

ndarray.prod
equivalent method

## numpy.doc.ufuncs

Section "Output arguments"

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow. That means that, on a 32-bit platform:

```
>>> x = np.array([536870910, 536870910, 536870910, 536870910])
>>> np.prod(x) #random
16
```


## Examples

By default, calculate the product of all elements:

```
>>> np.prod([1.,2.])
2.0
```

Even when the input array is two-dimensional:

```
>>> np.prod([[1.,2.],[3.,4.]])
24.0
```

But we can also specify the axis over which to multiply:

```
>>> np.prod([[1.,2.],[3.,4.]], axis=1)
array([ 2., 12.])
```

If the type of $x$ is unsigned, then the output type is the unsigned platform integer:

```
>>> x = np.array([1, 2, 3], dtype=np.uint8)
>>> np.prod(x).dtype == np.uint
True
```

If $x$ is of a signed integer type, then the output type is the default platform integer:

```
>>> x = np.array([1, 2, 3], dtype=np.int8)
>>> np.prod(x).dtype == np.int
True
```

numpy. sum ( a, axis=None, dtype=None, out=None)
Sum of array elements over a given axis.

## Parameters

a : array_like
Elements to sum.
axis : integer, optional
Axis over which the sum is taken. By default axis is None, and all elements are summed.
dtype : dtype, optional
The type of the returned array and of the accumulator in which the elements are summed. By default, the dtype of $a$ is used. An exception is when $a$ has an integer type with less precision than the default platform integer. In that case, the default platform integer is used instead.
out : ndarray, optional

Array into which the output is placed. By default, a new array is created. If out is given, it must be of the appropriate shape (the shape of $a$ with axis removed, i.e., numpy.delete(a.shape, axis)). Its type is preserved. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

sum_along_axis : ndarray
An array with the same shape as $a$, with the specified axis removed. If $a$ is a $0-\mathrm{d}$ array, or if axis is None, a scalar is returned. If an output array is specified, a reference to out is returned.

## See Also:

```
ndarray.sum
```

Equivalent method.
cumsum
Cumulative sum of array elements.
trapz
Integration of array values using the composite trapezoidal rule.
mean, average

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> np.sum([0.5, 1.5])
2.0
>>> np.sum([0.5, 0.7, 0.2, 1.5], dtype=np.int32)
1
>>> np.sum([[0, 1], [0, 5]])
6
>>> np.sum([[0, 1], [0, 5]], axis=0)
array([0, 6])
>>> np.sum([[0, 1], [0, 5]], axis=1)
array([1, 5])
```

If the accumulator is too small, overflow occurs:

```
>>> np.ones(128, dtype=np.int8).sum(dtype=np.int8)
```

-128
numpy. nansum (a, axis=None)
Return the sum of array elements over a given axis treating Not a Numbers (NaNs) as zero.

## Parameters

a : array_like
Array containing numbers whose sum is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the sum is computed. The default is to compute the sum of the flattened array.

## Returns

$\mathbf{y}$ : ndarray
An array with the same shape as a, with the specified axis removed. If a is a $0-\mathrm{d}$ array, or if axis is None, a scalar is returned with the same dtype as $a$.

## See Also:

## numpy.sum

Sum across array including Not a Numbers.
isnan
Shows which elements are Not a Number (NaN).
isfinite
Shows which elements are not: Not a Number, positive and negative infinity

## Notes

Numpy uses the IEEE Standard for Binary Floating-Point for Arithmetic (IEEE 754). This means that Not a Number is not equivalent to infinity. If positive or negative infinity are present the result is positive or negative infinity. But if both positive and negative infinity are present, the result is Not A Number (NaN).

Arithmetic is modular when using integer types (all elements of $a$ must be finite i.e. no elements that are NaNs, positive infinity and negative infinity because NaNs are floating point types), and no error is raised on overflow.

## Examples

```
>>> np.nansum(1)
1
>>> np.nansum([1])
1
>>> np.nansum([1, np.nan])
1.0
>>> a = np.array([[1, 1], [1, np.nan]])
>>> np.nansum(a)
3.0
>>> np.nansum(a, axis=0)
array([ 2., 1.])
```

When positive infinity and negative infinity are present

```
>>> np.nansum([1, np.nan, np.inf])
inf
>>> np.nansum([1, np.nan, np.NINF])
-inf
>>> np.nansum([1, np.nan, np.inf, np.NINF])
nan
```

numpy. cumprod ( $a$, axis=None, dtype=None, out=None)

Return the cumulative product of elements along a given axis.

## Parameters

a : array_like
Input array.
axis : int, optional
Axis along which the cumulative product is computed. By default the input is flattened.
dtype : dtype, optional

Type of the returned array, as well as of the accumulator in which the elements are multiplied. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used instead.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type of the resulting values will be cast if necessary.

## Returns

cumprod : ndarray
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## See Also:

numpy.doc.ufuncs
Section "Output arguments"

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> a = np.array([1,2,3])
>>> np.cumprod(a) # intermediate results 1, 1*2
... # total product 1*2*3 = 6
array([1, 2, 6])
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
>>> np.cumprod(a, dtype=float) # specify type of output
array([ 1., 2., 6., 24., 120., 720.])
```

The cumulative product for each column (i.e., over the rows) of $a$ :

```
>>> np.cumprod(a, axis=0)
array([[ 1, 2, 3],
    [ 4, 10, 18]])
```

The cumulative product for each row (i.e. over the columns) of $a$ :

```
>>> np.cumprod(a,axis=1)
```

array ([[ 1, 2, 6],
$[4,20,120]])$
numpy. cumsum (a, axis=None, dtype=None, out=None)
Return the cumulative sum of the elements along a given axis.

## Parameters

a : array_like
Input array.
axis : int, optional
Axis along which the cumulative sum is computed. The default (None) is to compute the cumsum over the flattened array.
dtype : dtype, optional

Type of the returned array and of the accumulator in which the elements are summed. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary. See doc.ufuncs (Section "Output arguments") for more details.

## Returns

cumsum_along_axis : ndarray.
A new array holding the result is returned unless out is specified, in which case a reference to out is returned. The result has the same size as $a$, and the same shape as $a$ if axis is not None or $a$ is a 1-d array.

## See Also:

## sum

Sum array elements.
trapz
Integration of array values using the composite trapezoidal rule.

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> a = np.array([[1,2,3], [4,5,6]])
>>> a
array([[1, 2, 3],
    [4, 5, 6]])
>>> np.cumsum(a)
array([ 1, 3, 6, 10, 15, 21])
>>> np.cumsum(a, dtype=float) # specifies type of output value(s)
array([ 1., 3., 6., 10., 15., 21.])
>>> np.cumsum(a,axis=0) # sum over rows for each of the 3 columns
array([[1, 2, 3],
    [5, 7, 9]])
>>> np.cumsum(a,axis=1) # sum over columns for each of the 2 rows
array([[ 1, 3, 6],
    [ 4, 9, 15]])
```

numpy.diff ( $a, n=1$, axis=- 1 )
Calculate the $n$-th order discrete difference along given axis.
The first order difference is given by out $[n]=a[n+1]-a[n]$ along the given axis, higher order differences are calculated by using diff recursively.

## Parameters

a : array_like
Input array
$\mathbf{n}$ : int, optional
The number of times values are differenced.
axis : int, optional
The axis along which the difference is taken, default is the last axis.

## Returns

 out : ndarrayThe $n$ order differences. The shape of the output is the same as $a$ except along axis where the dimension is smaller by $n$.

```
    See Also:
gradient,ediffld
    Examples
    >>> x = np.array([1, 2, 4, 7, 0])
    >>> np.diff(x)
    array([ 1, 2, 3, -7])
    >>> np.diff(x, n=2)
    array([ 1, 1, -10])
    >>> x = np.array([[1, 3, 6, 10], [0, 5, 6, 8]])
    >>> np.diff(x)
    array([[2, 3, 4],
            [5, 1, 2]])
>>> np.diff(x, axis=0)
array([[-1, 2, 0, -2]])
numpy.ediff1d(ary, to_end=None, to_begin=None)
The differences between consecutive elements of an array.
```


## Parameters

ary : array_like
If necessary, will be flattened before the differences are taken.
to_end : array_like, optional
Number(s) to append at the end of the returned differences.
to_begin : array_like, optional
Number(s) to prepend at the beginning of the returned differences.

## Returns

ed : ndarray
The differences. Loosely, this is ary.flat[1:] - ary.flat[:-1].

## See Also:

```
diff,gradient
```


## Notes

When applied to masked arrays, this function drops the mask information if the to_begin and/or to_end parameters are used.

## Examples

```
>>> x = np.array([1, 2, 4, 7, 0])
>>> np.ediff1d(x)
array([ 1, 2, 3, -7])
```

```
>>> np.ediff1d(x, to_begin=-99, to_end=np.array([88, 99]))
array([-99, 1, 2, 3, -7, 88, 99])
```

The returned array is always 1D.

```
>>> y = [[1, 2, 4], [1, 6, 24]]
>>> np.ediff1d(y)
array([ 1, 2, -3, 5, 18])
```

numpy.gradient ( $f$, *varargs)
Return the gradient of an N -dimensional array.
The gradient is computed using central differences in the interior and first differences at the boundaries. The returned gradient hence has the same shape as the input array.

## Parameters

f: array_like
An N -dimensional array containing samples of a scalar function.
‘*varargs' : scalars
0,1 , or N scalars specifying the sample distances in each direction, that is: $d x, d y, d z$,
... The default distance is 1 .

## Returns

$\mathbf{g}$ : ndarray
N arrays of the same shape as $f$ giving the derivative of $f$ with respect to each dimension.

## Examples

```
>>> x = np.array([1, 2, 4, 7, 11, 16], dtype=np.float)
>>> np.gradient(x)
array([ 1. , 1.5, 2.5, 3.5, 4.5, 5. ])
>>> np.gradient(x, 2)
array([ 0.5 , 0.75, 1.25, 1.75, 2.25, 2.5 ])
>>> np.gradient(np.array([[1, 2, 6], [3, 4, 5]], dtype=np.float))
[array([[ 2., 2., -1.],
            [ 2., 2., -1.]]),
array([[ 1. , 2.5, 4. ],
    [ 1. , 1. , 1. ]])]
```

numpy. cross ( $a, b$, axis $a=-1$, axisb $=-1$, axis $=-1$, axis $=$ None)
Return the cross product of two (arrays of) vectors.
The cross product of $a$ and $b$ in $R^{3}$ is a vector perpendicular to both $a$ and $b$. If $a$ and $b$ are arrays of vectors, the vectors are defined by the last axis of $a$ and $b$ by default, and these axes can have dimensions 2 or 3 . Where the dimension of either $a$ or $b$ is 2 , the third component of the input vector is assumed to be zero and the cross product calculated accordingly. In cases where both input vectors have dimension 2, the z-component of the cross product is returned.

## Parameters

a : array_like
Components of the first vector(s).
b : array_like
Components of the second vector(s).
axisa : int, optional

Axis of $a$ that defines the vector(s). By default, the last axis.
axisb : int, optional
Axis of $b$ that defines the vector(s). By default, the last axis.
axisc : int, optional
Axis of $c$ containing the cross product vector(s). By default, the last axis.
axis : int, optional
If defined, the axis of $a, b$ and $c$ that defines the vector(s) and cross product(s). Overrides axisa, axisb and axisc.

## Returns

c : ndarray
Vector cross product(s).

## Raises

ValueError :
When the dimension of the vector(s) in $a$ and/or $b$ does not equal 2 or 3 .

## See Also:

```
inner
```

Inner product
outer
Outer product.
ix
Construct index arrays.

## Examples

Vector cross-product.

```
>>> x = [1, 2, 3]
>>> y = [4, 5, 6]
>>> np.cross(x, y)
array([-3, 6, -3])
```

One vector with dimension 2.

```
>>> x = [1, 2]
>>> y = [4, 5, 6]
>>> np.cross(x, y)
array([12, -6, -3])
```

Equivalently:

```
>>> x = [1, 2, 0]
>>> y = [4, 5, 6]
>>> np.cross(x, y)
array([12, -6, -3])
```

Both vectors with dimension 2.

```
>>> x = [1,2]
>>> y = [4,5]
>>> np.cross(x, y)
-3
```

Multiple vector cross-products. Note that the direction of the cross product vector is defined by the right-hand rule.

```
>>> x = np.array([[1,2,3], [4,5,6]])
>>> y = np.array([[4,5,6], [1,2,3]])
>>> np.cross(x, y)
array([[-3, 6, -3],
    [ 3, -6, 3]])
```

The orientation of $c$ can be changed using the axisc keyword.

```
>>> np.cross(x, y, axisc=0)
array([[-3, 3],
    [ 6, -6],
    [-3, 3]])
```

Change the vector definition of $x$ and $y$ using axisa and axisb.

```
>>> x = np.array([[1,2,3], [4,5,6], [7, 8, 9]])
>>> y = np.array([[7, 8, 9], [4,5,6], [1,2,3]])
>>> np.cross(x, y)
array([[ -6, 12, -6],
    [ 0, 0, 0],
    [ 6, -12, 6]])
>>> np.cross(x, y, axisa=0, axisb=0)
array([[-24, 48, -24],
    [-30, 60, -30],
    [-36, 72, -36]])
```

numpy.trapz ( $y, x=$ None, $d x=1.0$, axis $=-1$ )
Integrate along the given axis using the composite trapezoidal rule.
Integrate $y(x)$ along given axis.

## Parameters

$\mathbf{y}$ : array_like
Input array to integrate.
$\mathbf{x}$ : array_like, optional
If $x$ is None, then spacing between all $y$ elements is $d x$.
dx : scalar, optional
If $x$ is None, spacing given by $d x$ is assumed. Default is 1 .
axis : int, optional
Specify the axis.

## Returns

out : float
Definite integral as approximated by trapezoidal rule.

## See Also:

```
sum, cumsum
```


## Notes

Image [R225] illustrates trapezoidal rule - $y$-axis locations of points will be taken from $y$ array, by default $x$-axis distances between points will be 1.0, alternatively they can be provided with $x$ array or with $d x$ scalar. Return value will be equal to combined area under the red lines.

## References

[R224], [R225]

## Examples

```
>>> np.trapz([1,2,3])
4.0
>>> np.trapz([1,2,3], x=[4,6,8])
8.0
>>> np.trapz([1,2,3], dx=2)
8.0
>>> a = np.arange(6).reshape (2, 3)
>>> a
array([[0, 1, 2],
    [3, 4, 5]])
>>> np.trapz(a, axis=0)
array([ 1.5, 2.5, 3.5])
>>> np.trapz(a, axis=1)
array([ 2., 8.])
```


### 3.13.5 Exponents and logarithms

| $\exp ()$ | Calculate the exponential of all elements in the input array. |
| :--- | :--- |
| $\operatorname{expm} 1()$ | Calculate $\exp (\mathrm{x})-1$ for all elements in the array. |
| $\exp 2()$ | Calculate $2 * * p$ for all $p$ in the input array. |
| $\log ()$ | Natural logarithm, element-wise. |
| $\log 10()$ | Return the base 10 logarithm of the input array, element-wise. |
| $\log 2()$ | Base-2 logarithm of $x$. |
| $\log 1 \mathrm{p}()$ | Return the natural logarithm of one plus the input array, element-wise. |
| $\operatorname{logaddexp}(x 1)$ | Logarithm of the sum of exponentiations of the inputs. |
| $\log \operatorname{loddexp} 2(\mathrm{x} 1)$ | Logarithm of the sum of exponentiations of the inputs in base-2. |
| numpy.exp $(x[$, out $])$ |  |

Calculate the exponential of all elements in the input array.

## Parameters

$\mathbf{x}$ : array_like
Input values.

## Returns

out : ndarray
Output array, element-wise exponential of $x$.

```
See Also:
expm1
Calculate \(\exp (\mathrm{x})-1\) for all elements in the array.
exp2
Calculate \(2 * * x\) for all elements in the array.
```


## Notes

The irrational number e is also known as Euler's number. It is approximately 2.718281, and is the base of the natural logarithm, $\ln$ (this means that, if $x=\ln y=\log _{e} y$, then $e^{x}=y$. For real input, exp ( x ) is always positive.

For complex arguments, $\mathrm{x}=\mathrm{a}+\mathrm{ib}$, we can write $e^{x}=e^{a} e^{i b}$. The first term, $e^{a}$, is already known (it is the real argument, described above). The second term, $e^{i b}$, is $\cos b+i \sin b$, a function with magnitude 1 and a periodic phase.

## References

[R18], [R19]

## Examples

Plot the magnitude and phase of exp (x) in the complex plane:

```
>>> import matplotlib.pyplot as plt
>>> x = np.linspace(-2*np.pi, 2*np.pi, 100)
>>> xx = x + lj * x[:, np.newaxis] # a + ib over complex plane
>>> out = np.exp(xx)
>>> plt.subplot(121)
>>> plt.imshow(np.abs(out),
... extent=[-2*np.pi, 2*np.pi, -2*np.pi, 2*np.pi])
>>> plt.title('Magnitude of exp(x)')
>>> plt.subplot(122)
>>> plt.imshow(np.angle(out),
... extent=[-2*np.pi, 2*np.pi, -2*np.pi, 2*np.pi])
>>> plt.title('Phase (angle) of exp(x)')
>>> plt.show()
```


numpy.expm1 (x[, out $]$ )
Calculate $\exp (\mathrm{x})-1$ for all elements in the array.

## Parameters

$\mathbf{x}$ : array_like

Input values.

## Returns

out : ndarray
Element-wise exponential minus one: out $=\exp (x)-1$.

## See Also:

$\log 1 p$
$\log (1+x)$, the inverse of expm1.

## Notes

This function provides greater precision than the formula $\exp (x)-1$ for small values of $x$.

## Examples

The true value of $\exp (1 e-10)-1$ is $1.00000000005 \mathrm{e}-10$ to about 32 significant digits. This example shows the superiority of expm1 in this case.

```
>>> np.expm1(1e-10)
1.00000000005e-10
>>> np.exp(1e-10) - 1
1.000000082740371e-10
```

numpy . exp2 (x[, out $]$ )

Calculate $2 * * p$ for all $p$ in the input array.

## Parameters

$\mathbf{x}$ : array_like
Input values.
out : ndarray, optional
Array to insert results into.

## Returns

out : ndarray
Element-wise 2 to the power $x$.

## See Also:

exp
calculate $\mathrm{x} * * \mathrm{p}$.

## Notes

New in version 1.3.0.

## Examples

```
>>> np.exp2([2, 3])
array([ 4., 8.])
```

numpy. $\log (x[$, out $])$
Natural logarithm, element-wise.
The natural logarithm $\log$ is the inverse of the exponential function, so that $\log (\exp (x))=x$. The natural logarithm is logarithm in base $e$.

## Parameters

$\mathbf{x}$ : array_like
Input value.

## Returns

$\mathbf{y}$ : ndarray
The natural logarithm of $x$, element-wise.

## See Also:

```
log10, log2, log1p, emath.log
```


## Notes

Logarithm is a multivalued function: for each $x$ there is an infinite number of $z$ such that $\exp (z)=x$. The convention is to return the $z$ whose imaginary part lies in [-pi, pi].

For real-valued input data types, log always returns real output. For each value that cannot be expressed as a real number or infinity, it yields nan and sets the invalid floating point error flag.

For complex-valued input, $\log$ is a complex analytical function that has a branch cut $[-i n f, 0]$ and is continuous from above on it. log handles the floating-point negative zero as an infinitesimal negative number, conforming to the C99 standard.

## References

[R41], [R42]

## Examples

```
>>> np.log([1, np.e, np.e**2, 0])
array([ 0., 1., 2., -Inf])
```

numpy. $\log 10(x[$, out $])$
Return the base 10 logarithm of the input array, element-wise.

## Parameters

$$
\begin{aligned}
& \mathbf{x}: \text { array_like } \\
& \quad \text { Input values. }
\end{aligned}
$$

## Returns

$\mathbf{y}$ : ndarray
The logarithm to the base 10 of $x$, element-wise. NaNs are returned where x is negative.

## See Also:

emath. $\log 10$

## Notes

Logarithm is a multivalued function: for each $x$ there is an infinite number of $z$ such that $10{ }^{*} z_{z}=x$. The convention is to return the $z$ whose imaginary part lies in $[-p i, p i]$.
For real-valued input data types, $\log 10$ always returns real output. For each value that cannot be expressed as a real number or infinity, it yields nan and sets the invalid floating point error flag.

For complex-valued input, $\log 10$ is a complex analytical function that has a branch cut $[$-inf, 0$]$ and is continuous from above on it. $\log 10$ handles the floating-point negative zero as an infinitesimal negative number, conforming to the C99 standard.

## References

[R43], [R44]

## Examples

```
>>> np.log10([1e-15, -3.])
array([-15., NaN])
```

numpy. $\log 2(x[$, out $])$
Base-2 logarithm of $x$.

## Parameters

$\mathbf{x}$ : array_like

## Input values.

## Returns

$\mathbf{y}$ : ndarray
Base-2 logarithm of $x$.

## See Also:

```
log, log10, log1p, emath.log2
```


## Notes

New in version 1.3.0. Logarithm is a multivalued function: for each $x$ there is an infinite number of $z$ such that $2 *_{z}=x$. The convention is to return the $z$ whose imaginary part lies in [-pi, pi].

For real-valued input data types, $\log 2$ always returns real output. For each value that cannot be expressed as a real number or infinity, it yields nan and sets the invalid floating point error flag.

For complex-valued input, $\log 2$ is a complex analytical function that has a branch cut [-inf, 0] and is continuous from above on it. $\log 2$ handles the floating-point negative zero as an infinitesimal negative number, conforming to the C99 standard.

## Examples

```
>>> x = np.array([0, 1, 2, 2**4])
>>> np.log2(x)
array([-Inf, 0., 1., 4.])
>>> xi = np.array([0+1.j, 1, 2+0.j, 4.j])
>>> np.log2(xi)
array([ 0.+2.26618007j, 0.+0.j , 1.+0.j , 2.+2.26618007j])
```

numpy. $\log 1 \mathrm{p}(x[$, out $])$

Return the natural logarithm of one plus the input array, element-wise.
Calculates $\log (1+x)$.

## Parameters

$\mathbf{x}$ : array_like
Input values.

## Returns

$\mathbf{y}$ : ndarray
Natural logarithm of $1+x$, element-wise.

## See Also:

expm1
$\exp (x)-1$, the inverse of $\log 1 p$.

## Notes

For real-valued input, $\log 1 p$ is accurate also for $x$ so small that $1+x==1$ in floating-point accuracy.
Logarithm is a multivalued function: for each $x$ there is an infinite number of $z$ such that $\exp (z)=1+x$. The convention is to return the $z$ whose imaginary part lies in [-pi, pi].

For real-valued input data types, $\log 1 p$ always returns real output. For each value that cannot be expressed as a real number or infinity, it yields nan and sets the invalid floating point error flag.

For complex-valued input, loglp is a complex analytical function that has a branch cut [-inf, -1] and is continuous from above on it. $\log 1 p$ handles the floating-point negative zero as an infinitesimal negative number, conforming to the C99 standard.

## References

[R45], [R46]

## Examples

```
>>> np.log1p(1e-99)
1e-99
>>> np.log(1 + 1e-99)
0.0
```

numpy.logaddexp ( $x 1, x 2[$, out $]$ )
Logarithm of the sum of exponentiations of the inputs.
Calculates $\log (\exp (x 1)+\exp (x 2))$. This function is useful in statistics where the calculated probabilities of events may be so small as to exceed the range of normal floating point numbers. In such cases the logarithm of the calculated probability is stored. This function allows adding probabilities stored in such a fashion.

```
Parameters
    x1, x2 : array_like
            Input values.
Returns
    result : ndarray
        Logarithm of exp(x1) + exp(x2).
```


## See Also:

logaddexp2
Logarithm of the sum of exponentiations of inputs in base-2.

## Notes

New in version 1.3.0.

## Examples

```
>>> prob1 = np.log (1e-50)
>>> prob2 = np.log(2.5e-50)
>>> prob12 = np.logaddexp(prob1, prob2)
>>> prob12
-113.87649168120691
```

```
>>> np.exp(prob12)
3.50000000000000057e-50
```

numpy. logaddexp2 ( $x 1, x 2[$, out $]$ )
Logarithm of the sum of exponentiations of the inputs in base- 2 .
Calculates $\log 2(2 * * x 1+2 * * x 2)$. This function is useful in machine learning when the calculated probabilities of events may be so small as to exceed the range of normal floating point numbers. In such cases the base-2 logarithm of the calculated probability can be used instead. This function allows adding probabilities stored in such a fashion.

## Parameters

$\mathbf{x 1}, \mathbf{x} 2$ : array_like
Input values.
out : ndarray, optional
Array to store results in.

## Returns

result : ndarray
Base- 2 logarithm of $2 * * x 1+2 * * x 2$.

## See Also:

logaddexp
Logarithm of the sum of exponentiations of the inputs.

## Notes

New in version 1.3.0.

## Examples

```
>>> prob1 = np.log2(1e-50)
>>> prob2 = np.log2(2.5e-50)
>>> prob12 = np.logaddexp2(prob1, prob2)
>>> prob1, prob2, prob12
(-166.09640474436813, -164.77447664948076, -164.28904982231052)
>>> 2**prob12
3.49999999999999914e-50
```


### 3.13.6 Other special functions

| i0(x) | Modified Bessel function of the first kind, order 0. |
| :--- | :--- |
| $\operatorname{sinc}(x)$ | Return the sinc function. |

numpy.io ( $x$ )
Modified Bessel function of the first kind, order 0.
Usually denoted $I_{0}$. This function does broadcast, but will not "up-cast" int dtype arguments unless accompanied by at least one float or complex dtype argument (see Raises below).

## Parameters

$\mathbf{x}$ : array_like, dtype float or complex
Argument of the Bessel function.

## Returns

out : ndarray, shape $=x$.shape, dtype $=x$.dtype
The modified Bessel function evaluated at each of the elements of $x$.

## Raises

TypeError: array cannot be safely cast to required type :
If argument consists exclusively of int dtypes.

## See Also:

```
scipy.special.iv,scipy.special.ive
```


## Notes

We use the algorithm published by Clenshaw [R28] and referenced by Abramowitz and Stegun [R29], for which the function domain is partitioned into the two intervals $[0,8]$ and ( 8 ,inf), and Chebyshev polynomial expansions are employed in each interval. Relative error on the domain [0,30] using IEEE arithmetic is documented [R30] as having a peak of $5.8 \mathrm{e}-16$ with an rms of $1.4 \mathrm{e}-16(\mathrm{n}=30000)$.

## References

[R28], [R29], [R30]

## Examples

```
>>> np.i0([0.])
array(1.0)
>>> np.i0([0., 1. + 2j])
array([ 1.00000000+0.j , 0.18785373+0.64616944j])
```

numpy. sinc ( $x$ )
Return the sinc function.
The sinc function is $\sin (\pi x) /(\pi x)$.

## Parameters

$\mathbf{x}$ : ndarray
Array (possibly multi-dimensional) of values for which to to calculate sinc (x).

## Returns

out : ndarray
$\operatorname{sinc}(x)$, which has the same shape as the input.

## Notes

$\operatorname{sinc}(0)$ is the limit value 1.
The name sinc is short for "sine cardinal" or "sinus cardinalis".
The sinc function is used in various signal processing applications, including in anti-aliasing, in the construction of a Lanczos resampling filter, and in interpolation.

For bandlimited interpolation of discrete-time signals, the ideal interpolation kernel is proportional to the sinc function.

## References

[R220], [R221]

## Examples

>>> import matplotlib.pyplot as plt
>>> plt.plot(x, np.sinc(x))
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.title("Sinc Function")
<matplotlib.text.Text object at 0x...>
>>> plt.ylabel("Amplitude")
<matplotlib.text. Text object at 0x...>
>>> plt.xlabel("X")
<matplotlib.text.Text object at 0x...>
>>> plt.show()


It works in 2-D as well:

```
>>> x = np.arange(-200., 201.)/50.
>>> xx = np.outer(x, x)
>>> plt.imshow(np.sinc(xx))
<matplotlib.image.AxesImage object at 0x...>
```



### 3.13.7 Floating point routines

| signbit () | Returns element-wise True where signbit is set (less than zero). |
| :--- | :--- |
| copysign(x1) | Change the sign of x 1 to that of x 2, element-wise. |
| frexp(out1) | Split the number, x, into a normalized fraction $(\mathrm{y} 1)$ and exponent $(\mathrm{y} 2)$ |
| ldexp(x1) | Compute $\mathrm{y}=\mathrm{x} 1^{*} 2^{* *} \mathrm{x} 2$. |
|  | numpy.signbit $(x[$, out $])$ |

Returns element-wise True where signbit is set (less than zero).

## Parameters

x: array_like :
The input value(s).
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output. See doc.ufuncs.

## Returns

result : ndarray of bool
Output array, or reference to out if that was supplied.
Examples

```
>>> np.signbit(-1.2)
True
>>> np.signbit(np.array([1, -2.3, 2.1]))
array([False, True, False], dtype=bool)
```

numpy.copysign ( $x 1, x 2[$, out $]$ )
Change the sign of $x 1$ to that of $x 2$, element-wise.
If both arguments are arrays or sequences, they have to be of the same length. If $x 2$ is a scalar, its sign will be copied to all elements of $x l$.

## Parameters

x1: array_like :
Values to change the sign of.
x2: array_like :
The sign of $x 2$ is copied to $x 1$.
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output. See doc.ufuncs.

## Returns

out : array_like
The values of $x 1$ with the sign of $x 2$.

## Examples

```
>>> np.copysign(1.3, -1)
-1.3
>>> 1/np.copysign(0, 1)
inf
>>> 1/np.copysign(0, -1)
-inf
>>> np.copysign([-1, 0, 1], -1.1)
array([-1., -0., -1.])
>>> np.copysign([-1, 0, 1], np.arange(3)-1)
array([-1., 0., 1.])
numpy.frexp (x[,outl, out2])
```

    Split the number, x , into a normalized fraction ( y 1 ) and exponent ( y 2 )
    numpy. $1 \operatorname{dexp}(x l, x 2[$, out $])$
Compute $\mathrm{y}=\mathrm{x} 1 * 2 * * \mathrm{x} 2$.

### 3.13.8 Arithmetic operations

| add(x1) | Add arguments element-wise. |
| :--- | :--- |
| reciprocal() | Return the reciprocal of the argument, element-wise. |
| negative() | Returns an array with the negative of each element of the original array. |
| multiply(x1) | Multiply arguments element-wise. |
| divide(x1) | Divide arguments element-wise. |
| power(x1) | First array elements raised to powers from second array, element-wise. |
| subtract(x1) | Subtract arguments, element-wise. |
| true_divide(x1) | Returns a true division of the inputs, element-wise. |
| floor_divide(x1) | Return the largest integer smaller or equal to the division of the inputs. |
| fmod(x1) | Return the element-wise remainder of division. |
| mod(x1) | Return element-wise remainder of division. |
| modf(out1) | Return the fractional and integral parts of an array, element-wise. |
| remainder(x1) | Return element-wise remainder of division. |
| numpy.add $(x 1, x 2[$, out $])$ |  |
| Add arguments element-wise. |  |

## Parameters

$\mathbf{x 1}, \mathbf{x} 2$ : array_like
The arrays to be added. If $x 1$. shape $!=x 2$. shape, they must be broadcastable to a common shape (which may be the shape of one or the other).

## Returns

$\mathbf{y}$ : ndarray or scalar
The sum of $x 1$ and $x 2$, element-wise. Returns a scalar if both $x 1$ and $x 2$ are scalars.

## Notes

Equivalent to $x 1+x 2$ in terms of array broadcasting.

## Examples

```
>>> np.add(1.0, 4.0)
5.0
>>> x1 = np.arange(9.0).reshape((3, 3))
>>> x2 = np.arange(3.0)
>>> np.add(x1, x2)
array([[ 0., 2., 4.],
    [ 3., 5., 7.],
    [ 6., 8., 10.]])
```

numpy.reciprocal ( $x[$, out $]$ )
Return the reciprocal of the argument, element-wise.
Calculates $1 / \mathrm{x}$.

## Parameters

$\mathbf{x}$ : array_like
Input array.

## Returns

$\mathbf{y}$ : ndarray
Return array.

## Notes

Note: This function is not designed to work with integers.
For integer arguments with absolute value larger than 1 the result is always zero because of the way Python handles integer division. For integer zero the result is an overflow.

## Examples

```
>>> np.reciprocal(2.)
0.5
>>> np.reciprocal([1, 2., 3.33])
array([ 1. , 0.5 , 0.3003003])
```

numpy. negative ( $x[$, out $]$ )
Returns an array with the negative of each element of the original array.

## Parameters

$\mathbf{x}$ : array_like or scalar
Input array.

## Returns

$\mathbf{y}$ : ndarray or scalar
Returned array or scalar: $y=-x$.
Examples

```
>>> np.negative([1.,-1.])
array([-1., 1.])
```

numpy.multiply (xl, $x 2$ [, out] $)$
Multiply arguments element-wise.

## Parameters

$\mathbf{x 1}, \mathbf{x} 2$ : array_like
Input arrays to be multiplied.

## Returns

y : ndarray
The product of $x 1$ and $x 2$, element-wise. Returns a scalar if both $x 1$ and $x 2$ are scalars.

## Notes

Equivalent to $x 1 * x 2$ in terms of array broadcasting.

## Examples

```
>>> np.multiply(2.0, 4.0)
8.0
>>> x1 = np.arange(9.0).reshape((3, 3))
>>> x2 = np.arange(3.0)
>>> np.multiply(x1, x2)
array([[ 0., 1., 4.],
            [ 0., 4., 10.],
            [ 0., 7., 16.]])
```

numpy.divide ( $x 1, x 2$ [, out $]$ )

Divide arguments element-wise.

## Parameters

$\mathbf{x 1}$ : array_like
Dividend array.
x2 : array_like
Divisor array.
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output. See doc.ufuncs.

## Returns

$\mathbf{y}:\{$ ndarray, scalar $\}$
The quotient $x 1 / x 2$, element-wise. Returns a scalar if both $x 1$ and $x 2$ are scalars.
See Also:

## seterr

Set whether to raise or warn on overflow, underflow and division by zero.

## Notes

Equivalent to $x 1 / x 2$ in terms of array-broadcasting.
Behavior on division by zero can be changed using seterr.
When both $x 1$ and $x 2$ are of an integer type, divide will return integers and throw away the fractional part. Moreover, division by zero always yields zero in integer arithmetic.

## Examples

```
>>> np.divide(2.0, 4.0)
0.5
>>> x1 = np.arange(9.0).reshape((3, 3))
>>> x2 = np.arange(3.0)
>>> np.divide(x1, x2)
array([[ NaN, 1. , 1. ],
    [ Inf, 4. , 2.5],
    [ Inf, 7. , 4. ]])
```

Note the behavior with integer types:

```
>>> np.divide(2, 4)
0
>>> np.divide(2, 4.)
0.5
```

Division by zero always yields zero in integer arithmetic, and does not raise an exception or a warning:

```
>>> np.divide(np.array([0, 1], dtype=int), np.array([0, 0], dtype=int))
array([0, 0])
```

Division by zero can, however, be caught using seterr:

```
>>> old_err_state = np.seterr(divide='raise')
>>> np.divide(1, 0)
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
FloatingPointError: divide by zero encountered in divide
>>> ignored_states = np.seterr(**old_err_state)
>>> np.divide(1, 0)
0
numpy • power ( \(x 1, x_{2}[\), out \(]\) )
```

First array elements raised to powers from second array, element-wise.
Raise each base in $x 1$ to the positionally-corresponding power in $x 2 . x 1$ and $x 2$ must be broadcastable to the same shape.

## Parameters

x1 : array_like
The bases.
x2 : array_like
The exponents.

## Returns

$\mathbf{y}$ : ndarray
The bases in $x 1$ raised to the exponents in $x 2$.

## Examples

Cube each element in a list.

```
>>> x1 = range(6)
>>> x1
[0, 1, 2, 3, 4, 5]
>>> np.power(x1, 3)
array([ 0, 1, 8, 27, 64, 125])
```

Raise the bases to different exponents.

```
>>> x2 = [1.0, 2.0, 3.0, 3.0, 2.0, 1.0]
>>> np.power(x1, x2)
array([ 0., 1., 8., 27., 16., 5.])
```

The effect of broadcasting.

```
>>> x2 = np.array([[1, 2, 3, 3, 2, 1], [1, 2, 3, 3, 2, 1]])
>>> x2
array([[1, 2, 3, 3, 2, 1],
    [1, 2, 3, 3, 2, 1]])
>>> np.power(x1, x2)
array([[ 0, 1, 8, 27, 16, 5],
    [ 0, 1, 8, 27, 16, 5]])
numpy.subtract (x1, x2[,out])
```

Subtract arguments, element-wise.

## Parameters

$\mathbf{x 1}, \mathbf{x} 2$ : array_like
The arrays to be subtracted from each other.

## Returns

## y : ndarray

The difference of $x 1$ and $x 2$, element-wise. Returns a scalar if both $x 1$ and $x 2$ are scalars.

## Notes

Equivalent to $\mathrm{x} 1-\mathrm{x} 2$ in terms of array broadcasting.

## Examples

```
>>> np.subtract(1.0, 4.0)
-3.0
>>> x1 = np.arange(9.0).reshape((3, 3))
>>> x2 = np.arange(3.0)
>>> np.subtract(x1, x2)
array([[ 0., 0., 0.],
            [ 3., 3., 3.],
            [ 6., 6., 6.]])
numpy.true_divide (xl, x2[,out])
Returns a true division of the inputs, element-wise.
```

Instead of the Python traditional 'floor division', this returns a true division. True division adjusts the output type to present the best answer, regardless of input types.

## Parameters

x1 : array_like
Dividend array.

$$
\mathbf{x 2} \text { : array_like }
$$

Divisor array.

## Returns

out : ndarray
Result is scalar if both inputs are scalar, ndarray otherwise.

## Notes

The floor division operator / / was added in Python 2.2 making / / and / equivalent operators. The default floor division operation of / can be replaced by true division with from $\qquad$ future $\qquad$ import division.

In Python 3.0, / / is the floor division operator and / the true division operator. The true_divide (x1, x 2 ) function is equivalent to true division in Python.

## Examples

```
>>> x = np.arange(5)
>>> np.true_divide(x, 4)
array([ 0. , 0.25, 0.5 , 0.75, 1. ])
>>> x/4
array([0, 0, 0, 0, 1])
>>> x//4
array([0, 0, 0, 0, 1])
>>> from __future__ import division
>>> x/4
array([ 0. , 0.25, 0.5 , 0.75, 1. ])
>>> x//4
array([0, 0, 0, 0, 1])
numpy.floor_divide(xl, x2[,out])
```

Return the largest integer smaller or equal to the division of the inputs.

## Parameters

$\mathbf{x 1}$ : array_like
Numerator.
x2 : array_like
Denominator.

## Returns

$\mathbf{y}$ : ndarray

$$
\mathrm{y}=\text { floor }(x 1 / x 2)
$$

## See Also:

## divide

Standard division.
floor
Round a number to the nearest integer toward minus infinity.
ceil
Round a number to the nearest integer toward infinity.

## Examples

```
>>> np.floor_divide(7,3)
2
>>> np.floor_divide([1., 2., 3., 4.], 2.5)
array([ 0., 0., 1., 1.])
```

numpy. fmod ( $x 1, x 2[$, out $]$ )

Return the element-wise remainder of division.
This is the NumPy implementation of the Python modulo operator \%.

## Parameters

$\mathbf{x 1}$ : array_like
Dividend.
x2 : array_like
Divisor.

## Returns

y: array_like
The remainder of the division of $x 1$ by $x 2$.

## See Also:

```
remainder
```

Modulo operation where the quotient is floor $(x 1 / x 2)$.

```
divide
```


## Notes

The result of the modulo operation for negative dividend and divisors is bound by conventions. In fmod, the sign of the remainder is the sign of the dividend. In remainder, the sign of the divisor does not affect the sign of the result.

## Examples

```
>>> np.fmod([-3, -2, -1, 1, 2, 3], 2)
array([-1, 0, -1, 1, 0, 1])
>>> np.remainder([-3, -2, -1, 1, 2, 3], 2)
array([1, 0, 1, 1, 0, 1])
>>> np.fmod([5, 3], [2, 2.])
array([ 1., 1.])
>>> a = np.arange(-3, 3).reshape(3, 2)
>>> a
array([[-3, -2],
    [-1, 0],
    [ 1, 2]])
>>> np.fmod(a, [2,2])
array([[-1, 0],
```

$$
\left.\left.\begin{array}{l}
{[-1,} \\
{[1,} \\
{[1,} \\
0]
\end{array}\right]\right)
$$

numpy.mod (x1, x2[, out])
Return element-wise remainder of division.
Computes x1 - floor $(x 1 / x 2)$ * $x 2$.

## Parameters

$\mathbf{x 1}$ : array_like
Dividend array.
x2 : array_like
Divisor array.
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output. See doc.ufuncs.

## Returns

y : ndarray
The remainder of the quotient $\mathrm{x} 1 / \mathrm{x} 2$, element-wise. Returns a scalar if both $x 1$ and $x 2$ are scalars.

## See Also:

divide,floor

## Notes

Returns 0 when $x 2$ is 0 and both $x 1$ and $x 2$ are (arrays of) integers.

## Examples

```
>>> np.remainder([4, 7], [2, 3])
array([0, 1])
>>> np.remainder(np.arange (7), 5)
array([0, 1, 2, 3, 4, 0, 1])
```

numpy $\operatorname{modf}(x[$, out 1, out 2$])$
Return the fractional and integral parts of an array, element-wise.
The fractional and integral parts are negative if the given number is negative.

## Parameters

$\mathbf{x}$ : array_like
Input array.

## Returns

y1 : ndarray
Fractional part of $x$.
y2 : ndarray
Integral part of $x$.

## Notes

For integer input the return values are floats.

## Examples

```
>>> np.modf([0, 3.5])
```

    (array([ 0. , 0.5]), array ([ 0., 3.]))
    >>> np.modf(-0.5)
$(-0.5,-0)$
numpy.remainder ( $x 1, x 2[$, out $]$ )
Return element-wise remainder of division.
Computes x1 - floor (x1 / x2) * x2.

## Parameters

$\mathbf{x 1}$ : array_like
Dividend array.
x2 : array_like
Divisor array.
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output. See doc.ufuncs.

## Returns

y: ndarray
The remainder of the quotient $\mathrm{x} 1 / \mathrm{x} 2$, element-wise. Returns a scalar if both $x 1$ and $x 2$ are scalars.

## See Also:

```
divide,floor
```


## Notes

Returns 0 when $x 2$ is 0 and both $x 1$ and $x 2$ are (arrays of) integers.

## Examples

```
>>> np.remainder([4, 7], [2, 3])
array([0, 1])
>>> np.remainder(np.arange(7), 5)
array([0, 1, 2, 3, 4, 0, 1])
```


### 3.13.9 Handling complex numbers

| angle $(z[, \operatorname{deg}])$ | Return the angle of the complex argument. <br> real (val) |
| :--- | :--- |
| Return the real part of the elements of the array. <br> imag(val) <br> con $j()$ | Return the imaginary part of the elements of the array. <br> Return the complex conjugate, element-wise. |
| numpy angle $(z, d e g=0)$ |  |
| Return the angle of the complex argument. |  |
| Parameters |  |
| $\mathbf{z}:$ array_like |  |

A complex number or sequence of complex numbers.
deg : bool, optional
Return angle in degrees if True, radians if False (default).

## Returns

 angle : \{ndarray, scalar\}The counterclockwise angle from the positive real axis on the complex plane, with dtype as numpy.float64.

## See Also:

```
arctan2,absolute
```


## Examples

```
>>> np.angle([1.0, 1.0j, 1+1j]) # in radians
array([ 0. , 1.57079633, 0.78539816])
>>> np.angle(1+1j, deg=True) # in degrees
45.0
```

numpy.real (val)

Return the real part of the elements of the array.

## Parameters <br> val : array_like <br> Input array.

## Returns

out : ndarray
Output array. If val is real, the type of val is used for the output. If val has complex elements, the returned type is float.

## See Also:

real_if_close, imag, angle

## Examples

```
>>> a = np.array([1+2j, 3+4j, 5+6j])
>>> a.real
array([ 1., 3., 5.])
>>> a.real = 9
>>> a
array([ 9.+2.j, 9.+4.j, 9.+6.j])
>>> a.real = np.array([9, 8, 7])
>>> a
array([ 9.+2.j, 8.+4.j, 7.+6.j])
```

numpy.imag (val)

Return the imaginary part of the elements of the array.

## Parameters

val : array_like
Input array.

## Returns

out : ndarray
Output array. If val is real, the type of val is used for the output. If val has complex elements, the returned type is float.

## See Also:

```
real, angle,real_if_close
```

Examples

```
>>> a = np.array([1+2j, 3+4j, 5+6j])
>>> a.imag
array([ 2., 4., 6.])
>>> a.imag = np.array([8, 10, 12])
>>> a
array([ 1. +8.j, 3.+10.j, 5.+12.j])
```

numpy. conj ( $x[$, out $]$ )
Return the complex conjugate, element-wise.
The complex conjugate of a complex number is obtained by changing the sign of its imaginary part.

## Parameters

$\mathbf{x}$ : array_like
Input value.

## Returns

$$
\mathbf{y} \text { : ndarray }
$$

The complex conjugate of $x$, with same dtype as $y$.

## Examples

```
>>> np.conjugate(1+2j)
(1-2j)
>>> x = np.eye(2) + 1j * np.eye(2)
>>> np.conjugate(x)
array([[ 1.-1.j, 0.-0.j],
    [ 0.-0.j, 1.-1.j]])
```


### 3.13.10 Miscellaneous

| convolve(a, v[, mode]) | Returns the discrete, linear convolution of two one-dimensional sequences. |
| :--- | :--- |
| clip(a, a_min, a_max[, out $])$ | Clip (limit) the values in an array. |
| sqrt() | Return the positive square-root of an array, element-wise. |
| square( | Return the element-wise square of the input. |
| absolute() | Calculate the absolute value element-wise. |
| fabs( | Compute the absolute values elementwise. |
| sign() | Returns an element-wise indication of the sign of a number. |
| maximum(x1) | Element-wise maximum of array elements. |
| minimum(x1) | Element-wise minimum of array elements. |
| nan_to_num(x) | Replace nan with zero and inf with finite numbers. |
| real_if_close(a[, tol]) | If complex input returns a real array if complex parts are close to zero. |
| interp(x, xp, fp[, left, right]) | One-dimensional linear interpolation. |

numpy . convolve ( $a, v$, mode $=$ 'full')
Returns the discrete, linear convolution of two one-dimensional sequences.
The convolution operator is often seen in signal processing, where it models the effect of a linear time-invariant system on a signal [R17]. In probability theory, the sum of two independent random variables is distributed according to the convolution of their individual distributions.

## Parameters

a : (N, ) array_like
First one-dimensional input array.
$\mathbf{v}$ : (M,) array_like
Second one-dimensional input array.
mode : \{ 'full', 'valid', 'same'\}, optional
'full':
By default, mode is 'full'. This returns the convolution at each point of overlap, with an output shape of ( $\mathrm{N}+\mathrm{M}-1$, ). At the end-points of the convolution, the signals do not overlap completely, and boundary effects may be seen.
'same':
Mode same returns output of length max (M, N). Boundary effects are still visible.
'valid':
Mode valid returns output of length max $(M, N)-\min (M, N)+1$. The convolution product is only given for points where the signals overlap completely. Values outside the signal boundary have no effect.

## Returns

out : ndarray
Discrete, linear convolution of $a$ and $v$.

## See Also:

## scipy.signal.fftconvolve

Convolve two arrays using the Fast Fourier Transform.
scipy.linalg.toeplitz
Used to construct the convolution operator.

## Notes

The discrete convolution operation is defined as

$$
(f * g)[n]=\sum_{m=-\infty}^{\infty} f[m] g[n-m]
$$

It can be shown that a convolution $x(t) * y(t)$ in time/space is equivalent to the multiplication $X(f) Y(f)$ in the Fourier domain, after appropriate padding (padding is necessary to prevent circular convolution). Since multiplication is more efficient (faster) than convolution, the function scipy.signal.fftconvolve exploits the FFT to calculate the convolution of large data-sets.

## References

[R17]

## Examples

Note how the convolution operator flips the second array before "sliding" the two across one another:

```
>>> np.convolve([1, 2, 3], [0, 1, 0.5])
array([ 0. , 1. , 2.5, 4. , 1.5])
```

Only return the middle values of the convolution. Contains boundary effects, where zeros are taken into account:

```
>>> np.convolve([1,2,3],[0,1,0.5], 'same')
array([ 1. , 2.5, 4. ])
```

The two arrays are of the same length, so there is only one position where they completely overlap:

```
>>> np.convolve([1,2,3],[0,1,0.5], 'valid')
array([ 2.5])
```

numpy.clip (a, a_min, a_max, out=None)

Clip (limit) the values in an array.
Given an interval, values outside the interval are clipped to the interval edges. For example, if an interval of $[0,1]$ is specified, values smaller than 0 become 0 , and values larger than 1 become 1 .

## Parameters

a : array_like
Array containing elements to clip.
a_min : scalar or array_like
Minimum value.
a_max : scalar or array_like
Maximum value. If $a \_m i n$ or $a \_m a x$ are array_like, then they will be broadcasted to the shape of $a$.
out : ndarray, optional
The results will be placed in this array. It may be the input array for in-place clipping. out must be of the right shape to hold the output. Its type is preserved.

## Returns

clipped_array : ndarray
An array with the elements of $a$, but where values $<a_{-} \min$ are replaced with $a \_$min, and those $>a \_m a x$ with $a \_m a x$.

## See Also:

numpy.doc.ufuncs
Section "Output arguments"

## Examples

```
>>> a = np.arange(10)
>>> np.clip(a, 1, 8)
array([1, 1, 2, 3, 4, 5, 6, 7, 8, 8])
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, 3, 6, out=a)
array([3, 3, 3, 3, 4, 5, 6, 6, 6, 6])
>>> a = np.arange(10)
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, [3,4,1,1,1,4,4,4,4,4], 8)
array([3, 4, 2, 3, 4, 5, 6, 7, 8, 8])
```

numpy.sqrt ( $x$ [,out $]$ )
Return the positive square-root of an array, element-wise.

## Parameters

$\mathbf{x}$ : array_like
The values whose square-roots are required.
out : ndarray, optional
Alternate array object in which to put the result; if provided, it must have the same shape as $x$

## Returns

$$
\mathbf{y} \text { : ndarray }
$$

An array of the same shape as $x$, containing the positive square-root of each element in $x$. If any element in $x$ is complex, a complex array is returned (and the square-roots of negative reals are calculated). If all of the elements in $x$ are real, so is $y$, with negative elements returning nan. If out was provided, $y$ is a reference to it.

## See Also:

## lib.scimath.sqrt

A version which returns complex numbers when given negative reals.

## Notes

sqrt has-consistent with common convention-as its branch cut the real "interval" [-inf, 0), and is continuous from above on it. (A branch cut is a curve in the complex plane across which a given complex function fails to be continuous.)

## Examples

```
>>> np.sqrt([1,4,9])
array([ 1., 2., 3.])
>>> np.sqrt([4, -1, -3+4J])
array([ 2.+0.j, 0.+1.j, 1.+2.j])
>>> np.sqrt([4, -1, numpy.inf])
array([ 2., NaN, Inf])
```

numpy. square ( $x[$, out $]$ )
Return the element-wise square of the input.

## Parameters

$\mathbf{x}$ : array_like
Input data.

## Returns

out : ndarray
Element-wise $x^{*} x$, of the same shape and dtype as $x$. Returns scalar if $x$ is a scalar.

## See Also:

numpy.linalg.matrix_power, sqrt, power

## Examples

```
>>> np.square([-1j, 1])
array([-1.-0.j, 1.+0.j])
```

numpy.absolute ( $x$ [, out $]$ )
Calculate the absolute value element-wise.

## Parameters

$\mathbf{x}$ : array_like
Input array.

## Returns

absolute : ndarray
An ndarray containing the absolute value of each element in $x$. For complex input, a + i.b, the absolute value is $\sqrt{a^{2}+b^{2}}$.

## Examples

```
>>> x = np.array([-1.2, 1.2])
>>> np.absolute(x)
array([ 1.2, 1.2])
>>> np.absolute(1.2 + 1j)
1.5620499351813308
```

Plot the function over [-10, 10]:

```
>>> import matplotlib.pyplot as plt
>>> x = np.linspace(-10, 10, 101)
>>> plt.plot(x, np.absolute(x))
>>> plt.show()
```



Plot the function over the complex plane:
$\ggg x x=x+1 j * x[:, n p . n e w a x i s]$
$\ggg$ plt.imshow(np.abs(xx), extent $=[-10,10,-10,10])$
>>> plt.show()

numpy. fabs ( $x[$, out $]$ )
Compute the absolute values elementwise.
This function returns the absolute values (positive magnitude) of the data in $x$. Complex values are not handled, use absolute to find the absolute values of complex data.

## Parameters

$\mathbf{x}$ : array_like
The array of numbers for which the absolute values are required. If $x$ is a scalar, the result $y$ will also be a scalar.
out : ndarray, optional
Array into which the output is placed. Its type is preserved and it must be of the right shape to hold the output. See doc.ufuncs.

## Returns

$\mathbf{y}:\{$ ndarray, scalar $\}$
The absolute values of $x$, the returned values are always floats.

## See Also:

## absolute

Absolute values including complex types.

## Examples

```
>>> np.fabs(-1)
1.0
>>> np.fabs([-1.2, 1.2])
array([ 1.2, 1.2])
numpy.sign (x[,out])
```

Returns an element-wise indication of the sign of a number.
The sign function returns -1 if $\mathrm{x}<0,0$ if $\mathrm{x}==0$, 1 if $\mathrm{x}>0$.

## Parameters

$$
\mathbf{x} \text { : array_like }
$$

Input values.

## Returns

y : ndarray
The sign of $x$.

## Examples

```
>>> np.sign([-5., 4.5])
array([-1., 1.])
>>> np.sign(0)
0
```

numpy .maximum ( $x 1, x 2[$, out $]$ )
Element-wise maximum of array elements.
Compare two arrays and returns a new array containing the element-wise maxima. If one of the elements being compared is a nan, then that element is returned. If both elements are nans then the first is returned. The latter distinction is important for complex nans, which are defined as at least one of the real or imaginary parts being a nan. The net effect is that nans are propagated.

## Parameters

$\mathbf{x 1}, \mathbf{x} 2$ : array_like
The arrays holding the elements to be compared. They must have the same shape, or shapes that can be broadcast to a single shape.

## Returns

$\mathbf{y}:\{$ ndarray, scalar $\}$
The maximum of $x 1$ and $x 2$, element-wise. Returns scalar if both $x 1$ and $x 2$ are scalars.

## See Also:

minimum
element-wise minimum
fmax
element-wise maximum that ignores nans unless both inputs are nans.
fmin
element-wise minimum that ignores nans unless both inputs are nans.

## Notes

Equivalent to np. where $(x 1>x 2, x 1, x 2)$ but faster and does proper broadcasting.

## Examples

```
>>> np.maximum([2, 3, 4], [1, 5, 2])
array([2, 5, 4])
>>> np.maximum(np.eye(2), [0.5, 2])
array([[ 1. , 2. ],
            [ 0.5, 2. ]])
>>> np.maximum([np.nan, 0, np.nan], [0, np.nan, np.nan])
array([ NaN, NaN, NaN])
>>> np.maximum(np.Inf, 1)
inf
```

numpy.minimum ( $x 1, x 2[$, out $]$ )
Element-wise minimum of array elements.
Compare two arrays and returns a new array containing the element-wise minima. If one of the elements being compared is a nan, then that element is returned. If both elements are nans then the first is returned. The latter distinction is important for complex nans, which are defined as at least one of the real or imaginary parts being a nan. The net effect is that nans are propagated.

## Parameters

$\mathbf{x 1}, \mathbf{x 2}$ : array_like
The arrays holding the elements to be compared. They must have the same shape, or shapes that can be broadcast to a single shape.

## Returns

$\mathbf{y}:\{$ ndarray, scalar $\}$
The minimum of $x 1$ and $x 2$, element-wise. Returns scalar if both $x 1$ and $x 2$ are scalars.

## See Also:

maximum
element-wise minimum that propagates nans.
fmax
element-wise maximum that ignores nans unless both inputs are nans.
fmin
element-wise minimum that ignores nans unless both inputs are nans.

## Notes

The minimum is equivalent to $n p$. where $(x 1<=x 2, x 1, x 2)$ when neither x 1 nor x 2 are nans, but it is faster and does proper broadcasting.

## Examples

```
>>> np.minimum([2, 3, 4], [1, 5, 2])
array([1, 3, 2])
>>> np.minimum(np.eye(2), [0.5, 2]) # broadcasting
array([[ 0.5, 0. ],
    [ 0. , 1. ]])
>>> np.minimum([np.nan, 0, np.nan],[0, np.nan, np.nan])
array([ NaN, NaN, NaN])
```

numpy . nan_to_num ( $x$ )

Replace nan with zero and inf with finite numbers.
Returns an array or scalar replacing Not a Number ( NaN ) with zero, (positive) infinity with a very large number and negative infinity with a very small (or negative) number.

## Parameters

$\mathbf{x}$ : array_like
Input data.

## Returns

out : ndarray, float

Array with the same shape as $x$ and dtype of the element in $x$ with the greatest precision. NaN is replaced by zero, and infinity (-infinity) is replaced by the largest (smallest or most negative) floating point value that fits in the output dtype. All finite numbers are upcast to the output dtype (default float64).

## See Also:

isinf
Shows which elements are negative or negative infinity.

```
isneginf
```

Shows which elements are negative infinity.

```
isposinf
```

Shows which elements are positive infinity.

```
isnan
```

Shows which elements are Not a Number (NaN).

```
isfinite
```

Shows which elements are finite (not NaN, not infinity)

## Notes

Numpy uses the IEEE Standard for Binary Floating-Point for Arithmetic (IEEE 754). This means that Not a Number is not equivalent to infinity.

## Examples

```
>>> np.set_printoptions(precision=8)
>>> x = np.array([np.inf, -np.inf, np.nan, -128, 128])
>>> np.nan_to_num(x)
array([ 1.79769313e+308, -1.79769313e+308, 0.00000000e+000,
    -1.28000000e+002, 1.28000000e+002])
```

numpy.real_if_close (a,tol=100)
If complex input returns a real array if complex parts are close to zero.
"Close to zero" is defined as $t o l *$ (machine epsilon of the type for $a$ ).

## Parameters

a : array_like
Input array.
tol : float
Tolerance in machine epsilons for the complex part of the elements in the array.

## Returns

out : ndarray
If $a$ is real, the type of $a$ is used for the output. If $a$ has complex elements, the returned type is float.

## See Also:

```
real,imag, angle
```


## Notes

Machine epsilon varies from machine to machine and between data types but Python floats on most platforms have a machine epsilon equal to $2.2204460492503131 \mathrm{e}-16$. You can use 'np.finfo(np.float).eps' to print out the machine epsilon for floats.

## Examples

```
>>> np.finfo(np.float).eps
2.2204460492503131e-16
>>> np.real_if_close([2.1 + 4e-14j], tol=1000)
array([ 2.1])
>>> np.real_if_close([2.1 + 4e-13j], tol=1000)
array([ 2.1 +4.00000000e-13j])
numpy.interp ( }x,xp,fp,left=None, right=None
```

One-dimensional linear interpolation.
Returns the one-dimensional piecewise linear interpolant to a function with given values at discrete data-points.

## Parameters

$\mathbf{x}$ : array_like
The x-coordinates of the interpolated values.
$\mathbf{x p}: 1-\mathrm{D}$ sequence of floats
The x -coordinates of the data points, must be increasing.
$\mathbf{f p}$ : 1-D sequence of floats
The $y$-coordinates of the data points, same length as $x p$.
left : float, optional
Value to return for $x<x p[0]$, default is $f p[0]$.
right : float, optional
Value to return for $x>x p[-1]$, defaults is $f p[-1]$.

## Returns

$\mathbf{y}:\{$ float, ndarray $\}$
The interpolated values, same shape as $x$.

## Raises

ValueError :
If $x p$ and $f p$ have different length

## Notes

Does not check that the $x$-coordinate sequence $x p$ is increasing. If $x p$ is not increasing, the results are nonsense.
A simple check for increasingness is:

```
np.all(np.diff(xp) > 0)
```


## Examples

```
>>> xp = [1, 2, 3]
>>> fp = [3, 2, 0]
>>> np.interp(2.5, xp, fp)
```

```
1.0
>>> np.interp([0, 1, 1.5, 2.72, 3.14], xp, fp)
array([ 3. , 3. , 2.5, 0.56, 0. ])
>>> UNDEF = -99.0
>>> np.interp(3.14, xp, fp, right=UNDEF)
-99.0
```

Plot an interpolant to the sine function:

```
>>> x = np.linspace(0, 2*np.pi, 10)
>>> y = np.sin(x)
>>> xvals = np.linspace(0, 2*np.pi, 50)
>>> yinterp = np.interp(xvals, x, y)
>>> import matplotlib.pyplot as plt
>>> plt.plot(x, y, 'o')
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.plot(xvals, yinterp, '-x')
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.show()
```



### 3.14 Functional programming

```
apply_along_axis(func1d, axis, arr, *args) Apply a function to 1-D slices along the given axis.
apply_over_axes(func,a, axes)
vectorize(pyfunc[, otypes, doc])
frompyfunc(func, nin, nout)
piecewise(x, condlist, funclist, *args, **kw)
Apply a function to 1-D slices along the given axis.
Apply a function repeatedly over multiple axes.
Generalized function class.
Takes an arbitrary Python function and returns a Numpy ufunc.
Evaluate a piecewise-defined function.
```

numpy.apply_along_axis (funcld, axis, arr, *args)
Apply a function to 1-D slices along the given axis.
Execute funcld(a, *args) where funcld operates on 1-D arrays and $a$ is a 1-D slice of arr along axis.

## Parameters

func1d : function

This function should accept 1-D arrays. It is applied to 1-D slices of arr along the specified axis.
axis : integer
Axis along which arr is sliced.
arr : ndarray
Input array.
args : any
Additional arguments to funcld.

## Returns

outarr : ndarray
The output array. The shape of outarr is identical to the shape of arr, except along the axis dimension, where the length of outarr is equal to the size of the return value of funcld. If funcld returns a scalar outarr will have one fewer dimensions than arr.

## See Also:

```
apply_over_axes
```

Apply a function repeatedly over multiple axes.

## Examples

```
>>> def my_func(a):
... """Average first and last element of a I-D array"""
... return (a[0] + a[-1]) * 0.5
>>> b = np.array([[1,2,3], [4,5,6], [7,8,9]])
>>> np.apply_along_axis(my_func, 0, b)
array([ 4., 5., 6.])
>>> np.apply_along_axis(my_func, 1, b)
array([ 2., 5., 8.])
```

For a function that doesn't return a scalar, the number of dimensions in outarr is the same as arr.

```
>>> def new_func(a):
... """Divide elements of a by 2."""
... return a * 0.5
>>> b = np.array([[1,2,3], [4,5,6], [7,8,9]])
>>> np.apply_along_axis(new_func, 0, b)
array([[ 0.5, 1. , 1.5],
    [2., 2.5, 3. ],
    [ 3.5, 4. , 4.5]])
```

numpy.apply_over_axes (func, a, axes)
Apply a function repeatedly over multiple axes.
func is called as res $=\operatorname{func}($ a, axis), where axis is the first element of axes. The result res of the function call must have either the same dimensions as $a$ or one less dimension. If res has one less dimension than $a$, a dimension is inserted before axis. The call to func is then repeated for each axis in axes, with res as the first argument.

## Parameters <br> func : function

This function must take two arguments, func ( $a$, axis).
a : array_like

Input array.
axes : array_like
Axes over which func is applied; the elements must be integers.

## Returns

val : ndarray
The output array. The number of dimensions is the same as $a$, but the shape can be different. This depends on whether func changes the shape of its output with respect to its input.

## See Also:

```
apply_along_axis
```

Apply a function to 1-D slices of an array along the given axis.

## Examples

```
>>> a = np.arange (24).reshape (2, 3,4)
>>> a
array([[[ 0, 1, 2, 3],
    [ 4, 5, 6, 7],
    [ 8, 9, 10, 11]],
    [[12, 13, 14, 15],
    [16, 17, 18, 19],
    [20, 21, 22, 23]]])
```

Sum over axes 0 and 2. The result has same number of dimensions as the original array:

```
>>> np.apply_over_axes(np.sum, a, [0,2])
array([[[ 60],
    [ 92],
    [124]]])
```

class numpy.vectorize (pyfunc, otypes='', doc=None)

## Generalized function class.

Define a vectorized function which takes a nested sequence of objects or numpy arrays as inputs and returns a numpy array as output. The vectorized function evaluates pyfunc over successive tuples of the input arrays like the python map function, except it uses the broadcasting rules of numpy.
The data type of the output of vectorized is determined by calling the function with the first element of the input. This can be avoided by specifying the otypes argument.

## Parameters

pyfunc : callable
A python function or method.
otypes : str or list of dtypes, optional
The output data type. It must be specified as either a string of typecode characters or a list of data type specifiers. There should be one data type specifier for each output.
doc: str, optional
The docstring for the function. If None, the docstring will be the pyfunc one.

## Examples

```
>>> def myfunc(a, b):
... """Return a-b if a>b, otherwise return a+b"""
... if a > b:
... return a - b
... else:
... return a + b
>>> vfunc = np.vectorize(myfunc)
>>> vfunc([1, 2, 3, 4], 2)
array([3, 4, 1, 2])
```

The docstring is taken from the input function to vectorize unless it is specified

```
>>> vfunc.__doc__
'Return a-b if a>b, otherwise return a+b'
>>> vfunc = np.vectorize(myfunc, doc='Vectorized 'myfunc'')
>>> vfunc.___doc__
'Vectorized 'myfunc''
```

The output type is determined by evaluating the first element of the input, unless it is specified

```
>>> out = vfunc([1, 2, 3, 4], 2)
>>> type(out[0])
<type 'numpy.int32'>
>>> vfunc = np.vectorize(myfunc, otypes=[np.float])
>>> out = vfunc([1, 2, 3, 4], 2)
>>> type(out[0])
<type 'numpy.float64'>
numpy. frompyfunc (func, nin, nout)
```

Takes an arbitrary Python function and returns a Numpy ufunc.
Can be used, for example, to add broadcasting to a built-in Python function (see Examples section).

## Parameters

func : Python function object
An arbitrary Python function.
nin : int
The number of input arguments.
nout : int
The number of objects returned by func.

## Returns

out : ufunc
Returns a Numpy universal function (ufunc) object.

## Notes

The returned ufunc always returns PyObject arrays.

## Examples

Use frompyfunc to add broadcasting to the Python function oct:

```
>>> oct_array = np.frompyfunc(oct, 1, 1)
>>> oct_array(np.array((10, 30, 100)))
array([012, 036, 0144], dtype=object)
>>> np.array((oct(10), oct(30), oct(100))) # for comparison
array(['012', '036', '0144'],
    dtype='|S4')
numpy.piecewise (x,condlist, funclist, *args, **kw)
Evaluate a piecewise-defined function.
```

Given a set of conditions and corresponding functions, evaluate each function on the input data wherever its condition is true.

## Parameters

$\mathbf{x}$ : ndarray
The input domain.
condlist : list of bool arrays
Each boolean array corresponds to a function in funclist. Wherever condlist $[i]$ is True, funclist $[i](x)$ is used as the output value.

Each boolean array in condlist selects a piece of $x$, and should therefore be of the same shape as $x$.

The length of condlist must correspond to that of funclist. If one extra function is given, i.e. if len (funclist) - len (condist) $==1$, then that extra function is the default value, used wherever all conditions are false.
funclist : list of callables, $\mathrm{f}(\mathrm{x}, * \operatorname{args}, * * \mathrm{kw})$, or scalars
Each function is evaluated over $x$ wherever its corresponding condition is True. It should take an array as input and give an array or a scalar value as output. If, instead of a callable, a scalar is provided then a constant function (lambda $x$ : scalar) is assumed.
args : tuple, optional
Any further arguments given to piecewise are passed to the functions upon execution, i.e., if called piecewise (..., ..., 1, ' $a^{\prime}$ ), then each function is called as $\mathrm{f}(\mathrm{x}, 1, \mathrm{a}$ ) .
$\mathbf{k w}$ : dict, optional
Keyword arguments used in calling piecewise are passed to the functions upon execution, i.e., if called piecewise (..., ..., lambda=1), then each function is called as $f(x, \quad l a m b d a=1)$.

## Returns

out : ndarray
The output is the same shape and type as x and is found by calling the functions in funclist on the appropriate portions of $x$, as defined by the boolean arrays in condlist. Portions not covered by any condition have undefined values.

## See Also:

choose, select, where

## Notes

This is similar to choose or select, except that functions are evaluated on elements of $x$ that satisfy the corresponding condition from condlist.

The result is:

```
    |--
    |funclist[0](x[condlist[0]])
out = |funclist[1](x[condlist[1]])
    | . . .
    |funclist[n2](x[condlist[n2]])
    | --
```


## Examples

Define the sigma function, which is -1 for $\mathrm{x}<0$ and +1 for $\mathrm{x}>=0$.

```
>>> x = np.arange(6) - 2.5
>>> np.piecewise(x, [x < 0, x >= 0], [-1, 1])
array([-1., -1., -1., 1., 1., 1.])
```

Define the absolute value, which is -x for $\mathrm{x}<0$ and x for $\mathrm{x}>=0$.

```
>>> np.piecewise(x, [x < 0, x >= 0], [lambda x: -x, lambda x: x])
array([ 2.5, 1.5, 0.5, 0.5, 1.5, 2.5])
```


### 3.15 Polynomials

### 3.15.1 Basics

```
poly1d(c_or_r[,r, variable]) A one-dimensional polynomial class.
polyval(p,x) Evaluate a polynomial at specific values.
poly(seq_of_zeros) Find the coefficients of a polynomial with the given sequence of roots.
roots(p) Return the roots of a polynomial with coefficients given in p.
```

class numpy.poly1d ( $c_{-} o r \_r, r=0$, variable $=$ None $)$
A one-dimensional polynomial class.
A convenience class, used to encapsulate "natural" operations on polynomials so that said operations may take on their customary form in code (see Examples).

## Parameters

c_or_r : array_like
The polynomial's coefficients, in decreasing powers, or if the value of the second parameter is True, the polynomial's roots (values where the polynomial evaluates to 0). For example, polyld ([1, 2, 3]) returns an object that represents $x^{2}+2 x+3$, whereas polyld([1, 2, 3], True) returns one that represents $(x-1)(x-2)(x-3)=$ $x^{3}-6 x^{2}+11 x-6$.
r: bool, optional
If True, $c_{-}$or_r specifies the polynomial's roots; the default is False.
variable : str, optional
Changes the variable used when printing $p$ from $x$ to variable (see Examples).

## Examples

Construct the polynomial $x^{2}+2 x+3$ :

```
>>> p = np.polyld([1, 2, 3])
>>> print np.polyld(p)
    2
1x+2x+3
```

Evaluate the polynomial at $x=0.5$ :

```
>>> p(0.5)
4.25
```

Find the roots:

```
>>> p.r
array([-1.+1.41421356j, -1.-1.41421356j])
>>> p(p.r)
array([ -4.44089210e-16+0.j, -4.44089210e-16+0.j])
```

These numbers in the previous line represent $(0,0)$ to machine precision
Show the coefficients:

```
>>> p.c
array([1, 2, 3])
```

Display the order (the leading zero-coefficients are removed):

```
>>> p.order
2
```

Show the coefficient of the $k$-th power in the polynomial (which is equivalent to p.c [ $-(i+1$ )] :

```
>>> p[1]
2
```

Polynomials can be added, subtracted, multiplied, and divided (returns quotient and remainder):

```
>>> p * p
poly1d([ 1, 4, 10, 12, 9])
>>> (p**3 + 4) / p
(polyld([ 1., 4., 10., 12., 9.]), poly1d([ 4.]))
```

asarray (p) gives the coefficient array, so polynomials can be used in all functions that accept arrays:

```
>>> p**2 # square of polynomial
polyld([ 1, 4, 10, 12, 9])
>>> np.square(p) # square of individual coefficients
array([1, 4, 9])
```

The variable used in the string representation of $p$ can be modified, using the variable parameter:

```
>>> p = np.poly1d([1,2,3], variable='z')
>>> print p
    2
1z+2 z + 3
```

Construct a polynomial from its roots:

```
>>> np.poly1d([1, 2], True)
poly1d([ 1, -3, 2])
```

This is the same polynomial as obtained by:

```
>>> np.poly1d([1, -1]) * np.poly1d([1, -2])
polyld([ 1, -3, 2])
```


## Attributes

```
coeffs
order
variable
```


## Methods

deriv
integ
numpy . polyval ( $p, x$ )
Evaluate a polynomial at specific values.
If $p$ is of length N , this function returns the value:
$\mathrm{p}[0] * \mathrm{x} * *(\mathrm{~N}-1)+\mathrm{p}[1] * \mathrm{x} * *(\mathrm{~N}-2)+\ldots+\mathrm{p}[\mathrm{N}-2] * \mathrm{x}+\mathrm{p}[\mathrm{N}-1]$
If $x$ is a sequence, then $p(x)$ is returned for each element of $x$. If $x$ is another polynomial then the composite polynomial $p(x(t))$ is returned.

## Parameters

$\mathbf{p}$ : array_like or poly1d object
1D array of polynomial coefficients (including coefficients equal to zero) from highest degree to the constant term, or an instance of poly1d.
$\mathbf{x}$ : array_like or poly1d object
A number, a 1D array of numbers, or an instance of poly1d, "at" which to evaluate $p$.

## Returns

values : ndarray or poly1d
If $x$ is a poly1d instance, the result is the composition of the two polynomials, i.e., $x$ is "substituted" in $p$ and the simplified result is returned. In addition, the type of $x$ array_like or poly1d-governs the type of the output: $x$ array_like $=>$ values array_like, $x$ a poly1d object $=>$ values is also.

## See Also:

poly1d
A polynomial class.

## Notes

Horner's scheme [R57] is used to evaluate the polynomial. Even so, for polynomials of high degree the values may be inaccurate due to rounding errors. Use carefully.

## References

[R57]

## Examples

```
>>> np.polyval([3,0,1], 5) # 3 * 5**2 + 0 * 5**1 + 1
7
>>> np.polyval([3,0,1], np.polyld(5))
polyld([ 76.])
>>> np.polyval(np.poly1d([3,0,1]), 5)
76
>>> np.polyval(np.polyld([3,0,1]), np.polyld(5))
polyld([ 76.])
```

numpy .poly (seq_of_zeros)
Find the coefficients of a polynomial with the given sequence of roots.
Returns the coefficients of the polynomial whose leading coefficient is one for the given sequence of zeros (multiple roots must be included in the sequence as many times as their multiplicity; see Examples). A square matrix (or array, which will be treated as a matrix) can also be given, in which case the coefficients of the characteristic polynomial of the matrix are returned.

## Parameters

seq_of_zeros : array_like, shape (N,) or (N, N)
A sequence of polynomial roots, or a square array or matrix object.

## Returns

c : ndarray
1D array of polynomial coefficients from highest to lowest degree:
$C[0] * x * *(N)+C[1] * x * *(N-1)+\ldots+C[N-1] * x+C[N]$
where $c[0]$ always equals 1 .

## Raises

ValueError :
If input is the wrong shape (the input must be a 1-D or square 2-D array).

## See Also:

polyval
Evaluate a polynomial at a point.
roots
Return the roots of a polynomial.
polyfit
Least squares polynomial fit.
poly1d
A one-dimensional polynomial class.

## Notes

Specifying the roots of a polynomial still leaves one degree of freedom, typically represented by an undetermined leading coefficient. [R53] In the case of this function, that coefficient - the first one in the returned array - is always taken as one. (If for some reason you have one other point, the only automatic way presently to leverage that information is to use polyfit.)
The characteristic polynomial, $p_{a}(t)$, of an $n$-by- $n$ matrix $\mathbf{A}$ is given by

$$
p_{a}(t)=\operatorname{det}(t \mathbf{I}-\mathbf{A})
$$

where $\mathbf{I}$ is the $n$-by- $n$ identity matrix. [R54]

## References

[R53], [R54]

## Examples

Given a sequence of a polynomial's zeros:

```
>>> np.poly((0, 0, 0)) # Multiple root example
array([1, 0, 0, 0])
```

The line above represents $\mathrm{z}^{* *} 3+0 * \mathrm{z}^{*} * 2+0 * \mathrm{z}+0$.

```
>>> np.poly((-1./2, 0, 1./2))
array([ 1. , 0. , -0.25, 0. ])
```

The line above represents $z^{* *} 3-z / 4$

```
>>> np.poly((np.random.random(1.)[0], 0, np.random.random(1.)[0]))
array([ 1. , -0.77086955, 0.08618131, 0. ]) #random
```

Given a square array object:

```
>>> P = np.array([[0, 1./3], [-1./2, 0]])
>>> np.poly(P)
array([ 1. , 0. 0.16666667])
```

Or a square matrix object:

```
>>> np.poly(np.matrix(P))
array([ 1. , 0. , 0.16666667])
```

Note how in all cases the leading coefficient is always 1.

```
numpy. roots (p)
```

Return the roots of a polynomial with coefficients given in p .
The values in the rank-1 array $p$ are coefficients of a polynomial. If the length of $p$ is $\mathrm{n}+1$ then the polynomial is described by:

```
p[0] * x**n + p[1] * x**(n-1) + ... + p[n-1]*x + p[n]
```


## Parameters

p : array_like
Rank-1 array of polynomial coefficients.

## Returns

out : ndarray
An array containing the complex roots of the polynomial.

## Raises

ValueError : :
When $p$ cannot be converted to a rank-1 array.

## See Also:

poly
Find the coefficients of a polynomial with a given sequence of roots.

## polyval

Evaluate a polynomial at a point.
polyfit
Least squares polynomial fit.
poly1d
A one-dimensional polynomial class.

## Notes

The algorithm relies on computing the eigenvalues of the companion matrix [R217].

## References

## [R217]

## Examples

```
>>> coeff = [3.2, 2, 1]
>>> np.roots(coeff)
array([-0.3125+0.46351241j, -0.3125-0.46351241j])
```


### 3.15.2 Fitting

polyfit(x, y, deg[, rcond, full]) Least squares polynomial fit.
numpy $\cdot$ polyfit ( $x, y$, deg, rcond=None, full=False)
Least squares polynomial fit.
Fit a polynomial $\mathrm{p}(\mathrm{x})=\mathrm{p}[0] * \mathrm{x} * * \operatorname{deg}+\ldots+\mathrm{p}[\mathrm{deg}]$ of degree deg to points $(x, y)$. Returns a vector of coefficients $p$ that minimises the squared error.

## Parameters

$\mathbf{x}$ : array_like, shape (M,)
$x$-coordinates of the $M$ sample points (x[i], $y[i]$ ).
$\mathbf{y}$ : array_like, shape (M,) or (M, K)
$y$-coordinates of the sample points. Several data sets of sample points sharing the same x -coordinates can be fitted at once by passing in a 2D-array that contains one dataset per column.
deg: int
Degree of the fitting polynomial
rcond : float, optional
Relative condition number of the fit. Singular values smaller than this relative to the largest singular value will be ignored. The default value is len $(x) * e p s$, where eps is the relative precision of the float type, about $2 \mathrm{e}-16$ in most cases.
full : bool, optional
Switch determining nature of return value. When it is False (the default) just the coefficients are returned, when True diagnostic information from the singular value decomposition is also returned.

## Returns

$\mathbf{p}$ : ndarray, shape (M,) or (M, K)

Polynomial coefficients, highest power first. If $y$ was 2-D, the coefficients for $k$-th data set are in $p[:, k]$.
residuals, rank, singular_values, rcond : present only if full $=$ True
Residuals of the least-squares fit, the effective rank of the scaled Vandermonde coefficient matrix, its singular values, and the specified value of rcond. For more details, see linalg.lstsq.

## Warns

## RankWarning :

The rank of the coefficient matrix in the least-squares fit is deficient. The warning is only raised if full = False.

The warnings can be turned off by

```
>>> import warnings
>>> warnings.simplefilter('ignore', np.RankWarningl)
```


## See Also:

polyval
Computes polynomial values.
linalg.lstsq
Computes a least-squares fit.
scipy.interpolate.UnivariateSpline
Computes spline fits.

## Notes

The solution minimizes the squared error

$$
E=\sum_{j=0}^{k}\left|p\left(x_{j}\right)-y_{j}\right|^{2}
$$

in the equations:

```
x[0]**n * p[n] + ... + x[0] * p[1] + p[0] = y[0]
x[1]**n * p[n] + ... + x[1] * p[1] + p[0] = y[1]
...
x[k]**n * p[n] + ... + x[k] * p[1] + p[0] = y[k]
```

The coefficient matrix of the coefficients $p$ is a Vandermonde matrix.
polyfit issues a RankWarning when the least-squares fit is badly conditioned. This implies that the best fit is not well-defined due to numerical error. The results may be improved by lowering the polynomial degree or by replacing $x$ by $x-x$.mean(). The rcond parameter can also be set to a value smaller than its default, but the resulting fit may be spurious: including contributions from the small singular values can add numerical noise to the result.

Note that fitting polynomial coefficients is inherently badly conditioned when the degree of the polynomial is large or the interval of sample points is badly centered. The quality of the fit should always be checked in these cases. When polynomial fits are not satisfactory, splines may be a good alternative.

## References

[R55], [R56]

## Examples

```
>>> x = np.array([0.0, 1.0, 2.0, 3.0, 4.0, 5.0])
>>>y = np.array([0.0, 0.8, 0.9, 0.1, -0.8, -1.0])
>>> z = np.polyfit(x, y, 3)
>>> z
array([ 0.08703704, -0.81349206, 1.69312169, -0.03968254])
```

It is convenient to use polyld objects for dealing with polynomials:

```
>>> p = np.polyld(z)
>>> p(0.5)
0.6143849206349179
>>> p(3.5)
-0.34732142857143039
>>> p(10)
22.579365079365115
```

High-order polynomials may oscillate wildly:

```
>>> p30 = np.polyld(np.polyfit(x, y, 30))
/... RankWarning: Polyfit may be poorly conditioned...
>>> p30(4)
-0.80000000000000204
>>> p30(5)
-0.99999999999999445
>>> p30(4.5)
-0.10547061179440398
```

Illustration:

```
>>> import matplotlib.pyplot as plt
>>> xp = np.linspace(-2, 6, 100)
>>> plt.plot(x, y, '.', xp, p(xp), '_', xp, p30(xp), ' --')
[<matplotlib.lines.Line2D object at 0x...>, <matplotlib.lines.Line2D object at 0x...>, <matpld
>>> plt.ylim(-2,2)
(-2, 2)
>>> plt.show()
```



### 3.15.3 Calculus

## polyder $(\mathrm{p}[, \mathrm{m}]) \quad$ Return the derivative of the specified order of a polynomial.

polyint(p[, m, k]) Return an antiderivative (indefinite integral) of a polynomial.
numpy.polyder ( $p, m=1$ )
Return the derivative of the specified order of a polynomial.

## Parameters

p : poly1d or sequence
Polynomial to differentiate. A sequence is interpreted as polynomial coefficients, see polyld.
m : int, optional
Order of differentiation (default: 1)

## Returns

der : poly1d
A new polynomial representing the derivative.

## See Also:

polyint
Anti-derivative of a polynomial.
poly1d
Class for one-dimensional polynomials.

## Examples

The derivative of the polynomial $x^{3}+x^{2}+x^{1}+1$ is:

```
>>> p = np.poly1d([1,1,1,1])
>>> p2 = np.polyder(p)
>>> p2
polyld([3, 2, 1])
```

which evaluates to:

```
>>> p2(2.)
17.0
```

We can verify this, approximating the derivative with $(\mathrm{f}(\mathrm{x}+\mathrm{h})-\mathrm{f}(\mathrm{x})) / \mathrm{h}$ :

```
>>> (p(2. + 0.001) - p(2.)) / 0.001
17.0070009999997857
```

The fourth-order derivative of a 3rd-order polynomial is zero:

```
>>> np.polyder(p, 2)
poly1d([6, 2])
>>> np.polyder(p, 3)
poly1d([6])
>>> np.polyder(p, 4)
poly1d([ 0.])
```

numpy.polyint ( $p, m=1, k=$ None)

Return an antiderivative (indefinite integral) of a polynomial.

The returned order $m$ antiderivative $P$ of polynomial $p$ satisfies $\frac{d^{m}}{d x^{m}} P(x)=p(x)$ and is defined up to $m-1$ integration constants $k$. The constants determine the low-order polynomial part

$$
\frac{k_{m-1}}{0!} x^{0}+\ldots+\frac{k_{0}}{(m-1)!} x^{m-1}
$$

of $P$ so that $P^{(j)}(0)=k_{m-j-1}$.

## Parameters

$\mathbf{p}:\{$ array_like, poly1d $\}$
Polynomial to differentiate. A sequence is interpreted as polynomial coefficients, see polyld.
m : int, optional
Order of the antiderivative. (Default: 1)
$\mathbf{k}$ : \{None, list of $m$ scalars, scalar $\}$, optional
Integration constants. They are given in the order of integration: those corresponding to highest-order terms come first.

If None (default), all constants are assumed to be zero. If $m=1$, a single scalar can be given instead of a list.

## See Also:

```
polyder
```

    derivative of a polynomial
    polyld.integ
equivalent method

## Examples

The defining property of the antiderivative:

```
>>> p = np.polyld([1,1,1])
>>> P = np.polyint(p)
>>> P
polyld([ 0.33333333, 0.5 , 1. , 0. ])
>>> np.polyder(P) == p
True
```

The integration constants default to zero, but can be specified:

```
>>> P = np.polyint(p, 3)
>>> P(0)
0.0
>>> np.polyder(P) (0)
0.0
>>> np.polyder(P, 2)(0)
0.0
>>> P = np.polyint(p, 3, k=[6,5,3])
>>> P
poly1d([ 0.01666667, 0.04166667, 0.16666667, 3., 5. , 3. ])
```

Note that $3=6 / 2$ !, and that the constants are given in the order of integrations. Constant of the highest-order polynomial term comes first:

```
>>> np.polyder(P, 2)(0)
6.0
>>> np.polyder(P, 1)(0)
5.0
>>> P(0)
3.0
```


### 3.15.4 Arithmetic

```
polyadd(a1, a2) Find the sum of two polynomials.
polydiv(u,v) Returns the quotient and remainder of polynomial division.
polymul(a1, a2) Find the product of two polynomials.
polysub(a1, a2) Difference (subtraction) of two polynomials.
```

numpy .polyadd (al, a2)

Find the sum of two polynomials.
Returns the polynomial resulting from the sum of two input polynomials. Each input must be either a poly1d object or a 1D sequence of polynomial coefficients, from highest to lowest degree.

## Parameters

a1, a2 : array_like or poly1d object
Input polynomials.

## Returns

out : ndarray or poly1d object
The sum of the inputs. If either input is a poly1d object, then the output is also a poly1d object. Otherwise, it is a 1D array of polynomial coefficients from highest to lowest degree.

## See Also:

poly1d
A one-dimensional polynomial class.
poly, polyadd, polyder, polydiv, polyfit, polyint, polysub, polyval

## Examples

```
>>> np.polyadd([1, 2], [9, 5, 4])
array([9, 6, 6])
```

Using poly1d objects:

```
>>> p1 = np.poly1d([1, 2])
>>> p2 = np.poly1d([9, 5, 4])
>>> print p1
1 x + 2
>>> print p2
    2
9x + 5 x + 4
>>> print np.polyadd(p1, p2)
    2
9x+6x+6
```

numpy.polydiv ( $u, v$ )
Returns the quotient and remainder of polynomial division.
The input arrays are the coefficients (including any coefficients equal to zero) of the "numerator" (dividend) and "denominator" (divisor) polynomials, respectively.

## Parameters

$\mathbf{u}$ : array_like or poly1d
Dividend polynomial's coefficients.
$\mathbf{v}$ : array_like or poly1d
Divisor polynomial's coefficients.

## Returns

$\mathbf{q}$ : ndarray
Coefficients, including those equal to zero, of the quotient.
r: ndarray
Coefficients, including those equal to zero, of the remainder.

## See Also:

```
poly,polyadd, polyder, polydiv, polyfit,polyint,polymul, polysub, polyval
```


## Notes

Both $u$ and $v$ must be $0-\mathrm{d}$ or $1-\mathrm{d}$ ( $\mathrm{ndim}=0$ or 1 ), but $u$.ndim need not equal $v . n d i m$. In other words, all four possible combinations $-\mathrm{u} . \mathrm{ndim}=\mathrm{v} . \mathrm{ndim}=0$, u.ndim $=\mathrm{v} . \mathrm{ndim}=1$, u.ndim $=1$, v.ndim $=0$, and u. ndim $=0, \mathrm{v}$. ndim $=1$-work.

## Examples

$$
\frac{3 x^{2}+5 x+2}{2 x+1}=1.5 x+1.75, \text { remainder } 0.25
$$

```
>>> x = np.array([3.0, 5.0, 2.0])
>>> y = np.array([2.0, 1.0])
>>> np.polydiv(x, y)
(array([ 1.5 , 1.75]), array([ 0.25]))
```

numpy.polymul (al, a2)
Find the product of two polynomials.
Finds the polynomial resulting from the multiplication of the two input polynomials. Each input must be either a poly1d object or a 1D sequence of polynomial coefficients, from highest to lowest degree.

## Parameters <br> $\mathbf{a 1}, \mathbf{a} 2$ : array_like or poly1d object <br> Input polynomials.

## Returns

out : ndarray or poly1d object
The polynomial resulting from the multiplication of the inputs. If either inputs is a poly1d object, then the output is also a poly1d object. Otherwise, it is a 1D array of polynomial coefficients from highest to lowest degree.

## See Also:

```
poly1d
```

A one-dimensional polynomial class.

```
poly, polyadd, polyder, polydiv, polyfit, polyint, polysub, polyval
```


## Examples

```
>>> np.polymul([1, 2, 3], [9, 5, 1])
array([ 9, 23, 38, 17, 3])
```

Using poly1d objects:

```
>>> p1 = np.poly1d([1, 2, 3])
>>> p2 = np.poly1d([9, 5, 1])
>>> print p1
    2
1 x + 2 x + 3
>>> print p2
            2
9x + 5 x + 1
>>> print np.polymul(p1, p2)
    4 3 2
9x+23x+38x + 17x + 3
```

numpy .polysub (al, a2)

Difference (subtraction) of two polynomials.
Given two polynomials $a 1$ and $a 2$, returns a1 - a2. $a 1$ and $a 2$ can be either array_like sequences of the polynomials' coefficients (including coefficients equal to zero), or polyld objects.

## Parameters

a1, a2 : array_like or poly1d
Minuend and subtrahend polynomials, respectively.

## Returns

out : ndarray or poly1d
Array or polyld object of the difference polynomial's coefficients.

## See Also:

```
polyval, polydiv, polymul, polyadd
```


## Examples

$$
\left(2 x^{2}+10 x-2\right)-\left(3 x^{2}+10 x-4\right)=\left(-x^{2}+2\right)
$$

```
>>> np.polysub([2, 10, -2], [3, 10, -4])
array([-1, 0, 2])
```


### 3.15.5 Warnings

## exception numpy. RankWarning

Issued by polyfit when the Vandermonde matrix is rank deficient.
For more information, a way to suppress the warning, and an example of RankWarning being issued, see polyfit.

### 3.16 Financial functions

### 3.16.1 Simple financial functions



- a present value, $p v$
- an interest rate compounded once per period, of which there are
- nper total
- a (fixed) payment, pmt, paid either
- at the beginning $($ when $=\{$ 'begin', 1$\}$ ) or the end $($ when $=\{$ 'end', 0$\})$ of each period


## Return:

the value at the end of the nper periods

## Parameters

rate : scalar or array_like of shape(M, )
Rate of interest as decimal (not per cent) per period
nper : scalar or array_like of shape(M, )
Number of compounding periods
pmt : scalar or array_like of shape(M, )
Payment
$\mathbf{p v}$ : scalar or array_like of shape(M, )
Present value
when : $\{\{$ 'begin', 1$\},\{$ 'end', 0$\}\},\{$ string, int $\}$, optional
When payments are due ('begin' (1) or 'end' (0)). Defaults to $\{$ 'end', 0$\}$.

## Returns

out : ndarray
Future values. If all input is scalar, returns a scalar float. If any input is array_like, returns future values for each input element. If multiple inputs are array_like, they all must have the same shape.

## Notes

The future value is computed by solving the equation:

```
fv +
pv*(1+rate)**nper +
pmt*(1 + rate*when)/rate*((1 + rate)**nper - 1) == 0
```

or, when rate $==0$ :

```
fv + pv + pmt * nper == 0
```


## References

## [WRW]

## Examples

What is the future value after 10 years of saving $\$ 100$ now, with an additional monthly savings of $\$ 100$. Assume the interest rate is 5\% (annually) compounded monthly?

```
>>> np.fv(0.05/12, 10*12, -100, -100)
15692.928894335748
```

By convention, the negative sign represents cash flow out (i.e. money not available today). Thus, saving $\$ 100$ a month at 5\% annual interest leads to $\$ 15,692.93$ available to spend in 10 years.

If any input is array_like, returns an array of equal shape. Let's compare different interest rates from the example above.

```
>>> a = np.array((0.05, 0.06, 0.07))/12
>>> np.fv(a, 10*12, -100, -100)
array([ 15692.92889434, 16569.87435405, 17509.44688102])
```

numpy . pv (rate, nper, pmt, fv=0.0, when='end')
Compute the present value.

## Given:

- a future value, $f v$
- an interest rate compounded once per period, of which there are
- nper total
- a (fixed) payment, pmt, paid either
- at the beginning (when $=\{$ 'begin', 1$\}$ ) or the end $($ when $=\{$ 'end', 0$\})$ of each period


## Return:

the value now

## Parameters

rate : array_like

Rate of interest (per period)
nper : array_like
Number of compounding periods
pmt : array_like
Payment
fv : array_like, optional
Future value
when : $\{$ \{'begin', 1$\},\{$ 'end', 0$\}\},\{$ string, int $\}$, optional
When payments are due ('begin' (1) or 'end' (0))

## Returns

out : ndarray, float
Present value of a series of payments or investments.

## Notes

The present value is computed by solving the equation:

```
fv +
pv*(1 + rate)**nper +
pmt*(1 + rate*when)/rate*((1 + rate)**nper - 1) = 0
```

or, when rate $=0$ :

```
fv + pv + pmt * nper = 0
```

for $p v$, which is then returned.

## References

[WRW]

## Examples

What is the present value (e.g., the initial investment) of an investment that needs to total $\$ 15692.93$ after 10 years of saving $\$ 100$ every month? Assume the interest rate is 5\% (annually) compounded monthly.

```
>>> np.pv(0.05/12, 10*12, -100, 15692.93)
-100.00067131625819
```

By convention, the negative sign represents cash flow out (i.e., money not available today). Thus, to end up with $\$ 15,692.93$ in 10 years saving $\$ 100$ a month at $5 \%$ annual interest, one's initial deposit should also be $\$ 100$.
If any input is array_like, pv returns an array of equal shape. Let's compare different interest rates in the example above:

```
>>> a = np.array((0.05, 0.04, 0.03))/12
>>> np.pv(a, 10*12, -100, 15692.93)
array([ -100.00067132, -649.26771385, -1273.78633713])
```

So, to end up with the same $\$ 15692.93$ under the same $\$ 100$ per month "savings plan," for annual interest rates of $4 \%$ and $3 \%$, one would need initial investments of $\$ 649.27$ and $\$ 1273.79$, respectively.

## Parameters

rate : scalar
The discount rate.
values : array_like, shape(M, )
The values of the time series of cash flows. The (fixed) time interval between cash flow "events" must be the same as that for which rate is given (i.e., if rate is per year, then precisely a year is understood to elapse between each cash flow event). By convention, investments or "deposits" are negative, income or "withdrawals" are positive; values must begin with the initial investment, thus values[0] will typically be negative.

## Returns

out : float
The NPV of the input cash flow series values at the discount rate.

## Notes

Returns the result of: [G50]

$$
\sum_{t=0}^{M} \frac{\text { values }_{t}}{\left(1+\text { rate }^{t}\right.}
$$

## References

[G50]

## Examples

```
>>> np.npv(0.281,[-100, 39, 59, 55, 20])
-0.0066187288356340801
```

(Compare with the Example given for numpy.lib.financial.irr)

```
numpy . pmt (rate, nper, pv,fv=0, when='end')
```

Compute the payment against loan principal plus interest.

## Given:

- a present value, $p v$ (e.g., an amount borrowed)
- a future value, fv (e.g., 0)
- an interest rate compounded once per period, of which there are
- nper total
- and (optional) specification of whether payment is made at the beginning (when $=\{$ 'begin', 1$\}$ ) or the end $(w h e n=\{$ 'end', 0$\}$ ) of each period


## Return:

the (fixed) periodic payment.

## Parameters

rate : array_like
Rate of interest (per period)
nper : array_like

Number of compounding periods
pv : array_like
Present value
fv : array_like (optional)
Future value $($ default $=0)$
when : $\{\{$ 'begin', 1$\}$, $\{$ 'end', 0$\}\}$, $\{$ string, int $\}$
When payments are due ('begin' (1) or 'end' (0))

## Returns

out : ndarray
Payment against loan plus interest. If all input is scalar, returns a scalar float. If any input is array_like, returns payment for each input element. If multiple inputs are array_like, they all must have the same shape.

## Notes

The payment is computed by solving the equation:

```
fv +
pv*(1 + rate)**nper +
pmt*(1 + rate*when)/rate*((1 + rate)**nper - 1) == 0
```

or, when rate $==0$ :

```
fv + pv + pmt * nper == 0
```

for pmt.
Note that computing a monthly mortgage payment is only one use for this function. For example, pmt returns the periodic deposit one must make to achieve a specified future balance given an initial deposit, a fixed, periodically compounded interest rate, and the total number of periods.

## References

[WRW]

## Examples

What is the monthly payment needed to pay off a $\$ 200,000$ loan in 15 years at an annual interest rate of $7.5 \%$ ?

```
>>> np.pmt(0.075/12, 12*15, 200000)
-1854.0247200054619
```

In order to pay-off (i.e., have a future-value of 0 ) the $\$ 200,000$ obtained today, a monthly payment of $\$ 1,854.02$ would be required. Note that this example illustrates usage of $f v$ having a default value of 0 .
numpy • ppmt (rate, per, nper, pv, fv=0.0, when='end')
Not implemented. Compute the payment against loan principal.

## Parameters <br> rate : array_like

Rate of interest (per period)
per : array_like, int
Amount paid against the loan changes. The per is the period of interest.
nper : array_like
Number of compounding periods
pv: array_like
Present value
fv : array_like, optional
Future value
when : $\{\{$ 'begin', 1$\}$, $\{$ 'end', 0$\}\}$, $\{$ string, int $\}$
When payments are due ('begin' (1) or 'end' (0))
See Also:
pmt, pv, ipmt
numpy.ipmt (rate, per, nper, pv, fv=0.0, when='end')
Not implemented. Compute the payment portion for loan interest.

## Parameters

rate : scalar or array_like of shape( M, )
Rate of interest as decimal (not per cent) per period
per : scalar or array_like of shape(M, )
Interest paid against the loan changes during the life or the loan. The per is the payment period to calculate the interest amount.
nper : scalar or array_like of shape(M, )
Number of compounding periods
pv : scalar or array_like of shape(M, )
Present value
fv : scalar or array_like of shape(M, ), optional
Future value
when : $\{$ \{'begin', 1$\}$, $\{$ 'end', 0$\}\}$, $\{$ string, int $\}$, optional
When payments are due ('begin' (1) or 'end' (0)). Defaults to $\{$ 'end', 0$\}$.

## Returns

out : ndarray
Interest portion of payment. If all input is scalar, returns a scalar float. If any input is array_like, returns interest payment for each input element. If multiple inputs are array_like, they all must have the same shape.

## See Also:

ppmt, pmt, pv

## Notes

The total payment is made up of payment against principal plus interest.

```
    pmt = ppmt + ipmt
```

numpy.irr (values)
Return the Internal Rate of Return (IRR).
This is the "average" periodically compounded rate of return that gives a net present value of 0.0 ; for a more complete explanation, see Notes below.

## Parameters

values : array_like, shape( N, )
Input cash flows per time period. By convention, net "deposits" are negative and net "withdrawals" are positive. Thus, for example, at least the first element of values, which represents the initial investment, will typically be negative.

## Returns

out : float
Internal Rate of Return for periodic input values.

## Notes

The IRR is perhaps best understood through an example (illustrated using np.irr in the Examples section below). Suppose one invests 100 units and then makes the following withdrawals at regular (fixed) intervals: 39, 59, 55, 20. Assuming the ending value is 0 , one's 100 unit investment yields 173 units; however, due to the combination of compounding and the periodic withdrawals, the "average" rate of return is neither simply $0.73 / 4$ nor $(1.73)^{\wedge} 0.25-1$. Rather, it is the solution (for $r$ ) of the equation:

$$
-100+\frac{39}{1+r}+\frac{59}{(1+r)^{2}}+\frac{55}{(1+r)^{3}}+\frac{20}{(1+r)^{4}}=0
$$

In general, for values $=\left[v_{0}, v_{1}, \ldots v_{M}\right]$, irr is the solution of the equation: [G31]

$$
\sum_{t=0}^{M} \frac{v_{t}}{(1+i r r)^{t}}=0
$$

## References

[G31]
Examples

```
>>> np.irr([-100, 39, 59, 55, 20])
0.2809484211599611
```

(Compare with the Example given for numpy.lib.financial.npv)
numpy.mirr (values, finance_rate, reinvest_rate)
Modified internal rate of return.

## Parameters

values : array_like
Cash flows (must contain at least one positive and one negative value) or nan is returned.
The first value is considered a sunk cost at time zero.
finance_rate : scalar
Interest rate paid on the cash flows
reinvest_rate : scalar

Interest rate received on the cash flows upon reinvestment

## Returns

out : float
Modified internal rate of return
numpy . nper (rate, pmt, $p v, f v=0$, when ='end')
Compute the number of periodic payments.

## Parameters

rate : array_like
Rate of interest (per period)
pmt : array_like
Payment
pv : array_like
Present value
fv : array_like, optional
Future value
when : $\{$ \{'begin', 1$\}$, $\{$ 'end', 0$\}\}$, $\{$ string, int $\}$, optional
When payments are due ('begin' (1) or 'end' (0))

## Notes

The number of periods nper is computed by solving the equation:

```
fv + pv*(1+rate)**nper + pmt*(1+rate*when)/rate*((1+rate)**nper-1) = 0
```

but if rate $=0$ then:

```
fv + pv + pmt*nper = 0
```


## Examples

If you only had $\$ 150 /$ month to pay towards the loan, how long would it take to pay-off a loan of $\$ 8,000$ at $7 \%$ annual interest?

```
>>> np.nper(0.07/12, -150, 8000)
64.073348770661852
```

So, over 64 months would be required to pay off the loan.
The same analysis could be done with several different interest rates and/or payments and/or total amounts to produce an entire table.

```
>>> np.nper(*(np.ogrid[0.07/12: 0.08/12: 0.01/12,
... -150 : -99 : 50 ,
... 8000 : 9001 : 1000]))
array([[[ 64.07334877, 74.06368256],
    [ 108.07548412, 127.99022654]],
    [[ 66.12443902, 76.87897353],
    [ 114.70165583, 137.90124779]]])
```

numpy.rate (nper, pmt, pv, fv, when='end', guess=0.10000000000000001, tol=9.9999999999999995e-07,
maxiter $=100$ )

Compute the rate of interest per period.

## Parameters

nper : array_like
Number of compounding periods
pmt : array_like
Payment
pv : array_like
Present value
fv : array_like
Future value
when : $\{$ 'begin', 1$\},\{$ 'end', 0$\}\}$, $\{$ string, int $\}$, optional
When payments are due ('begin' (1) or 'end' (0))
guess : float, optional
Starting guess for solving the rate of interest
tol : float, optional
Required tolerance for the solution
maxiter : int, optional
Maximum iterations in finding the solution

## Notes

The rate of interest is computed by iteratively solving the (non-linear) equation:

```
fv + pv*(1+rate)**nper + pmt*(1+rate*when)/rate * ((1+rate)**nper - 1) = 0
```

for rate.

## References

Wheeler, D. A., E. Rathke, and R. Weir (Eds.) (2009, May). Open Document Format for Office Applications (OpenDocument)v1.2, Part 2: Recalculated Formula (OpenFormula) Format - Annotated Version, PreDraft 12. Organization for the Advancement of Structured Information Standards (OASIS). Billerica, MA, USA. [ODT Document]. Available: http://www.oasis-open.org/committees/documents.php?wg_abbrev=officeformula OpenDocument-formula-20090508.odt

### 3.17 Set routines

### 3.17.1 Making proper sets

unique(ar[, return_index, return_inverse]) $\quad$ Find the unique elements of an array.
numpy.unique (ar, return_index=False, return_inverse $=$ False )
Find the unique elements of an array.
Returns the sorted unique elements of an array. There are two optional outputs in addition to the unique elements: the indices of the input array that give the unique values, and the indices of the unique array that reconstruct the input array.

## Parameters

ar : array_like
Input array. This will be flattened if it is not already 1-D.
return_index : bool, optional
If True, also return the indices of $a r$ that result in the unique array.
return_inverse : bool, optional
If True, also return the indices of the unique array that can be used to reconstruct $a r$.

## Returns

unique : ndarray
The sorted unique values.
unique_indices : ndarray, optional
The indices of the unique values in the (flattened) original array. Only provided if return_index is True.
unique_inverse : ndarray, optional
The indices to reconstruct the (flattened) original array from the unique array. Only provided if return_inverse is True.

## See Also:

## numpy.lib.arraysetops

Module with a number of other functions for performing set operations on arrays.

## Examples

```
>>> np.unique([1, 1, 2, 2, 3, 3])
array([1, 2, 3])
>>> a = np.array([[1, 1], [2, 3]])
>>> np.unique(a)
array([1, 2, 3])
```

Return the indices of the original array that give the unique values:

```
>>> a = np.array(['a', 'b', 'b', 'c', 'a'])
>>> u, indices = np.unique(a, return_index=True)
>>> u
array(['a', 'b', 'c'],
    dtype='|S1')
>>> indices
array([0, 1, 3])
>>> a[indices]
array(['a', 'b', 'c'],
    dtype='|S1')
```

Reconstruct the input array from the unique values:

```
>>> a = np.array([1, 2, 6, 4, 2, 3, 2])
>>> u, indices = np.unique(a, return_inverse=True)
>>> u
array([1, 2, 3, 4, 6])
>>> indices
array([0, 1, 4, 3, 1, 2, 1])
```

```
>>> u[indices]
array([1, 2, 6, 4, 2, 3, 2])
```


### 3.17.2 Boolean operations

```
in1d(ar1, ar2[, assume_unique]) Test whether each element of a 1D array is also present in a second
array.
intersect1d(ar1, ar2[, Find the intersection of two arrays.
assume_unique])
setdiff1d(ar1, ar2[, assume_unique]) Find the set difference of two arrays.
setxor1d(ar1, ar2[, assume_unique]) Find the set exclusive-or of two arrays.
union1d(ar1, ar2) Find the union of two arrays.
```

numpy.in1d (ar1, ar2, assume_unique=False)
Test whether each element of a 1D array is also present in a second array.
Returns a boolean array the same length as arl that is True where an element of arl is in ar2 and False otherwise.

## Parameters

ar1 : array_like, shape (M,)
Input array.
ar2 : array_like
The values against which to test each value of arl.
assume_unique : bool, optional
If True, the input arrays are both assumed to be unique, which can speed up the calculation. Default is False.

## Returns

mask : ndarray of bools, shape(M,)
The values arl[mask] are in ar2.

## See Also:

## numpy.lib.arraysetops

Module with a number of other functions for performing set operations on arrays.

## Notes

inld can be considered as an element-wise function version of the python keyword in, for 1D sequences. inld(a, b) is roughly equivalent to np.array ([item in b for item in a]). New in version 1.4.0.

## Examples

```
>>> test = np.array([0, 1, 2, 5, 0])
>>> states = [0, 2]
>>> mask = np.in1d(test, states)
>>> mask
array([ True, False, True, False, True], dtype=bool)
>>> test[mask]
array([0, 2, 0])
```

numpy.intersect1d(ar1, ar2, assume_unique=False)
Find the intersection of two arrays.
Return the sorted, unique values that are in both of the input arrays.

## Parameters

ar1, ar2 : array_like
Input arrays.
assume_unique : bool
If True, the input arrays are both assumed to be unique, which can speed up the calculation. Default is False.

## Returns

out : ndarray
Sorted 1D array of common and unique elements.

## See Also:

numpy.lib.arraysetops
Module with a number of other functions for performing set operations on arrays.

## Examples

```
>>> np.intersect1d([1, 3, 4, 3], [3, 1, 2, 1])
array([1, 3])
```

numpy.setdiffid (ar1, ar2, assume_unique=False)
Find the set difference of two arrays.
Return the sorted, unique values in arl that are not in ar2.

## Parameters

ar1: array_like
Input array.
ar2 : array_like
Input comparison array.
assume_unique : bool
If True, the input arrays are both assumed to be unique, which can speed up the calculation. Default is False.

## Returns

difference : ndarray
Sorted 1D array of values in arl that are not in ar2.
See Also:
numpy.lib.arraysetops
Module with a number of other functions for performing set operations on arrays.
Examples

```
>>> a = np.array([1, 2, 3, 2, 4, 1])
>>> b = np.array([3, 4, 5, 6])
>>> np.setdiff1d(a, b)
array([1, 2])
```

numpy.setxor1d (ar1, ar2, assume_unique=False)

Find the set exclusive-or of two arrays.
Return the sorted, unique values that are in only one (not both) of the input arrays.

## Parameters

ar1, ar2 : array_like
Input arrays.
assume_unique : bool
If True, the input arrays are both assumed to be unique, which can speed up the calculation. Default is False.

## Returns

xor : ndarray
Sorted 1D array of unique values that are in only one of the input arrays.

## Examples

```
>>> a = np.array([1, 2, 3, 2, 4])
>>> b = np.array([2, 3, 5, 7, 5])
>>> np.setxor1d(a,b)
array([1, 4, 5, 7])
```

numpy. union1d (arl, ar2)
Find the union of two arrays.
Return the unique, sorted array of values that are in either of the two input arrays.

## Parameters

ar1, ar2 : array_like
Input arrays. They are flattened if they are not already 1D.

## Returns

union : ndarray
Unique, sorted union of the input arrays.

## See Also:

numpy.lib.arraysetops
Module with a number of other functions for performing set operations on arrays.
Examples

```
>>> np.union1d([-1, 0, 1], [-2, 0, 2])
array([-2, -1, 0, 1, 2])
```


### 3.18 Window functions

### 3.18.1 Various windows

| bartlett(M) | Return the Bartlett window. |
| :--- | :--- |
| blackman(M) | Return the Blackman window. |
| hamming(M) | Return the Hamming window. |
| hanning(M) | Return the Hanning window. |
| kaiser(M, beta) | Return the Kaiser window. |
| numpy.bartlett $(M)$ |  |
| Return the Bartlett window. |  |

The Bartlett window is very similar to a triangular window, except that the end points are at zero. It is often used in signal processing for tapering a signal, without generating too much ripple in the frequency domain.

## Parameters

$\mathbf{M}$ : int
Number of points in the output window. If zero or less, an empty array is returned.

## Returns

out : array
The triangular window, normalized to one (the value one appears only if the number of samples is odd), with the first and last samples equal to zero.

## See Also:

blackman, hamming, hanning, kaiser

## Notes

The Bartlett window is defined as

$$
w(n)=\frac{2}{M-1}\left(\frac{M-1}{2}-\left|n-\frac{M-1}{2}\right|\right)
$$

Most references to the Bartlett window come from the signal processing literature, where it is used as one of many windowing functions for smoothing values. Note that convolution with this window produces linear interpolation. It is also known as an apodization (which means"removing the foot", i.e. smoothing discontinuities at the beginning and end of the sampled signal) or tapering function. The fourier transform of the Bartlett is the product of two sinc functions. Note the excellent discussion in Kanasewich.

## References

[R11], [R12], [R13], [R14], [R15]

## Examples

```
>>> np.bartlett(12)
array([ 0. , 0.18181818, 0.36363636, 0.54545455, 0.72727273,
    0.90909091, 0.90909091, 0.72727273, 0.54545455, 0.36363636,
    0.18181818, 0. ])
```

Plot the window and its frequency response (requires SciPy and matplotlib):

```
>>> from numpy import clip, log10, array, bartlett, linspace
>>> from numpy.fft import fft, fftshift
>>> import matplotlib.pyplot as plt
>>> window = bartlett(51)
>>> plt.plot(window)
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.title("Bartlett window")
<matplotlib.text.Text object at 0x...>
>>> plt.ylabel("Amplitude")
<matplotlib.text.Text object at 0x...>
>>> plt.xlabel("Sample")
<matplotlib.text.Text object at 0x...>
>>> plt.show()
```



```
>>> plt.figure()
<matplotlib.figure.Figure object at 0x...>
>>> A = fft(window, 2048) / 25.5
>>> mag = abs(fftshift(A))
>>> freq = linspace(-0.5,0.5,len(A))
>>> response = 20*log10(mag)
>>> response = clip(response,-100,100)
>>> plt.plot(freq, response)
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.title("Frequency response of Bartlett window")
<matplotlib.text.Text object at 0x...>
>>> plt.ylabel("Magnitude [dB]")
<matplotlib.text.Text object at 0x...>
>>> plt.xlabel("Normalized frequency [cycles per sample]")
<matplotlib.text.Text object at 0x...>
>>> plt.axis('tight')
(-0.5, 0.5, -100.0, ...)
>>> plt.show()
```


numpy.blackman ( $M$ )
Return the Blackman window.
The Blackman window is a taper formed by using the the first three terms of a summation of cosines. It was designed to have close to the minimal leakage possible. It is close to optimal, only slightly worse than a Kaiser window.

## Parameters

M : int
Number of points in the output window. If zero or less, an empty array is returned.

## Returns

out : ndarray
The window, normalized to one (the value one appears only if the number of samples is odd).

## See Also:

bartlett, hamming, hanning, kaiser

## Notes

The Blackman window is defined as

$$
w(n)=0.42-0.5 \cos (2 \pi n / M)+0.08 \cos (4 \pi n / M)
$$

Most references to the Blackman window come from the signal processing literature, where it is used as one of many windowing functions for smoothing values. It is also known as an apodization (which means "removing the foot", i.e. smoothing discontinuities at the beginning and end of the sampled signal) or tapering function. It is known as a "near optimal" tapering function, almost as good (by some measures) as the kaiser window.

## References

Blackman, R.B. and Tukey, J.W., (1958) The measurement of power spectra, Dover Publications, New York.
Oppenheim, A.V., and R.W. Schafer. Discrete-Time Signal Processing. Upper Saddle River, NJ: Prentice-Hall, 1999, pp. 468-471.

## Examples

```
>>> from numpy import blackman
>>> blackman(12)
array([ -1.38777878e-17, 3.26064346e-02, 1.59903635e-01,
    4.14397981e-01, 7.36045180e-01, 9.67046769e-01,
    9.67046769e-01, 7.36045180e-01, 4.14397981e-01,
    1.59903635e-01, 3.26064346e-02, -1.38777878e-17])
```

Plot the window and the frequency response:

```
>>> from numpy import clip, log10, array, blackman, linspace
>>> from numpy.fft import fft, fftshift
>>> import matplotlib.pyplot as plt
>>> window = blackman(51)
>>> plt.plot(window)
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.title("Blackman window")
<matplotlib.text.Text object at 0x...>
>>> plt.ylabel("Amplitude")
<matplotlib.text.Text object at 0x...>
>>> plt.xlabel("Sample")
<matplotlib.text.Text object at 0x...>
>>> plt.show()
```



```
>>> plt.figure()
<matplotlib.figure.Figure object at 0x...>
>>> A = fft(window, 2048) / 25.5
>>> mag = abs(fftshift(A))
>>> freq = linspace(-0.5,0.5,len(A))
>>> response = 20*log10(mag)
>>> response = clip(response,-100,100)
>>> plt.plot(freq, response)
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.title("Frequency response of Blackman window")
<matplotlib.text.Text object at 0x...>
>>> plt.ylabel("Magnitude [dB]")
<matplotlib.text.Text object at 0x...>
```

```
>>> plt.xlabel("Normalized frequency [cycles per sample]")
<matplotlib.text.Text object at 0x...>
>>> plt.axis('tight')
(-0.5, 0.5, -100.0, ...)
>>> plt.show()
```


numpy.hamming ( $M$ )
Return the Hamming window.
The Hamming window is a taper formed by using a weighted cosine.

## Parameters

M : int
Number of points in the output window. If zero or less, an empty array is returned.

## Returns

out : ndarray
The window, normalized to one (the value one appears only if the number of samples is odd).

## See Also:

bartlett, blackman, hanning, kaiser

## Notes

The Hamming window is defined as

$$
w(n)=0.54+0.46 \cos \left(\frac{2 \pi n}{M-1}\right) \quad 0 \leq n \leq M-1
$$

The Hamming was named for R. W. Hamming, an associate of J. W. Tukey and is described in Blackman and Tukey. It was recommended for smoothing the truncated autocovariance function in the time domain. Most references to the Hamming window come from the signal processing literature, where it is used as one of many windowing functions for smoothing values. It is also known as an apodization (which means "removing the foot", i.e. smoothing discontinuities at the beginning and end of the sampled signal) or tapering function.

## References

[R20], [R21], [R22], [R23]

## Examples

```
>>> np.hamming(12)
array([ 0.08 , 0.15302337, 0.34890909, 0.60546483, 0.84123594,
    0.98136677, 0.98136677, 0.84123594, 0.60546483, 0.34890909,
    0.15302337, 0.08 ])
```

Plot the window and the frequency response:

```
>>> from numpy.fft import fft, fftshift
>>> import matplotlib.pyplot as plt
>>> window = np.hamming(51)
>>> plt.plot(window)
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.title("Hamming window")
<matplotlib.text.Text object at 0x...>
>>> plt.ylabel("Amplitude")
<matplotlib.text.Text object at 0x...>
>>> plt.xlabel("Sample")
<matplotlib.text.Text object at 0x...>
>>> plt.show()
```



```
>>> plt.figure()
<matplotlib.figure.Figure object at 0x...>
>>> A = fft(window, 2048) / 25.5
>>> mag = np.abs(fftshift(A))
>>> freq = np.linspace(-0.5, 0.5, len(A))
>>> response = 20 * np.log10(mag)
>>> response = np.clip(response, -100, 100)
>>> plt.plot(freq, response)
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.title("Frequency response of Hamming window")
<matplotlib.text.Text object at 0x...>
>>> plt.ylabel("Magnitude [dB]")
```

```
<matplotlib.text.Text object at 0x...>
>>> plt.xlabel("Normalized frequency [cycles per sample]")
<matplotlib.text.Text object at 0x...>
>>> plt.axis('tight')
(-0.5, 0.5, -100.0, ...)
>>> plt.show()
```


numpy. hanning ( $M$ )
Return the Hanning window.
The Hanning window is a taper formed by using a weighted cosine.

## Parameters

M : int
Number of points in the output window. If zero or less, an empty array is returned.

## Returns

out : ndarray, shape(M,)
The window, normalized to one (the value one appears only if $M$ is odd).

## See Also:

bartlett, blackman, hamming, kaiser

## Notes

The Hanning window is defined as

$$
w(n)=0.5-0.5 \cos \left(\frac{2 \pi n}{M-1}\right) \quad 0 \leq n \leq M-1
$$

The Hanning was named for Julius van Hann, an Austrian meterologist. It is also known as the Cosine Bell. Some authors prefer that it be called a Hann window, to help avoid confusion with the very similar Hamming window.

Most references to the Hanning window come from the signal processing literature, where it is used as one of many windowing functions for smoothing values. It is also known as an apodization (which means "removing the foot", i.e. smoothing discontinuities at the beginning and end of the sampled signal) or tapering function.

## References

[R24], [R25], [R26], [R27]

## Examples

```
>>> from numpy import hanning
>>> hanning(12)
array([ 0. , 0.07937323, 0.29229249, 0.57115742, 0.82743037,
    0.97974649, 0.97974649, 0.82743037, 0.57115742, 0.29229249,
    0.07937323, 0. ])
```

Plot the window and its frequency response:

```
>>> from numpy.fft import fft, fftshift
>>> import matplotlib.pyplot as plt
>>> window = np.hanning(51)
>>> plt.plot(window)
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.title("Hann window")
<matplotlib.text.Text object at 0x...>
>>> plt.ylabel("Amplitude")
<matplotlib.text.Text object at 0x...>
>>> plt.xlabel("Sample")
<matplotlib.text.Text object at 0x...>
>>> plt.show()
```



```
>>> plt.figure()
<matplotlib.figure.Figure object at 0x...>
>>> A = fft(window, 2048) / 25.5
>>> mag = abs(fftshift(A))
>>> freq = np.linspace(-0.5,0.5,len(A))
>>> response = 20*np.log10(mag)
>>> response = np.clip(response,-100,100)
>>> plt.plot(freq, response)
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.title("Frequency response of the Hann window")
<matplotlib.text.Text object at 0x...>
```

```
>>> plt.ylabel("Magnitude [dB]")
<matplotlib.text.Text object at 0x...>
>>> plt.xlabel("Normalized frequency [cycles per sample]")
<matplotlib.text.Text object at 0x...>
>>> plt.axis('tight')
(-0.5, 0.5, -100.0, ...)
>>> plt.show()
```


numpy.kaiser ( $M$, beta)
Return the Kaiser window.
The Kaiser window is a taper formed by using a Bessel function.

## Parameters

M : int
Number of points in the output window. If zero or less, an empty array is returned.
beta : float
Shape parameter for window.

## Returns

out : array
The window, normalized to one (the value one appears only if the number of samples is odd).

## See Also:

bartlett, blackman, hamming, hanning

## Notes

The Kaiser window is defined as

$$
w(n)=I_{0}\left(\beta \sqrt{1-\frac{4 n^{2}}{(M-1)^{2}}}\right) / I_{0}(\beta)
$$

with

$$
-\frac{M-1}{2} \leq n \leq \frac{M-1}{2},
$$

where $I_{0}$ is the modified zeroth-order Bessel function.
The Kaiser was named for Jim Kaiser, who discovered a simple approximation to the DPSS window based on Bessel functions. The Kaiser window is a very good approximation to the Digital Prolate Spheroidal Sequence, or Slepian window, which is the transform which maximizes the energy in the main lobe of the window relative to total energy.

The Kaiser can approximate many other windows by varying the beta parameter.

| beta | Window shape |
| :--- | :--- |
| 0 | Rectangular |
| 5 | Similar to a Hamming |
| 6 | Similar to a Hanning |
| 8.6 | Similar to a Blackman |

A beta value of 14 is probably a good starting point. Note that as beta gets large, the window narrows, and so the number of samples needs to be large enough to sample the increasingly narrow spike, otherwise nans will get returned.

Most references to the Kaiser window come from the signal processing literature, where it is used as one of many windowing functions for smoothing values. It is also known as an apodization (which means "removing the foot", i.e. smoothing discontinuities at the beginning and end of the sampled signal) or tapering function.

## References

[R33], [R34], [R35]

## Examples

```
>>> from numpy import kaiser
>>> kaiser(12, 14)
array([ 7.72686684e-06, 3.46009194e-03, 4.65200189e-02,
    2.29737120e-01, 5.99885316e-01, 9.45674898e-01,
    9.45674898e-01, 5.99885316e-01, 2.29737120e-01,
    4.65200189e-02, 3.46009194e-03, 7.72686684e-06])
```

Plot the window and the frequency response:

```
>>> from numpy import clip, log10, array, kaiser, linspace
>>> from numpy.fft import fft, fftshift
>>> import matplotlib.pyplot as plt
>>> window = kaiser(51, 14)
>>> plt.plot(window)
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.title("Kaiser window")
<matplotlib.text.Text object at 0x...>
>>> plt.ylabel("Amplitude")
<matplotlib.text.Text object at 0x...>
>>> plt.xlabel("Sample")
<matplotlib.text.Text object at 0x...>
>>> plt.show()
```



```
>>> plt.figure()
<matplotlib.figure.Figure object at 0x...>
>>> A = fft(window, 2048) / 25.5
>>> mag = abs(fftshift(A))
>>> freq = linspace(-0.5,0.5,len(A))
>>> response = 20*log10(mag)
>>> response = clip(response,-100,100)
>>> plt.plot(freq, response)
[<matplotlib.lines.Line2D object at 0x...>]
>>> plt.title("Frequency response of Kaiser window")
<matplotlib.text.Text object at 0x...>
>>> plt.ylabel("Magnitude [dB]")
<matplotlib.text.Text object at 0x...>
>>> plt.xlabel("Normalized frequency [cycles per sample]")
<matplotlib.text.Text object at 0x...>
>>> plt.axis('tight')
(-0.5, 0.5, -100.0, ...)
>>> plt.show()
```



### 3.19 Floating point error handling

### 3.19.1 Setting and getting error handling

```
seterr([all, divide, over, under, invalid]) Set how floating-point errors are handled.
geterr() Get the current way of handling floating-point errors.
seterrcall(func) Set the floating-point error callback function or log object.
geterrcall() Return the current callback function used on floating-point errors.
errstate(**kwargs) Context manager for floating-point error handling.
numpy. seterr (all=None, divide=None, over=None, under=None, invalid=None)
Set how floating-point errors are handled.
Note that operations on integer scalar types (such as int16) are handled like floating point, and are affected by these settings.
```


## Parameters

all : \{ 'ignore', 'warn', 'raise', 'call', 'print', 'log'\}, optional Set treatment for all types of floating-point errors at once:

- ignore: Take no action when the exception occurs.
- warn: Print a RuntimeWarning (via the Python warnings module).
- raise: Raise a FloatingPointError.
- call: Call a function specified using the seterrcall function.
- print: Print a warning directly to stdout.
- log: Record error in a Log object specified by seterrcall.

The default is not to change the current behavior.
divide : \{ 'ignore', 'warn', 'raise', 'call', 'print', 'log'\}, optional
Treatment for division by zero.
over : \{ 'ignore', 'warn', 'raise', 'call', 'print', 'log'\}, optional
Treatment for floating-point overflow.
under : \{ 'ignore', 'warn', 'raise', 'call', 'print', 'log'\}, optional
Treatment for floating-point underflow.
invalid : \{ 'ignore', 'warn', 'raise', 'call', 'print', 'log'\}, optional
Treatment for invalid floating-point operation.
Returns
old_settings : dict
Dictionary containing the old settings.

## See Also:

seterrcall
Set a callback function for the 'call' mode.
geterr, geterrcall

## Notes

The floating-point exceptions are defined in the IEEE 754 standard [1]:
-Division by zero: infinite result obtained from finite numbers.

- Overflow: result too large to be expressed.
-Underflow: result so close to zero that some precision was lost.
-Invalid operation: result is not an expressible number, typically indicates that a NaN was produced.


## Examples

```
>>> old_settings = np.seterr(all='ignore') #seterr to known value
>>> np.seterr(over='raise')
{'over': 'ignore', 'divide': 'ignore', 'invalid': 'ignore',
    'under': 'ignore'}
>>> np.seterr(all='ignore') # reset to default
{'over': 'raise', 'divide': 'ignore', 'invalid': 'ignore', 'under': 'ignore' }
>>> np.int16(32000) * np.int16(3)
30464
>>> old_settings = np.seterr(all='warn', over='raise')
>>> np.int16(32000) * np.int16(3)
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
FloatingPointError: overflow encountered in short_scalars
>>> old_settings = np.seterr(all='print')
>>> np.geterr()
{'over': 'print', 'divide': 'print', 'invalid': 'print', 'under': 'print'}
>>> np.int16(32000) * np.int16(3)
Warning: overflow encountered in short_scalars
30464
```

numpy.geterr()

Get the current way of handling floating-point errors.

## Returns

 res : dictA dictionary with keys "divide", "over", "under", and "invalid", whose values are from the strings "ignore", "print", "log", "warn", "raise", and "call". The keys represent possible floating-point exceptions, and the values define how these exceptions are handled.

## See Also:

```
geterrcall, seterr,seterrcall
```


## Notes

For complete documentation of the types of floating-point exceptions and treatment options, see seterr.

## Examples

```
>>> np.geterr()
{'over': 'warn', 'divide': 'warn', 'invalid': 'warn',
'under': 'ignore'}
>>> np.arange(3.) / np.arange(3.)
array([ NaN, 1., 1.])
```

```
>>> oldsettings = np.seterr(all='warn', over='raise')
>>> np.geterr()
{'over': 'raise', 'divide': 'warn', 'invalid': 'warn', 'under': 'warn'}
>>> np.arange(3.) / np.arange(3.)
__main__:1: RuntimeWarning: invalid value encountered in divide
array([ NaN, 1., 1.])
numpy.seterrcall (func)
```

Set the floating-point error callback function or log object.
There are two ways to capture floating-point error messages. The first is to set the error-handler to 'call', using seterr. Then, set the function to call using this function.

The second is to set the error-handler to 'log', using seterr. Floating-point errors then trigger a call to the 'write' method of the provided object.

## Parameters

func : callable $f(e r r$, flag $)$ or object with write method
Function to call upon floating-point errors ('call'-mode) or object whose 'write' method is used to log such message ('log'-mode).
The call function takes two arguments. The first is the type of error (one of "divide", "over", "under", or "invalid"), and the second is the status flag. The flag is a byte, whose least-significant bits indicate the status:
[0 0 0 0 invalid over under invalid]
In other words, flags $=$ divide +2 *over +4 *under +8 *invalid.
If an object is provided, its write method should take one argument, a string.

## Returns

h: callable, log instance or None
The old error handler.

## See Also:

```
seterr,geterr,geterrcall
```


## Examples

Callback upon error:

```
>>> def err_handler(type, flag):
... print "Floating point error (%S), with flag %s" % (type, flag)
...
>>> saved_handler = np.seterrcall(err_handler)
>>> save_err = np.seterr(all='call')
>>> np.array([1, 2, 3]) / 0.0
Floating point error (divide by zero), with flag 1
array([ Inf, Inf, Inf])
>>> np.seterrcall(saved_handler)
<function err_handler at 0x...>
>>> np.seterr(**save_err)
{'over': 'call', 'divide': 'call', 'invalid': 'call', 'under': 'call' }
```

Log error message:

```
>>> class Log(object):
... def write(self, msg):
... print "LOG: %S" % msg
...
>>> log = Log()
>>> saved_handler = np.seterrcall(log)
>>> save_err = np.seterr(all='log')
>>> np.array([1, 2, 3]) / 0.0
LOG: Warning: divide by zero encountered in divide
<BLANKLINE>
array([ Inf, Inf, Inf])
>>> np.seterrcall(saved_handler)
<__main__.Log object at 0x...>
>>> np.seterr(**save_err)
{'over': 'log', 'divide': 'log', 'invalid': 'log', 'under': 'log'}
```

numpy.geterrcall()
Return the current callback function used on floating-point errors.
When the error handling for a floating-point error (one of "divide", "over", "under", or "invalid") is set to 'call' or 'log', the function that is called or the log instance that is written to is returned by geterrcall. This function or log instance has been set with seterrcall.

## Returns

errobj: callable, log instance or None
The current error handler. If no handler was set through seterrcall, None is returned.

## See Also:

```
seterrcall, seterr,geterr
```


## Notes

For complete documentation of the types of floating-point exceptions and treatment options, see seterr.

## Examples

```
>>> np.geterrcall() # we did not yet set a handler, returns None
>>> oldsettings = np.seterr(all='call')
>>> def err_handler(type, flag):
... print "Floating point error (%s), with flag %s" % (type, flag)
>>> oldhandler = np.seterrcall(err_handler)
>>> np.array([1, 2, 3]) / 0.0
Floating point error (divide by zero), with flag 1
array([ Inf, Inf, Inf])
>>> cur_handler = np.geterrcall()
>>> cur_handler is err_handler
True
```

class numpy. errstate (**kwargs)
Context manager for floating-point error handling.

Using an instance of errstate as a context manager allows statements in that context to execute with a known error handling behavior. Upon entering the context the error handling is set with seterr and seterrcall, and upon exiting it is reset to what it was before.

## Parameters

kwargs : \{divide, over, under, invalid\}
Keyword arguments. The valid keywords are the possible floating-point exceptions. Each keyword should have a string value that defines the treatment for the particular error. Possible values are \{ 'ignore', 'warn', 'raise', 'call', 'print', 'log'\}.

## See Also:

```
seterr,geterr,seterrcall,geterrcall
```


## Notes

The with statement was introduced in Python 2.5, and can only be used there by importing it: from __future__ import with_statement. In earlier Python versions the with statement is not available.

For complete documentation of the types of floating-point exceptions and treatment options, see seterr.

## Examples

```
>>> from __future__ import with_statement # use 'with' in Python 2.5
>>> olderr = np.seterr(all='ignore') # Set error handling to known state.
>>> np.arange(3) / 0.
array([ NaN, Inf, Inf])
>>> with np.errstate(divide='warn'):
... np.arange(3) / 0.
. .
__main__:2: RuntimeWarning: divide by zero encountered in divide
array([ NaN, Inf, Inf])
>>> np.sqrt(-1)
nan
>>> with np.errstate(invalid='raise'):
... np.sqrt(-1)
Traceback (most recent call last):
    File "<stdin>", line 2, in <module>
FloatingPointError: invalid value encountered in sqrt
```

Outside the context the error handling behavior has not changed:

```
>>> np.geterr()
{'over': 'warn', 'divide': 'warn', 'invalid': 'warn',
'under': 'ignore'}
```


### 3.19.2 Internal functions

```
seterrobj(errobj) Set the object that defines floating-point error handling.
geterrobj() Return the current object that defines floating-point error handling.
```

numpy.seterrobj (errobj)
Set the object that defines floating-point error handling.
The error object contains all information that defines the error handling behavior in Numpy. seterrobj is used internally by the other functions that set error handling behavior (seterr, seterrcall).

## Parameters

errobj : list
The error object, a list containing three elements: [internal numpy buffer size, error mask, error callback function].
The error mask is a single integer that holds the treatment information on all four floating point errors. The information for each error type is contained in three bits of the integer. If we print it in base 8, we can see what treatment is set for "invalid", "under", "over", and "divide" (in that order). The printed string can be interpreted with

- 0 : 'ignore’
- 1 : 'warn’
- 2 : 'raise’
- 3 : ‘call’
- 4 : 'print'
- 5 : 'log'


## See Also:

geterrobj, seterr, geterr, seterrcall, geterrcall, getbufsize, setbufsize

## Notes

For complete documentation of the types of floating-point exceptions and treatment options, see seterr.

## Examples

```
>>> old_errobj = np.geterrobj() # first get the defaults
>>> old_errobj
[10000, 0, None]
>>> def err_handler(type, flag):
... print "Floating point error (%S), with flag %s" % (type, flag)
...
>>> new_errobj = [20000, 12, err_handler]
>>> np.seterrobj(new_errobj)
>>> np.base_repr(12, 8) # int for divide=4 ('print') and over=1 ('warn')
'14'
>>> np.geterr()
{'over': 'warn', 'divide': 'print', 'invalid': 'ignore', 'under': 'ignore'}
>>> np.geterrcall() is err_handler
True
```

numpy.geterrobj()

Return the current object that defines floating-point error handling.
The error object contains all information that defines the error handling behavior in Numpy. geterrobj is used internally by the other functions that get and set error handling behavior (geterr, seterr, geterrcall, seterrcall).

## Returns

errobj : list
The error object, a list containing three elements: [internal numpy buffer size, error mask, error callback function].
The error mask is a single integer that holds the treatment information on all four floating point errors. The information for each error type is contained in three bits of the
integer. If we print it in base 8, we can see what treatment is set for "invalid", "under", "over", and "divide" (in that order). The printed string can be interpreted with

- 0 : 'ignore'
- 1 : 'warn’
- 2 : 'raise'
- 3 : 'call'
- 4 : 'print'
- 5 : 'log’


## See Also:

```
seterrobj, seterr,geterr, seterrcall, geterrcall, getbufsize, setbufsize
```


## Notes

For complete documentation of the types of floating-point exceptions and treatment options, see seterr.

## Examples

```
>>> np.geterrobj() # first get the defaults
[10000, 0, None]
>>> def err_handler(type, flag):
... print "Floating point error (%S), with flag %s" % (type, flag)
...
>>> old_bufsize = np.setbufsize(20000)
>>> old_err = np.seterr(divide='raise')
>>> old_handler = np.seterrcall(err_handler)
>>> np.geterrobj()
[20000, 2, <function err_handler at 0x91dcaac>]
>>> old_err = np.seterr(all='ignore')
>>> np.base_repr(np.geterrobj()[1], 8)
'0'
>>> old_err = np.seterr(divide='warn', over=' log', under='call',
    invalid='print')
>>> np.base_repr(np.geterrobj()[1], 8)
'4351'
```


### 3.20 Masked array operations

### 3.20.1 Constants

[^4]
### 3.20.2 Creation

## From existing data

```
ma.masked_array An array class with possibly masked values.
ma. array(data[, dtype, copy, order, mask, ...]) An array class with possibly masked values.
ma.copy
copy
ma.frombuffer(buffer[, dtype, count, offset]) Interpret a buffer as a 1-dimensional array.
ma.fromfunction(function, shape, **kwargs) Construct an array by executing a function over each coordinate.
ma.MaskedArray.copy([order]) Return a copy of the array.
```

numpy.ma.masked_array
alias of MaskedArray
numpy.ma.array (data, dtype=None, copy=False, order=False, mask=False, fill_value=None,
keep_mask=True, hard_mask=False, shrink=True, subok=True, ndmin=0)

An array class with possibly masked values.
Masked values of True exclude the corresponding element from any computation.
Construction

```
x = MaskedArray(data, mask=nomask, dtype=None,
copy=False, subok=True, ndmin=0, fill_value=None,
keep_mask=True, hard_mask=None, shrink=True)
```


## Parameters

data : array_like
Input data.
mask : sequence, optional
Mask. Must be convertible to an array of booleans with the same shape as data. True indicates a masked (i.e. invalid) data.
dtype : dtype, optional
Data type of the output. If dtype is None, the type of the data argument (data.dtype) is used. If dtype is not None and different from data.dtype, a copy is performed.
copy : bool, optional
Whether to copy the input data (True), or to use a reference instead. Default is False.
subok : bool, optional
Whether to return a subclass of MaskedArray if possible (True) or a plain MaskedArray. Default is True.
ndmin : int, optional
Minimum number of dimensions. Default is 0 .
fill_value : scalar, optional
Value used to fill in the masked values when necessary. If None, a default based on the data-type is used.
keep_mask : bool, optional
Whether to combine mask with the mask of the input data, if any (True), or to use only mask for the output (False). Default is True.
hard_mask : bool, optional
Whether to use a hard mask or not. With a hard mask, masked values cannot be unmasked. Default is False.
shrink : bool, optional
Whether to force compression of an empty mask. Default is True.

```
numpy.ma.copy
    copy a.copy(order='C')
            Return a copy of the array.
```


## Parameters

```
order : \{ ' \(C\) ', ' \(F\) ', ' \(A\) ' \(\}\), optional has the same order as the input.
Examples
```

```
>>> x = np.array([[1,2,3],[4,5,6]], order='F')
```

>>> x = np.array([[1,2,3],[4,5,6]], order='F')
>>> y = x.copy()
>>> y = x.copy()
>>> x.fill(0)
>>> x.fill(0)
>>> x
>>> x
array([[0, 0, 0],
array([[0, 0, 0],
[0, 0, 0]])
[0, 0, 0]])
>>> y
>>> y
array([[1, 2, 3],
array([[1, 2, 3],
[4, 5, 6]])
[4, 5, 6]])
>>> y.flags['C_CONTIGUOUS']
>>> y.flags['C_CONTIGUOUS']
True

```
True
```

By default, the result is stored in C-contiguous (row-major) order in memory. If order is $F$, the result has 'Fortran' (column-major) order. If order is 'A' ('Any'), then the result
numpy.ma.frombuffer (buffer, dtype=float, count=-1, offset=0)
Interpret a buffer as a 1-dimensional array.

## Parameters

buffer : buffer_like
An object that exposes the buffer interface.
dtype : data-type, optional
Data-type of the returned array; default: float.
count : int, optional
Number of items to read. -1 means all data in the buffer.
offset : int, optional
Start reading the buffer from this offset; default: 0.

## Notes

If the buffer has data that is not in machine byte-order, this should be specified as part of the data-type, e.g.:

```
>>> dt = np.dtype(int)
>>> dt = dt.newbyteorder('>')
>>> np.frombuffer(buf, dtype=dt)
```

The data of the resulting array will not be byteswapped, but will be interpreted correctly.

## Examples

```
>>> s = 'hello world'
>>> np.frombuffer(s, dtype='S1', count=5, offset=6)
array(['w', 'o', 'r', 'l', 'd'],
    dtype='|S1')
```

numpy.ma.fromfunction (function, shape, **kwargs)

Construct an array by executing a function over each coordinate.
The resulting array therefore has a value $f n(x, y, z)$ at coordinate $(x, y, z)$.

## Parameters <br> function : callable

The function is called with N parameters, each of which represents the coordinates of the array varying along a specific axis. For example, if shape were $(2,2)$, then the parameters would be two arrays, [ [0, 0], [1, 1]] and [ [0, 1], [0, 1]]. function must be capable of operating on arrays, and should return a scalar value.
shape : ( N, ) tuple of ints
Shape of the output array, which also determines the shape of the coordinate arrays passed to function.
dtype : data-type, optional
Data-type of the coordinate arrays passed to function. By default, dtype is float.

## Returns

out : any
The result of the call to function is passed back directly. Therefore the type and shape of out is completely determined by function.

## See Also:

indices, meshgrid

## Notes

Keywords other than shape and dtype are passed to function.

## Examples

```
>>> np.fromfunction(lambda i, j: i == j, (3, 3), dtype=int)
array([[ True, False, False],
    [False, True, False],
    [False, False, True]], dtype=bool)
>>> np.fromfunction(lambda i, j: i + j, (3, 3), dtype=int)
array([[0, 1, 2],
```

$[1,2,3]$,
$[2,3,4]])$

MaskedArray. copy (order $=$ ' $C$ ')
Return a copy of the array.

## Parameters

order : $\left\{{ }^{\prime} C\right.$ ', ' $F$ ', ' $A$ ' $\}$, optional
By default, the result is stored in C-contiguous (row-major) order in memory. If order is $F$, the result has 'Fortran' (column-major) order. If order is 'A' ('Any'), then the result has the same order as the input.

## Examples

```
>>> x = np.array([[1,2,3],[4,5,6]], order=' F')
>>> y = x.copy()
>>> x.fill(0)
>>> x
array([[0, 0, 0],
    [0, 0, 0]])
>>> y
array([[1, 2, 3],
    [4, 5, 6]])
>>> y.flags['C_CONTIGUOUS']
True
```


## Ones and zeros

| ma.empty(shape[, dtype, order]) | Return a new array of given shape and type, without initializing entries. |
| :--- | :--- |
| ma.empty_like(a[, dtype, order, subok]) | Return a new array with the same shape and type as a given array. |
| ma.masked_all(shape[, dtype]) | Empty masked array with all elements masked. |
| ma.masked_all_like(arr) | Empty masked array with the properties of an existing array. |
| ma.ones(shape[, dtype, order]) | Return a new array of given shape and type, filled with ones. |
| ma.zeros(shape[, dtype, order]) | Return a new array of given shape and type, filled with zeros. |

numpy.ma. empty (shape, dtype $=$ float, order $=$ ' $C$ ')
Return a new array of given shape and type, without initializing entries.

## Parameters

shape : int or tuple of int
Shape of the empty array
dtype : data-type, optional
Desired output data-type.
order : \{ 'C', 'F' $\}$, optional
Whether to store multi-dimensional data in C (row-major) or Fortran (column-major) order in memory.

## See Also:

empty_like, zeros, ones

## Notes

empty, unlike zeros, does not set the array values to zero, and may therefore be marginally faster. On the other hand, it requires the user to manually set all the values in the array, and should be used with caution.

## Examples

```
>>> np.empty([2, 2])
array([[ -9.74499359e+001, 6.69583040e-309],
    [ 2.13182611e-314, 3.06959433e-309]]) #random
>>> np.empty([2, 2], dtype=int)
array([[-1073741821, -1067949133],
    [ 496041986, 19249760]]) #random
```

numpy.ma.empty_like (a,dtype=None, order=' $K^{\prime}$, subok=True)

Return a new array with the same shape and type as a given array.

## Parameters

a : array_like
The shape and data-type of $a$ define these same attributes of the returned array.
dtype : data-type, optional
Overrides the data type of the result.
order : \{ ' C ', ' $F$ ', ' $A$ ', or ' $K$ ' \}, optional
Overrides the memory layout of the result. ' C ' means C -order, ' F ' means F -order, ' A ' means ' F ' if a is Fortran contiguous, ' C ' otherwise. ' K ' means match the layout of a as closely as possible.
subok : bool, optional.
If True, then the newly created array will use the sub-class type of 'a', otherwise it will be a base-class array. Defaults to True.

## Returns

out : ndarray
Array of uninitialized (arbitrary) data with the same shape and type as $a$.

## See Also:

ones_like
Return an array of ones with shape and type of input.
zeros_like
Return an array of zeros with shape and type of input.
empty
Return a new uninitialized array.
ones
Return a new array setting values to one.
zeros
Return a new array setting values to zero.

## Notes

This function does not initialize the returned array; to do that use zeros_like or ones_like instead. It may be marginally faster than the functions that do set the array values.

## Examples

```
>>> a = ([1,2,3], [4,5,6]) # a is array-like
>>> np.empty_like(a)
array([[-1073741821, -1073741821, 3], #random
    [ 0, 0, -1073741821]])
>>> a = np.array([[1., 2., 3.],[4.,5.,6.]])
>>> np.empty_like(a)
array([[ -2.00000715e+000, 1.48219694e-323, -2.00000572e+000],#random
    [4.38791518e-305, -2.00000715e+000, 4.17269252e-309]])
```

numpy.ma.masked_all (shape, dtype=<type 'float'>)
Empty masked array with all elements masked.
Return an empty masked array of the given shape and dtype, where all the data are masked.

## Parameters

shape : tuple
Shape of the required MaskedArray.
dtype : dtype, optional
Data type of the output.

## Returns

## a: MaskedArray

A masked array with all data masked.

## See Also:

masked_all_like
Empty masked array modelled on an existing array.

## Examples

```
>>> import numpy.ma as ma
>>> ma.masked_all((3, 3))
masked_array(data =
            [[-- -- --]
            [-- -- --]
            [-- -- --]],
                mask =
    [[ True True True]
    [ True True True]
    [ True True True]],
            fill_value=1e+20)
```

The dtype parameter defines the underlying data type.

```
>>> a = ma.masked_all((3, 3))
>>> a.dtype
dtype('float64')
>>> a = ma.masked_all((3, 3), dtype=np.int32)
>>> a.dtype
dtype('int32')
```

numpy.ma.masked_all_like (arr)

Empty masked array with the properties of an existing array.
Return an empty masked array of the same shape and dtype as the array arr, where all the data are masked.

## Parameters

arr: ndarray
An array describing the shape and dtype of the required MaskedArray.

## Returns

a : MaskedArray
A masked array with all data masked.

## Raises

## AttributeError :

If $a r r$ doesn't have a shape attribute (i.e. not an ndarray)

## See Also:

```
masked_all
```

Empty masked array with all elements masked.

## Examples

```
>>> import numpy.ma as ma
>>> arr = np.zeros((2, 3), dtype=np.float 32)
>>> arr
array([[ 0., 0., 0.],
    [ 0., 0., 0.]], dtype=float 32)
>>> ma.masked_all_like(arr)
masked_array(data =
    [[-- -- --]
    [-- -- --]],
            mask =
    [[ True True True]
    [ True True True]],
            fill_value=1e+20)
```

The dtype of the masked array matches the dtype of arr.

```
>>> arr.dtype
dtype('float32')
>>> ma.masked_all_like(arr).dtype
dtype('float32')
numpy.ma. ones (shape,dtype=None, order= 'C')
```

Return a new array of given shape and type, filled with ones.
Please refer to the documentation for zeros for further details.

## See Also:

zeros,ones_like

## Examples

```
>>> np.ones(5)
array([ 1., 1., 1., 1., 1.])
>>> np.ones((5,), dtype=np.int)
array([1, 1, 1, 1, 1])
```

```
>>> np.ones((2, 1))
array([[ 1.],
    [ 1.]])
>>> s=(2,2)
>>> np.ones(s)
array([[ 1., 1.],
    [ 1., 1.]])
```

numpy.ma. zeros (shape, dtype $=$ float, order=' $C^{\prime}$ )

Return a new array of given shape and type, filled with zeros.

## Parameters

shape : int or sequence of ints
Shape of the new array, e.g., $(2,3)$ or 2.
dtype : data-type, optional
The desired data-type for the array, e.g., numpy.int 8. Default is numpy.float 64.
order : \{ 'C', 'F'\}, optional
Whether to store multidimensional data in C - or Fortran-contiguous (row- or columnwise) order in memory.

## Returns

out : ndarray
Array of zeros with the given shape, dtype, and order.

## See Also:

zeros_like
Return an array of zeros with shape and type of input.

## ones_like

Return an array of ones with shape and type of input.
empty_like
Return an empty array with shape and type of input.
ones
Return a new array setting values to one.
empty
Return a new uninitialized array.

## Examples

```
>>> np.zeros(5)
array([ 0., 0., 0., 0., 0.])
>>> np.zeros((5,), dtype=numpy.int)
array([0, 0, 0, 0, 0])
>>> np.zeros((2, 1))
array([[ 0.],
            [ 0.]])
```

```
>>> s = (2,2)
>>> np.zeros(s)
array([[ 0., 0.],
    [ 0., 0.]])
>>> np.zeros((2,), dtype=[('x', 'i4'), ('Y', 'i4')]) # custom dtype
array([(0, 0), (0, 0)],
    dtype=[('x', '<i4'), ('y', '<i4')])
```


### 3.20.3 Inspecting the array

```
ma.all(self[, axis, out]) Check if all of the elements of a are true.
ma. any(self[, axis, out]) Check if any of the elements of }a\mathrm{ are true.
ma.count(a[, axis]) Count the non-masked elements of the array along the given axis.
ma.count_masked(arr[, axis]) Count the number of masked elements along the given axis.
ma.getmask(a)
ma.getmaskarray(arr)
ma.getdata(a[, subok])
ma.nonzero(self)
ma.shape(obj)
ma.size(obj[,axis])
ma.MaskedArray.data
ma.MaskedArray.mask
ma.MaskedArray.recordmask
ma.MaskedArray.all([axis,out]) Check if all of the elements of a are true.
ma.MaskedArray.any([axis,out]) Check if any of the elements of }a\mathrm{ are true.
ma.MaskedArray.count([axis]) Count the non-masked elements of the array along the given axis.
ma.MaskedArray.nonzero() Return the indices of unmasked elements that are not zero.
ma.shape(obj) Return the shape of an array.
ma.size(obj[,axis]) Return the number of elements along a given axis.
```

numpy.ma.all (self, axis=None, out=None)

Check if all of the elements of $a$ are true.
Performs a logical_and over the given axis and returns the result. Masked values are considered as True during computation. For convenience, the output array is masked where ALL the values along the current axis are masked: if the output would have been a scalar and that all the values are masked, then the output is masked.

## Parameters

axis: \{None, integer \}
Axis to perform the operation over. If None, perform over flattened array.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## See Also:

all
equivalent function

## Examples

```
>>> np.ma.array([1,2,3]).all()
True
>>> a = np.ma.array([1,2,3], mask=True)
>>> (a.all() is np.ma.masked)
True
```

numpy .ma. any (self, axis=None, out=None)

Check if any of the elements of $a$ are true.
Performs a logical_or over the given axis and returns the result. Masked values are considered as False during computation.

## Parameters

axis : $\{$ None, integer $\}$
Axis to perform the operation over. If None, perform over flattened array and return a scalar.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## See Also:

any
equivalent function
numpy.ma. count ( $a$, axis=None)
Count the non-masked elements of the array along the given axis.

## Parameters

axis : int, optional
Axis along which to count the non-masked elements. If axis is None, all non-masked elements are counted.

## Returns

result : int or ndarray
If axis is None, an integer count is returned. When axis is not None, an array with shape determined by the lengths of the remaining axes, is returned.

## See Also:

count_masked
Count masked elements in array or along a given axis.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.arange(6).reshape((2, 3))
>>> a[1, :] = ma.masked
>>> a
masked_array(data =
            [[00 1 2]
            [-- -- --]],
                mask =
            [[False False False]
```

```
[ True True True]],
    fill_value = 999999)
>>> a.count()
3
```

When the axis keyword is specified an array of appropriate size is returned.

```
>>> a.count(axis=0)
array([1, 1, 1])
>>> a.count(axis=1)
array([3, 0])
```

numpy.ma.count_masked (arr, axis=None)

Count the number of masked elements along the given axis.

## Parameters

arr : array_like
An array with (possibly) masked elements.
axis : int, optional
Axis along which to count. If None (default), a flattened version of the array is used.

## Returns

count : int, ndarray
The total number of masked elements (axis=None) or the number of masked elements along each slice of the given axis.

## See Also:

MaskedArray.count
Count non-masked elements.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(9).reshape((3,3))
>>> a = ma.array(a)
>>> a[1, 0] = ma.masked
>>> a[1, 2] = ma.masked
>>> a[2, 1] = ma.masked
>>> a
masked_array(data =
    [[\begin{array}{lll}{0}&{1}&{2}\end{array}]
    [-- 4 --]
    [6 -- 8]],
            mask =
    [[False False False]
    [ True False True]
    [False True False]],
            fill_value=999999)
>>> ma.count_masked(a)
3
```

When the axis keyword is used an array is returned.

```
>>> ma.count_masked(a, axis=0)
array([1, 1, 1])
```

```
>>> ma.count_masked(a, axis=1)
array([0, 2, 1])
```

numpy.ma.getmask (a)
Return the mask of a masked array, or nomask.
Return the mask of $a$ as an ndarray if $a$ is a MaskedArray and the mask is not nomask, else return nomask. To guarantee a full array of booleans of the same shape as a, use getmaskarray.

## Parameters

a : array_like
Input MaskedArray for which the mask is required.

## See Also:

getdata
Return the data of a masked array as an ndarray.
getmaskarray
Return the mask of a masked array, or full array of False.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.masked_equal([[1,2],[3,4]], 2)
>>> a
masked_array(data =
    [[lll
        [3 4]],
            mask =
        [[False True]
        [False False]],
            fill_value=999999)
        >>> ma.getmask(a)
        array([[False, True],
            [False, False]], dtype=bool)
```

Equivalently use the MaskedArray mask attribute.

```
>>> a.mask
array([[False, True],
    [False, False]], dtype=bool)
```

Result when mask $==$ nomask

```
>>> b = ma.masked_array([[1,2],[3,4]])
>>> b
masked_array(data =
    [[1 2]
    [3 4]],
                mask =
    False,
            fill_value=9999999)
>>> ma.nomask
False
>>> ma.getmask(b) == ma.nomask
True
>>> b.mask == ma.nomask
True
```

numpy.ma.getmaskarray (arr)
Return the mask of a masked array, or full boolean array of False.
Return the mask of arr as an ndarray if arr is a MaskedArray and the mask is not nomask, else return a full boolean array of False of the same shape as arr.

## Parameters

arr : array_like
Input MaskedArray for which the mask is required.

## See Also:

getmask
Return the mask of a masked array, or nomask.
getdata
Return the data of a masked array as an ndarray.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.masked_equal([[1,2],[3,4]], 2)
>>> a
masked_array(data =
            [[1 --]
            [3 4]],
                mask =
            [[False True]
            [False False]],
                    fill_value=999999)
>>> ma.getmaskarray(a)
array([[False, True],
                    [False, False]], dtype=bool)
```

Result when mask == nomask

```
>>> b = ma.masked_array([[1,2],[3,4]])
>>> b
masked_array(data =
            [[1 2]
            [3 4]],
                    mask =
            False,
                    fill_value=999999)
>>> >ma.getmaskarray(b)
array([[False, False],
                    [False, False]], dtype=bool)
```

numpy.ma.getdata ( $a$, subok=True)

Return the data of a masked array as an ndarray.
Return the data of $a$ (if any) as an ndarray if $a$ is a MaskedArray, else return $a$ as a ndarray or subclass (depending on subok) if not.

## Parameters

a : array_like
Input MaskedArray, alternatively a ndarray or a subclass thereof.
subok : bool

Whether to force the output to be a pure ndarray (False) or to return a subclass of ndarray if appropriate (True, default).

## See Also:

## getmask

Return the mask of a masked array, or nomask.

```
getmaskarray
```

Return the mask of a masked array, or full array of False.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.masked_equal([[1,2],[3,4]], 2)
>>> a
masked_array(data =
            [[1 --]
            [3 4]],
                    mask =
            [[False True]
            [False False]],
                    fill_value=999999)
>>> ma.getdata(a)
array([[1, 2],
                    [3, 4]])
```

Equivalently use the MaskedArray data attribute.

```
>>> a.data
array([[1, 2],
    [3, 4]])
```

numpy.ma.nonzero (self)
Return the indices of unmasked elements that are not zero.
Returns a tuple of arrays, one for each dimension, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

```
a[a.nonzero()]
```

To group the indices by element, rather than dimension, use instead:

```
np.transpose(a.nonzero())
```

The result of this is always a 2d array, with a row for each non-zero element.

## Parameters

None :

## Returns

tuple_of_arrays : tuple
Indices of elements that are non-zero.

## See Also:

numpy.nonzero
Function operating on ndarrays.

## flatnonzero

Return indices that are non-zero in the flattened version of the input array.

## ndarray.nonzero

Equivalent ndarray method.

```
count_nonzero
```

Counts the number of non-zero elements in the input array.

## Examples

```
>>> import numpy.ma as ma
>>> x = ma.array(np.eye(3))
>>> x
masked_array(data =
    [[ 1. 0. 0.]
    [ 0. 1. 0.]
    [ 0. 0. 1.]],
            mask =
    False,
        fill_value=1e+20)
>>> x.nonzero()
    (array([0, 1, 2]), array([0, 1, 2]))
```

Masked elements are ignored.

```
>>> x[1, 1] = ma.masked
>>> x
masked_array(data =
    [[1.0 0.0 0.0]
    [0.0 -- 0.0]
    [0.0 0.0 1.0]],
            mask =
    [[False False False]
    [False True False]
    [False False False]],
            fill_value=1e+20)
>>> x.nonzero()
(array([0, 2]), array([0, 2]))
```

Indices can also be grouped by element.

```
>>> np.transpose(x.nonzero())
array([[0, 0],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , ma.nonzero( $a>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a = ma.array([[1,2,3],[4,5,6],[7, 8,9]])
>>> a > 3
masked_array(data =
    [[False False False]
    [ True True True]
    [ True True True]],
            mask =
    False,
        fill_value=999999)
>>> ma.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the condition array can also be called.

```
>>> (a > 3).nonzero()
```

(array $([1,1,1,2,2,2]), \operatorname{array}([0,1,2,0,1,2]))$
numpy.ma.shape (obj)
Return the shape of an array.

## Parameters

a : array_like
Input array.

## Returns

shape : tuple of ints
The elements of the shape tuple give the lengths of the corresponding array dimensions.

## See Also:

## alen

ndarray.shape
Equivalent array method.

## Examples

```
>>> np.shape(np.eye(3))
(3, 3)
>>> np.shape([[1, 2]])
(1, 2)
>>> np.shape([0])
(1,)
>>> np.shape(0)
()
>>> a = np.array([(1, 2), (3, 4)], dtype=[('x', 'i4'), ('y', 'i4')])
>>> np.shape(a)
(2,)
>>> a.shape
(2, )
numpy.ma.size(obj, axis=None)
```

Return the number of elements along a given axis.

## Parameters

a : array_like
Input data.
axis : int, optional
Axis along which the elements are counted. By default, give the total number of elements.

## Returns

element_count : int
Number of elements along the specified axis.

```
See Also:
shape
dimensions of array
```


## ndarray.shape

dimensions of array
ndarray.size
number of elements in array

## Examples

```
>>> a = np.array([[1,2,3],[4,5,6]])
>>> np.size(a)
6
>>> np.size(a,1)
3
>>> np.size(a,0)
2
```

MaskedArray.data

Return the current data, as a view of the original underlying data.

```
MaskedArray.mask
```

Mask
MaskedArray. recordmask
Return the mask of the records. A record is masked when all the fields are masked.
MaskedArray.all (axis=None, out=None)
Check if all of the elements of $a$ are true.
Performs a logical_and over the given axis and returns the result. Masked values are considered as True during computation. For convenience, the output array is masked where ALL the values along the current axis are masked: if the output would have been a scalar and that all the values are masked, then the output is masked.

## Parameters

axis : $\{$ None, integer $\}$
Axis to perform the operation over. If None, perform over flattened array.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## See Also:

all
equivalent function
Examples

```
>>> np.ma.array([1,2,3]).all()
True
>>> a = np.ma.array([1,2,3], mask=True)
>>> (a.all() is np.ma.masked)
True
```

MaskedArray .any (axis=None, out=None)
Check if any of the elements of $a$ are true.
Performs a logical_or over the given axis and returns the result. Masked values are considered as False during computation.

## Parameters

axis : \{None, integer \}
Axis to perform the operation over. If None, perform over flattened array and return a scalar.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

```
    See Also:
    any
        equivalent function
```

MaskedArray.count (axis=None)
Count the non-masked elements of the array along the given axis.

## Parameters

axis : int, optional
Axis along which to count the non-masked elements. If axis is None, all non-masked elements are counted.

## Returns

result : int or ndarray
If axis is None, an integer count is returned. When axis is not None, an array with shape determined by the lengths of the remaining axes, is returned.

## See Also:

count_masked
Count masked elements in array or along a given axis.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.arange (6).reshape((2, 3))
>>> a[1, :] = ma.masked
>>> a
masked_array(data =
            [[0}1012
            [-- -- --]],
                mask =
            [[False False False]
            [ True True True]],
                    fill_value = 999999)
>>> a.count()
3
```

When the axis keyword is specified an array of appropriate size is returned.

```
>>> a.count(axis=0)
array([1, 1, 1])
>>> a.count(axis=1)
array([3, 0])
MaskedArray.nonzero()
```

Return the indices of unmasked elements that are not zero.

Returns a tuple of arrays, one for each dimension, containing the indices of the non-zero elements in that dimension. The corresponding non-zero values can be obtained with:

```
a[a.nonzero()]
```

To group the indices by element, rather than dimension, use instead:

```
np.transpose(a.nonzero())
```

The result of this is always a 2 d array, with a row for each non-zero element.

## Parameters

None :

## Returns

tuple_of_arrays : tuple
Indices of elements that are non-zero.

## See Also:

```
numpy.nonzero
```

Function operating on ndarrays.

## flatnonzero

Return indices that are non-zero in the flattened version of the input array.

## ndarray.nonzero

Equivalent ndarray method.
count_nonzero
Counts the number of non-zero elements in the input array.

## Examples

```
>>> import numpy.ma as ma
>>> x = ma.array(np.eye(3))
>>> x
masked_array(data =
    [[ 1. 0. 0.]
    [ 0. 1. 0.]
    [ 0. 0. 1.]],
            mask =
        False,
            fill_value=1e+20)
        >>> x.nonzero()
        (array([0, 1, 2]), array([0, 1, 2]))
```

Masked elements are ignored.

```
>>> x[1, 1] = ma.masked
>>> x
masked_array(data =
    [[1.0 0.0 0.0]
    [0.0 -- 0.0]
    [0.0 0.0 1.0]],
            mask =
    [[False False False]
    [False True False]
    [False False False]],
            fill_value=1e+20)
```

```
>>> x.nonzero()
(array([0, 2]), array([0, 2]))
```

Indices can also be grouped by element.

```
>>> np.transpose(x.nonzero())
array([[0, 0],
    [2, 2]])
```

A common use for nonzero is to find the indices of an array, where a condition is True. Given an array $a$, the condition $a>3$ is a boolean array and since False is interpreted as 0 , ma.nonzero( $\mathrm{a}>3$ ) yields the indices of the $a$ where the condition is true.

```
>>> a = ma.array([[1,2,3],[4,5,6],[7, 8,9]])
>>> a > 3
masked_array(data =
    [[False False False]
    [ True True True]
    [ True True True]],
            mask =
    False,
            fill_value=999999)
>>> ma.nonzero(a > 3)
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

The nonzero method of the condition array can also be called.

```
>>> (a > 3).nonzero()
(array([1, 1, 1, 2, 2, 2]), array([0, 1, 2, 0, 1, 2]))
```

numpy.ma.shape (obj)

Return the shape of an array.

## Parameters

a: array_like
Input array.

## Returns

shape : tuple of ints
The elements of the shape tuple give the lengths of the corresponding array dimensions.

## See Also:

alen
ndarray.shape
Equivalent array method.

## Examples

```
>>> np.shape(np.eye(3))
(3, 3)
>>> np.shape([[1, 2]])
(1, 2)
>>> np.shape([0])
(1,)
>>> np.shape(0)
()
```

```
>>> a = np.array([(1, 2), (3, 4)], dtype=[('x', 'i4'), ('y', 'i4')])
>>> np.shape(a)
(2,)
>>> a.shape
(2,)
```

numpy.ma.size (obj, axis=None)

Return the number of elements along a given axis.

## Parameters

 a: array_likeInput data.
axis : int, optional
Axis along which the elements are counted. By default, give the total number of elements.

## Returns

element_count : int
Number of elements along the specified axis.
See Also:
shape
dimensions of array
ndarray.shape
dimensions of array
ndarray.size
number of elements in array

## Examples

```
>>> a = np.array([[1,2,3],[4,5,6]])
>>> np.size(a)
6
>>> np.size(a,1)
3
>>> np.size(a,0)
2
```


### 3.20.4 Manipulating a MaskedArray

Changing the shape

| ma.ravel(self) | Returns a 1D version of self, as a view. |
| :---: | :---: |
| ma.reshape(a, new_shape[, order]) | Returns an array containing the same data with a new shape. |
| ma.resize(x, new_shape) | Return a new masked array with the specified size and shape. |
| ma.MaskedArray.flatten([order]) | Return a copy of the array collapsed into one dimension. |
| ma.MaskedArray.ravel() | Returns a 1D version of self, as a view. |
| ma.MaskedArray.reshape(*s, **kwargs) | Give a new shape to the array without changing its data. |
| ma.MaskedArray.resize(newshape[, refcheck, ...]) |  |

numpy.ma.ravel (self)
Returns a 1D version of self, as a view.

## Returns

MaskedArray :
Output view $\quad$ is of $\quad$ shape $\quad$ (self.size,) (or
(np.ma.product (self.shape), ).

Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 --]
    [7 -- 9]]
>>> print x.ravel()
[1 -- 3 -- 5 -- 7 -- 9]
```

numpy.ma.reshape ( $a$, new_shape, order $=$ ' $C$ ')
Returns an array containing the same data with a new shape.
Refer to MaskedArray.reshape for full documentation.
See Also:

MaskedArray.reshape
equivalent function
numpy.ma.resize ( $x$, new_shape)
Return a new masked array with the specified size and shape.
This is the masked equivalent of the numpy. resize function. The new array is filled with repeated copies of $x$ (in the order that the data are stored in memory). If $x$ is masked, the new array will be masked, and the new mask will be a repetition of the old one.

## See Also:

numpy.resize
Equivalent function in the top level NumPy module.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.array([[1, 2] ,[3, 4]])
>>> a[0, 1] = ma.masked
>>> a
masked_array(data =
    [[1 --]
    [3 4]],
            mask =
    [[False True]
    [False False]],
            fill_value = 999999)
>>> np.resize(a, (3, 3))
array([[1, 2, 3],
            [4, 1, 2],
            [3, 4, 1]])
>>> ma.resize(a, (3, 3))
masked_array(data =
    [[1 -- 3]
    [[4 1---]
    [3 4 1]],
            mask =
    [[False True False]
    [False False True]
    [False False False]],
            fill_value = 999999)
```

A MaskedArray is always returned, regardless of the input type.

```
>>> a = np.array([[1, 2] ,[3, 4]])
>>> ma.resize(a, (3, 3))
masked_array(data =
    [[\begin{array}{lll}{1}&{2}&{3}\end{array}]
    [4 4 1 2]
    [3 4 1]],
            mask =
    False,
            fill_value = 999999)
MaskedArray.flatten (order='C')
```

Return a copy of the array collapsed into one dimension.

## Parameters

order : \{ 'C', 'F', 'A'\}, optional
Whether to flatten in C (row-major), Fortran (column-major) order, or preserve the C/Fortran ordering from $a$. The default is ' C '.

## Returns

$\mathbf{y}$ : ndarray
A copy of the input array, flattened to one dimension.

## See Also:

ravel
Return a flattened array.
flat
A 1-D flat iterator over the array.

## Examples

```
>>> a = np.array([[1,2], [3,4]])
>>> a.flatten()
array([1, 2, 3, 4])
>>> a.flatten('F')
array([1, 3, 2, 4])
```

MaskedArray.ravel()

Returns a 1D version of self, as a view.

## Returns

## MaskedArray :

| Output | view | is | of | shape | (self.size, | (or |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | oduc | ff |  |  |  |  |

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 --]
    [7 -- 9]]
>>> print x.ravel()
[1 -- 3 -- 5 -- 7 -- 9]
MaskedArray.reshape (*s, **kwargs)
```

Give a new shape to the array without changing its data.
Returns a masked array containing the same data, but with a new shape. The result is a view on the original array; if this is not possible, a ValueError is raised.

## Parameters

shape : int or tuple of ints
The new shape should be compatible with the original shape. If an integer is supplied, then the result will be a 1-D array of that length.
order : \{ 'C', 'F' $\}$, optional
Determines whether the array data should be viewed as in C (row-major) or FORTRAN (column-major) order.

## Returns

reshaped_array : array
A new view on the array.

## See Also:

reshape
Equivalent function in the masked array module.
numpy.ndarray.reshape
Equivalent method on ndarray object.
numpy.reshape
Equivalent function in the NumPy module.

## Notes

The reshaping operation cannot guarantee that a copy will not be made, to modify the shape in place, use a.shape $=$ s

## Examples

```
>>> x = np.ma.array([[1,2],[3,4]], mask=[1,0,0,1])
>>> print x
[[-- 2]
    [3 --]]
>>> x = x.reshape((4,1))
>>> print x
[ [--]
    [2]
    [3]
    [--]]
```

MaskedArray.resize (newshape, refcheck=True, order=False)
Warning: This method does nothing, except raise a ValueError exception. A masked array does not own its data and therefore cannot safely be resized in place. Use the numpy.ma. resize function instead.

This method is difficult to implement safely and may be deprecated in future releases of NumPy.

## Modifying axes

| ma.swapaxes | swapaxes |
| :--- | :--- |
| ma.transpose(a[, axes]) | Permute the dimensions of an array. |
| ma.MaskedArray.swapaxes(axis1, axis2) | Return a view of the array with axis1 and axis2 interchanged. |
| ma.MaskedArray.transpose(*axes) | Returns a view of the array with axes transposed. |

numpy.ma.swapaxes
swapaxes a.swapaxes(axis1, axis2)
Return a view of the array with axis1 and axis 2 interchanged.
Refer to numpy. swapaxes for full documentation.

## See Also:

numpy.swapaxes
equivalent function
numpy.ma.transpose ( $a$, axes=None)
Permute the dimensions of an array.
This function is exactly equivalent to numpy. transpose.
See Also:
numpy.transpose
Equivalent function in top-level NumPy module.
Examples

```
>>> import numpy.ma as ma
>>> x = ma.arange(4).reshape((2,2))
>>> x[1, 1] = ma.masked
>>>> x
masked_array(data =
    [[\begin{array}{ll}{0}&{1]}\end{array}]
    [2 -- ]],
            mask =
    [[False False]
    [False True]],
            fill_value = 999999)
>>> ma.transpose(x)
masked_array(data =
    [[\begin{array}{ll}{0}&{2]}\end{array}]
    [1 --]],
            mask =
    [[False False]
    [False True]],
            fill_value = 999999)
```

MaskedArray.swapaxes (axis1, axis2)
Return a view of the array with axis1 and axis2 interchanged.
Refer to numpy. swapaxes for full documentation.

## See Also:

numpy.swapaxes
equivalent function
MaskedArray.transpose (*axes)
Returns a view of the array with axes transposed.
For a 1-D array, this has no effect. (To change between column and row vectors, first cast the 1-D array into a matrix object.) For a 2-D array, this is the usual matrix transpose. For an n-D array, if axes are given, their order indicates how the axes are permuted (see Examples). If axes are not provided and a. shape $=(i[0], i[1]$, ... $i[n-2], i[n-1])$, then a.transpose().shape $=(i[n-1], i[n-2], \ldots i[1]$, i[0]).

## Parameters

axes : None, tuple of ints, or $n$ ints

- None or no argument: reverses the order of the axes.
- tuple of ints: $i$ in the $j$-th place in the tuple means $a$ 's $i$-th axis becomes a.transpose()'s $j$-th axis.
- $n$ ints: same as an n-tuple of the same ints (this form is intended simply as a "convenience" alternative to the tuple form)


## Returns

out : ndarray
View of $a$, with axes suitably permuted.

## See Also:

ndarray.T
Array property returning the array transposed.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> a
array([[1, 2],
    [3, 4]])
>>> a.transpose()
array([[1, 3],
    [2, 4]])
>>> a.transpose((1, 0))
array([[1, 3],
    [2, 4]])
>>> a.transpose(1, 0)
array([[1, 3],
    [2, 4]])
```


## Changing the number of dimensions

```
ma.atleast_1d(*arys) Convert inputs to arrays with at least one dimension.
ma.atleast_2d(*arys) View inputs as arrays with at least two dimensions.
ma.atleast_3d(*arys) View inputs as arrays with at least three dimensions.
ma.expand_dims(x, axis) Expand the shape of an array.
ma.squeeze(a) Remove single-dimensional entries from the shape of an array.
ma.MaskedArray.squeeze() Remove single-dimensional entries from the shape of a.
ma.column_stack(tup) Stack 1-D arrays as columns into a 2-D array.
ma.concatenate(arrays[, axis]) Concatenate a sequence of arrays along the given axis.
ma.dstack(tup) Stack arrays in sequence depth wise (along third axis).
ma.hstack(tup) Stack arrays in sequence horizontally (column wise).
ma.hsplit(ary, indices_or_sections) Split an array into multiple sub-arrays horizontally (column-wise).
ma.mr_
ma.row_stack(tup) Stack arrays in sequence vertically (row wise).
ma.vstack(tup) Stack arrays in sequence vertically (row wise).
numpy.ma.atleast_1d(*arys)
```

Convert inputs to arrays with at least one dimension.
Scalar inputs are converted to 1-dimensional arrays, whilst higher-dimensional inputs are preserved.

## Parameters <br> array1, array2, ... : array_like

One or more input arrays.

## Returns

ret : ndarray
An array, or sequence of arrays, each with a.ndim $>=1$. Copies are made only if necessary.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> np.atleast_1d(1.0)
array([ 1.])
>>> x = np.arange(9.0).reshape (3,3)
>>> np.atleast_1d(x)
array([[ 0., 1., 2.],
    [ 3., 4., 5.],
    [ 6., 7., 8.]])
>>> np.atleast_1d(x) is x
True
>>> np.atleast_1d(1, [3, 4])
[array([1]), array([3, 4])]
numpy.ma.atleast_2d(*arys)
```

View inputs as arrays with at least two dimensions.

## Parameters

```
array1, array2, ... : array_like
```

One or more array-like sequences. Non-array inputs are converted to arrays. Arrays that already have two or more dimensions are preserved.

## Returns

res, res2, ... : ndarray
An array, or tuple of arrays, each with a.ndim $>=2$. Copies are avoided where possible, and views with two or more dimensions are returned.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> np.atleast_2d(3.0)
array([[ 3.]])
>>> x = np.arange(3.0)
>>> np.atleast_2d(x)
array([[ 0., 1., 2.]])
>>> np.atleast_2d(x).base is x
True
>>> np.atleast_2d(1, [1, 2], [[1, 2]])
[array([[1]]), array([[1, 2]]), array([[1, 2]])]
numpy.ma.atleast_3d(*arys)
```

View inputs as arrays with at least three dimensions.

## Parameters

array1, array2, ... : array_like
One or more array-like sequences. Non-array inputs are converted to arrays. Arrays that already have three or more dimensions are preserved.

## Returns

res1, res2, ... : ndarray
An array, or tuple of arrays, each with a.ndim $>=3$. Copies are avoided where possible, and views with three or more dimensions are returned. For example, a 1-D array of shape $(\mathrm{N}$, ) becomes a view of shape (1, $\mathrm{N}, ~ 1)$, and a 2-D array of shape $(M, N)$ becomes a view of shape ( $M, N, 1$ ).

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> np.atleast_3d(3.0)
array([[[ 3.]]])
>>> x = np.arange(3.0)
>>> np.atleast_3d(x).shape
(1, 3, 1)
>>> x = np.arange(12.0).reshape (4,3)
>>> np.atleast_3d(x).shape
(4, 3, 1)
>>> np.atleast_3d(x).base is x
True
>>> for arr in np.atleast_3d([1, 2], [[1, 2]], [[[1, 2]]]):
... print arr, arr.shape
...
[[[1]
    [2]]] (1, 2, 1)
[[ [1]
    [2]]] (1, 2, 1)
[[[l1 2]]] (1, 1, 2)
```

numpy.ma.expand_dims ( $x$, axis)
Expand the shape of an array.
Expands the shape of the array by including a new axis before the one specified by the axis parameter. This function behaves the same as numpy. expand_dims but preserves masked elements.

## See Also:

numpy.expand_dims
Equivalent function in top-level NumPy module.

## Examples

```
>>> import numpy.ma as ma
>>> x = ma.array([1, 2, 4])
>>> x[1] = ma.masked
>>> x
masked_array(data = [1 -- 4],
    mask = [False True False],
    fill_value = 999999)
>>> np.expand_dims(x, axis=0)
array([[1, 2, 4]])
>>> ma.expand_dims(x, axis=0)
```

```
masked_array(data =
    [[1 -- 4]],
        mask =
    [[False True False]],
            fill_value = 999999)
```

The same result can be achieved using slicing syntax with np.newaxis.

```
>>> x[np.newaxis, :]
masked_array(data =
    [[1 -- 4]],
        mask =
    [[False True False]],
            fill_value = 999999)
```

numpy.ma.squeeze (a)

Remove single-dimensional entries from the shape of an array.

## Parameters

a : array_like
Input data.

## Returns

squeezed : ndarray
The input array, but with with all dimensions of length 1 removed. Whenever possible, a view on $a$ is returned.

## Examples

```
>>> x = np.array([[[0], [1], [2]]])
>>> x.shape
(1, 3, 1)
>>> np.squeeze(x).shape
(3,)
MaskedArray.squeeze()
```

Remove single-dimensional entries from the shape of $a$.
Refer to numpy. squeeze for full documentation.

## See Also:

numpy.squeeze
equivalent function

```
numpy.ma.column_stack(tup)
```

Stack 1-D arrays as columns into a 2-D array.
Take a sequence of 1-D arrays and stack them as columns to make a single 2-D array. 2-D arrays are stacked as-is, just like with hstack. 1-D arrays are turned into 2-D columns first.

## Parameters

tup : sequence of 1-D or 2-D arrays.
Arrays to stack. All of them must have the same first dimension.

## Returns

stacked : 2-D array
The array formed by stacking the given arrays.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.column_stack((a,b))
array([[1, 2],
    [2, 3],
    [3, 4]])
```

numpy.ma.concatenate (arrays, axis=0)

Concatenate a sequence of arrays along the given axis.

## Parameters

arrays : sequence of array_like
The arrays must have the same shape, except in the dimension corresponding to axis (the first, by default).
axis : int, optional
The axis along which the arrays will be joined. Default is 0 .

## Returns

result : MaskedArray
The concatenated array with any masked entries preserved.

## See Also:

numpy. concatenate
Equivalent function in the top-level NumPy module.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.arange(3)
>>> a[1] = ma.masked
>>> b = ma.arange (2, 5)
>>> a
masked_array(data = [0 -- 2],
    mask = [False True False],
    fill_value = 999999)
>>> b
masked_array(data = [l 2 3 4}]\mp@code{,
    mask = False,
    fill_value = 999999)
>>> ma.concatenate([a, b])
masked_array(data = [0 -- 2 2 3 4 4}
    mask = [False True False False False False],
    fill_value = 999999)
```

```
numpy.ma.dstack (tup)
```

Stack arrays in sequence depth wise (along third axis).
Takes a sequence of arrays and stack them along the third axis to make a single array. Rebuilds arrays divided by dsplit. This is a simple way to stack 2D arrays (images) into a single 3D array for processing.

## Parameters

tup : sequence of arrays
Arrays to stack. All of them must have the same shape along all but the third axis.

## Returns

stacked : ndarray
The array formed by stacking the given arrays.

## See Also:

vstack
Stack along first axis.
hstack
Stack along second axis.
concatenate
Join arrays.
dsplit
Split array along third axis.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.dstack((a,b))
array([[[1, 2],
    [2, 3],
    [3, 4]]])
>>> a = np.array([[1],[2],[3]])
>>> b = np.array([[2],[3],[4]])
>>> np.dstack((a,b))
array([[[1, 2]],
    [[2, 3]],
    [[3, 4]]])
```

numpy.ma.hstack (tup)

Stack arrays in sequence horizontally (column wise).
Take a sequence of arrays and stack them horizontally to make a single array. Rebuild arrays divided by hsplit.

## Parameters

tup : sequence of ndarrays
All arrays must have the same shape along all but the second axis.

## Returns

stacked : ndarray
The array formed by stacking the given arrays.

```
See Also:
vstack
    Stack arrays in sequence vertically (row wise).
dstack
    Stack arrays in sequence depth wise (along third axis).
concatenate
    Join a sequence of arrays together.
hsplit
    Split array along second axis.
```


## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.hstack((a,b))
array([1, 2, 3, 2, 3, 4])
>>> a = np.array([[1],[2],[3]])
>>> b = np.array([[2],[3],[4]])
>>> np.hstack((a,b))
array([[1, 2],
    [2, 3],
    [3, 4]])
```

numpy.ma.hsplit (ary, indices_or_sections)

Split an array into multiple sub-arrays horizontally (column-wise).
Please refer to the split documentation. hsplit is equivalent to split with axis=1, the array is always split along the second axis regardless of the array dimension.

## See Also:

split
Split an array into multiple sub-arrays of equal size.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> x = np.arange(16.0).reshape(4, 4)
>>> x
array([[[ 0., 1., 2., 3.],
    [ 4., 5., 6., 7.],
    [ 8., 9., 10., 11.],
    [ 12., 13., 14., 15.]])
>>> np.hsplit(x, 2)
[array([[[ 0., 1.],
    [ 4., 5.],
    [ 8., 9.],
    [ 12., 13.]]),
    array([[[ 2., 3.],
    [ 6., 7.],
    [ 10., 11.],
    [ 14., 15.]])]
>>> np.hsplit(x, np.array([3, 6]))
[array([[ 0., 1., 2.],
    [ 4., 5., 6.],
    [ 8., 9., 10.],
    [ 12., 13., 14.]]),
    array([[[ 3.],
        [ 7.],
        [ 11.],
    [ 15.]]),
    array([], dtype=float64)]
```

With a higher dimensional array the split is still along the second axis.

```
>>> x = np.arange(8.0).reshape(2, 2, 2)
>>> x
array([[[ 0., 1.],
    [ 2., 3.]],
    [[ 4., 5.],
    [ 6., 7.]]])
>>> np.hsplit(x, 2)
[array([[[ 0., 1.]],
    [[ 4., 5.]]]),
array([[[ 2., 3.]],
    [[ 6., 7.]]])]
```

numpy.ma.mr_
Translate slice objects to concatenation along the first axis.
This is the masked array version of lib.index_tricks.RClass.

## See Also:

lib.index_tricks.RClass

## Examples

```
>>> np.ma.mr_[np.ma.array([1,2,3]), 0, 0, np.ma.array([4,5,6])]
array([1, 2, 3, 0, 0, 4, 5, 6])
numpy.ma.row_stack(tup)
```

Stack arrays in sequence vertically (row wise).

Take a sequence of arrays and stack them vertically to make a single array. Rebuild arrays divided by vsplit.

## Parameters

tup : sequence of ndarrays
Tuple containing arrays to be stacked. The arrays must have the same shape along all but the first axis.

## Returns

stacked : ndarray
The array formed by stacking the given arrays.

## See Also:

```
hstack
```

Stack arrays in sequence horizontally (column wise).

```
dstack
```

Stack arrays in sequence depth wise (along third dimension).

```
concatenate
```

Join a sequence of arrays together.
vsplit
Split array into a list of multiple sub-arrays vertically.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array([1, 2, 3])
>>> b = np.array([2, 3, 4])
>>> np.vstack((a,b))
array([[1, 2, 3],
    [2, 3, 4]])
>>> a = np.array([[1], [2], [3]])
>>> b = np.array([[2], [3], [4]])
>>> np.vstack((a,b))
array([[1],
    [2],
    [3],
    [2],
    [3],
    [4]])
numpy.ma.vstack (tup)
```

Stack arrays in sequence vertically (row wise).
Take a sequence of arrays and stack them vertically to make a single array. Rebuild arrays divided by vsplit.

## Parameters

tup : sequence of ndarrays

Tuple containing arrays to be stacked. The arrays must have the same shape along all but the first axis.

## Returns

stacked : ndarray
The array formed by stacking the given arrays.

```
See Also:
hstack
    Stack arrays in sequence horizontally (column wise).
dstack
```

    Stack arrays in sequence depth wise (along third dimension).
    concatenate
Join a sequence of arrays together.
vsplit
Split array into a list of multiple sub-arrays vertically.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array([1, 2, 3])
>>> b = np.array([2, 3, 4])
>>> np.vstack((a,b))
array([[1, 2, 3],
    [2, 3, 4]])
>>> a = np.array([[1], [2], [3]])
>>> b = np.array([[2], [3], [4]])
>>> np.vstack((a,b))
array([[1],
    [2],
    [3],
    [2],
    [3],
    [4]])
```


## Joining arrays

| ma.column_stack(tup) | Stack 1-D arrays as columns into a 2-D array. |
| :--- | :--- |
| ma.concatenate(arrays[, axis]) | Concatenate a sequence of arrays along the given axis. |
| ma.dstack(tup) | Stack arrays in sequence depth wise (along third axis). |
| ma.hstack(tup) | Stack arrays in sequence horizontally (column wise). |
| ma.vstack(tup) | Stack arrays in sequence vertically (row wise). |
| numpy.ma.column_stack (tup) |  |

Stack 1-D arrays as columns into a 2-D array.
Take a sequence of 1-D arrays and stack them as columns to make a single 2-D array. 2-D arrays are stacked as-is, just like with hstack. 1-D arrays are turned into 2-D columns first.

## Parameters

tup : sequence of 1-D or 2-D arrays.
Arrays to stack. All of them must have the same first dimension.

## Returns

stacked : 2-D array
The array formed by stacking the given arrays.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.column_stack((a,b))
array([[1, 2],
    [2, 3],
    [3, 4]])
```

numpy.ma.concatenate (arrays, axis=0)
Concatenate a sequence of arrays along the given axis.

## Parameters

arrays : sequence of array_like
The arrays must have the same shape, except in the dimension corresponding to axis (the first, by default).
axis : int, optional
The axis along which the arrays will be joined. Default is 0 .

## Returns

result : MaskedArray
The concatenated array with any masked entries preserved.

## See Also:

numpy. concatenate
Equivalent function in the top-level NumPy module.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.arange(3)
>>> a[1] = ma.masked
>>> b = ma.arange(2, 5)
>>> a
masked_array(data = [0 -- 2],
                    mask = [False True False],
            fill_value = 999999)
>>> b
masked_array(data = [2 3 4],
                    mask = False,
            fill_value = 999999)
>>> ma.concatenate([a, b])
masked_array(data = [0 -- 2 2 3 4],
```

```
        mask = [False True False False False False],
fill_value = 999999)
```

numpy.ma.dstack (tup)

Stack arrays in sequence depth wise (along third axis).
Takes a sequence of arrays and stack them along the third axis to make a single array. Rebuilds arrays divided by dsplit. This is a simple way to stack 2D arrays (images) into a single 3D array for processing.

## Parameters

tup : sequence of arrays
Arrays to stack. All of them must have the same shape along all but the third axis.

## Returns

stacked : ndarray
The array formed by stacking the given arrays.

## See Also:

vstack
Stack along first axis.
hstack
Stack along second axis.
concatenate
Join arrays.
dsplit
Split array along third axis.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.dstack((a,b))
array([[[1, 2],
    [2, 3],
    [3, 4]]])
>>> a = np.array([[1],[2],[3]])
>>> b = np.array([[2],[3],[4]])
>>> np.dstack((a,b))
array([[[1, 2]],
    [[2, 3]],
    [[3, 4]]])
```

numpy.ma.hstack (tup)

Stack arrays in sequence horizontally (column wise).
Take a sequence of arrays and stack them horizontally to make a single array. Rebuild arrays divided by hsplit.

## Parameters

tup : sequence of ndarrays
All arrays must have the same shape along all but the second axis.

## Returns

stacked : ndarray
The array formed by stacking the given arrays.

## See Also:

vstack
Stack arrays in sequence vertically (row wise).
dstack
Stack arrays in sequence depth wise (along third axis).

```
concatenate
```

Join a sequence of arrays together.
hsplit
Split array along second axis.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array((1,2,3))
>>> b = np.array((2,3,4))
>>> np.hstack((a,b))
array([1, 2, 3, 2, 3, 4])
>>> a = np.array([[1],[2],[3]])
>>> b = np.array([[2],[3],[4]])
>>> np.hstack((a,b))
array([[1, 2],
    [2, 3],
    [3, 4]])
numpy.ma.vstack (tup)
```

Stack arrays in sequence vertically (row wise).
Take a sequence of arrays and stack them vertically to make a single array. Rebuild arrays divided by vsplit.

## Parameters

tup : sequence of ndarrays
Tuple containing arrays to be stacked. The arrays must have the same shape along all but the first axis.

## Returns

stacked : ndarray
The array formed by stacking the given arrays.

## See Also:

hstack
Stack arrays in sequence horizontally (column wise).
dstack
Stack arrays in sequence depth wise (along third dimension).

```
concatenate
```

Join a sequence of arrays together.

```
vsplit
```

Split array into a list of multiple sub-arrays vertically.

## Notes

The function is applied to both the _data and the _mask, if any.

## Examples

```
>>> a = np.array([1, 2, 3])
>>> b = np.array([2, 3, 4])
>>> np.vstack((a,b))
array([[1, 2, 3],
    [2, 3, 4]])
>>> a = np.array([[1], [2], [3]])
>>> b = np.array([[2], [3], [4]])
>>> np.vstack((a,b))
array([[1],
    [2],
    [3],
    [2],
    [3],
    [4]])
```


### 3.20.5 Operations on masks

## Creating a mask

| ma.make_mask(m[, copy, shrink, dtype]) | Create a boolean mask from an array. |
| :--- | :--- |
| ma.make_mask_none(newshape[, dtype] $)$ | Return a boolean mask of the given shape, filled with False. |
| ma.mask_or(m1, m2[, copy, shrink]) | Combine two masks with the logical_or operator. |
| ma.make_mask_descr(ndtype) | Construct a dtype description list from a given dtype. |

numpy.ma.make_mask ( $m$, copy=False, shrink=True, dtype=<type 'numpy.bool_'>)
Create a boolean mask from an array.
Return $m$ as a boolean mask, creating a copy if necessary or requested. The function can accept any sequence that is convertible to integers, or nomask. Does not require that contents must be 0 s and 1 s , values of 0 are interepreted as False, everything else as True.

## Parameters

m : array_like
Potential mask.
copy : bool, optional
Whether to return a copy of $m$ (True) or $m$ itself (False).
shrink : bool, optional
Whether to shrink $m$ to nomask if all its values are False.
dtype : dtype, optional
Data-type of the output mask. By default, the output mask has a dtype of MaskType (bool). If the dtype is flexible, each field has a boolean dtype.

## Returns

result : ndarray
A boolean mask derived from $m$.

## Examples

```
>>> import numpy.ma as ma
>>> m = [True, False, True, True]
>>> ma.make_mask(m)
array([ True, False, True, True], dtype=bool)
>>> m = [1, 0, 1, 1]
>>> ma.make_mask(m)
array([ True, False, True, True], dtype=bool)
>>>m=[1, 0, 2, -3]
>>> ma.make_mask(m)
array([ True, False, True, True], dtype=bool)
```

Effect of the shrink parameter.

```
>>> m = np.zeros(4)
>>> m
array([ 0., 0., 0., 0.])
>>> ma.make_mask(m)
False
>>> ma.make_mask(m, shrink=False)
array([False, False, False, False], dtype=bool)
```

Using a flexible dtype.

```
>>> m = [1, 0, 1, 1]
>>> n = [0, 1, 0, 0]
>>> arr = []
>>> for man, mouse in zip(m, n):
... arr.append((man, mouse))
>>> arr
[(1, 0), (0, 1), (1, 0), (1, 0)]
>>> dtype = np.dtype({'names':['man', 'mouse'],
    'formats':[np.int, np.int]})
>>> arr = np.array(arr, dtype=dtype)
>>> arr
array([(1, 0), (0, 1), (1, 0), (1, 0)],
    dtype=[('man', '<i4'), ('mouse', '<i4')])
>>> ma.make_mask(arr, dtype=dtype)
```

```
array([(True, False), (False, True), (True, False), (True, False)],
    dtype=[('man', '|b1'), ('mouse', '|b1')])
```

numpy.ma.make_mask_none (newshape, dtype=None)
Return a boolean mask of the given shape, filled with False.
This function returns a boolean ndarray with all entries False, that can be used in common mask manipulations. If a complex dtype is specified, the type of each field is converted to a boolean type.

## Parameters

newshape : tuple
A tuple indicating the shape of the mask.

## dtype: \{None, dtype\}, optional :

If None, use a MaskType instance. Otherwise, use a new datatype with the same fields as dtype, converted to boolean types.

## Returns

result : ndarray
An ndarray of appropriate shape and dtype, filled with False.

## See Also:

make_mask
Create a boolean mask from an array.
make_mask_descr
Construct a dtype description list from a given dtype.

## Examples

```
>>> import numpy.ma as ma
>>> ma.make_mask_none((3,))
array([False, False, False], dtype=bool)
```

Defining a more complex dtype.

```
>>> dtype = np.dtype({'names':['foo', 'bar'],
    'formats':[np.float32, np.int]})
>>> dtype
dtype([('foo', '<f4'), ('bar', '<i4')])
>>> ma.make_mask_none((3,), dtype=dtype)
array([(False, False), (False, False), (False, False)],
    dtype=[('foo', '|b1'), ('bar', '|b1')])
```

numpy.ma.mask_or ( $m 1, m 2$, copy=False, shrink=True)
Combine two masks with the logical_or operator.
The result may be a view on $m 1$ or $m 2$ if the other is nomask (i.e. False).

## Parameters

m1, m2 : array_like
Input masks.
copy : bool, optional
If copy is False and one of the inputs is nomask, return a view of the other input mask. Defaults to False.
shrink : bool, optional
Whether to shrink the output to nomask if all its values are False. Defaults to True.

## Returns

 mask : output maskThe result masks values that are masked in either $m 1$ or $m 2$.

## Raises

ValueError :
If $m 1$ and $m 2$ have different flexible dtypes.

## Examples

```
>>> m1 = np.ma.make_mask([0, 1, 1, 0])
>>> m2 = np.ma.make_mask([1, 0, 0, 0])
>>> np.ma.mask_or(m1, m2)
array([ True, True, True, False], dtype=bool)
```

numpy.ma.make_mask_descr (ndtype)
Construct a dtype description list from a given dtype.
Returns a new dtype object, with the type of all fields in ndtype to a boolean type. Field names are not altered.

## Parameters

ndtype : dtype
The dtype to convert.

## Returns

result : dtype
A dtype that looks like ndtype, the type of all fields is boolean.

## Examples

```
>>> import numpy.ma as ma
>>> dtype = np.dtype({'names':['foo', 'bar'],
    'formats':[np.float32, np.int]})
>>> dtype
dtype([('foo', '<f4'), ('bar', '<i4')])
>>> ma.make_mask_descr(dtype)
dtype([('foo', '|b1'), ('bar', '|b1')])
>>> ma.make_mask_descr(np.float32)
<type 'numpy.bool_'>
```


## Accessing a mask

| ma.getmask(a) | Return the mask of a masked array, or nomask. |
| :--- | :--- |
| ma.getmaskarray(arr) | Return the mask of a masked array, or full boolean array of False. |
| ma.masked_array.mask | Mask |

numpy.ma.getmask (a)
Return the mask of a masked array, or nomask.
Return the mask of $a$ as an ndarray if $a$ is a MaskedArray and the mask is not nomask, else return nomask. To guarantee a full array of booleans of the same shape as a, use getmaskarray.

## Parameters

a : array_like

Input MaskedArray for which the mask is required.

## See Also:

## getdata

Return the data of a masked array as an ndarray.

## getmaskarray

Return the mask of a masked array, or full array of False.

## Examples

```
>>> import numpy.ma as ma
>>> a = ma.masked_equal([[1,2],[3,4]], 2)
>>> a
masked_array(data =
    [[1 --]
    [3 4]],
                mask =
        [[False True]
        [False False]],
            fill_value=999999)
>>> ma.getmask(a)
array([[False, True],
            [False, False]], dtype=bool)
```

Equivalently use the MaskedArray mask attribute.

```
>>> a.mask
array([[False, True],
    [False, False]], dtype=bool)
```

Result when mask $==$ nomask

```
>>> b = ma.masked_array([[1,2], [3,4]])
>>> b
masked_array(data =
    [[ll 2]
    [3 4]],
            mask =
    False,
            fill_value=999999)
>>> ma.nomask
False
>>> ma.getmask(b) == ma.nomask
True
>>> b.mask == ma.nomask
True
```

numpy.ma.getmaskarray (arr)

Return the mask of a masked array, or full boolean array of False.
Return the mask of arr as an ndarray if arr is a MaskedArray and the mask is not nomask, else return a full boolean array of False of the same shape as arr.

## Parameters

arr : array_like
Input MaskedArray for which the mask is required.

## See Also:

```
getmask
```

Return the mask of a masked array, or nomask.
getdata
Return the data of a masked array as an ndarray.
Examples

```
>>> import numpy.ma as ma
>>> a = ma.masked_equal([[1,2],[3,4]], 2)
>>> a
masked_array(data =
        [[1 --]
        [3 4]],
            mask =
        [[False True]
        [False False]],
            fill_value=999999)
>>> ma.getmaskarray(a)
array([[False, True],
            [False, False]], dtype=bool)
```

Result when mask $==$ nomask

```
>>> b = ma.masked_array([[1,2],[3,4]])
>>> b
masked_array(data =
    [[1 2]
    [3 4]],
                mask =
    False,
            fill_value=999999)
>>> >ma.getmaskarray(b)
array([[False, False],
    [False, False]], dtype=bool)
```

masked_array.mask
Mask

## Finding masked data

```
ma.flatnotmasked_contiguous(a) Find contiguous unmasked data in a masked array along the given axis.
ma.flatnotmasked_edges(a) Find the indices of the first and last unmasked values.
ma.notmasked_contiguous(a[,axis]) Find contiguous unmasked data in a masked array along the given axis.
ma.notmasked_edges(a[, axis]) Find the indices of the first and last unmasked values along an axis.
```

numpy.ma.flatnotmasked_contiguous (a)
Find contiguous unmasked data in a masked array along the given axis.

## Parameters

a : narray
The input array.

## Returns

slice_list : list
A sorted sequence of slices (start index, end index).

## See Also:

```
flatnotmasked_edges, notmasked_contiguous, notmasked_edges, clump_masked,
clump_unmasked
```


## Notes

Only accepts 2-D arrays at most.

## Examples

```
>>> a = np.ma.arange(10)
>>> np.ma.extras.flatnotmasked_contiguous(a)
slice(0, 10, None)
>>> mask = (a<3) | (a > 8) | (a == 5)
>>> a[mask] = np.ma.masked
>>> np.array(a[~a.mask])
array([3, 4, 6, 7, 8])
>>> np.ma.extras.flatnotmasked_contiguous(a)
[slice(3, 5, None), slice(6, 9, None)]
>>> a[:] = np.ma.masked
>>> print np.ma.extras.flatnotmasked_edges(a)
None
```

numpy.ma.flatnotmasked_edges (a)
Find the indices of the first and last unmasked values.
Expects a 1-D MaskedArray, returns None if all values are masked.

## Parameters

## arr : array_like

Input 1-D MaskedArray

## Returns

edges : ndarray or None
The indices of first and last non-masked value in the array. Returns None if all values are masked.

## See Also:

```
flatnotmasked_contiguous, notmasked_contiguous, notmasked_edges, clump_masked,
clump_unmasked
```


## Notes

Only accepts 1-D arrays.

## Examples

```
>>> a = np.ma.arange(10)
>>> flatnotmasked_edges(a)
[0,-1]
>>> mask = (a< 3) | (a > 8) | (a == 5)
>>> a[mask] = np.ma.masked
>>> np.array(a[~a.mask])
array([3, 4, 6, 7, 8])
```

```
>>> flatnotmasked_edges(a)
array([3, 8])
>>> a[:] = np.ma.masked
>>> print flatnotmasked_edges(ma)
None
```

numpy.ma.notmasked_contiguous (a, axis=None)
Find contiguous unmasked data in a masked array along the given axis.

## Parameters

a : array_like
The input array.
axis : int, optional
Axis along which to perform the operation. If None (default), applies to a flattened version of the array.

## Returns

endpoints : list
A list of slices (start and end indexes) of unmasked indexes in the array.

## See Also:

```
flatnotmasked_edges, flatnotmasked_contiguous, notmasked_edges, clump_masked,
clump_unmasked
```


## Notes

Only accepts 2-D arrays at most.

## Examples

```
>>> a = np.arange(9).reshape((3, 3))
>>> mask = np.zeros_like(a)
>>> mask[1:, 1:] = 1
>>> ma = np.ma.array(a, mask=mask)
>>> np.array(ma[~ma.mask])
array([0, 1, 2, 3, 6])
>>> np.ma.extras.notmasked_contiguous(ma)
[slice(0, 4, None), slice(6, 7, None)]
```

numpy.ma.notmasked_edges (a, axis=None)
Find the indices of the first and last unmasked values along an axis.
If all values are masked, return None. Otherwise, return a list of two tuples, corresponding to the indices of the first and last unmasked values respectively.

## Parameters

a : array_like
The input array.
axis : int, optional
Axis along which to perform the operation. If None (default), applies to a flattened version of the array.

## Returns

edges : ndarray or list
An array of start and end indexes if there are any masked data in the array. If there are no masked data in the array, edges is a list of the first and last index.

## See Also:

```
flatnotmasked_contiguous, flatnotmasked_edges, notmasked_contiguous,
clump_masked, clump_unmasked
```


## Examples

```
>>> a = np.arange(9).reshape((3, 3))
>>> m = np.zeros_like(a)
>>> m[1:, 1:] = 1
>>> am = np.ma.array(a, mask=m)
>>> np.array(am[~am.mask])
array([0, 1, 2, 3, 6])
>>> np.ma.extras.notmasked_edges(ma)
array([0, 6])
```


## Modifying a mask

| ma.mask_cols(a[, axis]) | Mask columns of a 2D array that contain masked values. |
| :--- | :--- |
| ma.mask_or(m1, m2[, copy, shrink]) | Combine two masks with the logical_or operator. |
| ma.mask_rowcols(a[, axis]) | Mask rows and/or columns of a 2D array that contain masked values. |
| ma.mask_rows(a[, axis]) | Mask rows of a 2D array that contain masked values. |
| ma.harden_mask(self) | Force the mask to hard. |
| ma.soften_mask(self) | Force the mask to soft. |
| ma.MaskedArray.harden_mask() | Force the mask to hard. |
| ma.MaskedArray.soften_mask() | Force the mask to soft. |
| ma.MaskedArray.shrink_mask() | Reduce a mask to nomask when possible. |
| ma.MaskedArray.unshare_mask() | Copy the mask and set the sharedmask flag to False. |

numpy.ma.mask_cols (a, axis=None)
Mask columns of a 2D array that contain masked values.
This function is a shortcut to mask_rowcols with axis equal to 1 .

## See Also:

mask_rowcols

## Mask rows and/or columns of a 2D array.

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.zeros((3, 3), dtype=np.int)
>>> a[1, 1] = 1
>>> a
array([[0, 0, 0],
    [0, 1, 0],
```

```
[0, 0, 0]])
>>> a = ma.masked_equal(a, 1)
>>> a
masked_array(data =
    [[0 0 0]
    [0 -- 0]
    [0 0 0]],
                mask =
    [[False False False]
    [False True False]
    [False False False]],
            fill_value=999999)
>>> ma.mask_cols(a)
masked_array(data =
    [[0 -- 0]
    [0 -- 0]
    [0 -- 0]],
        mask =
    [[False True False]
    [False True False]
    [False True False]],
        fill_value=999999)
```

numpy.ma.mask_or (m1, m2, copy=False, shrink=True)
Combine two masks with the logical_or operator.

The result may be a view on $m 1$ or $m 2$ if the other is nomask (i.e. False).

## Parameters

m1, m2 : array_like
Input masks.
copy : bool, optional
If copy is False and one of the inputs is nomask, return a view of the other input mask.
Defaults to False.
shrink : bool, optional
Whether to shrink the output to nomask if all its values are False. Defaults to True.

## Returns

mask : output mask
The result masks values that are masked in either $m 1$ or $m 2$.

## Raises

ValueError :
If $m 1$ and $m 2$ have different flexible dtypes.

## Examples

```
>>> m1 = np.ma.make_mask([0, 1, 1, 0])
>>> m2 = np.ma.make_mask([1, 0, 0, 0])
>>> np.ma.mask_or(m1, m2)
array([ True, True, True, False], dtype=bool)
```

numpy.ma.mask_rowcols (a, axis=None)
Mask rows and/or columns of a 2D array that contain masked values.

Mask whole rows and/or columns of a 2D array that contain masked values. The masking behavior is selected using the axis parameter.
-If axis is None, rows and columns are masked.
-If axis is 0 , only rows are masked.
-If axis is 1 or -1 , only columns are masked.

## Parameters

a : array_like, MaskedArray
The array to mask. If not a MaskedArray instance (or if no array elements are masked). The result is a MaskedArray with mask set to nomask (False). Must be a 2D array.
axis : int, optional
Axis along which to perform the operation. If None, applies to a flattened version of the array.

## Returns

a: MaskedArray
A modified version of the input array, masked depending on the value of the axis parameter.

## Raises

## NotImplementedError :

If input array $a$ is not 2 D .

## See Also:

```
mask_rows
```

Mask rows of a 2D array that contain masked values.

```
mask_cols
```

Mask cols of a 2D array that contain masked values.

```
masked_where
```

Mask where a condition is met.

## Notes

The input array's mask is modified by this function.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.zeros((3, 3), dtype=np.int)
>>> a[1, 1] = 1
>>> a
array([[0, 0, 0],
    [0, 1, 0],
    [0, 0, 0]])
>>> a = ma.masked_equal(a, 1)
>>> a
masked_array(data =
    [[0}0000
    [0 -- 0]
    [0 0 0]],
        mask =
```

```
[[False False False]
[False True False]
[False False False]],
            fill_value=999999)
>>> ma.mask_rowcols(a)
masked_array(data =
    [[0 -- 0]
    [-- -- --]
    [0 -- 0]],
        mask =
    [[False True False]
    [ True True True]
    [False True False]],
        fill_value=9999999)
```

numpy.ma.mask_rows (a, axis=None)
Mask rows of a 2D array that contain masked values.
This function is a shortcut to mask_rowcols with axis equal to 0 .

## See Also:

```
mask_rowcols
```

Mask rows and/or columns of a 2D array.
masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.zeros((3, 3), dtype=np.int)
>>> a[1, 1] = 1
>>> a
array([[0, 0, 0],
            [0, 1, 0],
            [0, 0, 0]])
>>> a = ma.masked_equal(a, 1)
>>> a
masked_array(data =
    [[0 0 0]
    [0 -- 0]
    [0 0 0 0]],
                mask =
    [[False False False]
    [False True False]
    [False False False]],
            fill_value=999999)
>>> ma.mask_rows(a)
masked_array(data =
    [[0 0 0]
    [-- -- --]
    [0 0 0]],
        mask =
    [[False False False]
    [ True True True]
    [False False False]],
        fill_value=999999)
```

numpy.ma.harden_mask (self)
Force the mask to hard.
Whether the mask of a masked array is hard or soft is determined by its hardmask property. harden_mask sets hardmask to True.

## See Also:

hardmask
numpy.ma.soften_mask (self)
Force the mask to soft.
Whether the mask of a masked array is hard or soft is determined by its hardmask property. soften_mask sets hardmask to False.

See Also:
hardmask
MaskedArray.harden_mask()
Force the mask to hard.
Whether the mask of a masked array is hard or soft is determined by its hardmask property. harden_mask sets hardmask to True.

## See Also:

hardmask
MaskedArray.soften_mask()
Force the mask to soft.
Whether the mask of a masked array is hard or soft is determined by its hardmask property. soften_mask sets hardmask to False.

## See Also:

hardmask
MaskedArray.shrink_mask()
Reduce a mask to nomask when possible.

## Parameters

None :

## Returns

## None :

## Examples

```
>>> x = np.ma.array([[1,2 ], [3, 4]], mask=[0]*4)
>>> x.mask
array([[False, False],
                    [False, False]], dtype=bool)
>>> x.shrink_mask()
>>> x.mask
False
```

MaskedArray.unshare_mask()

Copy the mask and set the sharedmask flag to False.
Whether the mask is shared between masked arrays can be seen from the sharedmask property. unshare_mask ensures the mask is not shared. A copy of the mask is only made if it was shared.

## See Also:

### 3.20.6 Conversion operations

```
> to a masked array
    ma.asarray(a[, dtype, order]) Convert the input to a masked array of the given data-type.
    ma.asanyarray(a[, dtype]) Convert the input to a masked array, conserving subclasses.
ma.fix_invalid(a[, mask, copy, fill_value]) Return input with invalid data masked and replaced by a fill
    value.
    ma.masked_equal(x, value[, copy]) Mask an array where equal to a given value.
ma.masked_greater(x, value[, copy]) Mask an array where greater than a given value.
ma.masked_greater_equal(x, value[, Mask an array where greater than or equal to a given value.
copy])
ma.masked_inside(x, v1, v2[, copy])
ma.masked_invalid(a[, copy])
ma.masked_less(x, value[, copy])
ma.masked_less_equal(x, value[, copy])
ma.masked_not_equal(x, value[, copy])
ma.masked_object(x, value[, copy, shrink])
ma.masked_outside(x, v1, v2[, copy])
ma.masked_values(x, value[, rtol, atol, ...])
ma.masked_where(condition, a[, copy]) Mask an array where a condition is met.
```

numpy.ma. asarray ( $a$, dtype=None, order=None)

Convert the input to a masked array of the given data-type.
No copy is performed if the input is already an ndarray. If $a$ is a subclass of MaskedArray, a base class MaskedArray is returned.

## Parameters

a : array_like
Input data, in any form that can be converted to a masked array. This includes lists, lists of tuples, tuples, tuples of tuples, tuples of lists, ndarrays and masked arrays.
dtype : dtype, optional
By default, the data-type is inferred from the input data.
order : \{ 'C', 'F' \}, optional
Whether to use row-major ('C') or column-major ('FORTRAN') memory representation. Default is ' C '.

## Returns

out : MaskedArray
Masked array interpretation of $a$.

## See Also:

asanyarray
Similar to asarray, but conserves subclasses.

## Examples

```
>>> x = np.arange(10.).reshape(2, 5)
>>> x
array([[ 0., 1., 2., 3., 4.],
    [ 5., 6., 7., 8., 9.]])
>>> np.ma.asarray(x)
masked_array(data =
    [[ 0. 1. 2. 3. 4.]
    [ 5. 6. 7. 8. 9.]],
                mask =
    False,
            fill_value = 1e+20)
>>> type(np.ma.asarray(x))
<class 'numpy.ma.core.MaskedArray'>
```

numpy.ma. asanyarray ( $a$, dtype=None)
Convert the input to a masked array, conserving subclasses.
If $a$ is a subclass of MaskedArray, its class is conserved. No copy is performed if the input is already an ndarray.

## Parameters

a : array_like
Input data, in any form that can be converted to an array.
dtype : dtype, optional
By default, the data-type is inferred from the input data.
order : \{ 'C', 'F' \}, optional
Whether to use row-major ('C') or column-major ('FORTRAN') memory representation. Default is ' C '.

## Returns

out : MaskedArray
MaskedArray interpretation of $a$.

## See Also:

```
asarray
```

Similar to asanyarray, but does not conserve subclass.

## Examples

```
>>> x = np.arange(10.).reshape(2, 5)
>>> x
array([[ 0., 1., 2., 3., 4.],
    [ 5., 6., 7., 8., 9.]])
>>> np.ma.asanyarray(x)
masked_array(data =
    [[ 0. 1. 2. 3. 4.]
    [ 5. 6. 7. 8. 9.]],
        mask =
        False,
            fill_value = 1e+20)
>>> type(np.ma.asanyarray(x))
<class 'numpy.ma.core.MaskedArray'>
```

numpy.ma.fix_invalid(a, mask=False, copy=True, fill_value=None)
Return input with invalid data masked and replaced by a fill value.
Invalid data means values of nan, inf, etc.

## Parameters

a : array_like
Input array, a (subclass of) ndarray.
copy : bool, optional
Whether to use a copy of $a$ (True) or to fix $a$ in place (False). Default is True.
fill_value : scalar, optional
Value used for fixing invalid data. Default is None, in which case the a.fill_value is used.

## Returns

b: MaskedArray
The input array with invalid entries fixed.

## Notes

A copy is performed by default.

## Examples

```
>>> x = np.ma.array([1., -1, np.nan, np.inf], mask=[1] + [0]*3)
>>> x
masked_array(data = [-- -1.0 nan inf],
                            mask = [ True False False False],
    fill_value = 1e+20)
>>> np.ma.fix_invalid(x)
masked_array(data = [-- -1.0 -- --],
            mask = [ True False True True],
            fill_value = 1e+20)
>>> fixed = np.ma.fix_invalid(x)
>>> fixed.data
array([ 1.00000000e+00, -1.000000000e+00, 1.000000000e+20,
    1.00000000e+20])
>>> x.data
array([ 1., -1., NaN, Inf])
```

numpy.ma.masked_equal ( $x$, value, copy=True)
Mask an array where equal to a given value.
This function is a shortcut to masked_where, with condition $=(x==$ value). For floating point arrays, consider using masked_values (x, value).

## See Also:

masked_where
Mask where a condition is met.
masked_values
Mask using floating point equality.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_equal(a, 2)
masked_array(data = [0 1 -- 3],
    mask = [False False True False],
    fill_value=999999)
```

numpy.ma.masked_greater ( $x$, value, copy=True)
Mask an array where greater than a given value.
This function is a shortcut to masked_where, with condition $=(\mathrm{x}>$ value $)$.

## See Also:

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_greater(a, 2)
masked_array(data = [0 1 2 --],
    mask = [False False False True],
    fill_value=999999)
```

numpy.ma.masked_greater_equal ( $x$, value, copy=True)
Mask an array where greater than or equal to a given value.
This function is a shortcut to masked_where, with condition $=(x>=$ value $)$.

## See Also:

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_greater_equal(a, 2)
masked_array(data = [0 1 -- --],
    mask = [False False True True],
    fill_value=999999)
```

numpy.ma.masked_inside ( $x, v 1, v 2$, copy=True)

Mask an array inside a given interval.
Shortcut to masked_where, where condition is True for $x$ inside the interval [v1,v2] (v1<= $\mathrm{x}<=\mathrm{v} 2$ ). The boundaries $v 1$ and $v 2$ can be given in either order.

## See Also:

## masked_where

Mask where a condition is met.

## Notes

The array $x$ is prefilled with its filling value.

## Examples

```
>>> import numpy.ma as ma
>>> x = [0.31, 1.2, 0.01, 0.2, -0.4, -1.1]
>>> ma.masked_inside(x, -0.3, 0.3)
masked_array(data = [0.31 1.2 -- -- -0.4 -1.1],
    mask = [False False True True False False],
    fill_value=1e+20)
```

The order of $v 1$ and $v 2$ doesn't matter.

```
>>> ma.masked_inside(x, 0.3, -0.3)
masked_array(data = [0.31 1.2 -- -- -0.4 -1.1],
    mask = [False False True True False False],
    fill_value=1e+20)
```

numpy.ma.masked_invalid (a, copy=True)

Mask an array where invalid values occur (NaNs or infs).
This function is a shortcut to masked_where, with condition $=\sim(n p . i s f i n i t e(a))$. Any pre-existing mask is conserved. Only applies to arrays with a dtype where NaNs or infs make sense (i.e. floating point types), but accepts any array_like object.

## See Also:

masked_where Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(5, dtype=np.float)
>>> a[2] = np.NaN
>>> a[3] = np.PINF
>>> a
array([ 0., 1., NaN, Inf, 4.])
>>> ma.masked_invalid(a)
masked_array(data = [0.0 1.0 -- -- 4.0],
mask = [False False True True False],
fill_value=1e+20)
```

numpy.ma.masked_less ( $x$, value, copy=True)
Mask an array where less than a given value.
This function is a shortcut to masked_where, with condition $=(x<$ value $)$.
See Also:
masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_less(a, 2)
masked_array(data = [-- -- 2 3],
    mask = [ True True False False],
    fill_value=999999)
```

numpy.ma.masked_less_equal ( $x$, value, copy=True)
Mask an array where less than or equal to a given value.
This function is a shortcut to masked_where, with condition $=(\mathrm{x}<=$ value $)$.

## See Also:

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_less_equal(a, 2)
masked_array(data = [-- -- -- 3],
mask = [ True True True False],
fill_value=999999)
```

numpy.ma.masked_not_equal ( $x$, value, copy=True)
Mask an array where not equal to a given value.
This function is a shortcut to masked_where, with condition $=(x!=$ value $)$.

## See Also:

masked_where
Mask where a condition is met.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_not_equal(a, 2)
masked_array(data = [-- -- 2 --],
mask = [ True True False True],
fill_value=999999)
```

numpy.ma.masked_object ( $x$, value, copy=True, shrink=True)
Mask the array $x$ where the data are exactly equal to value.
This function is similar to masked_values, but only suitable for object arrays: for floating point, use masked_values instead.

## Parameters

$\mathbf{x}$ : array_like

Array to mask
value : object
Comparison value
copy : \{True, False\}, optional
Whether to return a copy of $x$.
shrink : \{True, False \}, optional
Whether to collapse a mask full of False to nomask

## Returns

result : MaskedArray
The result of masking $x$ where equal to value.

## See Also:

masked_where
Mask where a condition is met.
masked_equal
Mask where equal to a given value (integers).
masked_values
Mask using floating point equality.

## Examples

```
>>> import numpy.ma as ma
>>> food = np.array(['green_eggs', 'ham'], dtype=object)
>>> # don't eat spoiled food
>>> eat = ma.masked_object(food, 'green_eggs')
>>> print eat
[-- ham]
>>> # plain ol' ham is boring
>>> fresh_food = np.array(['cheese', 'ham', 'pineapple'], dtype=object)
>>> eat = ma.masked_object(fresh_food, 'green_eggs')
>>> print eat
[cheese ham pineapple]
```

Note that mask is set to nomask if possible.

```
>>> eat
masked_array(data = [cheese ham pineapple],
    mask = False,
    fill_value=?)
```

numpy.ma.masked_outside ( $x, v 1, v 2$, copy=True)
Mask an array outside a given interval.
Shortcut to masked_where, where condition is True for $x$ outside the interval [v1,v2] ( $\mathrm{x}<\mathrm{v} 1) \mid(\mathrm{x}>\mathrm{v} 2)$. The boundaries $v 1$ and $v 2$ can be given in either order.

## See Also:

masked_where
Mask where a condition is met.

## Notes

The array $x$ is prefilled with its filling value.

## Examples

```
>>> import numpy.ma as ma
>>> x = [0.31, 1.2, 0.01, 0.2, -0.4, -1.1]
>>> ma.masked_outside(x, -0.3, 0.3)
masked_array(data = [-- -- 0.01 0.2 -- --],
    mask = [ True True False False True True],
    fill_value=1e+20)
```

The order of $v 1$ and $v 2$ doesn't matter.

```
>>> ma.masked_outside(x, 0.3, -0.3)
masked_array(data = [-- -- 0.01 0.2 -- --],
    mask = [ True True False False True True],
    fill_value=1e+20)
```

numpy.ma.masked_values $(x, \quad$ value,$\quad$ rtol $=1.0000000000000001 e-05, \quad$ atol $=1 e-08, \quad$ copy=True, shrink=True)
Mask using floating point equality.
Return a MaskedArray, masked where the data in array $x$ are approximately equal to value, i.e. where the following condition is True
(abs (x - value) <= atol+rtol*abs(value))
The fill_value is set to value and the mask is set to nomask if possible. For integers, consider using masked_equal.

## Parameters

$\mathbf{x}$ : array_like
Array to mask.
value : float
Masking value.
rtol : float, optional
Tolerance parameter.
atol : float, optional
Tolerance parameter (1e-8).
copy : bool, optional
Whether to return a copy of $x$.
shrink : bool, optional
Whether to collapse a mask full of False to nomask.

## Returns

result : MaskedArray
The result of masking $x$ where approximately equal to value.

## See Also:

masked_where
Mask where a condition is met.

```
masked_equal
```

Mask where equal to a given value (integers).

## Examples

```
>>> import numpy.ma as ma
>>> x = np.array([1, 1.1, 2, 1.1, 3])
>>> ma.masked_values(x, 1.1)
masked_array(data = [1.0 -- 2.0 -- 3.0],
    mask = [False True False True False],
    fill_value=1.1)
```

Note that mask is set to nomask if possible.

```
>>> ma.masked_values(x, 1.5)
masked_array(data = [ 1. 1.1 2. 1.1 3. ],
    mask = False,
    fill_value=1.5)
```

For integers, the fill value will be different in general to the result of masked_equal.

```
>>> x = np.arange(5)
>>> x
array([0, 1, 2, 3, 4])
>>> ma.masked_values(x, 2)
masked_array(data = [0 1 -- 3 4],
    mask = [False False True False False],
    fill_value=2)
>>> ma.masked_equal(x, 2)
masked_array(data = [0 1 -- 3 4],
    mask = [False False True False False],
    fill_value=999999)
```

numpy.ma.masked_where (condition, $a$, copy=True)
Mask an array where a condition is met.
Return $a$ as an array masked where condition is True. Any masked values of $a$ or condition are also masked in the output.

## Parameters

condition : array_like
Masking condition. When condition tests floating point values for equality, consider using masked_values instead.
a : array_like
Array to mask.
copy : bool
If True (default) make a copy of $a$ in the result. If False modify $a$ in place and return a view.

## Returns

result : MaskedArray
The result of masking $a$ where condition is True.

## See Also:

```
masked_values
```

Mask using floating point equality.
masked_equal
Mask where equal to a given value.
masked_not_equal
Mask where not equal to a given value.
masked_less_equal
Mask where less than or equal to a given value.

```
masked_greater_equal
```

Mask where greater than or equal to a given value.

```
masked_less
```

Mask where less than a given value.

```
masked_greater
```

Mask where greater than a given value.
masked_inside
Mask inside a given interval.
masked_outside
Mask outside a given interval.
masked_invalid
Mask invalid values (NaNs or infs).

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(4)
>>> a
array([0, 1, 2, 3])
>>> ma.masked_where(a <= 2, a)
masked_array(data = [-- -- -- 3],
    mask = [ True True True False],
    fill_value=999999)
```

Mask array $b$ conditional on $a$.

```
>>> b = ['a', ' b', 'c', 'd']
>>> ma.masked_where(a == 2, b)
masked_array(data = [a b -- d],
    mask = [False False True False],
    fill_value=N/A)
```

Effect of the copy argument.

```
>>> c = ma.masked_where(a <= 2, a)
>>> c
masked_array(data = [-- -- -- 3],
    mask = [ True True True False],
    fill_value=999999)
>>> c[0] = 99
>>> c
masked_array(data = [99 -- -- 3],
    mask = [False True True False],
    fill_value=999999)
>>> a
```

```
array([0, 1, 2, 3])
>>> c = ma.masked_where(a <= 2, a, copy=False)
>>> c[0] = 99
>>> C
masked_array(data = [99 -- -- 3],
    mask = [False True True False],
    fill_value=999999)
>>> a
array([99, 1, 2, 3])
```

When condition or $a$ contain masked values.

```
>>> a = np.arange(4)
>>> a = ma.masked_where(a == 2, a)
>>> a
masked_array(data = [0 1 -- 3],
    mask = [False False True False],
    fill_value=999999)
>>> b = np.arange(4)
>>> b = ma.masked_where(b == 0, b)
>>> b
masked_array(data = [-- 1 2 3],
    mask = [ True False False False],
    fill_value=999999)
>>> ma.masked_where(a == 3, b)
masked_array(data = [-- 1 -- --],
    mask = [ True False True True],
    fill_value=999999)
```


## > to a ndarray

```
ma.compress_cols(a)
ma.compress_rowcols(x[, axis])
ma.compress_rows(a)
ma. compressed(x)
ma.filled(a[, fill_value])
ma.MaskedArray.compressed() Return all the non-masked data as a 1-D array.
Suppress whole columns of a 2-D array that contain masked values.
Suppress the rows and/or columns of a 2-D array that contain
Suppress whole rows of a 2-D array that contain masked values.
Return all the non-masked data as a 1-D array.
Return input as an array with masked data replaced by a fill value.
ma.MaskedArray.filled([fill_value]) Return a copy of self, with masked values filled with a given value.
numpy.ma.compress_cols (a)
```

Suppress whole columns of a 2-D array that contain masked values.
This is equivalent to np.ma.extras.compress_rowcols (a, 1), see extras.compress_rowcols for details.

## See Also:

extras.compress_rowcols
numpy.ma.compress_rowcols ( $x$, axis=None)
Suppress the rows and/or columns of a 2-D array that contain masked values.
The suppression behavior is selected with the axis parameter.
-If axis is None, both rows and columns are suppressed.
-If axis is 0 , only rows are suppressed.
-If axis is 1 or -1 , only columns are suppressed.

## Parameters

axis : int, optional
Axis along which to perform the operation. Default is None.

## Returns

compressed_array : ndarray
The compressed array.

## Examples

```
>>> x = np.ma.array(np.arange(9).reshape(3, 3), mask=[[1, 0, 0],
... [1, 0, 0],
... [0, 0, 0]])
>>> x
masked_array(data =
    [[-- 1 2]
    [-- 4 5]
    [llll
            mask =
    [[ True False False]
    [ True False False]
    [False False False]],
            fill_value = 999999)
>>> np.ma.extras.compress_rowcols(x)
array([[7, 8]])
>>> np.ma.extras.compress_rowcols(x, 0)
array([[6, 7, 8]])
>>> np.ma.extras.compress_rowcols(x, 1)
array([[1, 2],
    [4, 5],
    [7, 8]])
```

numpy.ma.compress_rows (a)
Suppress whole rows of a 2-D array that contain masked values.
This is equivalent to np.ma.extras.compress_rowcols (a, 0 ), see extras.compress_rowcols for details.

## See Also:

extras.compress_rowcols
numpy.ma.compressed ( $x$ )
Return all the non-masked data as a 1-D array.
This function is equivalent to calling the "compressed" method of a MaskedArray, see MaskedArray.compressed for details.

## See Also:

MaskedArray. compressed
Equivalent method.
numpy.ma.filled (a, fill_value=None)
Return input as an array with masked data replaced by a fill value.
If $a$ is not a MaskedArray, $a$ itself is returned. If $a$ is a MaskedArray and fill_value is None, fill_value is set to a.fill_value.

## Parameters

a : MaskedArray or array_like
An input object.
fill_value : scalar, optional
Filling value. Default is None.

## Returns

a : ndarray
The filled array.

## See Also:

compressed

## Examples

```
>>> x = np.ma.array(np.arange(9).reshape(3, 3), mask=[[1, 0, 0],
... [1, 0, 0],
... [0, 0, 0]])
>>> x.filled()
array([[999999, 1, 2],
    [999999, 4, 5],
    [ 6, 7, 8]])
```

MaskedArray. compressed()

Return all the non-masked data as a 1-D array.

## Returns

data : ndarray
A new ndarray holding the non-masked data is returned.

## Notes

The result is not a MaskedArray!

## Examples

```
>>> x = np.ma.array(np.arange(5), mask=[0]*2 + [1]*3)
>>> x.compressed()
array([0, 1])
>>> type(x.compressed())
<type 'numpy.ndarray'>
MaskedArray.filled (fill_value=None)
Return a copy of self, with masked values filled with a given value.
```


## Parameters

fill_value : scalar, optional
The value to use for invalid entries (None by default). If None, the fill_value attribute of the array is used instead.

## Returns

filled_array : ndarray
A copy of self with invalid entries replaced by fill_value (be it the function argument or the attribute of self.

## Notes

The result is not a MaskedArray!

## Examples

```
>>> x = np.ma.array([1,2,3,4,5], mask=[0,0,1,0,1], fill_value=-999)
>>> x.filled()
array([1, 2, -999, 4, -999])
>>> type(x.filled())
<type 'numpy.ndarray'>
```

Subclassing is preserved. This means that if the data part of the masked array is a matrix, filled returns a matrix:

```
>>> x = np.ma.array(np.matrix([[1, 2], [3, 4]]), mask=[[0, 1], [1, 0]])
>>> x.filled()
matrix([[ 1, 999999],
    [999999, 4]])
```

$>$ to another object
ma.MaskedArray.tofile(fid[, sep, Save a masked array to a file in binary format.
format])
ma.MaskedArray.tolist([fill_value]) Return the data portion of the masked array as a hierarchical
Python list.
ma.MaskedArray.torecords()
ma.MaskedArray.tostring([fill_value,
order])
Transforms a masked array into a flexible-type array.
Return the array data as a string containing the raw bytes in the
array.
MaskedArray.tofile (fid, sep=', format='\%s')

Save a masked array to a file in binary format.
Warning: This function is not implemented yet.

## Raises

## NotImplementedError :

When tofile is called.
MaskedArray.tolist (fill_value=None)
Return the data portion of the masked array as a hierarchical Python list.
Data items are converted to the nearest compatible Python type. Masked values are converted to fill_value. If fill_value is None, the corresponding entries in the output list will be None.

## Parameters

fill_value : scalar, optional
The value to use for invalid entries. Default is None.

## Returns

result : list
The Python list representation of the masked array.

## Examples

```
>>> x = np.ma.array([[1,2,3], [4,5,6], [7,8,9]], mask=[0] + [1,0]*4)
>>> x.tolist()
[[1, None, 3], [None, 5, None], [7, None, 9]]
```

```
>>> x.tolist(-999)
[[1, -999, 3], [-999, 5, -999], [7, -999, 9]]
```

MaskedArray.torecords()
Transforms a masked array into a flexible-type array.
The flexible type array that is returned will have two fields:
-the _data field stores the _data part of the array.
-the _mask field stores the _mask part of the array.

## Parameters

## None :

## Returns

record : ndarray
A new flexible-type ndarray with two fields: the first element containing a value, the second element containing the corresponding mask boolean. The returned record shape matches self.shape.

## Notes

A side-effect of transforming a masked array into a flexible ndarray is that meta information (fill_value, ...) will be lost.

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 --]
    [7 -- 9]]
>>> print x.toflex()
[[(1, False) (2, True) (3, False)]
    [(4, True) (5, False) (6, True)]
    [(7, False) (8, True) (9, False)]]
MaskedArray.tostring (fill_value=None,order='C')
```

Return the array data as a string containing the raw bytes in the array.
The array is filled with a fill value before the string conversion.

## Parameters

fill_value : scalar, optional
Value used to fill in the masked values. Deafult is None, in which case MaskedArray.fill_value is used.
order : \{ ' C ', ' F ', ' A ' $\}$, optional
Order of the data item in the copy. Default is ' C '.

- 'C' - C order (row major).
- 'F' - Fortran order (column major).
- 'A' - Any, current order of array.
- None - Same as 'A'.


## See Also:

```
ndarray.tostring,tolist,tofile
```


## Notes

As for ndarray.tostring, information about the shape, dtype, etc., but also about fill_value, will be lost.

## Examples

```
>>> x = np.ma.array(np.array([[1, 2], [3, 4]]), mask=[[0, 1], [1, 0]])
>>> x.tostring()
'\x01\x00\x00\x00?B\x0f\x00?B\x0f\x00\x04\x00\x00\x00'
```


## Pickling and unpickling

ma. dump(a, F) Pickle a masked array to a file.
ma. dumps(a) Return a string corresponding to the pickling of a masked array.
ma.load(F) Wrapper around cPickle.load which accepts either a file-like object
ma.loads(strg) Load a pickle from the current string.
numpy.ma. dump ( $a, F$ )
Pickle a masked array to a file.
This is a wrapper around cPickle.dump.

## Parameters

a : MaskedArray
The array to be pickled.
F : str or file-like object
The file to pickle $a$ to. If a string, the full path to the file.
numpy.ma.dumps (a)
Return a string corresponding to the pickling of a masked array.
This is a wrapper around cPickle.dumps.

## Parameters

a : MaskedArray
The array for which the string representation of the pickle is returned.
numpy.ma.load (F)
Wrapper around cPickle.load which accepts either a file-like object or a filename.

## Parameters

F : str or file
The file or file name to load.

## See Also:

dump
Pickle an array

## Notes

This is different from numpy. load, which does not use cPickle but loads the NumPy binary .npy format.
numpy.ma.loads (strg)
Load a pickle from the current string.
The result of cPickle.loads (strg) is returned.

## Parameters

strg : str
The string to load.

## See Also:

dumps
Return a string corresponding to the pickling of a masked array.

## Filling a masked array

| ma.common_fill_value(a, b) | Return the common filling value of two masked arrays, if any. |
| :---: | :---: |
| ma.default_fill_value(obj) | Return the default fill value for the argument object. |
| ma.maximum_fill_value(obj) | Return the minimum value that can be represented by the dtype of an object. |
| ma.maximum_fill_value(obj) | Return the minimum value that can be represented by the dtype of an object. |
| ma.set_fill_value(a, fill_value) | Set the filling value of a , if a is a masked array. |
| ma.MaskedArray.get_fill_value() | Return the filling value of the masked array. |
| ma.MaskedArray.set_fill_value([valde\})the filling value of the masked array. |  |
| ma.MaskedArray.fill_value | Filling value. |

numpy.ma.common_fill_value $(a, b)$
Return the common filling value of two masked arrays, if any.
If a.fill_value == b.fill_value, return the fill value, otherwise return None.

## Parameters

$\mathbf{a}, \mathbf{b}$ : MaskedArray
The masked arrays for which to compare fill values.

## Returns

fill_value : scalar or None
The common fill value, or None.

## Examples

```
>>> x = np.ma.array([0, 1.], fill_value=3)
>>> y = np.ma.array([0, 1.], fill_value=3)
>>> np.ma.common_fill_value(x, y)
3.0
```

```
numpy.ma.default_fill_value(obj)
```

Return the default fill value for the argument object.
The default filling value depends on the datatype of the input array or the type of the input scalar:

| datatype | default |
| :--- | :--- |
| bool | True |
| int | 999999 |
| float | $1 . \mathrm{e} 20$ |
| complex | $1 . \mathrm{e} 20+0 \mathrm{j}$ |
| object | '?' |
| string | 'N/A' |

## Parameters

obj : ndarray, dtype or scalar
The array data-type or scalar for which the default fill value is returned.

## Returns

fill_value : scalar
The default fill value.

## Examples

```
>>> np.ma.default_fill_value(1)
999999
>>> np.ma.default_fill_value(np.array([1.1, 2., np.pi]))
1e+20
>>> np.ma.default_fill_value(np.dtype(complex))
(1e+20+0j)
```

numpy.ma.maximum_fill_value (obj)
Return the minimum value that can be represented by the dtype of an object.
This function is useful for calculating a fill value suitable for taking the maximum of an array with a given dtype.

## Parameters

obj : \{ndarray, dtype \}
An object that can be queried for it's numeric type.

## Returns

val : scalar
The minimum representable value.

## Raises

## TypeError :

If obj isn't a suitable numeric type.

## See Also:

minimum_fill_value
The inverse function.
set_fill_value
Set the filling value of a masked array.
MaskedArray.fill_value
Return current fill value.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.int8()
>>> ma.maximum_fill_value(a)
-128
>>> a = np.int32()
>>> ma.maximum_fill_value(a)
-2147483648
```

An array of numeric data can also be passed.

```
>>> a = np.array([1, 2, 3], dtype=np.int8)
>>> ma.maximum_fill_value(a)
-128
>>> a = np.array([1, 2, 3], dtype=np.float32)
>>> ma.maximum_fill_value(a)
-inf
```

numpy.ma.maximum_fill_value (obj)
Return the minimum value that can be represented by the dtype of an object.
This function is useful for calculating a fill value suitable for taking the maximum of an array with a given dtype.

## Parameters

obj : \{ndarray, dtype \}
An object that can be queried for it's numeric type.

## Returns

val : scalar
The minimum representable value.

## Raises

## TypeError :

If obj isn't a suitable numeric type.

## See Also:

minimum_fill_value
The inverse function.
set_fill_value
Set the filling value of a masked array.
MaskedArray.fill_value
Return current fill value.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.int8()
>>> ma.maximum_fill_value(a)
-128
>>> a = np.int32()
>>> ma.maximum_fill_value(a)
-2147483648
```

An array of numeric data can also be passed.

```
>>> a = np.array([1, 2, 3], dtype=np.int8)
>>> ma.maximum_fill_value(a)
-128
>>> a = np.array([1, 2, 3], dtype=np.float32)
>>> ma.maximum_fill_value(a)
-inf
numpy.ma.set_fill_value (a,fill_value)
```

Set the filling value of $a$, if $a$ is a masked array.
This function changes the fill value of the masked array $a$ in place. If $a$ is not a masked array, the function returns silently, without doing anything.

## Parameters

a: array_like
Input array.
fill_value : dtype
Filling value. A consistency test is performed to make sure the value is compatible with the dtype of $a$.

## Returns

## None :

Nothing returned by this function.

## See Also:

maximum_fill_value
Return the default fill value for a dtype.
MaskedArray.fill_value
Return current fill value.
MaskedArray.set_fill_value
Equivalent method.

## Examples

```
>>> import numpy.ma as ma
>>> a = np.arange(5)
>>> a
array([0, 1, 2, 3, 4])
>>> a = ma.masked_where(a < 3, a)
>>> a
masked_array(data = [-- -- -- 3 4],
    mask = [ True True True False False],
    fill_value=999999)
>>> ma.set_fill_value(a, -999)
>>> a
masked_array(data = [-- -- -- 3 4],
    mask = [ True True True False False],
    fill_value=-999)
```

Nothing happens if $a$ is not a masked array.

```
>>> a = range(5)
>>> a
[0, 1, 2, 3, 4]
```

```
>>> ma.set_fill_value(a, 100)
>>> a
[0, 1, 2, 3, 4]
>>> a = np.arange(5)
>>> a
array([0, 1, 2, 3, 4])
>>> ma.set_fill_value(a, 100)
>>> a
array([0, 1, 2, 3, 4])
```

MaskedArray.get_fill_value()

Return the filling value of the masked array.

## Returns

fill_value : scalar
The filling value.

## Examples

```
>>> for dt in [np.int32, np.int64, np.float64, np.complex128]:
... np.ma.array([0, 1], dtype=dt).get_fill_value()
. .
999999
999999
1e+20
(1e+20+0j)
>>> x = np.ma.array([0, 1.], fill_value=-np.inf)
>>> x.get_fill_value()
-inf
MaskedArray.set_fill_value (value=None)
```

Set the filling value of the masked array.

## Parameters

value : scalar, optional
The new filling value. Default is None, in which case a default based on the data type is used.

## See Also:

ma.set_fill_value
Equivalent function.

## Examples

```
>>> x = np.ma.array([0, 1.], fill_value=-np.inf)
>>> x.fill_value
-inf
>>> x.set_fill_value(np.pi)
>>> x.fill_value
3.1415926535897931
```

Reset to default:

```
>>> x.set_fill_value()
>>> x.fill_value
1e+20
```


### 3.20.7 Masked arrays arithmetics

## Arithmetics

| ma | Compute the anomalies (deviations from the arithmetic mean) along the given axis. |
| :---: | :---: |
| ma.anomalies(self[, axis, dtype]) | Compute the anomalies (deviations from the arithmetic mean) along the given axis. |
| ma. average (a[, axis, weights, returned]) | Return the weighted average of array over the given axis. |
| ma.conjugat | Retu |
| ma.corrcoef(x[, y, rowvar, bias, ...]) | Return correlation coefficients of the input array. |
| ma. $\operatorname{cov}(x[, y$, rowvar, bias, allow_masked, ddof]) | Estimate the covariance matrix. |
| ma. cumsum(self[, axis, dtype, | Return the cumulative sum of the elements along the given axis. |
| ma.cumprod(self[, axis, dtype, out]) | Return the cumulative product of the elements along the given axis. |
| ma.mean(self[, axis, dtype, out]) | Returns the average of the array elements. |
| ma.median(a[, axis, out, overwrite_input]) | Compute the median along the specified axis. |
| ma.power (a, b[, third]) | Returns element-wise base array raised to power from second array. |
| ma.prod(self[, axis, dtype, out]) | Return the product of the array elements over the given axis. |
| ma.std(self[, axis, dtype, out, ddof] | Compute the standard deviation along the specified axis. |
| ma.sum(self[, axis, dtype, out]) | Return the sum of the array elements over the given axis. |
| ma.var(self[, axis, dtype, out, ddof]) | Compute the variance along the specified axis. |
| ma.MaskedArray.anom([axis, dtype]) | Compute the anomalies (deviations from the arithmetic mean) along the given axis. |
| ma.MaskedArray.cumprod([axis, dtype, out]) | Return the cumulative product of the elements along the given axis. |
| ma.MaskedArray.cumsum([axis, dtype, out]) | Return the cumulative sum of the elements along the given axis. |
| ma.MaskedArray.mean([axis, dtype, out]) | Returns the average of the array elements. |
| ma.MaskedArray.prod([axis, dtype, out]) | Return the product of the array elements over the given axis. |
| ma.MaskedArray.std([axis, dtype, out, ddof]) | Compute the standard deviation along the specified axis. |
| ma.MaskedArray.sum([axis, dtype, out]) | Return the sum of the array elements over the given axis. |
| ma.MaskedArray.var([axis, dtype, out, ddof]) | Compute the variance along the specified axis. |

numpy.ma. anom (self, axis=None, dtype=None)
Compute the anomalies (deviations from the arithmetic mean) along the given axis.
Returns an array of anomalies, with the same shape as the input and where the arithmetic mean is computed along the given axis.

## Parameters

axis : int, optional

Axis over which the anomalies are taken. The default is to use the mean of the flattened array as reference.
dtype : dtype, optional
Type to use in computing the variance. For arrays of integer type the default is float 32 ; for arrays of float types it is the same as the array type.

```
See Also:
mean
            Compute the mean of the array.
Examples
>>> a = np.ma.array([1,2,3])
>>> a.anom()
masked_array(data = [-1. 0. 1.],
                    mask = False,
            fill_value = 1e+20)
```

numpy.ma.anomalies (self, axis=None, dtype=None)

Compute the anomalies (deviations from the arithmetic mean) along the given axis.
Returns an array of anomalies, with the same shape as the input and where the arithmetic mean is computed along the given axis.

## Parameters

axis : int, optional
Axis over which the anomalies are taken. The default is to use the mean of the flattened array as reference.
dtype : dtype, optional
Type to use in computing the variance. For arrays of integer type the default is float 32 ; for arrays of float types it is the same as the array type.

## See Also:

mean
Compute the mean of the array.

## Examples

```
>>> a = np.ma.array([1,2,3])
>>> a.anom()
masked_array(data = [-1. 0. 1.],
                    mask = False,
                    fill_value = 1e+20)
```

numpy.ma. average ( $a$, axis=None, weights $=$ None, returned $=$ False $)$

Return the weighted average of array over the given axis.

## Parameters

a : array_like
Data to be averaged. Masked entries are not taken into account in the computation.
axis : int, optional

Axis along which the variance is computed. The default is to compute the variance of the flattened array.
weights : array_like, optional
The importance that each element has in the computation of the average. The weights array can either be 1-D (in which case its length must be the size of $a$ along the given axis) or of the same shape as $a$. If weights=None, then all data in $a$ are assumed to have a weight equal to one.
returned : bool, optional
Flag indicating whether a tuple (result, sum of weights) should be returned as output (True), or just the result (False). Default is False.

## Returns

average, [sum_of_weights] : (tuple of) scalar or MaskedArray
The average along the specified axis. When returned is True, return a tuple with the average as the first element and the sum of the weights as the second element. The return type is $n p$.float64 if $a$ is of integer type, otherwise it is of the same type as $a$. If returned, sum_of_weights is of the same type as average.

## Examples

```
>>> a = np.ma.array([1., 2., 3., 4.], mask=[False, False, True, True])
>>> np.ma.average(a, weights=[3, 1, 0, 0])
1.25
>>> x = np.ma.arange(6.).reshape(3, 2)
>>> print x
[[ 0. 1.]
    [ 2. 3.]
    [ 4. 5.]]
>>> avg, sumweights = np.ma.average(x, axis=0, weights=[1, 2, 3],
... returned=True)
>>> print avg
[2.66666666667 3.66666666667]
numpy.ma.conjugate (x[,out ])
```

Return the complex conjugate, element-wise.
The complex conjugate of a complex number is obtained by changing the sign of its imaginary part.

## Parameters

$\mathbf{x}$ : array_like
Input value.

## Returns

y : ndarray
The complex conjugate of $x$, with same dtype as $y$.

## Examples

```
>>> np.conjugate(1+2j)
(1-2j)
>>> x = np.eye(2) + 1j * np.eye(2)
>>> np.conjugate(x)
```

```
array([[ 1.-1.j, 0.-0.j],
    [ 0.-0.j, 1.-1.j]])
```

numpy.ma.corrcoef ( $x, y=$ None, rowvar=True, bias=False, allow_masked=True, $d d o f=$ None $)$

Return correlation coefficients of the input array.
Except for the handling of missing data this function does the same as numpy. corrcoef. For more details and examples, see numpy. corrcoef.

## Parameters

$\mathbf{x}$ : array_like
A 1-D or 2-D array containing multiple variables and observations. Each row of $x$ represents a variable, and each column a single observation of all those variables. Also see rowvar below.
y : array_like, optional
An additional set of variables and observations. $y$ has the same shape as $x$.
rowvar : bool, optional
If rowvar is True (default), then each row represents a variable, with observations in the columns. Otherwise, the relationship is transposed: each column represents a variable, while the rows contain observations.
bias : bool, optional
Default normalization (False) is by ( $\mathrm{N}-1$ ), where N is the number of observations given (unbiased estimate). If bias is 1, then normalization is by N. This keyword can be overridden by the keyword ddof in numpy versions $>=1.5$.
allow_masked : bool, optional
If True, masked values are propagated pair-wise: if a value is masked in $x$, the corresponding value is masked in $y$. If False, raises an exception.
ddof : \{None, int \}, optional
New in version 1.5. If not None normalization is by ( N - ddof), where N is the number of observations; this overrides the value implied by bias. The default value is None.

## See Also:

numpy.corrcoef
Equivalent function in top-level NumPy module.
cov
Estimate the covariance matrix.
numpy.ma.cov ( $x, y=$ None, rowvar=True, bias=False, allow_masked=True, $d d o f=$ None $)$
Estimate the covariance matrix.
Except for the handling of missing data this function does the same as numpy.cov. For more details and examples, see numpy.cov.

By default, masked values are recognized as such. If $x$ and $y$ have the same shape, a common mask is allocated: if $x[i, j]$ is masked, then $y[i, j]$ will also be masked. Setting allow_masked to False will raise an exception if values are missing in either of the input arrays.

## Parameters

$\mathbf{x}$ : array_like

A 1-D or 2-D array containing multiple variables and observations. Each row of $x$ represents a variable, and each column a single observation of all those variables. Also see rowvar below.
$\mathbf{y}$ : array_like, optional
An additional set of variables and observations. $y$ has the same form as $x$.
rowvar : bool, optional
If rowvar is True (default), then each row represents a variable, with observations in the columns. Otherwise, the relationship is transposed: each column represents a variable, while the rows contain observations.
bias : bool, optional
Default normalization (False) is by ( $\mathrm{N}-1$ ), where N is the number of observations given (unbiased estimate). If bias is True, then normalization is by N. This keyword can be overridden by the keyword ddof in numpy versions $>=1.5$.
allow_masked : bool, optional
If True, masked values are propagated pair-wise: if a value is masked in $x$, the corresponding value is masked in $y$. If False, raises a ValueError exception when some values are missing.
ddof : \{None, int \}, optional
New in version 1.5. If not None normalization is by ( $N$ - ddof), where $N$ is the number of observations; this overrides the value implied by bias. The default value is None.

## Raises

## ValueError: :

Raised if some values are missing and allow_masked is False.

## See Also:

numpy.cov
numpy.ma. cumsum (self, axis=None, dtype=None, out=None)
Return the cumulative sum of the elements along the given axis. The cumulative sum is calculated over the flattened array by default, otherwise over the specified axis.
Masked values are set to 0 internally during the computation. However, their position is saved, and the result will be masked at the same locations.

## Parameters

axis : \{None, -1 , int \}, optional
Axis along which the sum is computed. The default (axis = None) is to compute over the flattened array. axis may be negative, in which case it counts from the last to the first axis.
dtype : \{None, dtype\}, optional
Type of the returned array and of the accumulator in which the elements are summed. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used.
out : ndarray, optional

Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

cumsum : ndarray.
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## Notes

The mask is lost if out is not a valid MaskedArray!
Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> marr = np.ma.array(np.arange(10), mask=[0,0,0,1,1,1,0,0,0,0])
>>> print marr.cumsum()
[00 1 3 -- -- -- 9 16 24 33]
```

numpy.ma. cumprod (self, axis=None, dtype=None, out=None)
Return the cumulative product of the elements along the given axis. The cumulative product is taken over the flattened array by default, otherwise over the specified axis.

Masked values are set to 1 internally during the computation. However, their position is saved, and the result will be masked at the same locations.

## Parameters

axis: \{None, -1 , int \}, optional
Axis along which the product is computed. The default (axis $=$ None) is to compute over the flattened array.
dtype : \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are multiplied. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

cumprod : ndarray
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## Notes

The mask is lost if out is not a valid MaskedArray!
Arithmetic is modular when using integer types, and no error is raised on overflow.
numpy .ma.mean (self, axis=None, dtype=None, out=None)
Returns the average of the array elements.
Masked entries are ignored. The average is taken over the flattened array by default, otherwise over the specified axis. Refer to numpy . mean for the full documentation.

## Parameters

a : array_like
Array containing numbers whose mean is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the means are computed. The default is to compute the mean of the flattened array.
dtype : dtype, optional
Type to use in computing the mean. For integer inputs, the default is float64; for floating point, inputs it is the same as the input dtype.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type will be cast if necessary.

## Returns

mean : ndarray, see dtype parameter above
If out=None, returns a new array containing the mean values, otherwise a reference to the output array is returned.

## See Also:

```
numpy.ma.mean
```

Equivalent function.

```
numpy.mean
```

Equivalent function on non-masked arrays.
numpy.ma. average
Weighted average.

## Examples

```
>>> a = np.ma.array([1,2,3], mask=[False, False, True])
>>> a
masked_array(data = [1 2 -- ],
                    mask = [False False True],
        fill_value = 999999)
>>> a.mean()
1.5
numpy.ma.median (a,axis=None,out=None,overwrite_input=False)
Compute the median along the specified axis.
Returns the median of the array elements.
```


## Parameters

a : array_like
Input array or object that can be converted to an array.
axis : int, optional
Axis along which the medians are computed. The default (None) is to compute the median along a flattened version of the array.
out : ndarray, optional

Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.
overwrite_input : bool, optional
If True, then allow use of memory of input array (a) for calculations. The input array will be modified by the call to median. This will save memory when you do not need to preserve the contents of the input array. Treat the input as undefined, but it will probably be fully or partially sorted. Default is False. Note that, if overwrite_input is True, and the input is not already an ndarray, an error will be raised.

## Returns

median : ndarray
A new array holding the result is returned unless out is specified, in which case a reference to out is returned. Return data-type is float64 for integers and floats smaller than float64, or the input data-type, otherwise.

## See Also:

mean

## Notes

Given a vector V with N non masked values, the median of V is the middle value of a sorted copy of $\mathrm{V}(\mathrm{Vs})$ - i.e. $\operatorname{Vs}[(\mathrm{N}-1) / 2]$, when N is odd, or $\{\operatorname{Vs}[\mathrm{N} / 2-1]+\operatorname{Vs}[\mathrm{N} / 2]\} / 2$ when N is even.

## Examples

```
>>> x = np.ma.array(np.arange(8), mask=[0]*4 + [1]*4)
>>> np.ma.extras.median(x)
1.5
>>> x = np.ma.array(np.arange(10).reshape(2, 5), mask=[0]*6 + [1]*4)
>>> np.ma.extras.median(x)
2.5
>>> np.ma.extras.median(x, axis=-1, overwrite_input=True)
masked_array(data = [ 2. 5.],
            mask = False,
    fill_value = 1e+20)
```

numpy.ma.power ( $a, b$, third=None)
Returns element-wise base array raised to power from second array.
This is the masked array version of numpy . power. For details see numpy . power.

## See Also:

numpy.power

## Notes

The out argument to numpy . power is not supported, third has to be None.
numpy.ma.prod (self, axis=None, dtype=None, out=None)
Return the product of the array elements over the given axis. Masked elements are set to 1 internally for computation.

## Parameters

axis : \{None, int \}, optional
Axis over which the product is taken. If None is used, then the product is over all the array elements.
dtype : \{None, dtype \}, optional
Determines the type of the returned array and of the accumulator where the elements are multiplied. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : \{None, array \}, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type will be cast if necessary.

## Returns

product_along_axis : \{array, scalar\}, see dtype parameter above.
Returns an array whose shape is the same as a with the specified axis removed. Returns a 0 d array when a is 1 d or axis=None. Returns a reference to the specified output array if specified.

## See Also:

prod
equivalent function

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> np.prod([1.,2.])
2.0
>>> np.prod([1.,2.], dtype=np.int32)
2
>>> np.prod([[1.,2.],[3.,4.]])
24.0
>>> np.prod([[1.,2.],[3.,4.]], axis=1)
array([ 2., 12.])
```

numpy.ma.std (self, axis=None, dtype=None, out=None, ddof=0)
Compute the standard deviation along the specified axis.
Returns the standard deviation, a measure of the spread of a distribution, of the array elements. The standard deviation is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a: array_like
Calculate the standard deviation of these values.
axis : int, optional
Axis along which the standard deviation is computed. The default is to compute the standard deviation of the flattened array.
dtype : dtype, optional
Type to use in computing the standard deviation. For arrays of integer type the default is float64, for arrays of float types it is the same as the array type.
out : ndarray, optional

Alternative output array in which to place the result. It must have the same shape as the expected output but the type (of the calculated values) will be cast if necessary.
ddof : int, optional
Means Delta Degrees of Freedom. The divisor used in calculations is N - ddof, where N represents the number of elements. By default $d d o f$ is zero.

## Returns

standard_deviation : ndarray, see dtype parameter above.
If out is None, return a new array containing the standard deviation, otherwise return a reference to the output array.

## See Also:

var, mean
numpy. doc. ufuncs
Section "Output arguments"

## Notes

The standard deviation is the square root of the average of the squared deviations from the mean, i.e., std $=$ sqrt (mean (abs (x - x.mean()) **2)).

The average squared deviation is normally calculated as $x . \operatorname{sum}() / N$, where $N=$ len(x). If, however, $d d o f$ is specified, the divisor $N$ - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of the infinite population. ddof $=0$ provides a maximum likelihood estimate of the variance for normally distributed variables. The standard deviation computed in this function is the square root of the estimated variance, so even with $d d o f=1$, it will not be an unbiased estimate of the standard deviation per se.

Note that, for complex numbers, std takes the absolute value before squaring, so that the result is always real and nonnegative.

For floating-point input, the std is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higheraccuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.std(a)
1.1180339887498949
>>> np.std(a, axis=0)
array([ 1., 1.])
>>> np.std(a, axis=1)
array([ 0.5, 0.5])
```

In single precision, $\operatorname{std}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.std(a)
0.45172946707416706
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.std(a, dtype=np.float64)
0.44999999925552653
```

numpy.ma.sum (self, axis=None, dtype=None, out=None)
Return the sum of the array elements over the given axis. Masked elements are set to 0 internally.

## Parameters

axis : \{None, -1 , int \}, optional
Axis along which the sum is computed. The default (axis $=$ None) is to compute over the flattened array.
dtype : \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are summed. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : \{None, ndarray \}, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

sum_along_axis : MaskedArray or scalar
An array with the same shape as self, with the specified axis removed. If self is a $0-\mathrm{d}$ array, or if axis is None, a scalar is returned. If an output array is specified, a reference to out is returned.

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 --]
    [7 -- 9]]
>>> print x.sum()
25
>>> print x.sum(axis=1)
[4 5 16]
>>> print x.sum(axis=0)
[8 5 12]
>>> print type(x.sum(axis=0, dtype=np.int64)[0])
<type 'numpy.int64'>
```

numpy.ma. var (self, axis=None, dtype=None, out=None, ddof=0)

Compute the variance along the specified axis.
Returns the variance of the array elements, a measure of the spread of a distribution. The variance is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Array containing numbers whose variance is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the variance is computed. The default is to compute the variance of the flattened array.
dtype : data-type, optional

Type to use in computing the variance. For arrays of integer type the default is float 32 ; for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output, but the type is cast if necessary.
ddof : int, optional
"Delta Degrees of Freedom": the divisor used in the calculation is N - ddof, where N represents the number of elements. By default ddof is zero.

## Returns

variance : ndarray, see dtype parameter above
If out $=$ None, returns a new array containing the variance; otherwise, a reference to the output array is returned.

## See Also:

std
Standard deviation
mean
Average
numpy.doc.ufuncs
Section "Output arguments"

## Notes

The variance is the average of the squared deviations from the mean, i.e., var $=$ mean (abs $(x-$ $x . m e a n()) * * 2$ ).

The mean is normally calculated as x . sum () / N , where $\mathrm{N}=$ len ( x$)$. If, however, ddof is specified, the divisor N - ddof is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of a hypothetical infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables.

Note that for complex numbers, the absolute value is taken before squaring, so that the result is always real and nonnegative.

For floating-point input, the variance is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float 32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1,2],[3,4]])
>>> np.var(a)
1.25
>>> np.var(a,0)
array([ 1., 1.])
>>> np.var(a,1)
array([ 0.25, 0.25])
```

In single precision, var() can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
```

```
>>> np.var(a)
0.20405951142311096
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.var(a, dtype=np.float64)
0.202499999932997387
>>> ((1-0.55)**2 + (0.1-0.55)**2)/2
0.202500000000000001
MaskedArray.anom (axis=None,dtype=None)
```

Compute the anomalies (deviations from the arithmetic mean) along the given axis.
Returns an array of anomalies, with the same shape as the input and where the arithmetic mean is computed along the given axis.

## Parameters

axis : int, optional
Axis over which the anomalies are taken. The default is to use the mean of the flattened array as reference.
dtype : dtype, optional
Type to use in computing the variance. For arrays of integer type
the default is float 32 ; for arrays of float types it is the same as the array type.

## See Also:

mean
Compute the mean of the array.

## Examples

```
>>> a = np.ma.array([1,2,3])
>>> a.anom()
masked_array(data = [-1. 0. 1.],
                    mask = False,
                    fill_value = 1e+20)
```

MaskedArray. cumprod (axis=None, dtype=None, out=None)

Return the cumulative product of the elements along the given axis. The cumulative product is taken over the flattened array by default, otherwise over the specified axis.
Masked values are set to 1 internally during the computation. However, their position is saved, and the result will be masked at the same locations.

## Parameters

axis : \{None, -1 , int \}, optional
Axis along which the product is computed. The default (axis $=$ None) is to compute over the flattened array.
dtype: \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are multiplied. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : ndarray, optional

Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

cumprod : ndarray
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## Notes

The mask is lost if out is not a valid MaskedArray!
Arithmetic is modular when using integer types, and no error is raised on overflow.
MaskedArray. cumsum (axis=None, dtype=None, out=None)
Return the cumulative sum of the elements along the given axis. The cumulative sum is calculated over the
flattened array by default, otherwise over the specified axis.
Masked values are set to 0 internally during the computation. However, their position is saved, and the result will be masked at the same locations.

## Parameters

axis: $\{$ None, -1 , int $\}$, optional
Axis along which the sum is computed. The default (axis $=$ None) is to compute over the flattened array. axis may be negative, in which case it counts from the last to the first axis.
dtype : \{None, dtype\}, optional
Type of the returned array and of the accumulator in which the elements are summed. If dtype is not specified, it defaults to the dtype of $a$, unless $a$ has an integer dtype with a precision less than that of the default platform integer. In that case, the default platform integer is used.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

cumsum : ndarray.
A new array holding the result is returned unless out is specified, in which case a reference to out is returned.

## Notes

The mask is lost if out is not a valid MaskedArray!
Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> marr = np.ma.array(np.arange(10), mask=[0,0,0,1,1,1,0,0,0,0])
>>> print marr.cumsum()
[0 1 3 -- -- -- 9 16 24 33]
```

MaskedArray.mean (axis=None, dtype=None, out=None)
Returns the average of the array elements.
Masked entries are ignored. The average is taken over the flattened array by default, otherwise over the specified axis. Refer to numpy.mean for the full documentation.

## Parameters

a : array_like
Array containing numbers whose mean is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the means are computed. The default is to compute the mean of the flattened array.
dtype : dtype, optional
Type to use in computing the mean. For integer inputs, the default is float64; for floating point, inputs it is the same as the input dtype.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type will be cast if necessary.

## Returns

mean : ndarray, see dtype parameter above
If out=None, returns a new array containing the mean values, otherwise a reference to the output array is returned.

## See Also:

```
numpy.ma.mean
```

Equivalent function.

```
numpy.mean
```

Equivalent function on non-masked arrays.

```
numpy.ma.average
```

Weighted average.

## Examples

```
>>> a = np.ma.array([1,2,3], mask=[False, False, True])
>>> a
masked_array(data = [1 2 --],
                    mask = [False False True],
        fill_value = 999999)
>>> a.mean()
1.5
MaskedArray.prod (axis=None,dtype=None,out=None)
```

Return the product of the array elements over the given axis. Masked elements are set to 1 internally for computation.

## Parameters

axis : \{None, int \}, optional
Axis over which the product is taken. If None is used, then the product is over all the array elements.
dtype : \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are multiplied. If dtype has the value None and the type of a is an integer type of precision
less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : \{None, array \}, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type will be cast if necessary.

## Returns

product_along_axis : \{array, scalar\}, see dtype parameter above.
Returns an array whose shape is the same as a with the specified axis removed. Returns a 0 d array when a is 1 d or axis=None. Returns a reference to the specified output array if specified.

## See Also:

prod
equivalent function

## Notes

Arithmetic is modular when using integer types, and no error is raised on overflow.

## Examples

```
>>> np.prod([1.,2.])
2.0
>>> np.prod([1.,2.], dtype=np.int32)
2
>>> np.prod([[1.,2.],[3.,4.]])
24.0
>>> np.prod([[1.,2.],[3.,4.]], axis=1)
array([ 2., 12.])
```

MaskedArray.std (axis=None, dtype=None, out=None, $d d o f=0$ )
Compute the standard deviation along the specified axis.
Returns the standard deviation, a measure of the spread of a distribution, of the array elements. The standard deviation is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Calculate the standard deviation of these values.
axis : int, optional
Axis along which the standard deviation is computed. The default is to compute the standard deviation of the flattened array.
dtype : dtype, optional
Type to use in computing the standard deviation. For arrays of integer type the default is float64, for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternative output array in which to place the result. It must have the same shape as the expected output but the type (of the calculated values) will be cast if necessary.
ddof : int, optional

Means Delta Degrees of Freedom. The divisor used in calculations is N - ddof, where N represents the number of elements. By default ddof is zero.

## Returns

standard_deviation : ndarray, see dtype parameter above.
If out is None, return a new array containing the standard deviation, otherwise return a reference to the output array.

## See Also:

var, mean
numpy.doc.ufuncs
Section "Output arguments"

## Notes

The standard deviation is the square root of the average of the squared deviations from the mean, i.e., std $=$ sqrt (mean (abs (x - x.mean()) **2)).

The average squared deviation is normally calculated as $\mathrm{x} . \operatorname{sum}() / \mathrm{N}$, where $\mathrm{N}=$ len(x). If, however, $d d o f$ is specified, the divisor $N-d d o f$ is used instead. In standard statistical practice, ddof=1 provides an unbiased estimator of the variance of the infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables. The standard deviation computed in this function is the square root of the estimated variance, so even with $d d o f=1$, it will not be an unbiased estimate of the standard deviation per se.
Note that, for complex numbers, std takes the absolute value before squaring, so that the result is always real and nonnegative.
For floating-point input, the std is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higheraccuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.std(a)
1.1180339887498949
>>> np.std(a, axis=0)
array([ 1., 1.])
>>> np.std(a, axis=1)
array([ 0.5, 0.5])
```

In single precision, $\operatorname{std}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.std(a)
0.45172946707416706
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.std(a, dtype=np.float64)
0.449999999925552653
```

MaskedArray. sum (axis=None, dtype=None, out=None)
Return the sum of the array elements over the given axis. Masked elements are set to 0 internally.

## Parameters

axis : $\{$ None, -1 , int $\}$, optional
Axis along which the sum is computed. The default (axis $=$ None) is to compute over the flattened array.
dtype : \{None, dtype\}, optional
Determines the type of the returned array and of the accumulator where the elements are summed. If dtype has the value None and the type of a is an integer type of precision less than the default platform integer, then the default platform integer precision is used. Otherwise, the dtype is the same as that of a.
out : \{None, ndarray\}, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.

## Returns

sum_along_axis : MaskedArray or scalar
An array with the same shape as self, with the specified axis removed. If self is a $0-\mathrm{d}$ array, or if axis is None, a scalar is returned. If an output array is specified, a reference to out is returned.

## Examples

```
>>> x = np.ma.array([[1,2,3],[4,5,6],[7,8,9]], mask=[0] + [1,0]*4)
>>> print x
[[1 -- 3]
    [-- 5 -- ]
    [7 -- 9]]
    >>> print x.sum()
    25
    >>> print x.sum(axis=1)
    [4 5 16]
    >>> print x.sum(axis=0)
    [8 5 12]
    >>> print type(x.sum(axis=0, dtype=np.int64)[0])
    <type 'numpy.int64'>
```

MaskedArray.var (axis=None, dtype=None, out=None, $d d o f=0$ )

Compute the variance along the specified axis.
Returns the variance of the array elements, a measure of the spread of a distribution. The variance is computed for the flattened array by default, otherwise over the specified axis.

## Parameters

a : array_like
Array containing numbers whose variance is desired. If $a$ is not an array, a conversion is attempted.
axis : int, optional
Axis along which the variance is computed. The default is to compute the variance of the flattened array.
dtype : data-type, optional
Type to use in computing the variance. For arrays of integer type the default is float32; for arrays of float types it is the same as the array type.
out : ndarray, optional
Alternate output array in which to place the result. It must have the same shape as the expected output, but the type is cast if necessary.
ddof : int, optional
"Delta Degrees of Freedom": the divisor used in the calculation is N - ddof, where N represents the number of elements. By default ddof is zero.

## Returns

variance : ndarray, see dtype parameter above
If out=None, returns a new array containing the variance; otherwise, a reference to the output array is returned.

## See Also:

std
Standard deviation
mean
Average
numpy.doc.ufuncs
Section "Output arguments"

## Notes

The variance is the average of the squared deviations from the mean, i.e., var $=$ mean (abs $(x-$ x.mean ()) **2).

The mean is normally calculated as $\mathrm{x} \cdot \operatorname{sum}() / \mathrm{N}$, where $\mathrm{N}=\operatorname{len}(\mathrm{x})$. If, however, $d d o f$ is specified, the divisor $N$ - ddof is used instead. In standard statistical practice, ddof $=1$ provides an unbiased estimator of the variance of a hypothetical infinite population. $d d o f=0$ provides a maximum likelihood estimate of the variance for normally distributed variables.

Note that for complex numbers, the absolute value is taken before squaring, so that the result is always real and nonnegative.

For floating-point input, the variance is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-accuracy accumulator using the dtype keyword can alleviate this issue.

## Examples

```
>>> a = np.array([[1,2],[3,4]])
>>> np.var(a)
1.25
>>> np.var(a,0)
array([ 1., 1.])
>>> np.var(a,1)
array([ 0.25, 0.25])
```

In single precision, $\operatorname{var}()$ can be inaccurate:

```
>>> a = np.zeros((2,512*512), dtype=np.float 32)
>>> a[0,:] = 1.0
>>> a[1,:] = 0.1
>>> np.var(a)
0.20405951142311096
```

Computing the standard deviation in float64 is more accurate:

```
>>> np.var(a, dtype=np.float64)
0.202499999932997387
>>> ((1-0.55)**2 + (0.1-0.55)**2)/2
0.202500000000000001
```


## Minimum/maximum

| ma.argmax(a[, axis, fill_value]) | Function version of the eponymous method. |
| :---: | :---: |
| ma.argmin(a[, axis, fill_value]) | Returns array of indices of the maximum values along the given axis. |
| $\operatorname{ma} \cdot \max (\mathrm{obj}[$, axis, out, fill_value]) | Return the maximum along a given axis. |
| ma.min(obj[, axis, out, fill_value]) | Return the minimum along a given axis. |
| ma.ptp(obj[, axis, out, fill_value]) | Return (maximum - minimum) along the the given dimension (i.e. |
| ma.MaskedArray.argmax([axis, fill_value, out]) | Returns array of indices of the maximum values along the given axis. |
| ma.MaskedArray.argmin([axis, fill_value, out]) | Return array of indices to the minimum values along the given axis. |
| ```ma.MaskedArray.max([axis, out, fil_value])``` | Return the maximum along a given axis. |
| ma.MaskedArray.min([axis, out, fill_value]) | Return the minimum along a given axis. |
| ma.MaskedArray.ptp([axis, out, fill_value]) | Return (maximum - minimum) along the the given dimension (i.e. |

```
numpy.ma.argmax (a,axis=None, fill_value=None)
```

Function version of the eponymous method.

```
numpy.ma.argmin (a,axis=None, fill_value=None)
```

Returns array of indices of the maximum values along the given axis. Masked values are treated as if they had the value fill_value.

## Parameters

axis : \{None, integer \}
If None, the index is into the flattened array, otherwise along the specified axis
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, the output of maximum_fill_value(self._data) is used instead.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

index_array : \{integer_array \}

## Examples

```
>>> a = np.arange(6).reshape (2,3)
>>> a.argmax()
5
>>> a.argmax(0)
array([1, 1, 1])
```

```
>>> a.argmax(1)
array([2, 2])
```

numpy.ma.max (obj, axis=None, out=None, fill_value=None)
Return the maximum along a given axis.

## Parameters

axis : \{None, int \}, optional
Axis along which to operate. By default, axis is None and the flattened input is used. out : array_like, optional

Alternative output array in which to place the result. Must be of the same shape and buffer length as the expected output.
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, use the output of maximum_fill_value().

## Returns

 amax : array_likeNew array holding the result. If out was specified, out is returned.

## See Also:

maximum_fill_value
Returns the maximum filling value for a given datatype.
numpy.ma.min (obj, axis=None, out=None, fill_value=None)
Return the minimum along a given axis.

## Parameters

axis: \{None, int \}, optional
Axis along which to operate. By default, axis is None and the flattened input is used. out : array_like, optional

Alternative output array in which to place the result. Must be of the same shape and buffer length as the expected output.
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, use the output of minimum_fill_value.

## Returns

 amin : array_likeNew array holding the result. If out was specified, out is returned.
See Also:
minimum_fill_value
Returns the minimum filling value for a given datatype.
numpy.ma.ptp (obj, axis=None, out=None, fill_value=None)
Return (maximum - minimum) along the the given dimension (i.e. peak-to-peak value).

## Parameters

axis: \{None, int \}, optional

Axis along which to find the peaks. If None (default) the flattened array is used.
out : \{None, array_like \}, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.
fill_value : \{var\}, optional
Value used to fill in the masked values.
Returns
ptp : ndarray.
A new array holding the result, unless out was specified, in which case a reference to out is returned.

MaskedArray.argmax (axis=None, fill_value=None, out=None)
Returns array of indices of the maximum values along the given axis. Masked values are treated as if they had the value fill_value.

## Parameters

axis: \{None, integer \}
If None, the index is into the flattened array, otherwise along the specified axis
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, the output of maximum_fill_value(self._data) is used instead.
out : \{None, array \}, optional
Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

index_array : \{integer_array \}

## Examples

```
>>> a = np.arange(6).reshape(2,3)
>>> a.argmax()
5
>>> a.argmax(0)
array([1, 1, 1])
>>> a.argmax(1)
array([2, 2])
```

MaskedArray.argmin (axis=None, fill_value=None, out=None)
Return array of indices to the minimum values along the given axis.

## Parameters

axis: \{None, integer $\}$
If None, the index is into the flattened array, otherwise along the specified axis
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, the output of minimum_fill_value(self._data) is used instead.
out : \{None, array \}, optional

Array into which the result can be placed. Its type is preserved and it must be of the right shape to hold the output.

## Returns

\{ndarray, scalar\} :
If multi-dimension input, returns a new ndarray of indices to the minimum values along the given axis. Otherwise, returns a scalar of index to the minimum values along the given axis.

## Examples

```
>>> x = np.ma.array(arange(4), mask=[1,1,0,0])
>>> x.shape = (2,2)
>>> print x
[[-- --]
    [2 3]]
>>> print x.argmin(axis=0, fill_value=-1)
[0 0]
>>> print x.argmin(axis=0, fill_value=9)
[1 1]
MaskedArray.max (axis=None,out=None,fill_value=None)
```

Return the maximum along a given axis.

## Parameters

axis: \{None, int \}, optional
Axis along which to operate. By default, axis is None and the flattened input is used.
out : array_like, optional
Alternative output array in which to place the result. Must be of the same shape and buffer length as the expected output.
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, use the output of maximum_fill_value().

## Returns

amax : array_like
New array holding the result. If out was specified, out is returned.
See Also:
maximum_fill_value
Returns the maximum filling value for a given datatype.
MaskedArray.min (axis=None, out=None, fill_value=None)
Return the minimum along a given axis.

## Parameters

axis : \{None, int \}, optional
Axis along which to operate. By default, axis is None and the flattened input is used.
out : array_like, optional
Alternative output array in which to place the result. Must be of the same shape and buffer length as the expected output.
fill_value : \{var\}, optional
Value used to fill in the masked values. If None, use the output of minimum_fill_value.

## Returns

 amin : array_likeNew array holding the result. If out was specified, out is returned.

## See Also:

minimum_fill_value
Returns the minimum filling value for a given datatype.

MaskedArray.ptp (axis=None, out=None, fill_value=None)
Return (maximum - minimum) along the the given dimension (i.e. peak-to-peak value).

## Parameters

axis: \{None, int \}, optional
Axis along which to find the peaks. If None (default) the flattened array is used.
out : \{None, array_like\}, optional
Alternative output array in which to place the result. It must have the same shape and buffer length as the expected output but the type will be cast if necessary.
fill_value : \{var\}, optional
Value used to fill in the masked values.

## Returns

ptp : ndarray.
A new array holding the result, unless out was specified, in which case a reference to out is returned.

## Sorting

ma.argsort(a[, axis, kind, order, fill_value])
ma.sort(a[, axis, kind, order, endwith, ...])
ma.MaskedArray.argsort([axis, kind, order, ...])
ma.MaskedArray.sort([axis, kind, order, ...])

Return an ndarray of indices that sort the array along the specified axis.
Sort the array, in-place
Return an ndarray of indices that sort the array along the specified axis.
Sort the array, in-place
numpy.ma. argsort (a, axis=None, kind='quicksort', order=None, fill_value=None)
Return an ndarray of indices that sort the array along the specified axis. Masked values are filled beforehand to fill_value.

## Parameters

axis : int, optional
Axis along which to sort. The default is -1 (last axis). If None, the flattened array is used.
fill_value : var, optional
Value used to fill the array before sorting. The default is the fill_value attribute of the input array.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## Returns

index_array : ndarray, int
Array of indices that sort $a$ along the specified axis. In other words, a[index_array] yields a sorted $a$.

## See Also:

sort
Describes sorting algorithms used.

## lexsort

Indirect stable sort with multiple keys.
ndarray.sort
Inplace sort.

## Notes

See sort for notes on the different sorting algorithms.

## Examples

```
>>> a = np.ma.array([3,2,1], mask=[False, False, True])
>>> a
masked_array(data = [3 2 -- ]}]
                    mask = [False False True],
    fill_value = 999999)
>>> a.argsort()
array([1, 0, 2])
```

numpy.ma.sort ( $a$, axis=-1, kind='quicksort', order=None, endwith=True, fill_value=None)
Sort the array, in-place

## Parameters

a : array_like
Array to be sorted.
axis : int, optional
Axis along which to sort. If None, the array is flattened before sorting. The default is -1 , which sorts along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is a structured array, this argument specifies which fields to compare first, second, and so on. This list does not need to include all of the fields.
endwith : \{True, False \}, optional

Whether missing values (if any) should be forced in the upper indices (at the end of the array) (True) or lower indices (at the beginning).
fill_value : \{var\}, optional
Value used internally for the masked values. If fill_value is not None, it supersedes endwith.

## Returns

sorted_array : ndarray
Array of the same type and shape as $a$.

## See Also:

ndarray.sort
Method to sort an array in-place.
argsort
Indirect sort.

## lexsort

Indirect stable sort on multiple keys.
searchsorted
Find elements in a sorted array.

## Notes

See sort for notes on the different sorting algorithms.

## Examples

```
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # Default
>>> a.sort()
>>> print a
[1 3 5 -- --]
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # Put missing values in the front
>>> a.sort(endwith=False)
>>> print a
[-- -- 1 3 5]
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # fill_value takes over endwith
>>> a.sort(endwith=False, fill_value=3)
>>> print a
    [1 -- -- 3 5]
```

MaskedArray. argsort ( axis=None, kind='quicksort', order=None, fill_value=None)

Return an ndarray of indices that sort the array along the specified axis. Masked values are filled beforehand to fill_value.

## Parameters

axis : int, optional
Axis along which to sort. The default is -1 (last axis). If None, the flattened array is used.
fill_value : var, optional

Value used to fill the array before sorting. The default is the fill_value attribute of the input array.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm.
order : list, optional
When $a$ is an array with fields defined, this argument specifies which fields to compare first, second, etc. Not all fields need be specified.

## Returns

index_array : ndarray, int
Array of indices that sort $a$ along the specified axis. In other words, a[index_array] yields a sorted $a$.

## See Also:

## sort

Describes sorting algorithms used.

## lexsort

Indirect stable sort with multiple keys.
ndarray.sort
Inplace sort.

## Notes

See sort for notes on the different sorting algorithms.

## Examples

```
>>> a = np.ma.array([3,2,1], mask=[False, False, True])
>>> a
masked_array(data = [3 2 -- ]}]\mathrm{ ,
    mask = [False False True],
    fill_value = 999999)
>>> a.argsort()
array([1, 0, 2])
```

MaskedArray.sort (axis=-1, kind='quicksort', order=None, endwith=True, fill_value=None)

Sort the array, in-place

## Parameters

a: array_like
Array to be sorted.
axis : int, optional
Axis along which to sort. If None, the array is flattened before sorting. The default is -1 , which sorts along the last axis.
kind : \{ 'quicksort', 'mergesort', 'heapsort' \}, optional
Sorting algorithm. Default is 'quicksort'.
order : list, optional
When $a$ is a structured array, this argument specifies which fields to compare first, second, and so on. This list does not need to include all of the fields.
endwith : \{True, False\}, optional
Whether missing values (if any) should be forced in the upper indices (at the end of the array) (True) or lower indices (at the beginning).
fill_value : \{var\}, optional
Value used internally for the masked values. If fill_value is not None, it supersedes endwith.

## Returns

sorted_array : ndarray
Array of the same type and shape as $a$.

## See Also:

## ndarray.sort

Method to sort an array in-place.

```
argsort
```

Indirect sort.

## lexsort

Indirect stable sort on multiple keys.

```
searchsorted
```

Find elements in a sorted array.

## Notes

See sort for notes on the different sorting algorithms.

## Examples

```
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # Default
>>> a.sort()
>>> print a
[1 [3 5 -- --]
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # Put missing values in the front
>>> a.sort(endwith=False)
>>> print a
[-- -- 1 3 5]
>>> a = ma.array([1, 2, 5, 4, 3],mask=[0, 1, 0, 1, 0])
>>> # fill_value takes over endwith
>>> a.sort(endwith=False, fill_value=3)
>>> print a
[1 -- -- 3 5]
```


## Algebra

| ma.diag(v[, k]) | Extract a diagonal or construct a diagonal array. |
| :--- | :--- |
| ma.dot $(\mathrm{a}, \mathrm{b}[$, strict $])$ | Return the dot product of two arrays. |
| ma.identity $(\mathrm{n}[$, dtype $])$ | Return the identity array. |
| ma.inner $(\mathrm{a}, \mathrm{b})$ | Inner product of two arrays. |
| ma.innerproduct $(\mathrm{a}, \mathrm{b})$ | Inner product of two arrays. |
| ma.outer $(\mathrm{a}, \mathrm{b})$ | Compute the outer product of two vectors. |
| ma.outerproduct $(\mathrm{a}, \mathrm{b})$ | Compute the outer product of two vectors. |
| ma.trace(self[, offset, axis1, axis $2, \ldots])$ | Return the sum along diagonals of the array. |
| ma.transpose(a[, axes]) | Permute the dimensions of an array. |
| ma.MaskedArray.trace([offset, axis1, axis2, $\ldots])$ | Return the sum along diagonals of the array. |
| ma.MaskedArray.transpose(*axes) | Returns a view of the array with axes transposed. |

numpy.ma.diag ( $v, k=0$ )
Extract a diagonal or construct a diagonal array.
This function is the equivalent of numpy. diag that takes masked values into account, see numpy.diag for details.

## See Also:

numpy.diag
Equivalent function for ndarrays.
numpy.ma.dot ( $a, b$, strict=False)
Return the dot product of two arrays.
Note: Works only with 2-D arrays at the moment.
This function is the equivalent of numpy. dot that takes masked values into account, see numpy. dot for details.

Parameters
$\mathbf{a}, \mathbf{b}$ : ndarray
Inputs arrays.
strict : bool, optional
Whether masked data are propagated (True) or set to 0 (False) for the computation. Default is False. Propagating the mask means that if a masked value appears in a row or column, the whole row or column is considered masked.

## See Also:

numpy.dot
Equivalent function for ndarrays.

## Examples

```
>>> a = ma.array([[1, 2, 3], [4, 5, 6]], mask=[[1, 0, 0], [0, 0, 0]])
>>> b = ma.array([[1, 2], [3, 4], [5, 6]], mask=[[1, 0], [0, 0], [0, 0]])
>>> np.ma.dot(a, b)
masked_array(data =
    [[21 26]
    [45 64]],
                                    mask =
    [[False False]
    [False False]],
```

```
            fill_value = 999999)
>>> np.ma.dot(a, b, strict=True)
masked_array(data =
    [[-- --]
    [-- 64]],
            mask =
    [[ True True]
    [ True False]],
            fill_value = 999999)
```

numpy.ma.identity ( $n$, dtype=None)

Return the identity array.
The identity array is a square array with ones on the main diagonal.

## Parameters

n : int
Number of rows (and columns) in $n \times n$ output.
dtype : data-type, optional
Data-type of the output. Defaults to float.

## Returns

out : ndarray
$n \times n$ array with its main diagonal set to one, and all other elements 0.

## Examples

```
>>> np.identity(3)
array([[ 1., 0., 0.],
    [ 0., 1., 0.],
    [ 0., 0., 1.]])
```

numpy.ma.inner ( $a, b$ )

Inner product of two arrays.
Ordinary inner product of vectors for 1-D arrays (without complex conjugation), in higher dimensions a sum product over the last axes.

## Parameters

$\mathbf{a}, \mathbf{b}$ : array_like
If $a$ and $b$ are nonscalar, their last dimensions of must match.

## Returns

out : ndarray
out.shape $=$ a.shape $[:-1]+$ b.shape $[:-1]$

## Raises

ValueError :
If the last dimension of $a$ and $b$ has different size.
See Also:

## tensordot

Sum products over arbitrary axes.
dot
Generalised matrix product, using second last dimension of $b$.
einsum
Einstein summation convention.

## Notes

Masked values are replaced by 0 .

## Examples

Ordinary inner product for vectors:

```
>>> a = np.array([1,2,3])
>>> b = np.array([0,1,0])
>>> np.inner(a, b)
2
```

A multidimensional example:

```
>>> a = np.arange(24).reshape((2, 3,4))
>>> b = np.arange(4)
>>> np.inner(a, b)
array([[ 14, 38, 62],
    [ 86, 110, 134]])
```

An example where $b$ is a scalar:
>>> np.inner(np.eye (2), 7)
array([[ 7., 0.],
[ 0., 7.]])
numpy.ma.innerproduct ( $a, b$ )

Inner product of two arrays.
Ordinary inner product of vectors for 1-D arrays (without complex conjugation), in higher dimensions a sum product over the last axes.

## Parameters

$\mathbf{a}, \mathbf{b}$ : array_like
If $a$ and $b$ are nonscalar, their last dimensions of must match.

## Returns

out : ndarray
out.shape $=$ a.shape $[:-1]+$ b.shape $[:-1]$

## Raises

## ValueError :

If the last dimension of $a$ and $b$ has different size.

## See Also:

tensordot
Sum products over arbitrary axes.
dot
Generalised matrix product, using second last dimension of $b$.

## einsum

Einstein summation convention.

## Notes

Masked values are replaced by 0 .

## Examples

Ordinary inner product for vectors:

```
>>> a = np.array([1,2,3])
>>> b = np.array([0,1,0])
>>> np.inner(a, b)
2
```

A multidimensional example:

```
>>> a = np.arange(24).reshape((2,3,4))
>>> b = np.arange (4)
>>> np.inner(a, b)
array([[ 14, 38, 62],
    [ 86, 110, 134]])
```

An example where $b$ is a scalar:

```
>>> np.inner(np.eye(2), 7)
array([[ 7., 0.],
    [ 0., 7.]])
```

numpy.ma.outer ( $a, b$ )
Compute the outer product of two vectors.
Given two vectors, $a=[a 0, a 1, \ldots, a M]$ and $b=[b 0, b 1, \ldots, b N]$, the outer product [R47] is:

```
[[a0*b0 a0*bb1 ... a0*bN ]
    [a1*b0 .
    [ ..
    [aM*b0 aM*bN ]]
```


## Parameters

$\mathbf{a}, \mathbf{b}$ : array_like, shape (M,), (N,)
First and second input vectors. Inputs are flattened if they are not already 1-dimensional.

## Returns

out : ndarray, shape ( $\mathrm{M}, \mathrm{N}$ )

```
out[i, j] = a[i] * b[j]
```


## See Also:

inner, einsum
Notes
Masked values are replaced by 0 .
References
[R47]

## Examples

Make a (very coarse) grid for computing a Mandelbrot set:

```
>>> rl = np.outer(np.ones((5,)), np.linspace(-2, 2, 5))
>>> rl
array([[-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.]])
>>> im = np.outer(1j*np.linspace(2, -2, 5), np.ones((5,)))
>>> im
array([[ 0.+2.j, 0.+2.j, 0.+2.j, 0.+2.j, 0.+2.j],
    [ 0.+1.j, 0.+1.j, 0.+1.j, 0.+1.j, 0.+1.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
    [ 0.-1.j, 0.-1.j, 0.-1.j, 0.-1.j, 0.-1.j],
    [ 0.-2.j, 0.-2.j, 0.-2.j, 0.-2.j, 0.-2.j]])
>>> grid = rl + im
>>> grid
array([[-2.+2.j, -1.+2.j, 0.+2.j, 1.+2.j, 2.+2.j],
    [-2.+1.j, -1.+1.j, 0.+1.j, 1.+1.j, 2.+1.j],
    [-2.+0.j, -1.+0.j, 0.+0.j, 1.+0.j, 2.+0.j],
    [-2.-1.j, -1.-1.j, 0.-1.j, 1.-1.j, 2.-1.j],
    [-2.-2.j, -1.-2.j, 0.-2.j, 1.-2.j, 2.-2.j]])
```

An example using a "vector" of letters:

```
>>> x = np.array(['a', 'b', 'c'], dtype=object)
>>> np.outer(x, [1, 2, 3])
array([[a, aa, aaa],
    [b, bb, b.b.b],
    [c, cc, ccc]], dtype=object)
```

numpy.ma.outerproduct ( $a, b$ )
Compute the outer product of two vectors.
Given two vectors, $a=[a 0, \mathrm{a} 1, \ldots, \mathrm{aM}]$ and $b=[\mathrm{b} 0, \mathrm{~b} 1, \ldots, \mathrm{bN}]$, the outer product [R48] is:

```
[[la0*b0 a0*b1 ... a0*bN ]
    [a1*b0 .
    [ ..
    [aM*b0 aM*bN ]]
```


## Parameters

$\mathbf{a}, \mathbf{b}$ : array_like, shape (M,), (N,)
First and second input vectors. Inputs are flattened if they are not already 1-dimensional.

## Returns

out : ndarray, shape $(\mathrm{M}, \mathrm{N})$

$$
\text { out }[i, j]=a[i] * b[j]
$$

## See Also:

inner, einsum

## Notes

Masked values are replaced by 0 .

## References

[R48]

## Examples

Make a (very coarse) grid for computing a Mandelbrot set:

```
>>> rl = np.outer(np.ones((5,)), np.linspace(-2, 2, 5))
>>> rl
array([[-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.],
    [-2., -1., 0., 1., 2.]])
>>> im = np.outer(1j*np.linspace(2, -2, 5), np.ones((5,)))
>>> im
array([[ 0.+2.j, 0.+2.j, 0.+2.j, 0.+2.j, 0.+2.j],
    [ 0.+1.j, 0.+1.j, 0.+1.j, 0.+1.j, 0.+1.j],
    [ 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
    [ 0.-1.j, 0.-1.j, 0.-1.j, 0.-1.j, 0.-1.j],
    [ 0.-2.j, 0.-2.j, 0.-2.j, 0.-2.j, 0.-2.j]])
>>> grid = rl + im
>>> grid
array([[-2.+2.j, -1.+2.j, 0.+2.j, 1.+2.j, 2.+2.j],
    [-2.+1.j, -1.+1.j, 0.+1.j, 1.+1.j, 2.+1.j],
    [-2.+0.j, -1.+0.j, 0.+0.j, 1.+0.j, 2.+0.j],
    [-2.-1.j, -1.-1.j, 0.-1.j, 1.-1.j, 2.-1.j],
    [-2.-2.j, -1.-2.j, 0.-2.j, 1.-2.j, 2.-2.j]])
```

An example using a "vector" of letters:

```
>>> x = np.array(['a', 'b', 'c'], dtype=object)
>>> np.outer(x, [1, 2, 3])
array([[a, aa, aaa],
    [b, bb, b.b.b],
    [c, cc, ccc]], dtype=object)
```

numpy.ma.trace (self, offset=0, axis1=0, axis $2=1$, dtype $=$ None, out=None) a.trace(offset=0, axis1=0, axis $2=1$, dtype $=$ None, out $=$ None )

Return the sum along diagonals of the array.
Refer to numpy.trace for full documentation.

## See Also:

numpy.trace equivalent function
numpy.ma.transpose ( $a$, axes=None)
Permute the dimensions of an array.
This function is exactly equivalent to numpy.transpose.
See Also:
numpy.transpose
Equivalent function in top-level NumPy module.

## Examples

```
>>> import numpy.ma as ma
>>> x = ma.arange(4).reshape((2,2))
>>> x[1, 1] = ma.masked
>>>> x
masked_array(data =
    [[[0 1]
    [2 --]],
    [[False False]
    [False True]],
            fill_value = 999999)
>>> ma.transpose(x)
masked_array(data =
    [[[0 2]
    [1 --]],
            mask =
    [[False False]
    [False True]],
            fill_value = 999999)
```

MaskedArray.trace (offset $=0$, axis $1=0$, axis $2=1$, dtype $=$ None, out $=$ None $)$

Return the sum along diagonals of the array.
Refer to numpy. trace for full documentation.

## See Also:

numpy.trace equivalent function

MaskedArray.transpose (*axes)
Returns a view of the array with axes transposed.
For a 1-D array, this has no effect. (To change between column and row vectors, first cast the 1-D array into a matrix object.) For a 2-D array, this is the usual matrix transpose. For an n-D array, if axes are given, their order indicates how the axes are permuted (see Examples). If axes are not provided and a. shape $=(i[0], i[1]$, $\ldots i[n-2], i[n-1])$, then a.transpose().shape $=(i[n-1], i[n-2], \ldots i[1]$, i [0]).

## Parameters

axes : None, tuple of ints, or $n$ ints

- None or no argument: reverses the order of the axes.
- tuple of ints: $i$ in the $j$-th place in the tuple means $a$ 's $i$-th axis becomes a.transpose()'s $j$-th axis.
- $n$ ints: same as an n-tuple of the same ints (this form is intended simply as a "convenience" alternative to the tuple form)


## Returns

out : ndarray
View of $a$, with axes suitably permuted.

## See Also:

## ndarray.T

Array property returning the array transposed.

## Examples

```
>>> a = np.array([[1, 2], [3, 4]])
>>> a
array([[1, 2],
    [3, 4]])
>>> a.transpose()
array([[1, 3],
    [2, 4]])
>>> a.transpose((1, 0))
array([[1, 3],
    [2, 4]])
>>> a.transpose(1, 0)
array([[1, 3],
    [2, 4]])
```


## Polynomial fit

| ma.vander(x[, n]) | Generate a Van der Monde matrix. |
| :--- | :--- |
| ma.polyfit(x, y, deg[, rcond, full]) | Least squares polynomial fit. |

numpy.ma. vander ( $x, n=$ None)
Generate a Van der Monde matrix.
The columns of the output matrix are decreasing powers of the input vector. Specifically, the $i$-th output column is the input vector raised element-wise to the power of $\mathrm{N}-\mathrm{i}-1$. Such a matrix with a geometric progression in each row is named for Alexandre-Theophile Vandermonde.

## Parameters

$\mathbf{x}$ : array_like
1-D input array.
$\mathbf{N}$ : int, optional
Order of (number of columns in) the output. If $N$ is not specified, a square array is returned ( $\mathrm{N}=$ len (x) ).

## Returns

out : ndarray
Van der Monde matrix of order $N$. The first column is $\mathrm{x}^{\wedge}(\mathrm{N}-1)$, the second $\mathrm{x}^{\wedge}(\mathrm{N}-2)$ and so forth.

## Notes

Masked values in the input array result in rows of zeros.

## Examples

```
>>> x = np.array([1, 2, 3, 5])
>>> N = 3
>>> np.vander(x, N)
array([[ 1, 1, 1],
    [ 4, 2, 1],
    [ 9, 3, 1],
    [25, 5, 1]])
```

```
>>> np.column_stack([x**(N-1-i) for i in range(N)])
array([[ 1, 1, 1],
    [ 4, 2, 1],
    [ 9, 3, 1],
    [25, 5, 1]])
>>> x = np.array([1, 2, 3, 5])
>>> np.vander(x)
array([[ 1, 1, 1, 1],
    [ 8, 4, 2, 1],
    [ 27, 9, 3, 1],
    [125, 25, 5, 1]])
```

The determinant of a square Vandermonde matrix is the product of the differences between the values of the input vector:

```
>>> np.linalg.det(np.vander(x))
48.000000000000043
>>>}(5-3)*(5-2)*(5-1)*(3-2)*(3-1)*(2-1
48
numpy.ma.polyfit (x, y, deg,rcond=None, full=False)
```

Least squares polynomial fit.
Fit a polynomial $\mathrm{p}(\mathrm{x})=\mathrm{p}[0] * \mathrm{x} * * \operatorname{deg}+\ldots+\mathrm{p}[\mathrm{deg}]$ of degree $d e g$ to points $(x, y)$. Returns a vector of coefficients $p$ that minimises the squared error.

## Parameters

$\mathbf{x}$ : array_like, shape (M,)
$x$-coordinates of the $M$ sample points (x[i], y[i]).
$\mathbf{y}$ : array_like, shape $(M$,$) or (M, K)$
$y$-coordinates of the sample points. Several data sets of sample points sharing the same x -coordinates can be fitted at once by passing in a 2D-array that contains one dataset per column.
deg : int
Degree of the fitting polynomial
rcond : float, optional
Relative condition number of the fit. Singular values smaller than this relative to the largest singular value will be ignored. The default value is len $(x) * e p s$, where eps is the relative precision of the float type, about $2 \mathrm{e}-16$ in most cases.
full : bool, optional
Switch determining nature of return value. When it is False (the default) just the coefficients are returned, when True diagnostic information from the singular value decomposition is also returned.

## Returns

$\mathbf{p}$ : ndarray, shape (M,) or (M, K)
Polynomial coefficients, highest power first. If $y$ was 2-D, the coefficients for $k$-th data set are in $\mathrm{p}[:, \mathrm{k}]$.
residuals, rank, singular_values, rcond : present only if full = True

Residuals of the least-squares fit, the effective rank of the scaled Vandermonde coefficient matrix, its singular values, and the specified value of rcond. For more details, see linalg.lstsq.

## Warns

## RankWarning :

The rank of the coefficient matrix in the least-squares fit is deficient. The warning is only raised if full = False.

The warnings can be turned off by

```
>>> import warnings
>>> warnings.simplefilter('ignore', np.RankWarning̣)
```


## See Also:

## polyval

Computes polynomial values.

## linalg.lstsq

Computes a least-squares fit.

```
scipy.interpolate.UnivariateSpline
```

Computes spline fits.

## Notes

Any masked values in x is propagated in y , and vice-versa.

## References

[R49], [R50]

## Examples

```
>>> x = np.array([0.0, 1.0, 2.0, 3.0, 4.0, 5.0])
>>> y = np.array([0.0, 0.8, 0.9, 0.1, -0.8, -1.0])
>>> z = np.polyfit(x, y, 3)
>>> Z
array([ 0.08703704, -0.81349206, 1.69312169, -0.03968254])
```

It is convenient to use polyld objects for dealing with polynomials:

```
>>> p = np.polyld(z)
>>> p(0.5)
0.6143849206349179
>>> p(3.5)
-0.34732142857143039
>>> p(10)
22.579365079365115
```

High-order polynomials may oscillate wildly:

```
>>> p30 = np.polyld(np.polyfit(x, y, 30))
/... RankWarning: Polyfit may be poorly conditioned...
>>> p30(4)
-0.800000000000000204
>>> p30(5)
-0.99999999999999445
```

```
>>> p30(4.5)
-0.10547061179440398
```

Illustration:

```
>>> import matplotlib.pyplot as plt
>>> xp = np.linspace(-2, 6, 100)
>>> plt.plot(x, y, '.', xp, p(xp), '-', xp, p30(xp), '--')
[<matplotlib.lines.Line2D object at 0x...>, <matplotlib.lines.Line2D object at 0x...>, <matpld
>>> plt.ylim(-2,2)
(-2, 2)
>>> plt.show()
```



## Clipping and rounding

```
ma.around
ma.clip(a, a_min, a_max[,out])
ma.round(a[, decimals, out])
ma.MaskedArray.clip(a_min, a_max[,
out])
ma.MaskedArray.round([decimals, out])
```

Round an array to the given number of decimals.
Clip (limit) the values in an array.
Return a copy of a, rounded to 'decimals' places.
Return an array whose values are limited to [a_min, a_max].
Return $a$ with each element rounded to the given number of decimals.
numpy.ma. around
Round an array to the given number of decimals.
Refer to around for full documentation.

## See Also:

around
equivalent function
numpy.ma.clip (a, a_min, a_max, out=None)
Clip (limit) the values in an array.

Given an interval, values outside the interval are clipped to the interval edges. For example, if an interval of $[0,1]$ is specified, values smaller than 0 become 0 , and values larger than 1 become 1 .

## Parameters

a : array_like
Array containing elements to clip.
a_min : scalar or array_like
Minimum value.
a_max : scalar or array_like
Maximum value. If $a \_m i n$ or $a \_m a x$ are array_like, then they will be broadcasted to the shape of $a$.
out : ndarray, optional
The results will be placed in this array. It may be the input array for in-place clipping. out must be of the right shape to hold the output. Its type is preserved.

## Returns

 clipped_array : ndarrayAn array with the elements of $a$, but where values $<a_{-} \min$ are replaced with $a_{-}$min, and those >a_max with $a_{-}$max.

## See Also:

numpy.doc.ufuncs
Section "Output arguments"

## Examples

```
>>> a = np.arange(10)
>>> np.clip(a, 1, 8)
array([1, 1, 2, 3, 4, 5, 6, 7, 8, 8])
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, 3, 6, out=a)
array([3, 3, 3, 3, 4, 5, 6, 6, 6, 6])
>>> a = np.arange(10)
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.clip(a, [3,4,1,1,1,4,4,4,4,4], 8)
array([3, 4, 2, 3, 4, 5, 6, 7, 8, 8])
```

numpy.ma.round ( $a$, decimals $=0$, out $=$ None)
Return a copy of a, rounded to 'decimals' places.
When 'decimals' is negative, it specifies the number of positions to the left of the decimal point. The real and imaginary parts of complex numbers are rounded separately. Nothing is done if the array is not of float type and 'decimals' is greater than or equal to 0 .

## Parameters

decimals : int
Number of decimals to round to. May be negative.
out : array_like
Existing array to use for output. If not given, returns a default copy of a.

## Notes

If out is given and does not have a mask attribute, the mask of a is lost!
MaskedArray.clip (a_min, a_max, out=None)
Return an array whose values are limited to [a_min, a_max].
Refer to numpy.clip for full documentation.

## See Also:

numpy.clip
equivalent function
MaskedArray.round (decimals=0, out=None)
Return $a$ with each element rounded to the given number of decimals.
Refer to numpy . around for full documentation.

## See Also:

numpy. around
equivalent function

## Miscellanea

```
ma.allequal(a, b[, fill_value])
ma.allclose(a, b[, masked_equal, rtol,
atol])
ma.apply_along_axis(func1d, axis,
arr, ...)
ma.arange([dtype])
ma.choose(indices, choices[, out, mode])
ma.ediff1d(arr[, to_end, to_begin])
ma.indices(dimensions[, dtype])
ma.where(condition[, x, y]) Return a masked array with elements from x or y, depending on
condition.
```

numpy.ma.allequal ( $a, b$, fill_value $=$ True $)$
Return True if all entries of $a$ and $b$ are equal, using fill_value as a truth value where either or both are masked.

## Parameters

$\mathbf{a , b}$ : array_like
Input arrays to compare.
fill_value : bool, optional
Whether masked values in a or $b$ are considered equal (True) or not (False).

## Returns

y: bool
Returns True if the two arrays are equal within the given tolerance, False otherwise. If either array contains NaN , then False is returned.

## See Also:

all, any, numpy.ma.allclose

## Examples

```
>>> a = ma.array([1e10, 1e-7, 42.0], mask=[0, 0, 1])
>>> a
masked_array(data = [10000000000.0 1e-07 --],
    mask = [False False True],
    fill_value=1e+20)
>>> b = array([1e10, 1e-7, -42.0])
>>> b
array([ 1.00000000e+10, 1.00000000e-07, -4.20000000e+01])
>>> ma.allequal(a, b, fill_value=False)
False
>>> ma.allequal(a, b)
True
```

numpy.ma.allclose ( $a, b$, masked_equal=True, rtol $=1.0000000000000001 e-05$, atol $=1 e-08$ )
Returns True if two arrays are element-wise equal within a tolerance.
This function is equivalent to allclose except that masked values are treated as equal (default) or unequal, depending on the masked_equal argument.

## Parameters

$\mathbf{a}, \mathbf{b}$ : array_like
Input arrays to compare.
masked_equal : bool, optional
Whether masked values in $a$ and $b$ are considered equal (True) or not (False). They are considered equal by default.
rtol : float, optional
Relative tolerance. The relative difference is equal to rtol $* \mathrm{~b}$. Default is $1 \mathrm{e}-5$.
atol : float, optional
Absolute tolerance. The absolute difference is equal to atol. Default is 1e-8.

## Returns

y: bool
Returns True if the two arrays are equal within the given tolerance, False otherwise. If either array contains NaN , then False is returned.

## See Also:

all, any
numpy.allclose
the non-masked allclose.

## Notes

If the following equation is element-wise True, then allclose returns True:

```
absolute(`a` - `b`) <= (`atol` + `rtol` * absolute(`b`))
```

Return True if all elements of $a$ and $b$ are equal subject to given tolerances.

## Examples

```
>>> a = ma.array([1e10, 1e-7, 42.0], mask=[0, 0, 1])
>>> a
masked_array(data = [10000000000.0 1e-07 --],
                    mask = [False False True],
    fill_value = 1e+20)
>>> b = ma.array([1e10, 1e-8, -42.0], mask=[0, 0, 1])
>>> ma.allclose(a, b)
False
>>> a = ma.array([1e10, 1e-8, 42.0], mask=[0, 0, 1])
>>> b = ma.array([1.00001e10, 1e-9, -42.0], mask=[0, 0, 1])
>>> ma.allclose(a, b)
True
>>> ma.allclose(a, b, masked_equal=False)
False
```

Masked values are not compared directly.

```
>>> a = ma.array([1e10, 1e-8, 42.0], mask=[0, 0, 1])
>>> b = ma.array([1.00001e10, 1e-9, 42.0], mask=[0, 0, 1])
>>> ma.allclose(a, b)
True
>>> ma.allclose(a, b, masked_equal=False)
False
```

numpy.ma.apply_along_axis (funcld, axis, arr, *args, **kwargs)

Apply a function to 1-D slices along the given axis.
Execute funcld(a, *args) where funcld operates on 1-D arrays and $a$ is a 1-D slice of arr along axis.

## Parameters

funcld : function
This function should accept 1-D arrays. It is applied to 1-D slices of arr along the specified axis.
axis : integer
Axis along which $a r r$ is sliced.
arr : ndarray
Input array.
args : any
Additional arguments to funcld.

## Returns

outarr : ndarray
The output array. The shape of outarr is identical to the shape of arr, except along the axis dimension, where the length of outarr is equal to the size of the return value of funcld. If funcld returns a scalar outarr will have one fewer dimensions than arr.

## See Also:

## apply_over_axes

Apply a function repeatedly over multiple axes.

## Examples

```
>>> def my_func(a):
... """Average first and last element of a I-D array"""
... return (a[0] + a[-1]) * 0.5
>>> b = np.array([[1,2,3], [4,5,6], [7,8,9]])
>>> np.apply_along_axis(my_func, 0, b)
array([ 4., 5., 6.])
>>> np.apply_along_axis(my_func, 1, b)
array([ 2., 5., 8.])
```

For a function that doesn't return a scalar, the number of dimensions in outarr is the same as arr.

```
>>> def new_func(a):
... """Divide elements of a by 2."""
... return a * 0.5
>>> b = np.array([[1,2,3], [4,5,6], [7,8,9]])
>>> np.apply_along_axis(new_func, 0, b)
array([[ 0.5, 1. , 1.5],
    [ 2. , 2.5, 3. ],
    [ 3.5, 4. , 4.5]])
```

numpy.ma. arange ([start], stop $[$, step $]$, dtype $=$ None)

Return evenly spaced values within a given interval.
Values are generated within the half-open interval [start, stop) (in other words, the interval including start but excluding stop). For integer arguments the function is equivalent to the Python built-in range function, but returns a ndarray rather than a list.

When using a non-integer step, such as 0.1 , the results will often not be consistent. It is better to use linspace for these cases.

## Parameters

start : number, optional
Start of interval. The interval includes this value. The default start value is 0 .
stop : number
End of interval. The interval does not include this value, except in some cases where step is not an integer and floating point round-off affects the length of out.
step : number, optional
Spacing between values. For any output out, this is the distance between two adjacent values, out [i+1] - out[i]. The default step size is 1. If step is specified, start must also be given.
dtype : dtype
The type of the output array. If dtype is not given, infer the data type from the other input arguments.

Returns
out : ndarray
Array of evenly spaced values.
For floating point arguments, the length of the result is ceil((stop start)/step). Because of floating point overflow, this rule may result in the last element of out being greater than stop.

## See Also:

## linspace

Evenly spaced numbers with careful handling of endpoints.
ogrid
Arrays of evenly spaced numbers in N -dimensions
mgrid
Grid-shaped arrays of evenly spaced numbers in N -dimensions

## Examples

```
>>> np.arange(3)
array([0, 1, 2])
>>> np.arange(3.0)
array([ 0., 1., 2.])
>>> np.arange (3,7)
array([3, 4, 5, 6])
>>> np.arange(3,7,2)
array([3, 5])
```

numpy.ma. choose (indices, choices, out=None, mode='raise')
Use an index array to construct a new array from a set of choices.
Given an array of integers and a set of $n$ choice arrays, this method will create a new array that merges each of the choice arrays. Where a value in $a$ is i , the new array will have the value that choices[i] contains in the same place.

## Parameters

a : ndarray of ints
This array must contain integers in $[0, n-1]$, where $n$ is the number of choices.
choices : sequence of arrays
Choice arrays. The index array and all of the choices should be broadcastable to the same shape.
out : array, optional
If provided, the result will be inserted into this array. It should be of the appropriate shape and dtype.
mode : \{ 'raise', 'wrap', 'clip' \}, optional
Specifies how out-of-bounds indices will behave.

- 'raise' : raise an error
- 'wrap' : wrap around
- 'clip' : clip to the range


## Returns

merged_array : array

## See Also:

choose
equivalent function

## Examples

```
>>> choice = np.array([[1,1,1], [2,2,2], [3,3,3]])
>>> a = np.array([2, 1, 0])
>>> np.ma.choose(a, choice)
masked_array(data = [3 2 1],
    mask = False,
    fill_value=999999)
```

numpy.ma.ediff1d (arr, to_end=None, to_begin=None)

Compute the differences between consecutive elements of an array.
This function is the equivalent of numpy.ediffid that takes masked values into account, see numpy.ediffld for details.

## See Also:

numpy.ediff1d
Equivalent function for ndarrays.
numpy.ma.indices (dimensions, dtype=<type 'int'>)
Return an array representing the indices of a grid.
Compute an array where the subarrays contain index values $0,1, \ldots$ varying only along the corresponding axis.

## Parameters <br> dimensions : sequence of ints

The shape of the grid.
dtype : dtype, optional
Data type of the result.

## Returns

grid : ndarray
The array of grid indices, grid.shape = (len(dimensions), ) + tuple(dimensions).

## See Also:

mgrid, meshgrid

## Notes

The output shape is obtained by prepending the number of dimensions in front of the tuple of dimensions, i.e. if dimensions is a tuple ( $r 0, \ldots, r N-1$ ) of length $N$, the output shape is ( $\mathrm{N}, \mathrm{r} 0, \ldots, r \mathrm{~N}-1$ ).

The subarrays grid [k] contains the $\mathrm{N}-\mathrm{D}$ array of indices along the $\mathrm{k}-\mathrm{th}$ axis. Explicitly:

```
grid[k,i0,i1,...,iN-1] = ik
```


## Examples

```
>>> grid = np.indices((2, 3))
>>> grid.shape
(2, 2, 3)
>>> grid[0] # row indices
array([[0, 0, 0],
            [1, 1, 1]])
>>> grid[1] # column indices
```

```
array([[0, 1, 2],
    [0, 1, 2]])
```

The indices can be used as an index into an array.

```
>>> x = np.arange (20).reshape(5, 4)
>>> row, col = np.indices((2, 3))
>>> x[row, col]
array([[0, 1, 2],
    [4, 5, 6]])
```

Note that it would be more straightforward in the above example to extract the required elements directly with $x[: 2,: 3]$.
numpy.ma. where (condition, $x=$ None, $y=$ None)
Return a masked array with elements from x or y , depending on condition.
Returns a masked array, shaped like condition, where the elements are from $x$ when condition is True, and from $y$ otherwise. If neither $x$ nor $y$ are given, the function returns a tuple of indices where condition is True (the result of condition. nonzero()).

## Parameters

condition : array_like, bool
The condition to meet. For each True element, yield the corresponding element from $x$, otherwise from $y$.
$\mathbf{x}, \mathbf{y}$ : array_like, optional
Values from which to choose. $x$ and $y$ need to have the same shape as condition, or be broadcast-able to that shape.

## Returns

out : MaskedArray or tuple of ndarrays
The resulting masked array if $x$ and $y$ were given, otherwise the result of condition. nonzero().

## See Also:

numpy.where
Equivalent function in the top-level NumPy module.

## Examples

```
>>> x = np.ma.array(np.arange(9.).reshape(3, 3), mask=[[0, 1, 0],
... [1, 0, 1],
... [0, 1, 0]])
>>> print x
[[0.0 -- 2.0]
    [-- 4.0 --]
    [6.0 -- 8.0]]
>>> np.ma.where(x > 5) # return the indices where x > 5
(array([2, 2]), array([0, 2]))
>>> print np.ma.where(x > 5, x, -3.1416)
[[-3.1416 -- -3.1416]
    [-- -3.1416 --]
    [6.0 -- 8.0]]
```


### 3.21 Numpy-specific help functions

### 3.21.1 Finding help

```
lookfor(what[, module, import_modules, ...]) Do a keyword search on docstrings.
numpy.lookfor (what, module=None, import_modules=True, regenerate=False, output=None)
```

Do a keyword search on docstrings.
A list of of objects that matched the search is displayed, sorted by relevance. All given keywords need to be found in the docstring for it to be returned as a result, but the order does not matter.

## Parameters

what : str
String containing words to look for.
module : str or list, optional
Name of module(s) whose docstrings to go through.
import_modules : bool, optional
Whether to import sub-modules in packages. Default is True.
regenerate : bool, optional
Whether to re-generate the docstring cache. Default is False.
output : file-like, optional
File-like object to write the output to. If omitted, use a pager.
See Also:
source, info

## Notes

Relevance is determined only roughly, by checking if the keywords occur in the function name, at the start of a docstring, etc.

## Examples

```
>>> np.lookfor('binary representation')
Search results for 'binary representation'
-------------------------------------------
numpy.binary_repr
    Return the binary representation of the input number as a string.
numpy.core.setup_common.long_double_representation
            Given a binary dump as given by GNU od -b, look for long double
numpy.base_repr
    Return a string representation of a number in the given base system.
```


### 3.21.2 Reading help

[^5]numpy.info (object=None, maxwidth=76, output=<open file '<stdout>', mode 'w' at 0x323070>, toplevel='nитру')
Get help information for a function, class, or module.

## Parameters

object : object or str, optional
Input object or name to get information about. If object is a numpy object, its docstring is given. If it is a string, available modules are searched for matching objects. If None, information about info itself is returned.
maxwidth : int, optional
Printing width.
output : file like object, optional
File like object that the output is written to, default is stdout. The object has to be opened in ' $w$ ' or 'a' mode.
toplevel : str, optional
Start search at this level.

## See Also:

source, lookfor

## Notes

When used interactively with an object, np.info(obj) is equivalent to help (obj) on the Python prompt or obj? on the IPython prompt.

## Examples

```
>>> np.info(np.polyval)
    polyval(p, x)
        Evaluate the polynomial p at x.
            ...
```

When using a string for object it is possible to get multiple results.

```
>>> np.info('fft')
    *** Found in numpy ***
Core FFT routines
...
    *** Found in numpy.fft ***
    fft(a, n=None, axis=-1)
    *** Repeat reference found in numpy.fft.fftpack ***
    *** Total of 3 references found. ***
```

numpy.source (object, output=<open file '<stdout>', mode ' $w$ ' at $0 x 323070>$ )
Print or write to a file the source code for a Numpy object.
The source code is only returned for objects written in Python. Many functions and classes are defined in C and will therefore not return useful information.

## Parameters

object : numpy object
Input object. This can be any object (function, class, module, ...).
output : file object, optional

If output not supplied then source code is printed to screen (sys.stdout). File object must be created with either write ' $w$ ' or append 'a' modes.

## See Also:

```
lookfor,info
```


## Examples

```
>>> np.source(np.interp)
In file: /usr/lib/python2.6/dist-packages/numpy/lib/function_base.py
def interp(x, xp, fp, left=None, right=None):
    """.... (full docstring printed)"""
    if isinstance(x, (float, int, number)):
            return compiled_interp([x], xp, fp, left, right).item()
    else:
            return compiled_interp(x, xp, fp, left, right)
```

The source code is only returned for objects written in Python.

```
>>> np.source(np.array)
Not available for this object.
```


### 3.22 Miscellaneous routines

### 3.22.1 Buffer objects

```
getbuffer() Create a buffer object from the given object referencing a slice of length size starting at offset.
newbuffer(size) Return a new uninitialized buffer object of size bytes
numpy.getbuffer (obj[,offset[, size]])
Create a buffer object from the given object referencing a slice of length size starting at offset.
Default is the entire buffer. A read-write buffer is attempted followed by a read-only buffer.
```


## Parameters

```
obj : object
offset : int, optional
size : int, optional
```


## Returns

```
buffer_obj : buffer
```


## Examples

```
>>> buf = np.getbuffer(np.ones(5), 1, 3)
```

>>> buf = np.getbuffer(np.ones(5), 1, 3)
>>> len(buf)
>>> len(buf)
3
3
>>> buf[0]
>>> buf[0]
'\x00'
'\x00'
>>> buf
>>> buf
<read-write buffer for 0x8af1e70, size 3, offset 1 at 0x8ba4ec0>
<read-write buffer for 0x8af1e70, size 3, offset 1 at 0x8ba4ec0>
numpy.newbuffer(size)
Return a new uninitialized buffer object of size bytes

```

\subsection*{3.22.2 Performance tuning}
\begin{tabular}{ll}
\hline alterdot & Change dot, vdot, and innerproduct to use accelerated BLAS functions. \\
restoredot & Restore dot, vdot, and innerproduct to the default non-BLAS \\
setbufsize(size) & Set the size of the buffer used in ufuncs. \\
getbufsize() & Return the size of the buffer used in ufuncs. \\
\hline
\end{tabular}
numpy.alterdot()
Change dot, vdot, and innerproduct to use accelerated BLAS functions.
Typically, as a user of Numpy, you do not explicitly call this function. If Numpy is built with an accelerated BLAS, this function is automatically called when Numpy is imported.

When Numpy is built with an accelerated BLAS like ATLAS, these functions are replaced to make use of the faster implementations. The faster implementations only affect float32, float64, complex64, and complex 128 arrays. Furthermore, the BLAS API only includes matrix-matrix, matrix-vector, and vector-vector products. Products of arrays with larger dimensionalities use the built in functions and are not accelerated.

\section*{See Also:}
restoredot
restoredot undoes the effects of alterdot.
numpy. restoredot ()
Restore dot, vdot, and innerproduct to the default non-BLAS implementations.
Typically, the user will only need to call this when troubleshooting and installation problem, reproducing the conditions of a build without an accelerated BLAS, or when being very careful about benchmarking linear algebra operations.

See Also:
alterdot
restoredot undoes the effects of alterdot.
numpy.setbufsize (size)
Set the size of the buffer used in ufuncs.
Parameters
size : int
Size of buffer.
numpy.getbufsize()
Return the size of the buffer used in ufuncs.

\subsection*{3.23 Test Support (numpy.testing)}

Common test support for all numpy test scripts.
This single module should provide all the common functionality for numpy tests in a single location, so that test scripts can just import it and work right away.

\subsection*{3.24 Asserts}
assert_almost_equal(actualRaise an assertion if two items are not equal up to desired precision. desired \([, \ldots]\) )
assert_approx_equal(actualRaise an assertion if two items are not equal up to significant digits. desired \([, \ldots]\) )
assert_array_almost_equaRaise an assertion if two objects are not equal up to desired precision.
\(\mathrm{y}[\), decimal, ...])
assert_array_equal(x, Raise an assertion if two array_like objects are not equal.
y [, err_msg, verbose])
assert_array_less(x,y[, Raise an assertion if two array_like objects are not ordered by less than.
err_msg, verbose])
assert_equal(actual, Raise an assertion if two objects are not equal. desired[, err_msg, verbose])
assert_raises(exception_clasF,Fail unless an exception of class exception_class is thrown by callable when callable, ...) invoked with arguments args and keyword arguments kwargs.
assert_warns(warning_class, Fail unless the given callable throws the specified warning.
func, \(* \operatorname{args}, * * \mathrm{kw})\)
assert_string_equal(actual,Test if two strings are equal.
desired)
numpy.testing.assert_almost_equal (actual, desired, decimal=7, err_msg='', verbose=True)
Raise an assertion if two items are not equal up to desired precision.
Note: It is recommended to use one of assert_allclose, assert_array_almost_equal_nulp or assert_array_max_ulp instead of this function for more consistent floating point comparisons.

The test is equivalent to abs (desired-actual) < \(0.5 * 10 * *(-\) decimal).
Given two objects (numbers or ndarrays), check that all elements of these objects are almost equal. An exception is raised at conflicting values. For ndarrays this delegates to assert_array_almost_equal

\section*{Parameters}
actual : array_like
The object to check.
desired : array_like
The expected object.
decimal : int, optional
Desired precision, default is 7 .
err_msg : str, optional
The error message to be printed in case of failure.
verbose : bool, optional
If True, the conflicting values are appended to the error message.

\section*{Raises}

\section*{AssertionError :}

If actual and desired are not equal up to specified precision.

\section*{See Also:}
assert_allclose
Compare two array_like objects for equality with desired relative and/or absolute precision.
assert_array_almost_equal_nulp, assert_array_max_ulp, assert_equal

\section*{Examples}
```

>>> import numpy.testing as npt
>>> npt.assert_almost_equal(2.3333333333333, 2.33333334)
>>> npt.assert_almost_equal(2.3333333333333, 2.33333334, decimal=10)
<type 'exceptions.AssertionError'>:
Items are not equal:
ACTUAL: 2.3333333333333002
DESIRED: 2.3333333399999998
>>> npt.assert_almost_equal(np.array([1.0,2.3333333333333]),
... np.array([1.0,2.33333334]), decimal=9)
...
<type 'exceptions.AssertionError'>:
Arrays are not almost equal
<BLANKLINE>
(mismatch 50.0%)
x: array([ 1. , 2.33333333])
y: array([ 1. , 2.33333334])

```
numpy.testing.assert_approx_equal (actual, desired, significant=7, err_msg='‘, verbose=True)
Raise an assertion if two items are not equal up to significant digits.
Note: It is recommended to use one of assert_allclose, assert_array_almost_equal_nulp or assert_array_max_ulp instead of this function for more consistent floating point comparisons.
Given two numbers, check that they are approximately equal. Approximately equal is defined as the number of significant digits that agree.

\section*{Parameters}
actual : scalar
The object to check.
desired : scalar
The expected object.
significant : int, optional
Desired precision, default is 7 .
err_msg : str, optional
The error message to be printed in case of failure.
verbose : bool, optional
If True, the conflicting values are appended to the error message.

\section*{Raises}

\section*{AssertionError :}

If actual and desired are not equal up to specified precision.

\section*{See Also:}
assert_allclose
Compare two array_like objects for equality with desired relative and/or absolute precision.
```

assert_array_almost_equal_nulp,assert_array_max_ulp,assert_equal

```

\section*{Examples}
```

>>> np.testing.assert_approx_equal(0.12345677777777e-20, 0.1234567e-20)
>>> np.testing.assert_approx_equal(0.12345670e-20, 0.12345671e-20,
significant=8)
>>> np.testing.assert_approx_equal(0.12345670e-20, 0.12345672e-20,
significant=8)
. .
<type 'exceptions.AssertionError'>:
Items are not equal to 8 significant digits:
ACTUAL: 1.234567e-021
DESIRED: 1.2345672000000001e-021

```
the evaluated condition that raises the exception is
```

>>> abs(0.12345670e-20/1e-21 - 0.12345672e-20/1e-21) >= 10**-(8-1)
True

```
numpy.testing.assert_array_almost_equal ( \(x, y\), decimal \(=6\), err_msg \(='\) ', verbose \(=\) True \()\)

Raise an assertion if two objects are not equal up to desired precision.
Note: It is recommended to use one of assert_allclose, assert_array_almost_equal_nulp or assert_array_max_ulp instead of this function for more consistent floating point comparisons.

The test verifies identical shapes and verifies values with abs(desired-actual) < 0.5 * 10**(-decimal).

Given two array_like objects, check that the shape is equal and all elements of these objects are almost equal. An exception is raised at shape mismatch or conflicting values. In contrast to the standard usage in numpy, NaNs are compared like numbers, no assertion is raised if both objects have NaNs in the same positions.

\section*{Parameters}
\(\mathbf{x}\) : array_like
The actual object to check.
\(\mathbf{y}\) : array_like
The desired, expected object.
decimal : int, optional
Desired precision, default is 6 .
err_msg : str, optional
The error message to be printed in case of failure.
verbose : bool, optional
If True, the conflicting values are appended to the error message.

\section*{Raises}

\section*{AssertionError :}

If actual and desired are not equal up to specified precision.

\section*{See Also:}

\section*{assert_allclose}

Compare two array_like objects for equality with desired relative and/or absolute precision.
```

assert_array_almost_equal_nulp, assert_array_max_ulp,assert_equal

```

\section*{Examples}
the first assert does not raise an exception
```

>>> np.testing.assert_array_almost_equal([1.0,2.333,np.nan],
[1.0,2.333,np.nan])
>>> np.testing.assert_array_almost_equal([1.0,2.33333,np.nan],
... [1.0,2.33339,np.nan], decimal=5)
...
<type 'exceptions.AssertionError'>:
AssertionError:
Arrays are not almost equal
<BLANKLINE>
(mismatch 50.0%)
x: array([ 1. , 2.33333, NaN])
y: array([ 1. , 2.33339, NaN])
>>> np.testing.assert_array_almost_equal([1.0,2.33333,np.nan],
... [1.0,2.33333, 5], decimal=5)
<type 'exceptions.ValueError'>:
ValueError:
Arrays are not almost equal
x: array([ 1. , 2.33333, NaN])
y: array([ 1. , 2.33333, 5. ])
numpy.testing.assert_array_equal (x,y,err_msg='`,verbose=True)

```

Raise an assertion if two array_like objects are not equal.
Given two array_like objects, check that the shape is equal and all elements of these objects are equal. An exception is raised at shape mismatch or conflicting values. In contrast to the standard usage in numpy, NaNs are compared like numbers, no assertion is raised if both objects have NaNs in the same positions.

The usual caution for verifying equality with floating point numbers is advised.

\section*{Parameters}
\(\mathbf{x}\) : array_like
The actual object to check.
\(\mathbf{y}\) : array_like
The desired, expected object.
err_msg : str, optional
The error message to be printed in case of failure.
verbose : bool, optional
If True, the conflicting values are appended to the error message.

\section*{Raises}

\section*{AssertionError :}

If actual and desired objects are not equal.

\section*{See Also:}
assert_allclose
Compare two array_like objects for equality with desired relative and/or absolute precision.
assert_array_almost_equal_nulp, assert_array_max_ulp, assert_equal

\section*{Examples}

The first assert does not raise an exception:
```

>>> np.testing.assert_array_equal([1.0,2.33333,np.nan],
... [np.exp(0),2.33333, np.nan])

```

Assert fails with numerical inprecision with floats:
```

>>> np.testing.assert_array_equal([1.0,np.pi,np.nan],
... [1, np.sqrt(np.pi)**2, np.nan])
...
<type 'exceptions.ValueError'>:
AssertionError:
Arrays are not equal
<BLANKLINE>
(mismatch 50.0%)
x: array([ 1. , 3.14159265, NaN])
y: array([ 1. , 3.14159265, NaN])

```

Use assert_allclose or one of the nulp (number of floating point values) functions for these cases instead:
```

>>> np.testing.assert_allclose([1.0,np.pi,np.nan],
... [1, np.sqrt(np.pi)**2, np.nan],
... rtol=1e-10, atol=0)
numpy.testing.assert_array_less (x, y, err_msg='',verbose=True)

```

Raise an assertion if two array_like objects are not ordered by less than.
Given two array_like objects, check that the shape is equal and all elements of the first object are strictly smaller than those of the second object. An exception is raised at shape mismatch or incorrectly ordered values. Shape mismatch does not raise if an object has zero dimension. In contrast to the standard usage in numpy, NaNs are compared, no assertion is raised if both objects have NaNs in the same positions.

\section*{Parameters}
\(\mathbf{x}\) : array_like
The smaller object to check.
\(\mathbf{y}\) : array_like
The larger object to compare.
err_msg : string
The error message to be printed in case of failure.
verbose : bool
If True, the conflicting values are appended to the error message.

\section*{Raises}

\section*{AssertionError :}

If actual and desired objects are not equal.

\section*{See Also:}
assert_array_equal
tests objects for equality
assert_array_almost_equal
test objects for equality up to precision

\section*{Examples}
```

>>> np.testing.assert_array_less([1.0, 1.0, np.nan], [1.1, 2.0, np.nan])
>>> np.testing.assert_array_less([1.0, 1.0, np.nan], [1, 2.0, np.nan])
...
<type 'exceptions.ValueError'>:
Arrays are not less-ordered
(mismatch 50.0%)
x: array([ 1., 1., NaN])
y: array([ 1., 2., NaN])
>>> np.testing.assert_array_less([1.0, 4.0], 3)
. .
<type 'exceptions.ValueError'>:
Arrays are not less-ordered
(mismatch 50.0%)
x: array([ 1., 4.])
y: array(3)
>>> np.testing.assert_array_less([1.0, 2.0, 3.0], [4])
-
<type 'exceptions.ValueError'>:
Arrays are not less-ordered
(shapes (3,), (1,) mismatch)
x: array([ 1., 2., 3.])
y: array([4])
numpy.testing.assert_equal (actual, desired, err_msg='`,verbose=True)

```

Raise an assertion if two objects are not equal.
Given two objects (scalars, lists, tuples, dictionaries or numpy arrays), check that all elements of these objects are equal. An exception is raised at the first conflicting values.

\section*{Parameters}
actual : array_like
The object to check.
desired : array_like
The expected object.
err_msg : str, optional
The error message to be printed in case of failure.
verbose : bool, optional
If True, the conflicting values are appended to the error message.

\section*{Raises}

\section*{AssertionError :}

If actual and desired are not equal.

\section*{Examples}
```

>>> np.testing.assert_equal([4,5], [4,6])
. .
<type 'exceptions.AssertionError'>:
Items are not equal:
item=1

```
```

ACTUAL: 5
DESIRED: 6
numpy.testing.assert_raises (exception_class, callable, *args, **kwargs)

```

Fail unless an exception of class exception_class is thrown by callable when invoked with arguments args and keyword arguments kwargs. If a different type of exception is thrown, it will not be caught, and the test case will be deemed to have suffered an error, exactly as for an unexpected exception.
numpy.testing.assert_warns (warning_class, func, *args, **kw)
Fail unless the given callable throws the specified warning.
A warning of class warning_class should be thrown by the callable when invoked with arguments args and keyword arguments kwargs. If a different type of warning is thrown, it will not be caught, and the test case will be deemed to have suffered an error.

\section*{Parameters}
warning_class : class
The class defining the warning that func is expected to throw.
func : callable
The callable to test.
*args : Arguments
Arguments passed to func.
**kwargs : Kwargs
Keyword arguments passed to func.

\section*{Returns}

None :
```

numpy.testing.assert_string_equal (actual, desired)

```

Test if two strings are equal.
If the given strings are equal, assert_string_equal does nothing. If they are not equal, an AssertionError is raised, and the diff between the strings is shown.

\section*{Parameters}
actual : str
The string to test for equality against the expected string.
desired : str
The expected string.

\section*{Examples}
```

>>> np.testing.assert_string_equal(' abc', 'abc')
>>> np.testing.assert_string_equal('abc', 'abcd')
Traceback (most recent call last):
File "<stdin>", line 1, in <module>
AssertionError: Differences in strings:

- abc+ abcd? +

```

\subsection*{3.24.1 Decorators}
```

decorators.deprecated([conditional]) Filter deprecation warnings while running the test suite.
decorators.knownfailureif(fail_condition@Make function raise KnownFailureTest exception if given
msg]) condition is true.
decorators.setastest([tf]) Signals to nose that this function is or is not a test.
decorators.skipif(skip_condition[,msg]) Make function raise SkipTest exception if a given condition is
true.
decorators.slow(t) Label a test as 'slow'.
decorate_methods(cls, decorator[, Apply a decorator to all methods in a class matching a regular
testmatch])
expression.
numpy.testing.decorators.deprecated (conditional=True)

```

Filter deprecation warnings while running the test suite.
This decorator can be used to filter DeprecationWarning's, to avoid printing them during the test suite run, while checking that the test actually raises a DeprecationWarning.

\section*{Parameters}
conditional : bool or callable, optional
Flag to determine whether to mark test as deprecated or not. If the condition is a callable, it is used at runtime to dynamically make the decision. Default is True.

\section*{Returns}
decorator : function
The deprecated decorator itself.

\section*{Notes}

New in version 1.4.0.
numpy.testing. decorators.knownfailureif (fail_condition, msg=None)
Make function raise KnownFailureTest exception if given condition is true.
If the condition is a callable, it is used at runtime to dynamically make the decision. This is useful for tests that may require costly imports, to delay the cost until the test suite is actually executed.

\section*{Parameters}
fail_condition : bool or callable
Flag to determine whether to mark the decorated test as a known failure (if True) or not (if False).
msg : str, optional
Message to give on raising a KnownFailureTest exception. Default is None.

\section*{Returns}
decorator : function
Decorator, which, when applied to a function, causes SkipTest to be raised when skip_condition is True, and the function to be called normally otherwise.

\section*{Notes}

The decorator itself is decorated with the nose.tools.make_decorator function in order to transmit function name, and various other metadata.
numpy.testing.decorators.setastest ( \(t f=\) True)
Signals to nose that this function is or is not a test.

\section*{Parameters}
tf : bool
If True, specifies that the decorated callable is a test. If False, specifies that the decorated callable is not a test. Default is True.

\section*{Notes}

This decorator can't use the nose namespace, because it can be called from a non-test module. See also istest and nottest in nose.tools.

\section*{Examples}
setastest can be used in the following way:
```

from numpy.testing.decorators import setastest
@setastest(False)
def func_with_test_in_name(arg1, arg2):
pass

```
numpy.testing.decorators.skipif (skip_condition, msg=None)

Make function raise SkipTest exception if a given condition is true.
If the condition is a callable, it is used at runtime to dynamically make the decision. This is useful for tests that may require costly imports, to delay the cost until the test suite is actually executed.

\section*{Parameters}
skip_condition : bool or callable
Flag to determine whether to skip the decorated test.
msg : str, optional
Message to give on raising a SkipTest exception. Default is None.

\section*{Returns}
decorator : function
Decorator which, when applied to a function, causes SkipTest to be raised when skip_condition is True, and the function to be called normally otherwise.

\section*{Notes}

The decorator itself is decorated with the nose.tools.make_decorator function in order to transmit function name, and various other metadata.
numpy.testing.decorators.slow \((t)\)
Label a test as 'slow'.
The exact definition of a slow test is obviously both subjective and hardware-dependent, but in general any individual test that requires more than a second or two should be labeled as slow (the whole suite consits of thousands of tests, so even a second is significant).

\section*{Parameters}
\(t\) : callable
The test to label as slow.

\section*{Returns}
t : callable
The decorated test \(t\).

\section*{Examples}

The numpy.testing module includes import decorators as dec. A test can be decorated as slow like this:
```

from numpy.testing import *
@dec.slow
def test_big(self):
print 'Big, slow test'

```
numpy.testing.decorate_methods (cls, decorator, testmatch=None)

Apply a decorator to all methods in a class matching a regular expression.
The given decorator is applied to all public methods of \(c l s\) that are matched by the regular expression testmatch (testmatch.search (methodname) ). Methods that are private, i.e. start with an underscore, are ignored.

\section*{Parameters}
cls : class
Class whose methods to decorate.
decorator : function
Decorator to apply to methods
testmatch : compiled regexp or str, optional
The regular expression. Default value is None, in which case the nose default (re.compile(r' (?:^|[\b_\.\%s-])[Tt]est' \% os.sep)) is used. If testmatch is a string, it is compiled to a regular expression first.

\subsection*{3.24.2 Test Running}
```

Tester Nose test runner.
run_module_suite([file_to_run])
rundocs([filename, raise_on_error]) Run doctests found in the given file.
numpy.testing.Tester
alias of NoseTester
numpy.testing.run_module_suite(file_to_run=None)
numpy.testing.rundocs (filename=None, raise_on_error=True)
Run doctests found in the given file.
By default rundocs raises an AssertionError on failure.

```

\section*{Parameters}
```

filename : str

```

The path to the file for which the doctests are run.
raise_on_error : bool
Whether to raise an AssertionError when a doctest fails. Default is True.

\section*{Notes}

The doctests can be run by the user/developer by adding the doctests argument to the test () call. For example, to run all tests (including doctests) for numpy. lib:

\subsection*{3.25 Mathematical functions with automatic domain (numpy.emath)}

Note: numpy.emath is a preferred alias for numpy.lib.scimath, available after numpy is imported. Wrapper functions to more user-friendly calling of certain math functions whose output data-type is different than the input data-type in certain domains of the input.

For example, for functions like \(l o g\) with branch cuts, the versions in this module provide the mathematically valid answers in the complex plane:
```

>>> import math
>>> from numpy.lib import scimath
>>> scimath.log(-math.exp(1)) == (1+1j*math.pi)
True

```

Similarly, sqrt, other base logarithms, power and trig functions are correctly handled. See their respective docstrings for specific examples.

\subsection*{3.26 Matrix library (numpy .matlib)}

This module contains all functions in the numpy namespace, with the following replacement functions that return matrices instead of ndarrays.

\subsection*{3.27 Optionally Scipy-accelerated routines (numpy . dual)}

Aliases for functions which may be accelerated by Scipy.
Scipy can be built to use accelerated or otherwise improved libraries for FFTs, linear algebra, and special functions. This module allows developers to transparently support these accelerated functions when scipy is available but still support users who have only installed Numpy.

\subsection*{3.27.1 Linear algebra}
\begin{tabular}{ll}
\hline cholesky(a) & Cholesky decomposition. \\
det(a) & Compute the determinant of an array. \\
eig(a) & Compute the eigenvalues and right eigenvectors of a square array. \\
eigh(a[, UPLO]) & Return the eigenvalues and eigenvectors of a Hermitian or symmetric matrix. \\
eigvals(a) & Compute the eigenvalues of a general matrix. \\
eigvalsh(a[, UPLO]) & Compute the eigenvalues of a Hermitian or real symmetric matrix. \\
inv(a) & Compute the (multiplicative) inverse of a matrix. \\
lstsq(a, b[, rcond]) & Return the least-squares solution to a linear matrix equation. \\
norm(x[, ord]) & Matrix or vector norm. \\
pinv(a[, rcond \(]\) & Compute the (Moore-Penrose) pseudo-inverse of a matrix. \\
solve(a, b) & Solve a linear matrix equation, or system of linear scalar equations. \\
svd(a[, full_matrices, compute_uv]) & Singular Value Decomposition. \\
\hline
\end{tabular}

\subsection*{3.27.2 FFT}
\begin{tabular}{ll}
\hline\(f f t(a[, n\), axis \(])\) & Compute the one-dimensional discrete Fourier Transform. \\
fft2(a[, s, axes]) & Compute the 2-dimensional discrete Fourier Transform \\
fftn \((a[, s, a x e s])\) & Compute the N-dimensional discrete Fourier Transform. \\
ifft(a[, n, axis] \()\) & Compute the one-dimensional inverse discrete Fourier Transform. \\
ifft2(a[, s, axes]) & Compute the 2-dimensional inverse discrete Fourier Transform. \\
ifftn(a[, s, axes]) & Compute the N-dimensional inverse discrete Fourier Transform. \\
\hline
\end{tabular}

\subsection*{3.27.3 Other}
i0(x) Modified Bessel function of the first kind, order 0.

\subsection*{3.28 Numarray compatibility (numpy . numarray)}

\subsection*{3.29 Old Numeric compatibility (numpy.oldnumeric)}

\subsection*{3.30 C-Types Foreign Function Interface (numpy. ctypeslib)}
numpy.ctypeslib.as_array (obj, shape=None)
Create a numpy array from a ctypes array or a ctypes POINTER. The numpy array shares the memory with the ctypes object.

The size parameter must be given if converting from a ctypes POINTER. The size parameter is ignored if converting from a ctypes array
numpy.ctypeslib.as_ctypes (obj)
Create and return a ctypes object from a numpy array. Actually anything that exposes the \(\qquad\) array_interface is accepted.
numpy.ctypeslib.ctypes_load_library (*args, **kwds)
ctypes_load_library is deprecated, use load_library instead!
numpy.ctypeslib.load_library (libname, loader_path)
numpy.ctypeslib.ndpointer (dtype=None, ndim=None, shape=None, flags=None)
Array-checking restype/argtypes.
An ndpointer instance is used to describe an ndarray in restypes and argtypes specifications. This approach is more flexible than using, for example, POINTER (c_double), since several restrictions can be specified, which are verified upon calling the ctypes function. These include data type, number of dimensions, shape and flags. If a given array does not satisfy the specified restrictions, a TypeError is raised.

\section*{Parameters}
dtype : data-type, optional
Array data-type.
ndim : int, optional
Number of array dimensions.
shape : tuple of ints, optional

Array shape.
flags : str or tuple of str
Array flags; may be one or more of:
- C_CONTIGUOUS / C / CONTIGUOUS
- F_CONTIGUOUS / F / FORTRAN
- OWNDATA / O
- WRITEABLE / W
- ALIGNED / A
- UPDATEIFCOPY / U

\section*{Returns}
klass : ndpointer type object
A type object, which is an _ndtpr instance containing dtype, ndim, shape and flags information.

\section*{Raises}

TypeError :
If a given array does not satisfy the specified restrictions.

\section*{Examples}
```

>>> clib.somefunc.argtypes = [np.ctypeslib.ndpointer(dtype=np.float64,
... ndim=1,
... flags='C_CONTIGUOUS')]
>>> clib.somefunc(np.array([1, 2, 3], dtype=np.float64))
...

```

\subsection*{3.31 String operations}

This module provides a set of vectorized string operations for arrays of type numpy.string_ or numpy. unicode_. All of them are based on the string methods in the Python standard library.

\subsection*{3.31.1 String operations}
\begin{tabular}{|c|c|}
\hline \(\operatorname{add}(\mathrm{x} 1, \mathrm{x} 2)\) & Return (x1 + x2), that is string concatenation, element-wise for a pair of array_likes of str or unicode. \\
\hline multiply \((\mathrm{a}, \mathrm{i})\) & Return ( \(\mathrm{a} * \mathrm{i}\) ), that is string multiple concatenation, element-wise. \\
\hline mod(a, values) & Return (a \% i ), that is pre-Python 2.6 string formatting \\
\hline capitalize(a) & Return a copy of \(a\) with only the first character of each element capitalized. \\
\hline center(a, width[, fillchar]) & Return a copy of \(a\) with its elements centered in a string of length width. \\
\hline decode(a[, encoding, errors]) & Calls str.decode element-wise. \\
\hline encode (a[, encoding, errors]) & Calls str.encode element-wise. \\
\hline join(sep, seq) & Return a string which is the concatenation of the strings in the sequence seq. \\
\hline l just(a, width[, fillchar]) & Return an array with the elements of \(a\) left-justified in a string of length width. \\
\hline lower(a) & Return an array with the elements of \(a\) converted to lowercase. \\
\hline \[
\begin{aligned}
& \text { lstrip(a[, } \\
& \text { chars]) }
\end{aligned}
\] & For each element in \(a\), return a copy with the leading characters removed. \\
\hline partition(a, sep) & Partition each element in \(a\) around sep. \\
\hline replace(a, old, new[, count]) & For each element in \(a\), return a copy of the string with all occurrences of substring old replaced by new. \\
\hline rjust(a, width[, fillchar]) & Return an array with the elements of \(a\) right-justified in a string of length width. \\
\hline rpartition(a, sep) & Partition each element in \(a\) around sep. \\
\hline rsplit(a[, sep, maxsplit]) & For each element in \(a\), return a list of the words in the string, using sep as the delimiter string. \\
\hline \[
\begin{aligned}
& \text { rstrip(a[, } \\
& \text { chars]) }
\end{aligned}
\] & For each element in \(a\), return a copy with the trailing characters removed. \\
\hline split(a[, sep, maxsplit]) & For each element in \(a\), return a list of the words in the string, using sep as the delimiter string. \\
\hline \begin{tabular}{l}
splitlines(a[, \\
keepends])
\end{tabular} & For each element in \(a\), return a list of the lines in the element, breaking at line boundaries. \\
\hline strip(a[, chars]) & For each element in \(a\), return a copy with the leading and trailing characters removed. \\
\hline swapcase(a) & For each element in \(a\), return a copy of the string with uppercase characters converted to lowercase and vice versa. \\
\hline title(a) & For each element in \(a\), return a titlecased version of the string: words start with uppercase characters, all remaining cased characters are lowercase. \\
\hline translate(a, table[, deletechars]) & For each element in \(a\), return a copy of the string where all characters occurring in the optional argument deletechars are removed, and the remaining characters have been mapped through the given translation table. \\
\hline upper(a) & Return an array with the elements of \(a\) converted to uppercase. \\
\hline zfill(a, width) & Return the numeric string left-filled with zeros in a string of length width. \\
\hline
\end{tabular}
numpy.core.defchararray.add (xl, \(x 2\) )
Return ( \(\mathrm{x} 1+\mathrm{x} 2\) ), that is string concatenation, element-wise for a pair of array_likes of str or unicode.

\section*{Parameters}
\(\mathbf{x 1}\) : array_like of str or unicode
\(\mathbf{x 2}\) : array_like of str or unicode

\section*{Returns}
out : ndarray

Output array of string_ or unicode_, depending on input types
numpy.core.defchararray.multiply ( \(a, i\) )
Return (a*i), that is string multiple concatenation, element-wise.
Values in \(i\) of less than 0 are treated as 0 (which yields an empty string).

\section*{Parameters}
a : array_like of str or unicode
i : array_like of ints

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input types
numpy.core.defchararray.mod ( \(a\), values)
Return (a \% i), that is pre-Python 2.6 string formatting (iterpolation), element-wise for a pair of array_likes of str or unicode.

\section*{Parameters}
a : array_like of str or unicode
values : array_like of values
These values will be element-wise interpolated into the string.

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input types

\section*{See Also:}
str. \(\qquad\) mod \(\qquad\)
numpy.core.defchararray. capitalize (a)
Return a copy of \(a\) with only the first character of each element capitalized.
Calls str.capitalize element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input types

\section*{See Also:}
str.capitalize

\section*{Examples}
```

>>> c = np.array(['a1b2','1b2a','b2a1','2a1b'],'S4'); c
array(['a1b2', '1b2a', 'b2a1', '2a1b'],
dtype='|S4')
>>> np.char.capitalize(c)
array(['A1b2', '1b2a', 'B2a1', '2a1b'],
dtype='|S4')

```
```

numpy.core.defchararray. center ( $a$, width, fillchar=' ')

```

Return a copy of \(a\) with its elements centered in a string of length width.
Calls str.center element-wise.

\section*{Parameters}
a : array_like of str or unicode
width : int
The length of the resulting strings
fillchar : str or unicode, optional
The padding character to use (default is space).

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input types

\section*{See Also:}
str.center
numpy. core.defchararray.decode ( \(a\), encoding \(=\) None, errors \(=\) None)
Calls str.decode element-wise.
The set of available codecs comes from the Python standard library, and may be extended at runtime. For more information, see the codecs module.

\section*{Parameters}
a : array_like of str or unicode
encoding : str, optional
The name of an encoding
errors : str, optional
Specifies how to handle encoding errors

\section*{Returns}
out : ndarray

\section*{See Also:}
```

    str.decode
    ```

\section*{Notes}

The type of the result will depend on the encoding specified.

\section*{Examples}
```

>>> c = np.array(['aAaAaA', ' aA ', 'abBABba'])
>>> c
array(['aAaAaA', ' aA ', 'abBABba'],
dtype='|S7')
>>> np.char.encode(c, encoding='cp037')
array(['\x81\xc1\x81\xc1\x81\xc1', '@@\x81\xc1@@',
'\x81\x82\xc2\xc1\xc2\x82\x81'],
dtype='|S7')

```
numpy.core.defchararray.encode (a, encoding=None, errors=None)
Calls str.encode element-wise.
The set of available codecs comes from the Python standard library, and may be extended at runtime. For more information, see the codecs module.

\section*{Parameters}
a : array_like of str or unicode
encoding : str, optional
The name of an encoding
errors : str, optional
Specifies how to handle encoding errors

\section*{Returns}
out : ndarray

\section*{See Also:}
str.encode

\section*{Notes}

The type of the result will depend on the encoding specified.
numpy.core.defchararray.join (sep, seq)
Return a string which is the concatenation of the strings in the sequence seq.
Calls str.join element-wise.

\section*{Parameters}
sep : array_like of str or unicode
seq : array_like of str or unicode

\section*{Returns} out : ndarray

Output array of str or unicode, depending on input types
See Also:
str.join
numpy. core.defchararray.ljust ( \(a\), width, fillchar=' ')
Return an array with the elements of \(a\) left-justified in a string of length width.
Calls str:ljust element-wise.

\section*{Parameters}
a : array_like of str or unicode
width : int
The length of the resulting strings
fillchar : str or unicode, optional
The character to use for padding

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.ljust
numpy.core.defchararray.lower (a)
Return an array with the elements of \(a\) converted to lowercase.
Call str:lower element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array-like of str or unicode

\section*{Returns}
out : ndarray, str or unicode
Output array of str or unicode, depending on input type

\section*{See Also:}
str.lower

\section*{Examples}
```

>>> c = np.array(['A1B C', '1BCA', 'BCA1']); c
array(['A1B C', '1BCA', 'BCA1'],
dtype='|S5')
>>> np.char.lower(c)
array(['a1b c', '1bca', 'bca1'],
dtype='|S5')

```
numpy. core.defchararray.lstrip ( \(a\), chars=None)

For each element in \(a\), return a copy with the leading characters removed.
Calls str:lstrip element-wise.

\section*{Parameters}
a : array-like of str or unicode
chars : str or unicode, optional
The chars argument is a string specifying the set of characters to be removed. If omitted or None, the chars argument defaults to removing whitespace. The chars argument is not a prefix; rather, all combinations of its values are stripped.

\section*{Returns}
out : ndarray, str or unicode
Output array of str or unicode, depending on input type

\section*{See Also:}
```

str.lstrip

```

\section*{Examples}
```

>>> c = np.array(['aAaAaA', ' aA ', 'abBABba'])
>>> c
array(['aAaAaA', ' aA ', 'abBABba'],
dtype='|S7')
>>> np.char.lstrip(c, 'a') \# 'a' unstripped from c[l] because whitespace leading
array(['AaAaA', ' aA ', 'bBABba'],
dtype='|S7')

```
```

>>> np.char.lstrip(c, 'A') \# leaves c unchanged
array(['aAaAaA', ' aA ', 'abBABba'],
dtype='|S7')
>>> (np.char.lstrip(c, ' ') == np.char.lstrip(c, '')).all()
... \# XXX: is this a regression? this line now returns False
... \# np.char.lstrip(c,'') does not modify c at all.
True
>>> (np.char.lstrip(c, ' ') == np.char.lstrip(c, None)).all()
True
numpy.core.defchararray.partition (a, sep)

```

Partition each element in \(a\) around sep.
Calls str.partition element-wise.
For each element in \(a\), split the element as the first occurrence of sep, and return 3 strings containing the part before the separator, the separator itself, and the part after the separator. If the separator is not found, return 3 strings containing the string itself, followed by two empty strings.

\section*{Parameters}
a : array-like of str or unicode
sep : str or unicode

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type. The output array will have an extra dimension with 3 elements per input element.

\section*{See Also:}
str.partition
numpy. core.defchararray.replace ( \(a\), old, new, count=None)
For each element in \(a\), return a copy of the string with all occurrences of substring old replaced by new.
Calls str.replace element-wise.

\section*{Parameters}
a : array-like of str or unicode
old, new : str or unicode
count : int, optional
If the optional argument count is given, only the first count occurrences are replaced.

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.replace
numpy. core.defchararray.rjust ( \(a\), width, fillchar=' ')
Return an array with the elements of \(a\) right-justified in a string of length width.
Calls str.rjust element-wise.

\section*{Parameters}
a : array_like of str or unicode
width : int
The length of the resulting strings
fillchar : str or unicode, optional
The character to use for padding

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
```

    str.rjust
    numpy.core.defchararray.rpartition(a, sep)
Partition each element in a around sep.
Calls str.rpartition element-wise.

```

For each element in \(a\), split the element as the last occurrence of sep, and return 3 strings containing the part before the separator, the separator itself, and the part after the separator. If the separator is not found, return 3 strings containing the string itself, followed by two empty strings.

\section*{Parameters}
\(\mathbf{a}\) : array-like of str or unicode
sep : str or unicode

\section*{Returns}
out : ndarray
Output array of string or unicode, depending on input type. The output array will have an extra dimension with 3 elements per input element.

\section*{See Also:}
str.rpartition
numpy.core.defchararray.rsplit ( \(a\), sep=None, maxsplit=None)
For each element in \(a\), return a list of the words in the string, using sep as the delimiter string.
Calls str.rsplit element-wise.
Except for splitting from the right, rsplit behaves like split.

\section*{Parameters}
a : array_like of str or unicode
sep : str or unicode, optional
If sep is not specified or None, any whitespace string is a separator.
maxsplit : int, optional
If maxsplit is given, at most maxsplit splits are done, the rightmost ones.

\section*{Returns}
out : ndarray
Array of list objects

\section*{See Also:}
str.rsplit,split
numpy.core.defchararray.rstrip ( \(a\), chars=None)
For each element in \(a\), return a copy with the trailing characters removed.
Calls str.rstrip element-wise.

\section*{Parameters}
\(\mathbf{a}\) : array-like of str or unicode
chars : str or unicode, optional
The chars argument is a string specifying the set of characters to be removed. If omitted or None, the chars argument defaults to removing whitespace. The chars argument is not a suffix; rather, all combinations of its values are stripped.

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.rstrip
Examples
```

>>> c = np.array(['aAaAaA', 'abBABba'], dtype='S7'); c
array(['aAaAaA', 'abBABba'],
dtype='|S7')
>>> np.char.rstrip(c, 'a')
array(['aAaAaA', 'abBABb'],
dtype='|S7')
>>> np.char.rstrip(c, 'A')
array(['aAaAa', 'abBABba'],
dtype='|S7')
numpy.core.defchararray.split (a, sep=None, maxsplit=None)

```

For each element in \(a\), return a list of the words in the string, using sep as the delimiter string.
Calls str.rsplit element-wise.

\section*{Parameters}
a : array_like of str or unicode
sep : str or unicode, optional
If sep is not specified or None, any whitespace string is a separator.
maxsplit : int, optional
If maxsplit is given, at most maxsplit splits are done.

\section*{Returns}
out : ndarray
Array of list objects

\section*{See Also:}
str.split,rsplit
numpy.core.defchararray.splitlines ( \(a\), keepends=None)
For each element in \(a\), return a list of the lines in the element, breaking at line boundaries.
Calls str.splitlines element-wise.

\section*{Parameters}
a : array_like of str or unicode
keepends : bool, optional
Line breaks are not included in the resulting list unless keepends is given and true.

\section*{Returns}
out : ndarray
Array of list objects

\section*{See Also:}
```

    str.splitlines
    numpy.core.defchararray.strip (a, chars=None)

```

For each element in \(a\), return a copy with the leading and trailing characters removed.
Calls str.rstrip element-wise.

\section*{Parameters}
a : array-like of str or unicode
chars : str or unicode, optional
The chars argument is a string specifying the set of characters to be removed. If omitted or None, the chars argument defaults to removing whitespace. The chars argument is not a prefix or suffix; rather, all combinations of its values are stripped.

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.strip

\section*{Examples}
```

>>> c = np.array(['aAaAaA', ' aA ', 'abBABba'])
>>> c
array(['aAaAaA', ' aA ', 'abBABba'],
dtype='|S7')
>>> np.char.strip(c)
array(['aAaAaA', 'aA', 'abBABba'],
dtype='|S7')
>>> np.char.strip(c, 'a') \# 'a' unstripped from c[I] because whitespace leads
array(['AaAaA', ' aA ', 'bBABb'],
dtype='|S7')
>>> np.char.strip(c, 'A') \# 'A' unstripped from c[I] because (unprinted) ws trails
array(['aAaAa', ' aA ', 'abBABba'],
dtype='|S7')

```
numpy.core.defchararray.swapcase (a)
For each element in \(a\), return a copy of the string with uppercase characters converted to lowercase and vice versa.

Calls str.swapcase element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array-like of str or unicode

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
```

str.swapcase

```

Examples
```

>>> c=np.array(['a1B C','1b Ca','b Ca1','cA1b'],'S5'); C
array(['a1B c', '1b Ca', 'b Ca1', 'cA1b'],
dtype='|S5')
>>> np.char.swapcase(c)
array(['A1b C', '1B CA', 'B CA1', 'Ca1B'],
dtype='|S5')

```
numpy.core.defchararray.title (a)

For each element in \(a\), return a titlecased version of the string: words start with uppercase characters, all remaining cased characters are lowercase.

Calls str.title element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array-like of str or unicode

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.title

\section*{Examples}
```

>>> c=np.array(['a1b c','1b ca','b ca1','ca1b'],'S5'); c
array(['a1b c', '1b ca', 'b ca1', 'calb'],
dtype='|S5')
>>> np.char.title(c)
array(['A1B C', '1B Ca', 'B Ca1', 'Ca1B'],
dtype='|S5')

```
numpy. core.defchararray.translate (a, table, deletechars=None)

For each element in \(a\), return a copy of the string where all characters occurring in the optional argument deletechars are removed, and the remaining characters have been mapped through the given translation table.

Calls str.translate element-wise.

\section*{Parameters}
a : array-like of str or unicode
table : str of length 256
deletechars : str

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.translate
numpy.core.defchararray.upper ( \(a\) )
Return an array with the elements of \(a\) converted to uppercase.
Calls str.upper element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array-like of str or unicode

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.upper
Examples
```

>>> c = np.array(['a1b c', '1bca', 'bca1']); c
array(['alb c', '1bca', 'bca1'],
dtype='|S5')
>>> np.char.upper(c)
array(['A1B C', '1BCA', 'BCA1'],
dtype='|S5')

```
numpy.core.defchararray.zfill (a, width)

Return the numeric string left-filled with zeros in a string of length width.
Calls str.zfill element-wise.

\section*{Parameters}
a : array-like of str or unicode
width : int

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.zfill

\subsection*{3.31.2 Comparison}

Unlike the standard numpy comparison operators, the ones in the char module strip trailing whitespace characters before performing the comparison.
\begin{tabular}{ll}
\hline equal(x1, x2) & Return (x1==x2) element-wise. \\
not_equal(x1, x2) & Return \((x 1!=x 2)\) element-wise. \\
greater_equal(x1, x2) & Return \((x 1>=x 2)\) element-wise. \\
less_equal(x1, x2) & Return \((x 1<=x 2)\) element-wise. \\
greater(x1, x2) & Return \((x 1>x 2)\) element-wise. \\
less(x1, x2) & Return \((x 1<x 2)\) element-wise. \\
\hline
\end{tabular}
numpy. core.defchararray.equal ( \(x 1, x 2\) )
Return (x1 == x2) element-wise.
Unlike numpy . equal, this comparison is performed by first stripping whitespace characters from the end of the string. This behavior is provided for backward-compatibility with numarray.

\section*{Parameters}
\(\mathbf{x 1}, \mathbf{x 2}\) : array_like of str or unicode
Input arrays of the same shape.

\section*{Returns} out : \{ndarray, bool\}

Output array of bools, or a single bool if x 1 and x 2 are scalars.
See Also:
not_equal, greater_equal, less_equal, greater, less
numpy.core.defchararray.not_equal ( \(x 1, x 2\) )
Return (x1 != x2) element-wise.
Unlike numpy. not_equal, this comparison is performed by first stripping whitespace characters from the end of the string. This behavior is provided for backward-compatibility with numarray.

\section*{Parameters}
\(\mathbf{x 1}, \mathbf{x} 2\) : array_like of str or unicode
Input arrays of the same shape.

\section*{Returns}
out : \{ndarray, bool\}
Output array of bools, or a single bool if x 1 and x 2 are scalars.

\section*{See Also:}
equal, greater_equal, less_equal, greater, less
```

numpy.core.defchararray.greater_equal (x1, x2)

```

Return (x1 >= x2) element-wise.
Unlike numpy.greater_equal, this comparison is performed by first stripping whitespace characters from the end of the string. This behavior is provided for backward-compatibility with numarray.

\section*{Parameters}
\(\mathbf{x 1}, \mathbf{x} \mathbf{2}\) : array_like of str or unicode
Input arrays of the same shape.

\section*{Returns}
out : \{ndarray, bool\}
Output array of bools, or a single bool if x 1 and x 2 are scalars.

\section*{See Also:}
equal, not_equal, less_equal, greater, less
numpy. core.defchararray.less_equal \((x 1, x 2)\)
Return ( \(\mathrm{x} 1<=\mathrm{x} 2\) ) element-wise.
Unlike numpy. less_equal, this comparison is performed by first stripping whitespace characters from the end of the string. This behavior is provided for backward-compatibility with numarray.

\section*{Parameters}
\(\mathbf{x 1}, \mathbf{x} 2\) : array_like of str or unicode
Input arrays of the same shape.

\section*{Returns}
out : \{ndarray, bool\}
Output array of bools, or a single bool if x 1 and x 2 are scalars.

\section*{See Also:}
equal, not_equal, greater_equal, greater, less
numpy. core.defchararray.greater ( \(x 1, x 2\) )
Return ( \(\mathrm{x} 1>\mathrm{x} 2\) ) element-wise.
Unlike numpy . greater, this comparison is performed by first stripping whitespace characters from the end of the string. This behavior is provided for backward-compatibility with numarray.

\section*{Parameters}
\(\mathbf{x 1}, \mathbf{x} 2\) : array_like of str or unicode
Input arrays of the same shape.

\section*{Returns}
out : \{ndarray, bool\}
Output array of bools, or a single bool if x 1 and x 2 are scalars.
See Also:
equal, not_equal, greater_equal, less_equal, less
numpy. core. defchararray.less ( \(x 1, x 2\) )
Return (x1 < x2) element-wise.
Unlike numpy.greater, this comparison is performed by first stripping whitespace characters from the end of the string. This behavior is provided for backward-compatibility with numarray.

\section*{Parameters}
\(\mathbf{x 1}, \mathbf{x} 2\) : array_like of str or unicode
Input arrays of the same shape.

\section*{Returns}
out : \{ndarray, bool \(\}\)
Output array of bools, or a single bool if x 1 and x 2 are scalars.

\section*{See Also:}
equal, not_equal, greater_equal, less_equal, greater

\subsection*{3.31.3 String information}
\begin{tabular}{|c|c|}
\hline count (a, sub[, start, end]) & Returns an array with the number of non-overlapping occurrences of substring sub in the range [start, end]. \\
\hline find(a, sub[, start, end]) & For each element, return the lowest index in the string where substring sub is found. \\
\hline index(a, sub[, start, end]) & Like find, but raises ValueError when the substring is not found. \\
\hline isalpha(a) & Returns true for each element if all characters in the string are alphabetic and there is at least one character, false otherwise. \\
\hline isdecimal(a) & For each element in \(a\), return True if there are only decimal \\
\hline isdigit(a) & Returns true for each element if all characters in the string are digits and there is at least one character, false otherwise. \\
\hline islower(a) & Returns true for each element if all cased characters in the string are lowercase and there is at least one cased character, false otherwise. \\
\hline isnumeric(a) & For each element in \(a\), return True if there are only numeric \\
\hline isspace(a) & Returns true for each element if there are only whitespace characters in the string and there is at least one character, false otherwise. \\
\hline istitle(a) & Returns true for each element if the element is a titlecased string and there is at least one character, false otherwise. \\
\hline isupper(a) & Returns true for each element if all cased characters in the string are uppercase and there is at least one character, false otherwise. \\
\hline rfind(a, sub[, start, end]) & For each element in \(a\), return the highest index in the string where substring sub is found, such that sub is contained within [start, end]. \\
\hline rindex(a, sub[, start, end]) & Like rfind, but raises ValueError when the substring sub is \\
\hline startswith(a, prefix[, start, end]) & Returns a boolean array which is True where the string element \\
\hline
\end{tabular}
```

numpy.core.defchararray.count ( a, sub, start=0, end=None)

```

Returns an array with the number of non-overlapping occurrences of substring sub in the range [start, end].
Calls str.count element-wise.

\section*{Parameters}
a : array_like of str or unicode
sub: str or unicode
The substring to search for.
start, end : int, optional
Optional arguments start and end are interpreted as slice notation to specify the range in which to count.

\section*{Returns}
out : ndarray
Output array of ints.

\section*{See Also:}
str.count
Examples
```

>>> c = np.array(['aAaAaA', ' aA ', 'abBABba'])
>>> C
array(['aAaAaA', ' aA ', 'abBABba'],

```
```

    dtype='|S7')
    >>> np.char.count(c, 'A')
array([3, 1, 1])
>>> np.char.count(c, 'aA')
array([3, 1, 0])
>>> np.char.count(c, 'A', start=1, end=4)
array([2, 1, 1])
>>> np.char.count(c, 'A', start=1, end=3)
array([1, 0, 0])
numpy.core.defchararray.find (a, sub, start=0, end=None)

```

For each element, return the lowest index in the string where substring sub is found.
Calls str.find element-wise.
For each element, return the lowest index in the string where substring sub is found, such that sub is contained in the range [start, end].

\section*{Parameters}
a : array_like of str or unicode
sub : str or unicode
start, end : int, optional
Optional arguments start and end are interpreted as in slice notation.

\section*{Returns}
out : ndarray or int
Output array of ints. Returns -1 if sub is not found.
See Also:
```

    str.find
    ```
numpy. core.defchararray.index ( \(a, s u b\), \(s t a r t=0\), end \(=\) None)

Like find, but raises ValueError when the substring is not found.
Calls strindex element-wise.

\section*{Parameters}
\(\mathbf{a}\) : array_like of str or unicode
sub : str or unicode
start, end : int, optional

\section*{Returns}
out : ndarray
Output array of ints. Returns -1 if \(s u b\) is not found.

\section*{See Also:}
find, str.find
numpy.core.defchararray.isalpha (a)
Returns true for each element if all characters in the string are alphabetic and there is at least one character, false otherwise.
Calls str.isalpha element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of bools

\section*{See Also:}
str.isalpha
numpy. core. defchararray.isdecimal (a)
For each element in \(a\), return True if there are only decimal characters in the element.
Calls unicode.isdecimal element-wise.
Decimal characters include digit characters, and all characters that that can be used to form decimal-radix numbers, e.g. U+0660, ARABIC-INDIC DIGIT ZERO.

\section*{Parameters}
a : array-like of unicode

\section*{Returns}
out : ndarray
Array of booleans

\section*{See Also:}
unicode.isdecimal
numpy.core.defchararray.isdigit (a)
Returns true for each element if all characters in the string are digits and there is at least one character, false otherwise.

Calls strisdigit element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of bools

\section*{See Also:}
str.isdigit
numpy. core. defchararray.islower (a)
Returns true for each element if all cased characters in the string are lowercase and there is at least one cased character, false otherwise.

Calls strislower element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of bools

\section*{See Also:}
str.islower
numpy. core. defchararray.isnumeric (a)
For each element in \(a\), return True if there are only numeric characters in the element.
Calls unicode.isnumeric element-wise.
Numeric characters include digit characters, and all characters that have the Unicode numeric value property, e.g. U+2155, VULGAR FRACTION ONE FIFTH.

\section*{Parameters}
a : array-like of unicode

\section*{Returns}
out : ndarray
Array of booleans
See Also:
unicode.isnumeric
numpy. core. defchararray.isspace (a)
Returns true for each element if there are only whitespace characters in the string and there is at least one character, false otherwise.
Calls strisspace element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of bools

\section*{See Also:}
str.isspace
numpy.core.defchararray.istitle (a)
Returns true for each element if the element is a titlecased string and there is at least one character, false otherwise.

Call stristitle element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of bools
See Also:
str.istitle
numpy.core.defchararray.isupper (a)
Returns true for each element if all cased characters in the string are uppercase and there is at least one character, false otherwise.

Call strisupper element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of bools

\section*{See Also:}
str.isupper
numpy.core.defchararray.rfind ( \(a\), sub, start=0, end=None)
For each element in \(a\), return the highest index in the string where substring sub is found, such that sub is contained within [start, end].
Calls str.rfind element-wise.

\section*{Parameters}
a : array-like of str or unicode
sub : str or unicode
start, end : int, optional
Optional arguments start and end are interpreted as in slice notation.

\section*{Returns}
out : ndarray
Output array of ints. Return -1 on failure.

\section*{See Also:}
str.rfind
numpy.core.defchararray.rindex ( \(a\), sub, start \(=0\), end=None)
Like rfind, but raises ValueError when the substring sub is not found.
Calls str.rindex element-wise.

\section*{Parameters}
a : array-like of str or unicode
sub : str or unicode
start, end : int, optional

\section*{Returns}
out : ndarray
Output array of ints.

\section*{See Also:}
rfind, str.rindex
numpy.core.defchararray.startswith ( \(a\), prefix, start=0, end=None)
Returns a boolean array which is True where the string element in \(a\) starts with prefix, otherwise False.
Calls str.startswith element-wise.

\section*{Parameters}
a : array_like of str or unicode
suffix : str
start, end : int, optional
With optional start, test beginning at that position. With optional end, stop comparing at that position.

\section*{Returns}
out : ndarray
Array of booleans

\section*{See Also:}
str.startswith

\subsection*{3.31.4 Convenience class}

> chararray Provides a convenient view on arrays of string and unicode values.
class numpy. core. defchararray.chararray
Provides a convenient view on arrays of string and unicode values.
Note: The chararray class exists for backwards compatibility with Numarray, it is not recommended for new development. Starting from numpy 1.4, if one needs arrays of strings, it is recommended to use arrays of dtype object_, string_ or unicode_, and use the free functions in the numpy. char module for fast vectorized string operations.

Versus a regular Numpy array of type str or unicode, this class adds the following functionality:
1.values automatically have whitespace removed from the end when indexed
2.comparison operators automatically remove whitespace from the end when comparing values
3.vectorized string operations are provided as methods (e.g. endswith) and infix operators (e.g. " + ", " \(\star\) ", " \% ")
chararrays should be created using numpy. char. array or numpy. char. asarray, rather than this constructor directly.

This constructor creates the array, using buffer (with offset and strides) if it is not None. If buffer is None, then constructs a new array with strides in "C order", unless both len (shape) >= 2 and order='Fortran', in which case strides is in "Fortran order".

\section*{Parameters}
shape : tuple
Shape of the array.
itemsize : int, optional
Length of each array element, in number of characters. Default is 1 .
unicode : bool, optional
Are the array elements of type unicode (True) or string (False). Default is False.
buffer : int, optional
Memory address of the start of the array data. Default is None, in which case a new array is created.
offset : int, optional
Fixed stride displacement from the beginning of an axis? Default is 0 . Needs to be \(>=0\).
strides : array_like of ints, optional
Strides for the array (see ndarray.strides for full description). Default is None.
order : \{'C', 'F'\}, optional
The order in which the array data is stored in memory: ' C ' -> "row major" order (the default), 'F' -> "column major" (Fortran) order.

\section*{Examples}
```

>>> charar = np.chararray((3, 3))
>>> charar[:] = 'a'
>>> charar
chararray([['a', 'a', 'a'],
['a', 'a', 'a'],
['a', 'a', 'a']],
dtype='|S1')
>>> charar = np.chararray(charar.shape, itemsize=5)
>>> charar[:] = 'abc'
>>> charar
chararray([['abc', 'abc', 'abc'],
['abc', 'abc', 'abc'],
['abc', 'abc', 'abc']],
dtype='|S5')

```

\section*{Methods}
```

astype
argsort
count(a, sub[, start, end])
decode(a[, encoding, errors]) Calls
dump
dumps
encode(a[, encoding, errors]) Calls
endswith(a, suffix[, start, end])
fill
find(a, sub[, start, end]) For each element, return the lowest index
flatten
getfield
index(a, sub[, start, end])
isalnum(a)
isalpha(a)
isdecimal(a)
isdigit(a)
islower(a)
isnumeric(a)
isspace(a)
istitle(a)
isupper(a)

```


Table 3.3 - continued from

numpy. core.defchararray.count ( \(a\), sub, start \(=0\), end \(=\) None)
Returns an array with the number of non-overlapping occurrences of substring sub in the range [start, end].

Calls str.count element-wise.

\section*{Parameters}
a : array_like of str or unicode
sub : str or unicode
The substring to search for.
start, end : int, optional
Optional arguments start and end are interpreted as slice notation to specify the range
in which to count.

\section*{Returns}
out : ndarray
Output array of ints.

\section*{See Also:}
str.count

\section*{Examples}
```

>>> c = np.array(['aAaAaA', ' aA ', 'abBABba'])
>>> c
array(['aAaAaA', ' aA ', 'abBABba'],
dtype='|S7')
>>> np.char.count(c, 'A')
array([3, 1, 1])
>>> np.char.count(c, 'aA')
array([3, 1, 0])
>>> np.char.count(c, 'A', start=1, end=4)
array([2, 1, 1])
>>> np.char.count(c, 'A', start=1, end=3)
array([1, 0, 0])

```
numpy. core.defchararray.decode ( \(a\), encoding=None, errors=None)
Calls str.decode element-wise.
The set of available codecs comes from the Python standard library, and may be extended at runtime. For more information, see the codecs module.

\section*{Parameters}
a : array_like of str or unicode
encoding : str, optional
The name of an encoding
errors : str, optional
Specifies how to handle encoding errors

\section*{Returns}
out : ndarray

\section*{See Also:}
str.decode

\section*{Notes}

The type of the result will depend on the encoding specified.

\section*{Examples}
```

>>> c = np.array(['aAaAaA', ' aA ', 'abBABba'])
>>> c
array(['aAaAaA', ' aA ', 'abBABba'],
dtype='|S7')
>>> np.char.encode(c, encoding=' cp037')
array(['\x81\xc1\x81\xc1\x81\xc1', '@@\x81\xc1@@',
'\x81\x82\xc2\xc1\xc2\x82\x81' ],
dtype='|S7')

```
numpy. core.defchararray.encode (a, encoding=None, errors=None)
Calls str.encode element-wise.
The set of available codecs comes from the Python standard library, and may be extended at runtime. For more information, see the codecs module.

\section*{Parameters}
\(\mathbf{a}\) : array_like of str or unicode
encoding : str, optional
The name of an encoding
errors : str, optional
Specifies how to handle encoding errors

\section*{Returns} out : ndarray

\section*{See Also:}
```

str.encode

```

\section*{Notes}

The type of the result will depend on the encoding specified.
numpy.core.defchararray.find ( \(a\), sub, start \(=0\), end \(=\) None)
For each element, return the lowest index in the string where substring sub is found.
Calls str.find element-wise.
For each element, return the lowest index in the string where substring sub is found, such that sub is contained in the range [start, end].

\section*{Parameters}
a : array_like of str or unicode
sub : str or unicode
start, end : int, optional
Optional arguments start and end are interpreted as in slice notation.

\section*{Returns}
out : ndarray or int
Output array of ints. Returns -1 if sub is not found.

\section*{See Also:}
str.find
numpy. core.defchararray.index ( \(a, s u b\), start \(=0\), end \(=\) None)
Like find, but raises ValueError when the substring is not found.
Calls strindex element-wise.

\section*{Parameters}
a : array_like of str or unicode
sub : str or unicode
start, end : int, optional

\section*{Returns}
out : ndarray
Output array of ints. Returns -1 if sub is not found.

\section*{See Also:}
find, str.find
numpy.core.defchararray.isalpha (a)
Returns true for each element if all characters in the string are alphabetic and there is at least one character, false otherwise.

Calls strisalpha element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of bools

\section*{See Also:}
str.isalpha
numpy.core.defchararray.isdecimal (a)
For each element in \(a\), return True if there are only decimal characters in the element.
Calls unicode isdecimal element-wise.
Decimal characters include digit characters, and all characters that that can be used to form decimal-radix numbers, e.g. U+0660, ARABIC-INDIC DIGIT ZERO.

\section*{Parameters}
a : array-like of unicode

\section*{Returns}
out : ndarray
Array of booleans

\section*{See Also:}
unicode.isdecimal
numpy.core.defchararray.isdigit (a)
Returns true for each element if all characters in the string are digits and there is at least one character, false otherwise.

Calls strisdigit element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of bools

\section*{See Also:}
str.isdigit
numpy. core.defchararray.islower (a)
Returns true for each element if all cased characters in the string are lowercase and there is at least one cased character, false otherwise.

Calls str.islower element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of bools

\section*{See Also:}
str.islower
numpy.core.defchararray.isnumeric (a)
For each element in \(a\), return True if there are only numeric characters in the element.
Calls unicode.isnumeric element-wise.
Numeric characters include digit characters, and all characters that have the Unicode numeric value property, e.g. U+2155, VULGAR FRACTION ONE FIFTH.

\section*{Parameters}
a : array-like of unicode

\section*{Returns}
out : ndarray
Array of booleans

\section*{See Also:}
unicode.isnumeric
numpy. core.defchararray.isspace (a)
Returns true for each element if there are only whitespace characters in the string and there is at least one character, false otherwise.
Calls strisspace element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of bools

\section*{See Also:}
str.isspace
numpy. core.defchararray.istitle (a)
Returns true for each element if the element is a titlecased string and there is at least one character, false otherwise.

\section*{Call str.istitle element-wise.}

For 8-bit strings, this method is locale-dependent.

\section*{Parameters} a : array_like of str or unicode

\section*{Returns} out : ndarray

Output array of bools

\section*{See Also:}
str.istitle
numpy. core.defchararray.isupper (a)
Returns true for each element if all cased characters in the string are uppercase and there is at least one character, false otherwise.

Call strisupper element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of bools
See Also:
str.isupper
numpy.core.defchararray.join (sep, seq)
Return a string which is the concatenation of the strings in the sequence seq.
Calls str.join element-wise.

\section*{Parameters}
sep : array_like of str or unicode
seq : array_like of str or unicode

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input types

\section*{See Also:}
str.join
numpy. core.defchararray.ljust (a, width, fillchar=' ')
Return an array with the elements of \(a\) left-justified in a string of length width.
Calls str.ljust element-wise.

\section*{Parameters}
a : array_like of str or unicode
width : int
The length of the resulting strings
fillchar : str or unicode, optional

The character to use for padding

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.ljust
numpy.core.defchararray.lower (a)
Return an array with the elements of \(a\) converted to lowercase.
Call str.lower element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array-like of str or unicode

\section*{Returns}
out : ndarray, str or unicode
Output array of str or unicode, depending on input type

\section*{See Also:}
str.lower
Examples
```

>>> c = np.array(['A1B C', '1BCA', 'BCA1']); c
array(['A1B C', '1BCA', 'BCA1'],
dtype='|S5')
>>> np.char.lower(c)
array(['a1b c', '1bca', 'bca1'],
dtype='|S5')
numpy.core.defchararray.lstrip (a,chars=None)

```

For each element in \(a\), return a copy with the leading characters removed.
Calls str:lstrip element-wise.

\section*{Parameters}
a : array-like of str or unicode
chars : str or unicode, optional
The chars argument is a string specifying the set of characters to be removed. If omitted or None, the chars argument defaults to removing whitespace. The chars argument is not a prefix; rather, all combinations of its values are stripped.

\section*{Returns}
out : ndarray, str or unicode
Output array of str or unicode, depending on input type

\section*{See Also:}
str.lstrip

\section*{Examples}
```

>>> c = np.array(['aAaAaA', ' aA ', 'abBABba'])
>>> c
array(['aAaAaA', , aA ', 'abBABba'],
dtype='|S7')
>>> np.char.lstrip(c, 'a') \# 'a' unstripped from c[I] because whitespace leading
array(['AaAaA', ' aA ', 'bBABba'],
dtype='|S7')
>>> np.char.lstrip(c, 'A') \# leaves c unchanged
array(['aAaAaA', ' aA ', 'abBABba'],
dtype='|S7')
>>> (np.char.lstrip(c, ' ') == np.char.lstrip(c, '')).all()
... \# XXX: is this a regression? this line now returns False
... \# np.char.lstrip(c,'') does not modify c at all.
True
>>> (np.char.lstrip(c, ' ') == np.char.lstrip(c, None)).all()
True

```
numpy. core.defchararray.replace ( \(a\), old, new, count=None)
For each element in \(a\), return a copy of the string with all occurrences of substring old replaced by new.
Calls str.replace element-wise.

\section*{Parameters}
a : array-like of str or unicode
old, new : str or unicode
count : int, optional
If the optional argument count is given, only the first count occurrences are replaced.

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.replace
numpy.core.defchararray.rfind ( \(a\), sub, start \(=0\), end=None)
For each element in \(a\), return the highest index in the string where substring sub is found, such that sub is contained within [start, end].

Calls str.rfind element-wise.

\section*{Parameters}
a : array-like of str or unicode
sub : str or unicode
start, end : int, optional
Optional arguments start and end are interpreted as in slice notation.

\section*{Returns \\ out : ndarray}

Output array of ints. Return -1 on failure.

\section*{See Also:}
str.rfind
numpy.core.defchararray.rindex ( \(a\), sub, start=0, end=None)
Like rfind, but raises ValueError when the substring sub is not found.
Calls str.rindex element-wise.

\section*{Parameters}
a : array-like of str or unicode
sub : str or unicode
start, end : int, optional

\section*{Returns}
out : ndarray
Output array of ints.

\section*{See Also:}
rfind, str.rindex
numpy. core.defchararray.rjust ( \(a\), width, fillchar=' ')
Return an array with the elements of \(a\) right-justified in a string of length width.
Calls str.rjust element-wise.

\section*{Parameters}
a : array_like of str or unicode
width : int
The length of the resulting strings
fillchar : str or unicode, optional
The character to use for padding

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.rjust
numpy.core.defchararray.rsplit (a, sep=None, maxsplit=None)
For each element in \(a\), return a list of the words in the string, using sep as the delimiter string.
Calls str.rsplit element-wise.
Except for splitting from the right, rsplit behaves like split.

\section*{Parameters}
a : array_like of str or unicode
sep : str or unicode, optional
If sep is not specified or None, any whitespace string is a separator.
maxsplit : int, optional
If maxsplit is given, at most maxsplit splits are done, the rightmost ones.

\section*{Returns}
out : ndarray
Array of list objects

\section*{See Also:}
str.rsplit, split
numpy. core.defchararray.rstrip (a, chars=None)
For each element in \(a\), return a copy with the trailing characters removed.
Calls str.rstrip element-wise.

\section*{Parameters}
a : array-like of str or unicode
chars : str or unicode, optional
The chars argument is a string specifying the set of characters to be removed. If omitted or None, the chars argument defaults to removing whitespace. The chars argument is not a suffix; rather, all combinations of its values are stripped.

\section*{Returns \\ out : ndarray}

Output array of str or unicode, depending on input type

\section*{See Also:}
str.rstrip
Examples
```

>>> c = np.array(['aAaAaA', 'abBABba'], dtype='S7'); c
array(['aAaAaA', 'abBABba'],
dtype=' | S7')
>>> np.char.rstrip(c, 'a')
array(['aAaAaA', 'abBABb'],
dtype=' | S7')
>>> np.char.rstrip(c, 'A')
array(['aAaAa', 'abBABba'],
dtype='|S7')
numpy.core.defchararray.split ( $a$, sep=None, maxsplit=None)

```

For each element in \(a\), return a list of the words in the string, using sep as the delimiter string.
Calls str.rsplit element-wise.

\section*{Parameters}
a : array_like of str or unicode
sep : str or unicode, optional
If sep is not specified or None, any whitespace string is a separator.
maxsplit : int, optional
If maxsplit is given, at most maxsplit splits are done.

\section*{Returns}
out : ndarray
Array of list objects

\section*{See Also:}
```

str.split,rsplit

```
numpy.core.defchararray.splitlines ( \(a\), keepends=None)
For each element in \(a\), return a list of the lines in the element, breaking at line boundaries.
Calls str.splitlines element-wise.

\section*{Parameters}
a : array_like of str or unicode
keepends : bool, optional
Line breaks are not included in the resulting list unless keepends is given and true.

\section*{Returns}
out : ndarray
Array of list objects
See Also:
str.splitlines
numpy. core.defchararray.startswith (a, prefix, start=0, end=None)
Returns a boolean array which is True where the string element in \(a\) starts with prefix, otherwise False.
Calls str.startswith element-wise.

\section*{Parameters}
a : array_like of str or unicode
suffix : str
start, end : int, optional
With optional start, test beginning at that position. With optional end, stop comparing at that position.

\section*{Returns}
out : ndarray
Array of booleans

\section*{See Also:}
str.startswith
numpy. core.defchararray.strip (a, chars=None)
For each element in \(a\), return a copy with the leading and trailing characters removed.
Calls str.rstrip element-wise.

\section*{Parameters}
a : array-like of str or unicode
chars : str or unicode, optional
The chars argument is a string specifying the set of characters to be removed. If omitted or None, the chars argument defaults to removing whitespace. The chars argument is not a prefix or suffix; rather, all combinations of its values are stripped.

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.strip

\section*{Examples}
```

>>> c = np.array(['aAaAaA', ' aA ', 'abBABba' ])
>>> C
array(['aAaAaA', ' aA ', 'abBABba'],
dtype=' | S7')
>>> np.char.strip(c)
array(['aAaAaA', 'aA', 'abBABba' ],
dtype=' | S7')
>>> np.char.strip(c, 'a') \# 'a' unstripped from c[l] because whitespace leads
array(['AaAaA', ' aA ', 'bBABb'],
dtype='|S7')
>>> np.char.strip(c, 'A') \# 'A' unstripped from c[l] because (unprinted) ws trails
array(['aAaAa', ' aA ', 'abBABba'],
dtype='|S7')

```
numpy. core.defchararray.swapcase (a)
For each element in \(a\), return a copy of the string with uppercase characters converted to lowercase and vice versa.

Calls str.swapcase element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array-like of str or unicode

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.swapcase

\section*{Examples}
```

>>> c=np.array(['a1B c','1b Ca','b Ca1','cA1b'],'S5'); c
array(['a1B c', '1b Ca', 'b Ca1', 'cA1b'],
dtype='|S5')
>>> np.char.swapcase(c)
array(['A1b C', '1B cA', 'B cA1', 'Ca1B'],
dtype='|S5')

```
numpy. core.defchararray.title (a)
For each element in \(a\), return a titlecased version of the string: words start with uppercase characters, all remaining cased characters are lowercase.

Calls str.title element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array-like of str or unicode

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
```

str.title

```

\section*{Examples}
```

>>> c=np.array(['a1b c','1b ca','b ca1','ca1b'],'S5'); c
array(['a1b c', '1b ca', 'b ca1', 'ca1b'],
dtype='|S5')
>>> np.char.title(c)
array(['A1B C', '1B Ca', 'B Ca1', 'Ca1B'],
dtype='|S5')

```
numpy. core.defchararray.translate ( \(a\), table, deletechars=None)
For each element in \(a\), return a copy of the string where all characters occurring in the optional argument deletechars are removed, and the remaining characters have been mapped through the given translation table.

Calls str.translate element-wise.

\section*{Parameters}
a : array-like of str or unicode
table : str of length 256
deletechars : str

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.translate
numpy.core.defchararray. upper (a)
Return an array with the elements of \(a\) converted to uppercase.
Calls strupper element-wise.
For 8-bit strings, this method is locale-dependent.

\section*{Parameters}
a : array-like of str or unicode

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
```

str.upper

```

\section*{Examples}
```

>>> c = np.array(['a1b c', '1bca', 'bca1']); c
array(['a1b c', '1bca', 'bca1'],
dtype='|S5')
>>> np.char.upper(c)
array(['A1B C', '1BCA', 'BCA1'],
dtype='|S5')
numpy.core.defchararray.zfill (a, width)

```

Return the numeric string left-filled with zeros in a string of length width.
Calls str.zfill element-wise.

\section*{Parameters}
a : array-like of str or unicode
width : int

\section*{Returns}
out : ndarray
Output array of str or unicode, depending on input type

\section*{See Also:}
str.zfill

\section*{PACKAGING (NUMPY.DISTUTILS)}

NumPy provides enhanced distutils functionality to make it easier to build and install sub-packages, auto-generate code, and extension modules that use Fortran-compiled libraries. To use features of NumPy distutils, use the setup command from numpy.distutils.core. A useful Configuration class is also provided in numpy. distutils.misc_util that can make it easier to construct keyword arguments to pass to the setup function (by passing the dictionary obtained from the todict() method of the class). More information is available in the NumPy Distutils Users Guide in <site-packages>/numpy / doc/DISTUTILS.txt.

\subsection*{4.1 Modules in numpy.distutils}

\subsection*{4.1.1 misc_util}
```

get_numpy_include_dirs()
dict_append(d, **kws)
appendpath(prefix, path)
allpath(name)
Convert a /-separated pathname to one using the OS's path separator.
dot_join(*args)
generate_config_py(targetGenerate config.py file containing system_info information used during building
the package.
get_cmd(cmdname[,
_cache])
terminal_has_colors()
red_text(s)
green_text(s)
yellow_text(s)
blue_text(s)
cyan_text(s)
cyg2win32(path)
all_strings(lst) Return True if all items in 1st are string objects.
has_£_sources(sources) Return True if sources contains Fortran files
has_cxx_sources(sources) Return True if sources contains C++ files
filter_sources(sources) Return four lists of filenames containing
get_dependencies(sources)
is_local_src_dir(directoryleturn true if directory is local directory.
get_ext_source_files(ext)
get_script_files(scripts)

```
numpy.distutils.misc_util.get_numpy_include_dirs()
```

numpy.distutils.misc_util.dict_append ( $d, * * k w s$ )
numpy.distutils.misc_util.appendpath (prefix, path)

```
numpy.distutils.misc_util.allpath (name)
    Convert a /-separated pathname to one using the OS's path separator.
numpy.distutils.misc_util.dot_join(*args)
numpy.distutils.misc_util.generate_config_py (target)
    Generate config.py file containing system_info information used during building the package.
    Usage:
        config['py_modules'].append((packagename, '__config_,',generate_config_py))
numpy.distutils.misc_util.get_cmd (cmdname,_cache=\{\})
numpy.distutils.misc_util.terminal_has_colors()
numpy.distutils.misc_util.red_text ( \(s\) )
numpy.distutils.misc_util.green_text ( \(s\) )
numpy.distutils.misc_util.yellow_text (s)
numpy.distutils.misc_util.blue_text (s)
numpy.distutils.misc_util.cyan_text (s)
numpy.distutils.misc_util.cyg2win32 (path)
numpy.distutils.misc_util.all_strings (lst)
    Return True if all items in 1st are string objects.
numpy.distutils.misc_util.has_f_sources (sources)
    Return True if sources contains Fortran files
numpy.distutils.misc_util.has_cxx_sources (sources)
    Return True if sources contains C++ files
numpy.distutils.misc_util.filter_sources (sources)
    Return four lists of filenames containing C, C++, Fortran, and Fortran 90 module sources, respectively.
numpy.distutils.misc_util.get_dependencies (sources)
numpy.distutils.misc_util.is_local_src_dir(directory)
    Return true if directory is local directory.
numpy.distutils.misc_util.get_ext_source_files (ext)
```

numpy.distutils.misc_util.get_script_files(scripts)

```
class numpy.distutils.misc_util.Configuration(package_name=None, parent_name=None,
                                    top_path=None, package_path=None, **at-
                                    trs)

Construct a configuration instance for the given package name. If parent_name is not None, then construct the package as a sub-package of the parent_name package. If top_path and package_path are None then they are assumed equal to the path of the file this instance was created in. The setup.py files in the numpy distribution are good examples of how to use the Configuration instance.
```

todict()

```

Return a dictionary compatible with the keyword arguments of distutils setup function.
Examples
>>> setup(**config.todict())
get_distribution()
Return the distutils distribution object for self.
get_subpackage (subpackage_name, subpackage_path=None, parent_name=None, caller_level=1) Return list of subpackage configurations.

Parameters
subpackage_name: str,None :
Name of the subpackage to get the configuration. '*' in subpackage_name is handled as a wildcard.
subpackage_path: str :
If None, then the path is assumed to be the local path plus the subpackage_name. If a setup.py file is not found in the subpackage_path, then a default configuration is used.

\section*{parent_name: str :}

Parent name.
add_subpackage (subpackage_name, subpackage_path=None, standalone=False)
Add a sub-package to the current Configuration instance.
This is useful in a setup.py script for adding sub-packages to a package.

\section*{Parameters}
subpackage_name: str :
name of the subpackage
subpackage_path: str :
if given, the subpackage path such as the subpackage is in subpackage_path / subpackage_name. If None,the subpackage is assumed to be located in the local path / subpackage_name.
standalone: bool :
add_data_files (*files)
Add data files to configuration data_files.

\section*{Parameters}
files: sequence :
Argument(s) can be either
- 2-sequence (<datadir prefix \(>,<\) path to data file(s) \(>\) )
- paths to data files where python datadir prefix defaults to package dir.

\section*{Notes}

The form of each element of the files sequence is very flexible allowing many combinations of where to get the files from the package and where they should ultimately be installed on the system. The most basic usage is for an element of the files argument sequence to be a simple filename. This will cause that file from the local path to be installed to the installation path of the self.name package (package path). The file argument can also be a relative path in which case the entire relative path will be installed into the package directory. Finally, the file can be an absolute path name in which case the file will be found at the absolute path name but installed to the package path.
This basic behavior can be augmented by passing a 2-tuple in as the file argument. The first element of the tuple should specify the relative path (under the package install directory) where the remaining sequence of files should be installed to (it has nothing to do with the file-names in the source distribution). The second element of the tuple is the sequence of files that should be installed. The files in this sequence can be filenames, relative paths, or absolute paths. For absolute paths the file will be installed in the top-level package installation directory (regardless of the first argument). Filenames and relative path names will be installed in the package install directory under the path name given as the first element of the tuple.

Rules for installation paths:
\[
\begin{aligned}
& \text { 1.file.txt -> (., file.txt)-> parent/file.txt } \\
& \text { 2.foo/file.txt }->\text { (foo, foo/file.txt) }->\text { parent/foo/file.txt } \\
& \text { 3./foo/bar/file.txt -> (., /foo/bar/file.txt) }->\text { parent/file.txt } \\
& \text { 4.*.txt -> parent/a.txt, parent/b.txt } \\
& \text { 5.foo/*.txt -> parent/foo/a.txt, parent/foo/b.txt } \\
& \text { 6./.txt -> (, */.txt) -> parent/c/a.txt, parent/d/b.txt } \\
& \text { 7.(sun, file.txt) -> parent/sun/file.txt } \\
& \text { 8.(sun, bar/file.txt) -> parent/sun/file.txt } \\
& \text { 9.(sun, /foo/bar/file.txt) -> parent/sun/file.txt } \\
& \text { 10.(sun, *.txt) -> parent/sun/a.txt, parent/sun/b.txt } \\
& \text { 11.(sun, bar/*.txt) -> parent/sun/a.txt, parent/sun/b.txt } \\
& \text { 12.(sun/, */.txt) -> parent/sun/c/a.txt, parent/d/b.txt }
\end{aligned}
\]

An additional feature is that the path to a data-file can actually be a function that takes no arguments and returns the actual path(s) to the data-files. This is useful when the data files are generated while building the package.

\section*{Examples}

Add files to the list of data_files to be included with the package.
```

>>> self.add_data_files('foo.dat',
... ('fun', ['gun.dat', 'nun/pun.dat', '/tmp/sun.dat']),
... 'bar/cat.dat',
... '/full/path/to/can.dat')

```
will install these data files to:
```

<package install directory>/
foo.dat
fun/
gun.dat
nun/
pun.dat
sun.dat
bar/
car.dat
can.dat

```
where <package install directory> is the package (or sub-package) directory such as '/usr/lib/python2.4/site-packages/mypackage' ('C: Python2.4 Lib site-packages mypackage') or '/usr/lib/python2.4/site- packages/mypackage/mysubpackage' ('C: Python2.4 Lib site-packages mypackage mysubpackage').

\section*{add_data_dir (data_path)}

Recursively add files under data_path to data_files list.
Recursively add files under data_path to the list of data_files to be installed (and distributed). The data_path can be either a relative path-name, or an absolute path-name, or a 2-tuple where the first argument shows where in the install directory the data directory should be installed to.

\section*{Parameters}

\section*{data_path: seq,str :}

Argument can be either
- 2-sequence (<datadir suffix>,<path to data directory>)
- path to data directory where python datadir suffix defaults to package dir.

\section*{Notes}

\section*{Rules for installation paths:}
foo/bar \(\rightarrow\) (foo/bar, foo/bar) -> parent/foo/bar (gun, foo/bar) -> parent/gun foo/* -> (foo/a, foo/a), (foo/b, foo/b) -> parent/foo/a, parent/foo/b (gun, foo/) -> (gun, foo/a), (gun, foo/b) -> gun (gun/, foo/) -> parent/gun/a, parent/gun/b/foo/bar -> (bar, /foo/bar) -> parent/bar (gun, /foo/bar) -> parent/gun (fun//gun/*, sun/foo/bar) -> parent/fun/foo/gun/bar

\section*{Examples}

For example suppose the source directory contains fun/foo.dat and fun/bar/car.dat:
```

>>> self.add_data_dir('fun')
>>> self.add__data_dir(('sun', 'fun'))
>>> self.add__data_dir(('gun', '/full/path/to/fun'))

```

Will install data-files to the locations:
```

<package install directory>/
fun/
foo.dat
bar/
car.dat
sun/
foo.dat
bar/
car.dat
gun/

```
```

foo.dat

```
car.dat

\section*{add_include_dirs (*paths)}

Add paths to configuration include directories.
Add the given sequence of paths to the beginning of the include_dirs list. This list will be visible to all extension modules of the current package.
add_headers (*files)
Add installable headers to configuration.
Add the given sequence of files to the beginning of the headers list. By default, headers will be installed under <python- include \(>/<\) self.name.replace( \({ }^{\prime},,^{\prime}, /\) ') \(>/\) directory. If an item of files is a tuple, then its first argument specifies the actual installation location relative to the <python-include> path.

Parameters
files: str, seq :
Argument(s) can be either:
- 2-sequence (<includedir suffix>,<path to header file(s)>)
- path(s) to header file(s) where python includedir suffix will default to package name.
```

add_extension (name, sources, **kw)

```

Add extension to configuration.
Create and add an Extension instance to the ext_modules list. This method also takes the following optional keyword arguments that are passed on to the Extension constructor.

\section*{Parameters}
name: str :
name of the extension
sources: seq :
list of the sources. The list of sources may contain functions (called source generators) which must take an extension instance and a build directory as inputs and return a source file or list of source files or None. If None is returned then no sources are generated. If the Extension instance has no sources after processing all source generators, then no extension module is built.

\section*{include_dirs: :}
define_macros: :
undef_macros: :
library_dirs: :

\section*{libraries: :}
runtime_library_dirs: :
extra_objects: :
extra_compile_args: :
extra_link_args: :
export_symbols: :
swig_opts: :

\section*{depends: :}

The depends list contains paths to files or directories that the sources of the extension module depend on. If any path in the depends list is newer than the extension module, then the module will be rebuilt.

\section*{language: :}
f2py_options: :
module_dirs: :
extra_info: dict,list :
dict or list of dict of keywords to be appended to keywords.

\section*{Notes}

The self.paths(...) method is applied to all lists that may contain paths.
add_library (name, sources, **build_info)
Add library to configuration.

\section*{Parameters}
name : str
Name of the extension.
sources : sequence
List of the sources. The list of sources may contain functions (called source generators) which must take an extension instance and a build directory as inputs and return a source file or list of source files or None. If None is returned then no sources are generated. If the Extension instance has no sources after processing all source generators, then no extension module is built.
build_info : dict, optional
The following keys are allowed:
- depends
- macros
- include_dirs
- extra_compiler_args
- f2py_options
- language
add_scripts (*files)
Add scripts to configuration.
Add the sequence of files to the beginning of the scripts list. Scripts will be installed under the \(<\) prefix \(>/\) bin/ directory.
add_installed_library (name, sources, install_dir, build_info=None)
Similar to add_library, but the specified library is installed.
Most C libraries used with distutils are only used to build python extensions, but libraries built through this method will be installed so that they can be reused by third-party packages.

\section*{Parameters}
name : str

Name of the installed library.
sources : sequence
List of the library's source files. See add_library for details.
install_dir : str
Path to install the library, relative to the current sub-package.
build_info : dict, optional
The following keys are allowed:
- depends
- macros
- include_dirs
- extra_compiler_args
- f2py_options
- language

\section*{Returns}

None :

\section*{See Also:}
add_library, add_npy_pkg_config, get_info

\section*{Notes}

The best way to encode the options required to link against the specified C libraries is to use a "libname.ini" file, and use get_info to retrieve the required options (see add_npy_pkg_config for more information).
add_npy_pkg_config (template, install_dir, subst_dict=None)
Generate and install a npy-pkg config file from a template.
The config file generated from template is installed in the given install directory, using subst_dict for variable substitution.

\section*{Parameters \\ template: str}

The path of the template, relatively to the current package path.

\section*{install_dir : str}

Where to install the npy-pkg config file, relatively to the current package path.
subst_dict : dict, optional
If given, any string of the form @key@ will be replaced by subst_dict [key] in the template file when installed. The install prefix is always available through the variable @prefix@, since the install prefix is not easy to get reliably from setup.py.

\section*{See Also:}
add_installed_library, get_info
Notes
This works for both standard installs and in-place builds, i.e. the @prefix@ refer to the source directory for in-place builds.

\section*{Examples}
```

config.add_npy_pkg_config('foo.ini.in', 'lib', {'foo': bar})

```

Assuming the foo.ini.in file has the following content:
```

[meta]
Name=@foo@
Version=1.0
Description=dummy description
[default]
Cflags=-I@prefix@/include
Libs=

```

The generated file will have the following content:
```

[meta]
Name=bar
Version=1.0
Description=dummy description
[default]
Cflags=-Iprefix_dir/include
Libs=

```
and will be installed as foo.ini in the 'lib' subpath.
paths (*paths, **kws)
Apply glob to paths and prepend local_path if needed.
Applies glob.glob(...) to each path in the sequence (if needed) and pre-pends the local_path if needed. Because this is called on all source lists, this allows wildcard characters to be specified in lists of sources for extension modules and libraries and scripts and allows path-names be relative to the source directory.
```

get_config_cmd()

```

Returns the numpy.distutils config command instance.
```

get_build_temp_dir()

```

Return a path to a temporary directory where temporary files should be placed.

\section*{have_f77c ()}

Check for availability of Fortran 77 compiler.
Use it inside source generating function to ensure that setup distribution instance has been initialized.

\section*{Notes}

True if a Fortran 77 compiler is available (because a simple Fortran 77 code was able to be compiled successfully).
have_f90c()
Check for availability of Fortran 90 compiler.
Use it inside source generating function to ensure that setup distribution instance has been initialized.

\section*{Notes}

True if a Fortran 90 compiler is available (because a simple Fortran 90 code was able to be compiled successfully)
get_version (version_file=None, version_variable=None)
Try to get version string of a package.

Return a version string of the current package or None if the version information could not be detected.

\section*{Notes}

This method scans files named __version__.py, <packagename>_version.py, version.py, and __svn_version__.py for string variables version, __version__, and <packagename>_version, until a version number is found.
make_svn_version_py (delete=True)
Appends a data function to the data_files list that will generate __svn_version__.py file to the current package directory.

Generate package __svn_version_.py file from SVN revision number, it will be removed after python exits but will be available when sdist, etc commands are executed.

\section*{Notes}

If __svn_version__.py existed before, nothing is done.
This is intended for working with source directories that are in an SVN repository.
make_config_py (name='__config_-')
Generate package __config__.py file containing system_info information used during building the package.
This file is installed to the package installation directory.
get_info (*names)
Get resources information.
Return information (from system_info.get_info) for all of the names in the argument list in a single dictionary.

\subsection*{4.1.2 Other modules}
```

system_info.get_info(name[, notfound_action]) notfound_action:
system_info.get_standard_file(fname) Returns a list of files named 'fname' from
cpuinfo.cpu
log.set_verbosity(v[, force])
exec_command exec_command
numpy.distutils.system_info.get_info(name, notfound_action=0)

```

\section*{notfound_action:}

0 - do nothing 1 - display warning message 2 - raise error
```

numpy.distutils.system_info.get_standard_file(fname)

```

Returns a list of files named 'fname' from 1) System-wide directory (directory-location of this module) 2) Users HOME directory (os.environ['HOME']) 3) Local directory
```

numpy.distutils.cpuinfo.cpu

```
numpy.distutils.log.set_verbosity (v,force=False)
exec_command

Implements exec_command function that is (almost) equivalent to commands.getstatusoutput function but on NT, DOS systems the returned status is actually correct (though, the returned status values may be different by a factor). In addition, exec_command takes keyword arguments for (re-)defining environment variables.

\section*{Provides functions:}
exec_command - execute command in a specified directory and in the modified environment.
find_executable - locate a command using info from environment variable PATH. Equivalent to posix which command.

Author: Pearu Peterson <pearu@cens.ioc.ee> Created: 11 January 2003
Requires: Python 2.x

\section*{Succesfully tested on:}
os.name | sys.platform | comments ——_-_ -_——— posix | linux2 | Debian (sid) Linux, Python 2.1.3+, 2.2.3+, 2.3.3

PyCrust 0.9.3, Idle 1.0.2
posix I linux2 I Red Hat 9 Linux, Python 2.1.3, 2.2.2, 2.3.2 posix I sunos5 I SunOS 5.9, Python 2.2, 2.3.2 posix I darwin I Darwin 7.2.0, Python 2.3 nt I win32 I Windows Me

Python 2.3(EE), Idle 1.0, PyCrust 0.7.2 Python 2.1.1 Idle 0.8
nt I win32 I Windows 98, Python 2.1.1. Idle 0.8 nt I win32 I Cygwin 98-4.10, Python 2.1.1(MSC) - echo tests
fail i.e. redefining environment variables may not work. FIXED: don't use cygwin echo! Comment: also \(\mathrm{cmd} / \mathrm{c}\) echo will not work but redefining environment variables do work.
posix I cygwin I Cygwin 98-4.10, Python 2.3.3(cygming special) nt I win32 I Windows XP, Python 2.3.3
Known bugs: - Tests, that send messages to stderr, fail when executed from MSYS prompt
because the messages are lost at some point.

\section*{Functions}
```

exec_command(command, **env[, execute_in,...]) Return (status,output) of executed command.
find_executable(exe[, path,_cache]) Return full path of a executable or None.
get_exception()
get_pythonexe()
is_sequence(seq)
make_temp_file([suffix, prefix, text])
open_latin1(filename[, mode])
quote_arg(arg)
splitcmdline(line)
temp_file_name()
test(**kws)
test_cl(**kws)
test_execute_in(**kws)
test_nt(**kws)
test_posix(**kws)
test_svn(**kws)

```

\subsection*{4.2 Building Installable C libraries}

Conventional C libraries (installed through add_library) are not installed, and are just used during the build (they are statically linked). An installable C library is a pure C library, which does not depend on the python C runtime, and is installed such that it may be used by third-party packages. To build and install the C library, you just use the method add_installed_library instead of add_library, which takes the same arguments except for an additional install_dir argument:
>>> config.add_installed_library('foo', sources=['foo.c'], install_dir='lib')

\subsection*{4.2.1 npy-pkg-config files}

To make the necessary build options available to third parties, you could use the npy-pkg-config mechanism implemented in numpy. distutils. This mechanism is based on a ini file which contains all the options. A .ini file is very similar to .pc files as used by the pkg-config unix utility:
```

[meta]
Name: foo
Version: 1.0
Description: foo library
[variables]
prefix = /home/user/local
libdir = \${prefix}/lib
includedir = ${prefix}/include
[default]
cflags = -I${includedir}
libs = -L\${libdir} -lfoo

```

Generally, the file needs to be generated during the build, since it needs some information known at build time only (e.g. prefix). This is mostly automatic if one uses the Configuration method add_npy_pkg_config. Assuming we have a template file foo.ini.in as follows:
```

[meta]
Name: foo
Version: @version@
Description: foo library
[variables]
prefix = @prefix@
libdir = \${prefix}/lib
includedir = ${prefix}/include
[default]
cflags = -I${includedir}
libs = -L\${libdir} -lfoo

```
and the following code in setup.py:
```

>>> config.add_installed_library('foo', sources=['foo.c'], install_dir='lib')
>>> subst = {'version': '1.0'}
>>> config.add_npy_pkg_config('foo.ini.in', 'lib', subst_dict=subst)

```

This will install the file foo.ini into the directory package_dir/lib, and the foo.ini file will be generated from foo.ini.in, where each @version@ will be replaced by subst_dict ['version' ]. The dictionary has an additional prefix substitution rule automatically added, which contains the install prefix (since this is not easy to get from setup.py).
npy-pkg-config files can also be installed at the same location as used for numpy, using the path returned from get_npy_pkg_dir function.

\subsection*{4.2.2 Reusing a C library from another package}

Info are easily retrieved from the get_info function in numpy. distutils.misc_util:
```

>>> info = get_info('npymath')
>>> config.add_extension('foo', sources=['foo.c'], extra_info=**info)

```

An additional list of paths to look for .ini files can be given to get_info.

\subsection*{4.3 Conversion of .src files}

NumPy distutils supports automatic conversion of source files named <somefile>.src. This facility can be used to maintain very similar code blocks requiring only simple changes between blocks. During the build phase of setup, if a template file named <somefile>.src is encountered, a new file named <somefile> is constructed from the template and placed in the build directory to be used instead. Two forms of template conversion are supported. The first form occurs for files named named <file>.ext.src where ext is a recognized Fortran extension (f, f90, f95, f77, for, ftn, pyf). The second form is used for all other cases.

\subsection*{4.3.1 Fortran files}

This template converter will replicate all function and subroutine blocks in the file with names that contain '<...>' according to the rules in '<...>'. The number of comma-separated words in '<...>' determines the number of times the block is repeated. What these words are indicates what that repeat rule, '<...>', should be replaced with in each block. All of the repeat rules in a block must contain the same number of comma-separated words indicating the number of times that block should be repeated. If the word in the repeat rule needs a comma, leftarrow, or rightarrow, then prepend it with a backslash ' '. If a word in the repeat rule matches ' \(<\) index>' then it will be replaced with the <index>-th word in the same repeat specification. There are two forms for the repeat rule: named and short.

\section*{Named repeat rule}

A named repeat rule is useful when the same set of repeats must be used several times in a block. It is specified using <rule1=item1, item2, item3,.., itemN>, where N is the number of times the block should be repeated. On each repeat of the block, the entire expression, '<...>' will be replaced first with item1, and then with item2, and so forth until N repeats are accomplished. Once a named repeat specification has been introduced, the same repeat rule may be used in the current block by referring only to the name (i.e. \(<\) rule \(1>\).

\section*{Short repeat rule}

A short repeat rule looks like <item1, item2, item3, ..., itemN>. The rule specifies that the entire expression, '<...>' should be replaced first with item1, and then with item2, and so forth until N repeats are accomplished.

\section*{Pre-defined names}

The following predefined named repeat rules are available:
- <prefix=s,d,c,z>
- <_c=s,d,c,z>
- <_t=real, double precision, complex, double complex>
- <ftype=real, double precision, complex, double complex>
- <ctype=float, double, complex_float, complex_double>
- <ftypereal=float, double precision, \(10, \backslash 1>\)
- <ctypereal=float, double, \0, \1>

\subsection*{4.3.2 Other files}

Non-Fortran files use a separate syntax for defining template blocks that should be repeated using a variable expansion similar to the named repeat rules of the Fortran-specific repeats. The template rules for these files are:
1. "/**begin repeat "on a line by itself marks the beginning of a segment that should be repeated.
2. Named variable expansions are defined using \#name=item1, item2, item3, ..., itemN\# and placed on successive lines. These variables are replaced in each repeat block with corresponding word. All named variables in the same repeat block must define the same number of words.
3. In specifying the repeat rule for a named variable, item*N is short- hand for item, item, ,.., item repeated N times. In addition, parenthesis in combination with \(* \mathrm{~N}\) can be used for grouping several items that should be repeated. Thus, \#name=(item1, item2)*4\# is equivalent to \#name=item1, item2, item1, item2, item1, item2, item1, item2\#
4. "*/ "on a line by itself marks the end of the the variable expansion naming. The next line is the first line that will be repeated using the named rules.
5. Inside the block to be repeated, the variables that should be expanded are specified as @ name@.
6. "/**end repeat**/"on a line by itself marks the previous line as the last line of the block to be repeated.

\title{
NUMPY C-API
}

Beware of the man who won't be bothered with details.
- William Feather, Sr. The truth is out there.
- Chris Carter, The X Files

NumPy provides a C-API to enable users to extend the system and get access to the array object for use in other routines. The best way to truly understand the C-API is to read the source code. If you are unfamiliar with (C) source code, however, this can be a daunting experience at first. Be assured that the task becomes easier with practice, and you may be surprised at how simple the C-code can be to understand. Even if you don't think you can write C-code from scratch, it is much easier to understand and modify already-written source code then create it de novo.

Python extensions are especially straightforward to understand because they all have a very similar structure. Admittedly, NumPy is not a trivial extension to Python, and may take a little more snooping to grasp. This is especially true because of the code-generation techniques, which simplify maintenance of very similar code, but can make the code a little less readable to beginners. Still, with a little persistence, the code can be opened to your understanding. It is my hope, that this guide to the C-API can assist in the process of becoming familiar with the compiled-level work that can be done with NumPy in order to squeeze that last bit of necessary speed out of your code.

\subsection*{5.1 Python Types and C-Structures}

Several new types are defined in the C-code. Most of these are accessible from Python, but a few are not exposed due to their limited use. Every new Python type has an associated PyOb ject \(*\) with an internal structure that includes a pointer to a "method table" that defines how the new object behaves in Python. When you receive a Python object into C code, you always get a pointer to a PyObject structure. Because a PyObject structure is very generic and defines only PyObject_HEAD, by itself it is not very interesting. However, different objects contain more details after the PyOb ject_HEAD (but you have to cast to the correct type to access them - or use accessor functions or macros).

\subsection*{5.1.1 New Python Types Defined}

Python types are the functional equivalent in \(C\) of classes in Python. By constructing a new Python type you make available a new object for Python. The ndarray object is an example of a new type defined in C. New types are defined in C by two basic steps:
1. creating a C-structure (usually named Py \{Name\}Object) that is binary- compatible with the PyObject structure itself but holds the additional information needed for that particular object;
2. populating the PyTypeObject table (pointed to by the ob_type member of the PyObject structure) with pointers to functions that implement the desired behavior for the type.

Instead of special method names which define behavior for Python classes, there are "function tables" which point to functions that implement the desired results. Since Python 2.2, the PyTypeObject itself has become dynamic which allows C types that can be "sub-typed "from other C-types in C, and sub-classed in Python. The children types inherit the attributes and methods from their parent(s).

There are two major new types: the ndarray ( PyArray_Type ) and the ufunc ( PyUFunc_Type ). Additional types play a supportive role: the PyArrayIter_Type, the PyArrayMultiIter_Type, and the PyArrayDescr_Type. The PyArrayIter_Type is the type for a flat iterator for an ndarray (the object that is returned when getting the flat attribute). The PyArrayMultiIter_Type is the type of the object returned when calling broadcast (). It handles iteration and broadcasting over a collection of nested sequences. Also, the PyArrayDescr_Type is the data-type-descriptor type whose instances describe the data. Finally, there are 21 new scalar-array types which are new Python scalars corresponding to each of the fundamental data types available for arrays. An additional 10 other types are place holders that allow the array scalars to fit into a hierarchy of actual Python types.

\section*{PyArray_Type}

PyArray_Type
The Python type of the ndarray is PyArray_Type. In C, every ndarray is a pointer to a PyArrayObject structure. The ob_type member of this structure contains a pointer to the PyArray_Type typeobject.

\section*{PyArrayObject}

The PyArrayObject C-structure contains all of the required information for an array. All instances of an ndarray (and its subclasses) will have this structure. For future compatibility, these structure members should normally be accessed using the provided macros. If you need a shorter name, then you can make use of NPY_AO which is defined to be equivalent to PyArrayOb ject.
```

typedef struct PyArrayObject {
PyObject_HEAD
char *data;
int nd;
npy_intp *dimensions;
npy_intp *strides;
PyObject *base;
PyArray_Descr *descr;
int flags;
PyObject *weakreflist;
} PyArrayObject;

```

\section*{PyArrayObject. PyObject_HEAD}

This is needed by all Python objects. It consists of (at least) a reference count member (ob_refcnt ) and a pointer to the typeobject (ob_type ). (Other elements may also be present if Python was compiled with special options see Include/object.h in the Python source tree for more information). The ob_type member points to a Python type object.
char *PyArrayObject. data
A pointer to the first element of the array. This pointer can (and normally should) be recast to the data type of the array.

\section*{int PyArrayObject.nd}

An integer providing the number of dimensions for this array. When nd is 0 , the array is sometimes called a rank-0 array. Such arrays have undefined dimensions and strides and cannot be accessed. NPY_MAXDIMS is the largest number of dimensions for any array.

\section*{npy_intp PyArrayObject. dimensions}

An array of integers providing the shape in each dimension as long as nd \(\geq 1\). The integer is always large enough to hold a pointer on the platform, so the dimension size is only limited by memory.

\section*{npy_intp *PyArrayObject.strides}

An array of integers providing for each dimension the number of bytes that must be skipped to get to the next element in that dimension.

\section*{PyObject *PyArrayObject.base}

This member is used to hold a pointer to another Python object that is related to this array. There are two use cases: 1) If this array does not own its own memory, then base points to the Python object that owns it (perhaps another array object), 2) If this array has the NPY_UPDATEIFCOPY flag set, then this array is a working copy of a "misbehaved" array. As soon as this array is deleted, the array pointed to by base will be updated with the contents of this array.

\section*{PyArray_Descr *PyArrayObject.descr}

A pointer to a data-type descriptor object (see below). The data-type descriptor object is an instance of a new built-in type which allows a generic description of memory. There is a descriptor structure for each data type supported. This descriptor structure contains useful information about the type as well as a pointer to a table of function pointers to implement specific functionality.

\section*{int PyArrayObject.flags}

Flags indicating how the memory pointed to by data is to be interpreted. Possible flags are NPY_C_CONTIGUOUS, NPY_F_CONTIGUOUS, NPY_OWNDATA, NPY_ALIGNED, NPY_WRITEABLE, and NPY_UPDATEIFCOPY.

PyObject *PyArrayObject. weakreflist
This member allows array objects to have weak references (using the weakref module).

\section*{PyArrayDescr_Type}

\section*{PyArrayDescr_Type}

The PyArrayDescr_Type is the built-in type of the data-type-descriptor objects used to describe how the bytes comprising the array are to be interpreted. There are 21 statically-defined PyArray_Descr objects for the built-in data-types. While these participate in reference counting, their reference count should never reach zero. There is also a dynamic table of user-defined PyArray_Descr objects that is also maintained. Once a data-type-descriptor object is "registered" it should never be deallocated either. The function PyArray_DescrFromType (...) can be used to retrieve a PyArray_Descr object from an enumerated type-number (either built-in or user- defined).

\section*{PyArray_Descr}

The format of the PyArray_Descr structure that lies at the heart of the PyArrayDescr_Type is
```

typedef struct {
PyObject_HEAD
PyTypeObject *typeobj;
char kind;
char type;
char byteorder;
char unused;
int flags;
int type_num;
int elsize;
int alignment;
PyArray_ArrayDescr *subarray;
PyObject *fields;
PyArray_ArrFuncs *f;
} PyArray_Descr;

```
PyTypeObject *PyArray_Descr.typeobj

Pointer to a typeobject that is the corresponding Python type for the elements of this array. For the builtin
types, this points to the corresponding array scalar. For user-defined types, this should point to a user-defined typeobject. This typeobject can either inherit from array scalars or not. If it does not inherit from array scalars, then the NPY_USE_GETITEM and NPY_USE_SETITEM flags should be set in the flags member.
char PyArray_Descr.kind
A character code indicating the kind of array (using the array interface typestring notation). A ' \(b\) ' represents Boolean, a ' i ' represents signed integer, a ' \(u\) ' represents unsigned integer, ' f ' represents floating point, ' c ' represents complex floating point, 'S' represents 8-bit character string, ' \(U\) ' represents 32 -bit/character unicode string, and ' V ' repesents arbitrary.
```

char PyArray_Descr.type

```

A traditional character code indicating the data type.
char PyArray_Descr.byteorder
A character indicating the byte-order: ' \(>\) ' (big-endian), '<' (little- endian), '=' (native), 'l' (irrelevant, ignore). All builtin data- types have byteorder ' \(=\) '.

\section*{int PyArray_Descr.flags}

A data-type bit-flag that determines if the data-type exhibits object- array like behavior. Each bit in this member is a flag which are named as:

\section*{NPY_ITEM_REFCOUNT}

\section*{NPY_ITEM_HASOBJECT}

Indicates that items of this data-type must be reference counted (using Py_INCREF and Py_DECREF ).

\section*{NPY_ITEM_LISTPICKLE}

Indicates arrays of this data-type must be converted to a list before pickling.

\section*{NPY_ITEM_IS_POINTER}

Indicates the item is a pointer to some other data-type

\section*{NPY_NEEDS_INIT}

Indicates memory for this data-type must be initialized (set to 0 ) on creation.

\section*{NPY_NEEDS_PYAPI}

Indicates this data-type requires the Python C-API during access (so don't give up the GIL if array access is going to be needed).

NPY_USE_GETITEM
On array access use the \(f->g e t i t e m\) function pointer instead of the standard conversion to an array scalar. Must use if you don't define an array scalar to go along with the data-type.

\section*{NPY_USE_SETITEM}

When creating a \(0-\mathrm{d}\) array from an array scalar use \(f->\) setitem instead of the standard copy from an array scalar. Must use if you don't define an array scalar to go along with the data-type.

NPY_FROM_FIELDS
The bits that are inherited for the parent data-type if these bits are set in any field of the data-type. Currently ( NPY_NEEDS_INITINPY_LIST_PICKLE I NPY_ITEM_REFCOUNT I NPY_NEEDS_PYAPI ).

\section*{NPY_OBJECT_DTYPE_FLAGS}

Bits set for the object data-type: ( NPY_LIST_PICKLE \| NPY_USE_GETITEM | NPY_ITEM_IS_POINTERINPY_REFCOUNT I NPY_NEEDS_INITINPY_NEEDS_PYAPI).
PyDataType_FLAGCHK (PyArray_Descr *dtype, int flags)
Return true if all the given flags are set for the data-type object.
PyDataType_REFCHK (PyArray_Descr *dtype)
Equivalent to PyDataType_FLAGCHK (dtype, NPY_ITEM_REFCOUNT).

\section*{int PyArray_Descr.type_num}

A number that uniquely identifies the data type. For new data-types, this number is assigned when the data-type is registered.
int PyArray_Descr.elsize
For data types that are always the same size (such as long), this holds the size of the data type. For flexible data types where different arrays can have a different elementsize, this should be 0 .
int PyArray_Descr.alignment
A number providing alignment information for this data type. Specifically, it shows how far from the start of a 2-element structure (whose first element is a char ), the compiler places an item of this type: offsetof (struct \{char c; type v;\}, v)

PyArray_ArrayDescr *PyArray_Descr.subarray
If this is non- NULL, then this data-type descriptor is a C-style contiguous array of another data-type descriptor. In other-words, each element that this descriptor describes is actually an array of some other base descriptor. This is most useful as the data-type descriptor for a field in another data-type descriptor. The fields member should be NULL if this is non- NULL (the fields member of the base descriptor can be non- NULL however). The PyArray_ArrayDescr structure is defined using
```

typedef struct {
PyArray_Descr *base;
PyObject *shape;
} PyArray_ArrayDescr;

```

The elements of this structure are:
PyArray_Descr *PyArray_ArrayDescr.base
The data-type-descriptor object of the base-type.
PyObject *PyArray_ArrayDescr. shape
The shape (always C-style contiguous) of the sub-array as a Python tuple.
PyObject *PyArray_Descr.fields
If this is non-NULL, then this data-type-descriptor has fields described by a Python dictionary whose keys are names (and also titles if given) and whose values are tuples that describe the fields. Recall that a data-type-descriptor always describes a fixed-length set of bytes. A field is a named sub-region of that total, fixed-length collection. A field is described by a tuple composed of another data- type-descriptor and a byte offset. Optionally, the tuple may contain a title which is normally a Python string. These tuples are placed in this dictionary keyed by name (and also title if given).

PyArray_ArrFuncs *PyArray_Descr.f
A pointer to a structure containing functions that the type needs to implement internal features. These functions are not the same thing as the universal functions (ufuncs) described later. Their signatures can vary arbitrarily.

\section*{PyArray_ArrFuncs}

Functions implementing internal features. Not all of these function pointers must be defined for a given type. The required members are nonzero, copyswap, copyswapn, setitem, getitem, and cast. These are assumed to be non- NULL and NULL entries will cause a program crash. The other functions may be NULL which will just mean reduced functionality for that data-type. (Also, the nonzero function will be filled in with a default function if it is NULL when you register a user-defined data-type).
```

typedef struct {
PyArray_VectorUnaryFunc *cast[PyArray_NTYPES];
PyArray_GetItemFunc *getitem;
PyArray_SetItemFunc *setitem;
PyArray_CopySwapNFunc *copyswapn;
PyArray_CopySwapFunc *copyswap;
PyArray_CompareFunc *compare;
PyArray_ArgFunc *argmax;

```
```

    PyArray_DotFunc *dotfunc;
    PyArray_ScanFunc *scanfunc;
    PyArray_FromStrFunc *fromstr;
    PyArray_NonzeroFunc *nonzero;
    PyArray_FillFunc *fill;
    PyArray_FillWithScalarFunc *fillwithscalar;
    PyArray_SortFunc *sort[PyArray_NSORTS];
    PyArray_ArgSortFunc *argsort[PyArray_NSORTS];
    PyObject *castdict;
    PyArray_ScalarKindFunc *scalarkind;
    int **cancastscalarkindto;
    int *cancastto;
    int listpickle
    } PyArray_ArrFuncs;

```

The concept of a behaved segment is used in the description of the function pointers. A behaved segment is one that is aligned and in native machine byte-order for the data-type. The nonzero, copyswap, copyswapn, getitem, and setitem functions can (and must) deal with mis-behaved arrays. The other functions require behaved memory segments.
```

void cast(void *from, void *to, npy_intp n, void *fromarr,
void *toarr)

```

An array of function pointers to cast from the current type to all of the other builtin types. Each function casts a contiguous, aligned, and notswapped buffer pointed at by from to a contiguous, aligned, and notswapped buffer pointed at by to The number of items to cast is given by \(n\), and the arguments fromarr and toarr are interpreted as PyArrayObjects for flexible arrays to get itemsize information.

PyObject *getitem (void *data, void *arr)
A pointer to a function that returns a standard Python object from a single element of the array object arr pointed to by data. This function must be able to deal with "misbehaved "(misaligned and/or swapped) arrays correctly.
int setitem (PyObject \(*\) item, void \(*\) data, void \(* a r r\) )
A pointer to a function that sets the Python object item into the array, arr, at the position pointed to by data . This function deals with "misbehaved" arrays. If successful, a zero is returned, otherwise, a negative one is returned (and a Python error set).
```

void copyswapn(void *dest, npy_intp dstride, void *src,

```
npy_intp sstride, npy_intp n, int swap, void *arr)
void copyswap (void *dest, void *src, int swap, void *arr)
These members are both pointers to functions to copy data from src to dest and swap if indicated. The value of arr is only used for flexible (NPY_STRING, NPY_UNICODE, and NPY_VOID) arrays (and is obtained from arr->descr->elsize). The second function copies a single value, while the first loops over \(n\) values with the provided strides. These functions can deal with misbehaved \(s r c\) data. If \(s r c\) is NULL then no copy is performed. If swap is 0 , then no byteswapping occurs. It is assumed that dest and src do not overlap. If they overlap, then use memmove (...) first followed by copyswap ( n ) with NULL valued src.
int compare (const void* \(d l\), const void* \(d 2\), void* arr)
A pointer to a function that compares two elements of the array, arr, pointed to by d 1 and d 2 . This function requires behaved arrays. The return value is 1 if \(* d 1>* d 2,0\) if \(* d 1==* d 2\), and -1 if \(* d 1<\) * d2. The array object arr is used to retrieve itemsize and field information for flexible arrays.
```

int argmax(void* data, npy_intp n, npy_intp* max_ind,

```

\section*{void* arr)}

A pointer to a function that retrieves the index of the largest of \(n\) elements in arr beginning at the element pointed to by data. This function requires that the memory segment be contiguous and behaved. The return value is always 0 . The index of the largest element is returned in max_ind.
```

void dotfunc(void* ip1, npy_intp is1, void* ip2, npy_intp is2,
void* op, npy_intp n, void* arr)

```

A pointer to a function that multiplies two n -length sequences together, adds them, and places the result in element pointed to by op of arr. The start of the two sequences are pointed to by ip1 and ip2. To get to the next element in each sequence requires a jump of is1 and is2 bytes, respectively. This function requires behaved (though not necessarily contiguous) memory.
int scanfunc (FILE* \(f d\), void* ip, void* sep, void* arr)
A pointer to a function that scans (scanf style) one element of the corresponding type from the file descriptor fd into the array memory pointed to by ip. The array is assumed to be behaved. If sep is not NULL, then a separator string is also scanned from the file before returning. The last argument arr is the array to be scanned into. A 0 is returned if the scan is successful. A negative number indicates something went wrong: -1 means the end of file was reached before the separator string could be scanned, -4 means that the end of file was reached before the element could be scanned, and -3 means that the element could not be interpreted from the format string. Requires a behaved array.
int fromstr (char* str, void* ip, char** endptr, void* arr)
A pointer to a function that converts the string pointed to by str to one element of the corresponding type and places it in the memory location pointed to by ip. After the conversion is completed, *endptr points to the rest of the string. The last argument arr is the array into which ip points (needed for variable-size data- types). Returns 0 on success or -1 on failure. Requires a behaved array.

Bool nonzero (void* data, void* arr)
A pointer to a function that returns TRUE if the item of arr pointed to by data is nonzero. This function can deal with misbehaved arrays.
void fill (void* data, npy_intp length, void* arr)
A pointer to a function that fills a contiguous array of given length with data. The first two elements of the array must already be filled- in. From these two values, a delta will be computed and the values from item 3 to the end will be computed by repeatedly adding this computed delta. The data buffer must be well-behaved.
void fillwithscalar(void* buffer, npy_intp length,
void* value, void* arr)
A pointer to a function that fills a contiguous buffer of the given length with a single scalar value whose address is given. The final argument is the array which is needed to get the itemsize for variable-length arrays.
int sort (void* start, npy_intp length, void* arr)
An array of function pointers to a particular sorting algorithms. A particular sorting algorithm is obtained using a key (so far PyArray_QUICKSORT, :data‘PyArray_HEAPSORT', and PyArray_MERGESORT are defined). These sorts are done in-place assuming contiguous and aligned data.
int argsort (void* start, npy_intp* result, npy_intp length,
void *arr)
An array of function pointers to sorting algorithms for this data type. The same sorting algorithms as for sort are available. The indices producing the sort are returned in result (which must be initialized with indices 0 to length-1 inclusive).

PyObject * castdict
Either NULL or a dictionary containing low-level casting functions for user- defined data-types. Each function is wrapped in a PyCObject * and keyed by the data-type number.
PyArray_SCALARKIND scalarkind (PyArrayObject* arr)
A function to determine how scalars of this type should be interpreted. The argument is NULL or a 0 -dimensional array containing the data (if that is needed to determine the kind of scalar). The return value must be of type PyArray_SCALARKIND.
int **cancastscalarkindto
Either NULL or an array of PyArray_NSCALARKINDS pointers. These pointers should each be either NULL or a pointer to an array of integers (terminated by PyArray_NOTYPE) indicating data-types that a scalar of this data-type of the specified kind can be cast to safely (this usually means without losing precision).
int * cancastto
Either NULL or an array of integers (terminated by PyArray_NOTYPE ) indicated data-types that this data-type can be cast to safely (this usually means without losing precision).
int listpickle
Unused.
The PyArray_Type typeobject implements many of the features of Python objects including the tp_as_number, tp_as_sequence, tp_as_mapping, and tp_as_buffer interfaces. The rich comparison (tp_richcompare) is also used along with new-style attribute lookup for methods (tp_methods) and properties (tp_getset). The PyArray_Type can also be sub-typed.

Tip: The tp_as_number methods use a generic approach to call whatever function has been registered for handling the operation. The function PyNumeric_SetOps(..) can be used to register functions to handle particular mathematical operations (for all arrays). When the umath module is imported, it sets the numeric operations for all arrays to the corresponding ufuncs. The tp_str and tp_repr methods can also be altered using PyString_SetStringFunction(...).

\section*{PyUFunc_Type}

\section*{PyUFunc_Type}

The ufunc object is implemented by creation of the PyUFunc_Type. It is a very simple type that implements only basic getattribute behavior, printing behavior, and has call behavior which allows these objects to act like functions. The basic idea behind the ufunc is to hold a reference to fast 1-dimensional (vector) loops for each data type that supports the operation. These one-dimensional loops all have the same signature and are the key to creating a new ufunc. They are called by the generic looping code as appropriate to implement the N -dimensional function. There are also some generic 1-d loops defined for floating and complexfloating arrays that allow you to define a ufunc using a single scalar function (e.g. atanh).

\section*{PyUFuncObject}

The core of the ufunc is the PyUFuncOb ject which contains all the information needed to call the underlying C-code loops that perform the actual work. It has the following structure:
```

typedef struct {
PyObject_HEAD
int nin;
int nout;
int nargs;
int identity;
PyUFuncGenericFunction *functions;
void **data;
int ntypes;
int check_return;
char *name;

```
```

    char *types;
    char *doc;
    void *ptr;
    PyObject *obj;
        PyObject *userloops;
    } PyUFuncObject;
    ```
PyUFuncObject.PyObject_HEAD
    required for all Python objects.
int PyUFuncObject.nin
    The number of input arguments.
int PyUFuncObject. nout
    The number of output arguments.
int PyUFuncObject.nargs

The total number of arguments (nin + nout). This must be less than NPY_MAXARGS.

\section*{int PyUFuncObject.identity}

Either PyUFunc_One, PyUFunc_Zero, or PyUFunc_None to indicate the identity for this operation. It is only used for a reduce-like call on an empty array.
```

void PyUFuncObject.functions(char** args, npy_intp* dims,

```

\section*{npy_intp* steps, void* extradata)}

An array of function pointers - one for each data type supported by the ufunc. This is the vector loop that is called to implement the underlying function dims [0] times. The first argument, args, is an array of nargs pointers to behaved memory. Pointers to the data for the input arguments are first, followed by the pointers to the data for the output arguments. How many bytes must be skipped to get to the next element in the sequence is specified by the corresponding entry in the steps array. The last argument allows the loop to receive extra information. This is commonly used so that a single, generic vector loop can be used for multiple functions. In this case, the actual scalar function to call is passed in as extradata. The size of this function pointer array is ntypes.

\section*{void **PyUFuncObject. data}

Extra data to be passed to the 1-d vector loops or NULL if no extra-data is needed. This C-array must be the same size (i.e. ntypes) as the functions array. NULL is used if extra_data is not needed. Several C-API calls for UFuncs are just 1-d vector loops that make use of this extra data to receive a pointer to the actual function to call.

\section*{int PyUFuncObject.ntypes}

The number of supported data types for the ufunc. This number specifies how many different 1-d loops (of the builtin data types) are available.
int PyUFuncObject.check_return
Obsolete and unused. However, it is set by the corresponding entry in the main ufunc creation routine: PyUFunc_FromFuncAndData (...).
char *PyUFuncObject. name
A string name for the ufunc. This is used dynamically to build the __doc__ attribute of ufuncs.
char *PyUFuncObject.types
An array of nargs \(\times\) ntypes 8-bit type_numbers which contains the type signature for the function for each of the supported (builtin) data types. For each of the ntypes functions, the corresponding set of type numbers in this array shows how the args argument should be interpreted in the 1-d vector loop. These type numbers do not have to be the same type and mixed-type ufuncs are supported.
char *PyUFuncObject. doc
Documentation for the ufunc. Should not contain the function signature as this is generated dynamically
when \(\qquad\) is retrieved.
void *PyUFuncObject.ptr
Any dynamically allocated memory. Currently, this is used for dynamic ufuncs created from a python function to store room for the types, data, and name members.
PyObject *PyUFuncObject. obj
For ufuncs dynamically created from python functions, this member holds a reference to the underlying Python function.

PyObject *PyUFuncObject. userloops
A dictionary of user-defined 1-d vector loops (stored as CObject ptrs) for user-defined types. A loop may be registered by the user for any user-defined type. It is retrieved by type number. User defined type numbers are always larger than NPY_USERDEF.

\section*{PyArraylter_Type}

\section*{PyArrayIter_Type}

This is an iterator object that makes it easy to loop over an N-dimensional array. It is the object returned from the flat attribute of an ndarray. It is also used extensively throughout the implementation internals to loop over an N -dimensional array. The tp_as_mapping interface is implemented so that the iterator object can be indexed (using 1-d indexing), and a few methods are implemented through the tp_methods table. This object implements the next method and can be used anywhere an iterator can be used in Python.

\section*{PyArrayIterObject}

The C-structure corresponding to an object of PyArrayIter_Type is the PyArrayIterobject. The PyArrayIterObject is used to keep track of a pointer into an N-dimensional array. It contains associated information used to quickly march through the array. The pointer can be adjusted in three basic ways: 1) advance to the "next" position in the array in a C-style contiguous fashion, 2) advance to an arbitrary N -dimensional coordinate in the array, and 3) advance to an arbitrary one-dimensional index into the array. The members of the PyArrayIterObject structure are used in these calculations. Iterator objects keep their own dimension and strides information about an array. This can be adjusted as needed for "broadcasting," or to loop over only specific dimensions.
```

typedef struct {
PyObject_HEAD
int nd_m1;
npy_intp index;
npy_intp size;
npy_intp coordinates[NPY_MAXDIMS];
npy_intp dims_m1[NPY_MAXDIMS];
npy_intp strides[NPY_MAXDIMS];
npy_intp backstrides[NPY_MAXDIMS];
npy_intp factors[NPY_MAXDIMS];
PyArrayObject *ao;
char *dataptr;
Bool contiguous;
} PyArrayIterObject;
int PyArrayIterObject.nd_m1
$N-1$ where $N$ is the number of dimensions in the underlying array.
npy_intp PyArrayIterObject.index
The current 1-d index into the array.
npy_intp PyArrayIterObject.size
The total size of the underlying array.

```
npy_intp *PyArrayIterObject.coordinates
An \(N\)-dimensional index into the array.
npy_intp *PyArrayIterObject.dims_m1
The size of the array minus 1 in each dimension.

\section*{npy_intp *PyArrayIterObject.strides}

The strides of the array. How many bytes needed to jump to the next element in each dimension.
```

npy_intp *PyArrayIterObject.backstrides

```

How many bytes needed to jump from the end of a dimension back to its beginning. Note that backstrides \([\mathrm{k}]=\) strides \([\mathrm{k}] * \mathrm{~d}\) ims_ml [k], but it is stored here as an optimization.

\section*{npy_intp *PyArrayIterObject.factors}

This array is used in computing an N -d index from a 1-d index. It contains needed products of the dimensions.

\section*{PyArrayObject *PyArrayIterObject.ao}

A pointer to the underlying ndarray this iterator was created to represent.
char *PyArrayIterObject. dataptr
This member points to an element in the ndarray indicated by the index.

\section*{Bool PyArrayIterObject.contiguous}

This flag is true if the underlying array is NPY_C_CONTIGUOUS. It is used to simplify calculations when possible.

How to use an array iterator on a C-level is explained more fully in later sections. Typically, you do not need to concern yourself with the internal structure of the iterator object, and merely interact with it through the use of the macros PyArray_ITER_NEXT (it), PyArray_ITER_GOTO (it, dest), or PyArray_ITER_GOTO1D (it, index). All of these macros require the argument \(i t\) to be a PyArrayIterObject *.

\section*{PyArrayMultilter_Type}

\section*{PyArrayMultiIter_Type}

This type provides an iterator that encapsulates the concept of broadcasting. It allows \(N\) arrays to be broadcast together so that the loop progresses in C-style contiguous fashion over the broadcasted array. The corresponding C-structure is the PyArrayMultiIterobject whose memory layout must begin any object, obj, passed in to the PyArray_Broadcast (obj) function. Broadcasting is performed by adjusting array iterators so that each iterator represents the broadcasted shape and size, but has its strides adjusted so that the correct element from the array is used at each iteration.

PyArrayMultiIterObject
```

typedef struct {
PyObject_HEAD
int numiter;
npy_intp size;
npy_intp index;
int nd;
npy_intp dimensions[NPY_MAXDIMS];
PyArrayIterObject *iters[NPY_MAXDIMS];
} PyArrayMultiIterObject;
PyArrayMultiIterObject.PyObject_HEAD

```

Needed at the start of every Python object (holds reference count and type identification).
```

int PyArrayMultiIterObject.numiter

```

The number of arrays that need to be broadcast to the same shape.
npy_intp PyArrayMultiIterObject.size
The total broadcasted size.
npy_intp PyArrayMultiIterObject.index
The current (1-d) index into the broadcasted result.
int PyArrayMultiIterObject.nd
The number of dimensions in the broadcasted result.
npy_intp *PyArrayMultiIterObject. dimensions
The shape of the broadcasted result (only nd slots are used).
PyArrayIterObject **PyArrayMultiIterObject.iters
An array of iterator objects that holds the iterators for the arrays to be broadcast together. On return, the iterators are adjusted for broadcasting.

\section*{PyArrayNeighborhoodlter_Type}

\section*{PyArrayNeighborhoodIter_Type}

This is an iterator object that makes it easy to loop over an N -dimensional neighborhood.

\section*{PyArrayNeighborhoodIterObject}

The C-structure corresponding to an object of PyArrayNeighborhoodIter_Type is the PyArrayNeighborhoodIterobject.

\section*{PyArrayFlags_Type}

\section*{PyArrayFlags_Type}

When the flags attribute is retrieved from Python, a special builtin object of this type is constructed. This special type makes it easier to work with the different flags by accessing them as attributes or by accessing them as if the object were a dictionary with the flag names as entries.

\section*{ScalarArrayTypes}

There is a Python type for each of the different built-in data types that can be present in the array Most of these are simple wrappers around the corresponding data type in C. The C-names for these types are Py \{TYPE \}ArrType_Type where \{TYPE \} can be

\author{
Bool, Byte, Short, Int, Long, LongLong, UByte, UShort, UInt, ULong, ULongLong, Half, Float,
} Double, LongDouble, CFloat, CDouble, CLongDouble, String, Unicode, Void, and Object.
These type names are part of the C-API and can therefore be created in extension C-code. There is also a PyIntpArrType_Type and a PyUIntpArrType_Type that are simple substitutes for one of the integer types that can hold a pointer on the platform. The structure of these scalar objects is not exposed to C-code. The function PyArray_ScalarAsCtype (..) can be used to extract the C-type value from the array scalar and the function PyArray_Scalar (...) can be used to construct an array scalar from a C-value.

\subsection*{5.1.2 Other C-Structures}

A few new C-structures were found to be useful in the development of NumPy. These C-structures are used in at least one C-API call and are therefore documented here. The main reason these structures were defined is to make it easy to use the Python ParseTuple C-API to convert from Python objects to a useful C-Object.

\section*{PyArray_Dims}

\section*{PyArray_Dims}

This structure is very useful when shape and/or strides information is supposed to be interpreted. The structure is:
```

typedef struct {
npy_intp *ptr;
int len;
} PyArray_Dims;

```

The members of this structure are
```

npy_intp *PyArray_Dims.ptr

```

A pointer to a list of (npy_intp) integers which usually represent array shape or array strides.
int PyArray_Dims.len
The length of the list of integers. It is assumed safe to access ptr [0] to ptr [len-1].

\section*{PyArray_Chunk}

\section*{PyArray_Chunk}

This is equivalent to the buffer object structure in Python up to the ptr member. On 32-bit platforms (i.e. if NPY_SIZEOF_INT == NPY_SIZEOF_INTP ) or in Python 2.5, the len member also matches an equivalent member of the buffer object. It is useful to represent a generic single- segment chunk of memory.
```

typedef struct {
PyObject_HEAD
PyObject *base;
void *ptr;
npy_intp len;
int flags;
} PyArray_Chunk;

```

The members are

\section*{PyArray_Chunk.PyObject_HEAD}

Necessary for all Python objects. Included here so that the PyArray_Chunk structure matches that of the buffer object (at least to the len member).

\section*{PyObject *PyArray_Chunk. base}

The Python object this chunk of memory comes from. Needed so that memory can be accounted for properly.
void *PyArray_Chunk.ptr
A pointer to the start of the single-segment chunk of memory.
npy_intp PyArray_Chunk.len
The length of the segment in bytes.
int PyArray_Chunk.flags
Any data flags (e.g. NPY_WRITEABLE ) that should be used to interpret the memory.

\section*{PyArrayInterface}

\section*{See Also:}

The Array Interface

\section*{PyArrayInterface}

The PyArrayInterface structure is defined so that NumPy and other extension modules can use the rapid array interface protocol. The \(\qquad\) array_struct \(\qquad\) method of an object that supports the rapid array interface protocol should return a Pycobject that contains a pointer to a PyArrayInterface structure with the relevant details of the array. After the new array is created, the attribute should be DECREF'd which will free the PyArrayInterface structure. Remember to INCREF the object (whose __array_struct__ attribute was retrieved) and point the base member of the new PyArrayObject to this same object. In this way the memory for the array will be managed correctly.
```

typedef struct {
int two;
int nd;
char typekind;
int itemsize;
int flags;
npy_intp *shape;
npy_intp *strides;
void *data;
PyObject *descr;
} PyArrayInterface;

```
int PyArrayInterface.two
    the integer 2 as a sanity check.
int PyArrayInterface.nd
    the number of dimensions in the array.
char PyArrayInterface.typekind

A character indicating what kind of array is present according to the typestring convention with ' \(t\) ' -> bitfield, 'b' -> Boolean, 'i' -> signed integer, 'u' -> unsigned integer, 'f' -> floating point, 'c' -> complex floating point, ' O ' -> object, ' S ' -> string, 'U' -> unicode, 'V' -> void.

\section*{int PyArrayInterface.itemsize}

The number of bytes each item in the array requires.

\section*{int PyArrayInterface.flags}

Any of the bits NPY_C_CONTIGUOUS (1), NPY_F_CONTIGUOUS (2), NPY_ALIGNED (0x100), NPY_NOTSWAPPED (0x200), or NPY_WRITEABLE (0x400) to indicate something about the data. The NPY_ALIGNED, NPY_C_CONTIGUOUS, and NPY_F_CONTIGUOUS flags can actually be determined from the other parameters. The flag NPY_ARR_HAS_DESCR (0x800) can also be set to indicate to objects consuming the version 3 array interface that the descr member of the structure is present (it will be ignored by objects consuming version 2 of the array interface).

\section*{npy_intp *PyArrayInterface.shape}

An array containing the size of the array in each dimension.

\section*{npy_intp *PyArrayInterface.strides}

An array containing the number of bytes to jump to get to the next element in each dimension.

\section*{void *PyArrayInterface.data}

A pointer to the first element of the array.

\section*{PyObject *PyArrayInterface.descr}

A Python object describing the data-type in more detail (same as the descr key in __array_interface__). This can be NULL if typekind and itemsize provide enough information. This field is also ignored unless ARR_HAS_DESCR flag is on in flags.

\section*{Internally used structures}

Internally, the code uses some additional Python objects primarily for memory management. These types are not accessible directly from Python, and are not exposed to the C-API. They are included here only for completeness and assistance in understanding the code.

\section*{PyUFuncLoopObject}

A loose wrapper for a C -structure that contains the information needed for looping. This is useful if you are trying to understand the ufunc looping code. The PyUFuncLoopobject is the associated C-structure. It is defined in the ufuncobject. h header.

\section*{PyUFuncReduceObject}

A loose wrapper for the C-structure that contains the information needed for reduce-like methods of ufuncs. This is useful if you are trying to understand the reduce, accumulate, and reduce-at code. The PyUFuncReduceOb ject is the associated C-structure. It is defined in the ufuncobject. h header.

\section*{PyUFunc_Loop1d}

A simple linked-list of C-structures containing the information needed to define a 1-d loop for a ufunc for every defined signature of a user-defined data-type.

\section*{PyArrayMapIter_Type}

Advanced indexing is handled with this Python type. It is simply a loose wrapper around the Cstructure containing the variables needed for advanced array indexing. The associated C-structure, PyArrayMapIterObject, is useful if you are trying to understand the advanced-index mapping code. It is defined in the arrayobject. h header. This type is not exposed to Python and could be replaced with a C-structure. As a Python type it takes advantage of reference- counted memory management.

\subsection*{5.2 System configuration}

When NumPy is built, information about system configuration is recorded, and is made available for extension modules using Numpy's C API. These are mostly defined in numpyconfig.h (included in ndarrayobject.h). The public symbols are prefixed by NPY_*. Numpy also offers some functions for querying information about the platform in use.

For private use, Numpy also constructs a config. h in the NumPy include directory, which is not exported by Numpy (that is a python extension which use the numpy C API will not see those symbols), to avoid namespace pollution.

\subsection*{5.2.1 Data type sizes}

The NPY_SIZEOF_\{CTYPE \} constants are defined so that sizeof information is available to the pre-processor.
NPY_SIZEOF_SHORT

NPY_SIZEOF_INT

NPY_SIZEOF_LONG

NPY_SIZEOF_LONG_LONG

NPY_SIZEOF_PY_LONG_LONG
```

NPY_SIZEOF_FLOAT
NPY_SIZEOF_DOUBLE
NPY_SIZEOF_LONG_DOUBLE
NPY_SIZEOF_PY_INTPTR_T
Size of a pointer on this platform (sizeof(void *)) (A macro defines NPY_SIZEOF_INTP as well.)

```

\subsection*{5.2.2 Platform information}
```

NPY_CPU_X86
NPY_CPU_AMD64
NPY_CPU_IA64
NPY_CPU_PPC
NPY_CPU_PPC64
NPY_CPU_SPARC
NPY_CPU_SPARC64
NPY_CPU_S390
NPY_CPU_PARISC
New in version 1.3.0. CPU architecture of the platform; only one of the above is defined.
Defined in numpy/npy_cpu.h
NPY_LITTLE_ENDIAN
NPY_BIG_ENDIAN
NPY_BYTE_ORDER
New in version 1.3.0. Portable alternatives to the endian.h macros of GNU Libc. If big endian, NPY_BYTE_ORDER == NPY_BIG_ENDIAN, and similarly for little endian architectures.
Defined in numpy/npy_endian.h.
PyArray_GetEndianness()
New in version 1.3.0. Returns the endianness of the current platform. One of NPY_CPU_BIG, NPY_CPU_LITTLE, or NPY_CPU_UNKNOWN_ENDIAN.

```

\subsection*{5.3 Data Type API}

The standard array can have 24 different data types (and has some support for adding your own types). These data types all have an enumerated type, an enumerated type-character, and a corresponding array scalar Python type object (placed in a hierarchy). There are also standard C typedefs to make it easier to manipulate elements of the given data type. For the numeric types, there are also bit-width equivalent C typedefs and named typenumbers that make it easier to select the precision desired.

Warning: The names for the types in c code follows c naming conventions more closely. The Python names for these types follow Python conventions. Thus, NPY_FLOAT picks up a 32-bit float in C, but numpy.float_in Python corresponds to a 64-bit double. The bit-width names can be used in both Python and C for clarity.

\subsection*{5.3.1 Enumerated Types}

There is a list of enumerated types defined providing the basic 24 data types plus some useful generic names. Whenever the code requires a type number, one of these enumerated types is requested. The types are all called NPY_\{NAME \} where \{NAME \} can be
```

BOOL, BYTE, UBYTE, SHORT, USHORT, INT, UINT, LONG, ULONG, LONGLONG, ULONGLONG, HALF, FLOAT, DOUBLE, LONGDOUBLE, CFLOAT, CDOUBLE, CLONGDOUBLE, DATETIME, TIMEDELTA, OBJECT, STRING, UNICODE, VOID

```

NTYPES, NOTYPE, USERDEF, DEFAULT_TYPE
The various character codes indicating certain types are also part of an enumerated list. References to type characters (should they be needed at all) should always use these enumerations. The form of them is NPY_\{NAME \} LTR where \{NAME \} can be

BOOL, BYTE, UBYTE, SHORT, USHORT, INT, UINT, LONG, ULONG, LONGLONG, ULONGLONG, HALF, FLOAT, DOUBLE, LONGDOUBLE, CFLOAT, CDOUBLE, CLONGDOUBLE, DATETIME, TIMEDELTA, OBJECT, STRING, VOID

INTP, UINTP
GENBOOL, SIGNED, UNSIGNED, FLOATING, COMPLEX
The latter group of \{NAME \} s corresponds to letters used in the array interface typestring specification.

\subsection*{5.3.2 Defines}

Max and min values for integers
NPY_MAX_INT \{bits \}

NPY_MAX_UINT \{bits \}

NPY_MIN_INT \{bits \}
These are defined for \(\{\) bits \(\}=8,16,32,64,128\), and 256 and provide the maximum (minimum) value of the corresponding (unsigned) integer type. Note: the actual integer type may not be available on all platforms (i.e. 128 -bit and 256 -bit integers are rare).

NPY_MIN_\{type\}
This is defined for \(\{\) type \(\}=\) BYTE, SHORT, INT, LONG, LONGLONG, INTP

\section*{NPY_MAX_\{type\}}

This is defined for all defined for \(\{\) type \(\}=\) BYTE, UBYTE, SHORT, USHORT, INT, UINT, LONG, ULONG, LONGLONG, ULONGLONG, INTP, UINTP

\section*{Number of bits in data types}

All NPY_SIZEOF_\{CTYPE\} constants have corresponding NPY_BITSOF_\{CTYPE\} constants defined. The NPY_BITSOF_\{CTYPE \} constants provide the number of bits in the data type. Specifically, the available \{CTYPE\}S are

\author{
BOOL, CHAR, SHORT, INT, LONG, LONGLONG, FLOAT, DOUBLE, LONGDOUBLE
}

\section*{Bit-width references to enumerated typenums}

All of the numeric data types (integer, floating point, and complex) have constants that are defined to be a specific enumerated type number. Exactly which enumerated type a bit-width type refers to is platform dependent. In particular, the constants available are PyArray_\{NAME \} \{BITS \} where \{NAME \} is INT, UINT, FLOAT, COMPLEX and \(\{\) BITS \(\}\) can be \(8,16,32,64,80,96,128,160,192,256\), and 512 . Obviously not all bit-widths are available on all platforms for all the kinds of numeric types. Commonly 8-, 16-, 32-, 64-bit integers; 32-, 64-bit floats; and 64-, 128-bit complex types are available.

\section*{Integer that can hold a pointer}

The constants PyArray_INTP and PyArray_UINTP refer to an enumerated integer type that is large enough to hold a pointer on the platform. Index arrays should always be converted to PyArray_INTP, because the dimension of the array is of type npy_intp.

\subsection*{5.3.3 C-type names}

There are standard variable types for each of the numeric data types and the bool data type. Some of these are already available in the C -specification. You can create variables in extension code with these types.

\section*{Boolean}
```

npy_bool

```
unsigned char; The constants NPY_FALSE and NPY_TRUE are also defined.

\section*{(Un)Signed Integer}

Unsigned versions of the integers can be defined by pre-pending a ' \(u\) ' to the front of the integer name.
```

npy_(u) byte
(unsigned) char
npy_(u) short
(unsigned) short
npy_(u) int
(unsigned) int
npy_(u) long
(unsigned) long int

```
```

npy_(u) longlong

```
(unsigned long long int)
npy_(u) intp
(unsigned) Py_intptr_t (an integer that is the size of a pointer on the platform).
(Complex) Floating point
```

npy_(c) float
float

```
npy_(c) double
    double
npy_(c) longdouble
    long double
complex types are structures with .real and .imag members (in that order).

\section*{Bit-width names}

There are also typedefs for signed integers, unsigned integers, floating point, and complex floating point types of specific bit- widths. The available type names are
```

npy_int{bits}, npy_uint {bits}, npy_float{bits}, and npy_complex{bits}

```
where \(\{\) bits \(\}\) is the number of bits in the type and can be \(\mathbf{8}, \mathbf{1 6}, \mathbf{3 2}, \mathbf{6 4}, 128\), and 256 for integer types; 16, \(\mathbf{3 2}, \mathbf{6 4}\), \(80,96,128\), and 256 for floating-point types; and \(32, \mathbf{6 4}, \mathbf{1 2 8}, 160,192\), and 512 for complex-valued types. Which bit-widths are available is platform dependent. The bolded bit-widths are usually available on all platforms.

\subsection*{5.3.4 Printf Formatting}

For help in printing, the following strings are defined as the correct format specifier in printf and related commands.
```

NPY_LONGLONG_FMT, NPY_ULONGLONG_FMT, NPY_INTP_FMT, NPY_UINTP_FMT,
NPY_LONGDOUBLE_FMT

```

\subsection*{5.4 Array API}

The test of a first-rate intelligence is the ability to hold two opposed ideas in the mind at the same time, and still retain the ability to function.
- F. Scott Fitzgerald For a successful technology, reality must take precedence over public relations, for Nature cannot be fooled.
- Richard P. Feynman

\subsection*{5.4.1 Array structure and data access}

These macros all access the PyArrayOb ject structure members. The input argument, obj, can be any Pyobject * that is directly interpretable as a PyArrayObject * (any instance of the PyArray_Type and its sub-types).
void *PyArray_DATA (PyObject *obj)
char *PyArray_BYTES (PyObject *obj)
These two macros are similar and obtain the pointer to the data-buffer for the array. The first macro can (and should be) assigned to a particular pointer where the second is for generic processing. If you have not guaranteed a contiguous and/or aligned array then be sure you understand how to access the data in the array to avoid memory and/or alignment problems.
```

npy_intp *PyArray_DIMS (PyObject *arr)
npy_intp *PyArray_STRIDES (PyObject* arr)
npy_intp PyArray_DIM(PyObject* arr, int n)
Return the shape in the }\mp@subsup{n}{}{\mathrm{ th }}\mathrm{ dimension.
npy_intp PyArray_STRIDE (PyObject* arr, int n)
Return the stride in the n th dimension.
PyObject *PyArray_BASE (PyObject* arr)
PyArray_Descr *PyArray_DESCR(PyObject* arr)
int PyArray_FLAGS (PyObject* arr)
int PyArray_ITEMSIZE (PyObject* arr)

```

Return the itemsize for the elements of this array.
```

int PyArray_TYPE (PyObject* arr)

```

Return the (builtin) typenumber for the elements of this array.

\section*{PyObject *PyArray_GETITEM (PyObject* arr, void* itemptr)}

Get a Python object from the ndarray, arr, at the location pointed to by itemptr. Return NULL on failure.
int PyArray_SETITEM (PyObject* arr, void* itemptr, PyObject* obj)
Convert obj and place it in the ndarray, arr, at the place pointed to by itemptr. Return -1 if an error occurs or 0 on success.
```

npy_intp PyArray_SIZE (PyObject* arr)

```

Returns the total size (in number of elements) of the array.
npy_intp PyArray_Size (PyObject* obj)
Returns 0 if obj is not a sub-class of bigndarray. Otherwise, returns the total number of elements in the array.
Safer version of PyArray_SIZE (obj).
npy_intp PyArray_NBYTES (PyObject* arr)
Returns the total number of bytes consumed by the array.

\section*{Data access}

These functions and macros provide easy access to elements of the ndarray from C. These work for all arrays. You may need to take care when accessing the data in the array, however, if it is not in machine byte-order, misaligned, or not writeable. In other words, be sure to respect the state of the flags unless you know what you are doing, or have previously guaranteed an array that is writeable, aligned, and in machine byte-order using PyArray_FromAny. If you wish to handle all types of arrays, the copyswap function for each type is useful for handling misbehaved arrays. Some platforms (e.g. Solaris) do not like misaligned data and will crash if you de-reference a misaligned pointer. Other platforms (e.g. x86 Linux) will just work more slowly with misaligned data.
void* PyArray_GetPtr (PyArrayObject* aobj, npy_intp* ind)
Return a pointer to the data of the ndarray, aobj, at the N -dimensional index given by the c-array, ind, (which must be at least aobj ->nd in size). You may want to typecast the returned pointer to the data type of the ndarray.
void* PyArray_GETPTR1 (PyObject* obj, <npy_intp>i)
void* PyArray_GETPTR2 (PyObject* obj, <npy_intp> \(\left.i,<n p y \_i n t p>j\right)\)
void* PyArray_GETPTR3 (PyObject* obj, <npy_intp> \(\left.i,<n p y \_i n t p>j,<n p y \_i n t p>k\right)\)
void* PyArray_GETPTR4 (PyObject* obj, <npy_intp> \(\left.i,<n p y \_i n t p>j,<n p y \_i n t p>k,<n p y \_i n t p>l\right)\)
Quick, inline access to the element at the given coordinates in the ndarray, \(o b j\), which must have respectively 1 , 2 , 3 , or 4 dimensions (this is not checked). The corresponding \(i, j, k\), and \(l\) coordinates can be any integer but will be interpreted as npy_intp. You may want to typecast the returned pointer to the data type of the ndarray.

\subsection*{5.4.2 Creating arrays}

\section*{From scratch}

PyObject* PyArray_NewFromDescr (PyTypeObject* subtype, PyArray_Descr* descr, int nd, npy_intp* dims, npy_intp* strides, void* data, int flags, PyObject* obj)
This is the main array creation function. Most new arrays are created with this flexible function. The returned object is an object of Python-type subtype, which must be a subtype of PyArray_Type. The array has \(n d\) dimensions, described by dims. The data-type descriptor of the new array is descr. If subtype is not \&PyArray_Type (e.g. a Python subclass of the ndarray), then obj is the object to pass to the __array_finalize__ method of the subclass. If data is NULL, then new memory will be allocated and flags can be non-zero to indicate a Fortran-style contiguous array. If data is not NULL, then it is assumed to point to the memory to be used for the array and the flags argument is used as the new flags for the array (except the state of NPY_OWNDATA and UPDATEIFCOPY flags of the new array will be reset). In addition, if data is non-NULL, then strides can also be provided. If strides is NULL, then the array strides are computed as C-style contiguous (default) or Fortran-style contiguous (flags is nonzero for data \(=\) NULL or flags \& NPY_F_CONTIGUOUS is nonzero non-NULL data). Any provided dims and strides are copied into newly allocated dimension and strides arrays for the new array object.
```

PyObject* PyArray_NewLikeArray (PyArrayObject* prototype, NPY_ORDER order, PyArray_Descr*
descr, int subok)

```

New in version 1.6.
This function steals a reference to descr if it is not NULL.
This array creation routine allows for the convenient creation of a new array matching an existing array's shapes and memory layout, possibly changing the layout and/or data type.

When order is NPY_ANYORDER, the result order is NPY_FORTRANORDER if prototype is a fortran array, NPY_CORDER otherwise. When order is NPY_KEEPORDER, the result order matches that of prototype, even when the axes of prototype aren't in C or Fortran order.

If descr is NULL, the data type of prototype is used.
If subok is 1 , the newly created array will use the sub-type of prototype to create the new array, otherwise it will create a base-class array.

PyObject* PyArray_New (PyTypeObject* subtype, int nd, npy_intp* dims, int type_num, npy_intp* strides, void* data, int itemsize, int flags, PyObject* obj)
This is similar to PyArray_DescrNew (...) except you specify the data-type descriptor with type_num and
itemsize, where type_num corresponds to a builtin (or user-defined) type. If the type always has the same number of bytes, then itemsize is ignored. Otherwise, itemsize specifies the particular size of this array.

Warning: If data is passed to PyArray_NewFromDescr or PyArray_New, this memory must not be deallocated until the new array is deleted. If this data came from another Python object, this can be accomplished using Py_INCREF on that object and setting the base member of the new array to point to that object. If strides are passed in they must be consistent with the dimensions, the itemsize, and the data of the array.

PyObject* PyArray_SimpleNew (int \(n d\), npy_intp* dims, int typenum)
Create a new unitialized array of type, typenum, whose size in each of \(n d\) dimensions is given by the integer array, dims. This function cannot be used to create a flexible-type array (no itemsize given).

PyObject* PyArray_SimpleNewFromData (int nd, npy_intp* dims, int typenum, void* data)
Create an array wrapper around data pointed to by the given pointer. The array flags will have a default that the data area is well-behaved and C-style contiguous. The shape of the array is given by the dims c-array of length \(n d\). The data-type of the array is indicated by typenum.

PyObject* PyArray_SimpleNewFromDescr (int nd, npy_intp* dims, PyArray_Descr* descr)
Create a new array with the provided data-type descriptor, descr, of the shape deteremined by \(n d\) and dims.
PyArray_FILLWBYTE (PyObject* obj, int val)
Fill the array pointed to by obj -which must be a (subclass of) bigndarray-with the contents of val (evaluated as a byte).

PyObject* PyArray_Zeros (int nd, npy_intp* dims, PyArray_Descr* dtype, int fortran)
Construct a new nd -dimensional array with shape given by dims and data type given by dtype. If fortran is non-zero, then a Fortran-order array is created, otherwise a C-order array is created. Fill the memory with zeros (or the 0 object if dtype corresponds to PyArray_OBJECT ).
PyObject* PyArray_ZEROS (int \(n d\), npy_intp* dims, int type_num, int fortran)
Macro form of PyArray_Zeros which takes a type-number instead of a data-type object.
PyObject* PyArray_Empty (int nd, npy_intp* dims, PyArray_Descr* dtype, int fortran)
Construct a new nd -dimensional array with shape given by dims and data type given by dtype. If fortran is non-zero, then a Fortran-order array is created, otherwise a C-order array is created. The array is uninitialized unless the data type corresponds to PyArray_OBJECT in which case the array is filled with Py_None.

PyObject* PyArray_EMPTY (int nd, npy_intp* dims, int typenum, int fortran)
Macro form of PyArray_Empty which takes a type-number, typenum, instead of a data-type object.
PyObject* PyArray_Arange (double start, double stop, double step, int typenum)
Construct a new 1-dimensional array of data-type, typenum, that ranges from start to stop (exclusive) in increments of step. Equivalent to arange (start, stop, step, dtype).

PyObject* PyArray_ArangeObj (PyObject* start, PyObject* stop, PyObject* step, PyArray_Descr* de-
scr)
Construct a new 1-dimensional array of data-type determined by descr, that ranges from start to stop (exclusive) in increments of step. Equivalent to arange( start, stop, step, typenum ).

\section*{From other objects}

PyObject* PyArray_FromAny (PyObject* op, PyArray_Descr* dtype, int min_depth, int max_depth, int requirements, PyObject* context)
This is the main function used to obtain an array from any nested sequence, or object that exposes the array interface, op. The parameters allow specification of the required dtype, the minimum (min_depth) and maximum (max_depth) number of dimensions acceptable, and other requirements for the array. The dtype argument needs to be a PyArray_Descr structure indicating the desired data-type (including required byteorder). The dtype argument may be NULL, indicating that any data-type (and byteorder) is acceptable. Unless FORCECAST is
present in flags, this call will generate an error if the data type cannot be safely obtained from the object. If you want to use NULL for the dtype and ensure the array is notswapped then use PyArray_CheckFromAny. A value of 0 for either of the depth parameters causes the parameter to be ignored. Any of the following array flags can be added (e.g. using l) to get the requirements argument. If your code can handle general (e.g. strided, byte-swapped, or unaligned arrays) then requirements may be 0 . Also, if op is not already an array (or does not expose the array interface), then a new array will be created (and filled from \(o p\) using the sequence protocol). The new array will have NPY_DEFAULT as its flags member. The context argument is passed to the __array__ method of op and is only used if the array is constructed that way. Almost always this parameter is NULL.

\section*{NPY_C_CONTIGUOUS}

Make sure the returned array is C-style contiguous

\section*{NPY_F_CONTIGUOUS}

Make sure the returned array is Fortran-style contiguous.

\section*{NPY_ALIGNED}

Make sure the returned array is aligned on proper boundaries for its data type. An aligned array has the data pointer and every strides factor as a multiple of the alignment factor for the data-type- descriptor.

\section*{NPY_WRITEABLE}

Make sure the returned array can be written to.

\section*{NPY_ENSURECOPY}

Make sure a copy is made of \(o p\). If this flag is not present, data is not copied if it can be avoided.

\section*{NPY ENSUREARRAY}

Make sure the result is a base-class ndarray or bigndarray. By default, if \(o p\) is an instance of a subclass of the bigndarray, an instance of that same subclass is returned. If this flag is set, an ndarray object will be returned instead.

\section*{NPY FORCECAST}

Force a cast to the output type even if it cannot be done safely. Without this flag, a data cast will occur only if it can be done safely, otherwise an error is reaised.

\section*{NPY_UPDATEIFCOPY}

If \(o p\) is already an array, but does not satisfy the requirements, then a copy is made (which will satisfy the requirements). If this flag is present and a copy (of an object that is already an array) must be made, then the corresponding NPY_UPDATEIFCOPY flag is set in the returned copy and op is made to be read-only. When the returned copy is deleted (presumably after your calculations are complete), its contents will be copied back into \(o p\) and the \(o p\) array will be made writeable again. If \(o p\) is not writeable to begin with, then an error is raised. If \(o p\) is not already an array, then this flag has no effect.

\section*{NPY BEHAVED}

NPY_ALIGNED I NPY_WRITEABLE

\section*{NPY_CARRAY}

NPY_C_CONTIGUOUS I NPY_BEHAVED
NPY_CARRAY_RO
NPY_C_CONTIGUOUS I NPY_ALIGNED

\section*{NPY_FARRAY}

NPY_F_CONTIGUOUS I NPY_BEHAVED

\section*{NPY_FARRAY_RO}

NPY_F_CONTIGUOUS I NPY_ALIGNED

\section*{NPY_DEFAULT}

NPY_CARRAY

\section*{NPY_IN_ARRAY}

NPY_CONTIGUOUS I NPY_ALIGNED
NPY_IN_FARRAY
NPY_F_CONTIGUOUS I NPY_ALIGNED
NPY_OUT_ARRAY
NPY_C_CONTIGUOUS INPY_WRITEABLE I NPY_ALIGNED
NPY_OUT_FARRAY
NPY_F_CONTIGUOUS I NPY_WRITEABLE I NPY_ALIGNED
NPY_INOUT_ARRAY
NPY_C_CONTIGUOUS I NPY_WRITEABLE I NPY_ALIGNED I NPY_UPDATEIFCOPY
NPY_INOUT_FARRAY
NPY_F_CONTIGUOUS I NPY_WRITEABLE I NPY_ALIGNED I NPY_UPDATEIFCOPY
int PyArray_GetArrayParamsFromObject (PyObject* op, PyArray_Descr* requested_dtype, npy_bool writeable, PyArray_Descr** out_dtype, int* out_ndim, npy_intp* out_dims, PyArrayObject** out_arr, PyObject* context)
New in version 1.6. Retrieves the array parameters for viewing/converting an arbitrary PyObject* to a NumPy array. This allows the "innate type and shape" of Python list-of-lists to be discovered without actually converting to an array. PyArray_FromAny calls this function to analyze its input.
In some cases, such as structured arrays and the __array__ interface, a data type needs to be used to make sense of the object. When this is needed, provide a Descr for 'requested_dtype', otherwise provide NULL. This reference is not stolen. Also, if the requested dtype doesn't modify the interpretation of the input, out_dtype will still get the "innate" dtype of the object, not the dtype passed in 'requested_dtype'.

If writing to the value in 'op' is desired, set the boolean 'writeable' to 1 . This raises an error when 'op' is a scalar, list of lists, or other non-writeable 'op'. This differs from passing NPY_WRITEABLE to PyArray_FromAny, where the writeable array may be a copy of the input.

When success ( 0 return value) is returned, either out_arr is filled with a non-NULL PyArrayObject and the rest of the parameters are untouched, or out_arr is filled with NULL, and the rest of the parameters are filled.

Typical usage:
```

PyArrayObject *arr = NULL;
PyArray_Descr *dtype = NULL;
int ndim = 0;
npy_intp dims[NPY_MAXDIMS];
if (PyArray_GetArrayParamsFromObject(op, NULL, 1, \&dtype,
\&ndim, \&dims, \&arr, NULL) < O) {
return NULL;
}
if (arr == NULL) {
... validate/change dtype, validate flags, ndim, etc ...
// Could make custom strides here too
arr = PyArray_NewFromDescr(\&PyArray_Type, dtype, ndim,
dims, NULL,
fortran ? NPY_F_CONTIGUOUS : 0,
NULL);
if (arr == NULL) {
return NULL;
}
if (PyArray_CopyObject(arr, op) < 0) {
Py_DECREF(arr);

```
```

        return NULL;
        }
    }
else {
... in this case the other parameters weren't filled, just
validate and possibly copy arr itself ...
}
... use arr ...

```

PyObject* PyArray_CheckFromAny (PyObject* op, PyArray_Descr* dtype, int min_depth, int max_depth, int requirements, PyObject* context)
Nearly identical to PyArray_FromAny (...) except requirements can contain NPY_NOTSWAPPED (overriding the specification in dtype) and NPY_ELEMENTSTRIDES which indicates that the array should be aligned in the sense that the strides are multiples of the element size.

\section*{NPY_NOTSWAPPED}

Make sure the returned array has a data-type descriptor that is in machine byte-order, over-riding any specification in the dtype argument. Normally, the byte-order requirement is determined by the dtype argument. If this flag is set and the dtype argument does not indicate a machine byte-order descriptor (or is NULL and the object is already an array with a data-type descriptor that is not in machine byte- order), then a new data-type descriptor is created and used with its byte-order field set to native.

\section*{NPY_BEHAVED_NS}

NPY_ALIGNED I NPY_WRITEABLEINPY_NOTSWAPPED

\section*{NPY_ELEMENTSTRIDES}

Make sure the returned array has strides that are multiples of the element size.
PyObject* PyArray_FromArray (PyArrayObject* op, PyArray_Descr* newtype, int requirements)
Special case of PyArray_FromAny for when op is already an array but it needs to be of a specific newtype (including byte-order) or has certain requirements.

PyObject* PyArray_FromStructInterface (PyObject* op)
Returns an ndarray object from a Python object that exposes the \(\qquad\) array_struct \(\qquad\) - method and follows the array interface protocol. If the object does not contain this method then a borrowed reference to Py_NotImplemented is returned.

PyObject* PyArray_FromInterface (PyObject*op)
Returns an ndarray object from a Python object that exposes the __array_shape__ and __array_typestr__ methods following the array interface protocol. If the object does not contain one of these method then a borrowed reference to Py_Not Implemented is returned.

PyObject* PyArray_FromArrayAttr (PyObject* op, PyArray_Descr* dtype, PyObject* context)
Return an ndarray object from a Python object that exposes the __array__ method. The __array__ method can take 0,1 , or 2 arguments ([dtype, context]) where context is used to pass information about where the __array__ method is being called from (currently only used in ufuncs).

PyObject* PyArray_ContiguousFromAny (PyObject* op, int typenum, int min_depth, int max_depth)
This function returns a (C-style) contiguous and behaved function array from any nested sequence or array interface exporting object, op, of (non-flexible) type given by the enumerated typenum, of minimum depth min_depth, and of maximum depth max_depth. Equivalent to a call to PyArray_FromAny with requirements set to NPY_DEFAULT and the type_num member of the type argument set to typenum.

PyObject *PyArray_FromObject (PyObject *op, int typenum, int min_depth, int max_depth)
Return an aligned and in native-byteorder array from any nested sequence or array-interface exporting object, op, of a type given by the enumerated typenum. The minimum number of dimensions the array can have is given by min_depth while the maximum is max_depth. This is equivalent to a call to PyArray_FromAny with requirements set to BEHAVED.

PyObject* PyArray_EnsureArray (PyObject* op)
This function steals a reference to op and makes sure that op is a base-class ndarray. It special cases array scalars, but otherwise calls PyArray_FromAny (op, NULL, 0, 0, NPY_ENSUREARRAY).

PyObject* PyArray_FromString (char* string, npy_intp slen, PyArray_Descr* dtype, npy_intp num, char* sep)
Construct a one-dimensional ndarray of a single type from a binary or (ASCII) text string of length slen. The data-type of the array to-be-created is given by dtype. If num is -1 , then copy the entire string and return an appropriately sized array, otherwise, num is the number of items to copy from the string. If sep is NULL (or ""), then interpret the string as bytes of binary data, otherwise convert the sub-strings separated by sep to items of data-type dtype. Some data-types may not be readable in text mode and an error will be raised if that occurs. All errors return NULL.

PyObject* PyArray_FromFile (FILE* fp, PyArray_Descr* dtype, npy_intp num, char* sep)
Construct a one-dimensional ndarray of a single type from a binary or text file. The open file pointer is \(f p\), the data-type of the array to be created is given by dtype. This must match the data in the file. If num is -1 , then read until the end of the file and return an appropriately sized array, otherwise, num is the number of items to read. If sep is NULL (or ""), then read from the file in binary mode, otherwise read from the file in text mode with sep providing the item separator. Some array types cannot be read in text mode in which case an error is raised.

PyObject* PyArray_FromBuffer (PyObject* buf, PyArray_Descr* dtype, npy_intp count, npy_intp offset)
Construct a one-dimensional ndarray of a single type from an object, buf, that exports the (single-segment) buffer protocol (or has an attribute __buffer__ that returns an object that exports the buffer protocol). A writeable buffer will be tried first followed by a read- only buffer. The NPY_WRITEABLE flag of the returned array will reflect which one was successful. The data is assumed to start at offset bytes from the start of the memory location for the object. The type of the data in the buffer will be interpreted depending on the datatype descriptor, dtype. If count is negative then it will be determined from the size of the buffer and the requested itemsize, otherwise, count represents how many elements should be converted from the buffer.
int PyArray_CopyInto (PyArrayObject* dest, PyArrayObject* src)
Copy from the source array, src, into the destination array, dest, performing a data-type conversion if necessary. If an error occurs return -1 (otherwise 0 ). The shape of src must be broadcastable to the shape of dest. The data areas of dest and src must not overlap.
int PyArray_MoveInto (PyArrayObject* dest, PyArrayObject* src)
Move data from the source array, src, into the destination array, dest, performing a data-type conversion if necessary. If an error occurs return -1 (otherwise 0 ). The shape of src must be broadcastable to the shape of dest. The data areas of dest and src may overlap.

PyArrayObject* PyArray_GETCONTIGUOUS (PyObject* op)
If op is already (C-style) contiguous and well-behaved then just return a reference, otherwise return a (contiguous and well-behaved) copy of the array. The parameter op must be a (sub-class of an) ndarray and no checking for that is done.

PyObject* PyArray_FROM_O (PyObject* obj)
Convert obj to an ndarray. The argument can be any nested sequence or object that exports the array interface. This is a macro form of PyArray_FromAny using NULL, \(0,0,0\) for the other arguments. Your code must be able to handle any data-type descriptor and any combination of data-flags to use this macro.

PyObject* PyArray_FROM_OF (PyObject* obj, int requirements)
Similar to PYArray_FROM_O except it can take an argument of requirements indicating properties the resulting array must have. Available requirements that can be enforced are NPY_CONTIGUOUS, NPY_F_CONTIGUOUS, NPY_ALIGNED, NPY_WRITEABLE, NPY_NOTSWAPPED, NPY_ENSURECOPY, NPY_UPDATEIFCOPY, NPY_FORCECAST, and NPY_ENSUREARRAY. Standard combinations of flags can also be used:

PyObject* PyArray_FROM_OT (PyObject* obj, int typenum)
Similar to PyArray_FROM_O except it can take an argument of typenum specifying the type-number the returned array.

PyObject* PyArray_FROM_OTF (PyObject* obj, int typenum, int requirements)
Combination of PyArray_FROM_OF and PyArray_FROM_OT allowing both a typenum and a flags argument to be provided..

PyObject* PyArray_FROMANY (PyObject* obj, int typenum, int min, int max, int requirements)
Similar to PyArray_FromAny except the data-type is specified using a typenumber. PyArray_DescrFromType (typenum) is passed directly to PyArray_FromAny. This macro also adds NPY_DEFAULT to requirements if NPY_ENSURECOPY is passed in as requirements.

PyObject *PyArray_CheckAxis (PyObject* obj, int* axis, int requirements)
Encapsulate the functionality of functions and methods that take the axis= keyword and work properly with None as the axis argument. The input array is obj, while *axis is a converted integer (so that >=MAXDIMS is the None value), and requirements gives the needed properties of obj. The output is a converted version of the input so that requirements are met and if needed a flattening has occurred. On output negative values of *axis are converted and the new value is checked to ensure consistency with the shape of obj.

\subsection*{5.4.3 Dealing with types}

\section*{General check of Python Type}

\section*{PyArray_Check (op)}

Evaluates true if op is a Python object whose type is a sub-type of PyArray_Type.
PyArray_CheckExact (op)
Evaluates true if \(o p\) is a Python object with type PyArray_Type.
PyArray_HasArrayInterface (op, out)
If op implements any part of the array interface, then out will contain a new reference to the newly created ndarray using the interface or out will contain NULL if an error during conversion occurs. Otherwise, out will contain a borrowed reference to Py_Not Implemented and no error condition is set.

PyArray_HasArrayInterfaceType (op, type, context, out)
If op implements any part of the array interface, then out will contain a new reference to the newly created ndarray using the interface or out will contain NULL if an error during conversion occurs. Otherwise, out will contain a borrowed reference to Py_NotImplemented and no error condition is set. This version allows setting of the type and context in the part of the array interface that looks for the __array__ attribute.

PyArray_IsZeroDim(op)
Evaluates true if \(o p\) is an instance of (a subclass of) PyArray_Type and has 0 dimensions.
PyArray_IsScalar (op, cls)
Evaluates true if \(o p\) is an instance of Py\{cls \}ArrType_Type.
PyArray_CheckScalar (op)
Evaluates true if \(o p\) is either an array scalar (an instance of a sub-type of PyGenericArr_Type ), or an instance of (a sub-class of) PyArray_Type whose dimensionality is 0 .

PyArray_IsPythonScalar (op)
Evaluates true if \(o p\) is a builtin Python "scalar" object (int, float, complex, str, unicode, long, bool).
PyArray_IsAnyScalar(op)
Evaluates true if op is either a Python scalar or an array scalar (an instance of a sub- type of PyGenericArr_Type).

\section*{Data-type checking}

For the typenum macros, the argument is an integer representing an enumerated array data type. For the array type checking macros the argument must be a PyObject * that can be directly interpreted as a PyArrayObject *.
```

PYTypeNum_ISUNSIGNED (num)
PyDataType_ISUNSIGNED (descr)
PyArray_ISUNSIGNED (obj)
Type represents an unsigned integer.
PyTypeNum_ISSIGNED (num)
PyDataType_ISSIGNED (descr)
PyArray_ISSIGNED (obj)
Type represents a signed integer.
PyTypeNum_ISINTEGER(num)
PyDataType_ISINTEGER(descr)
PyArray_ISINTEGER(obj)
Type represents any integer.
PyTypeNum_ISFLOAT (num)
PyDataType_ISFLOAT (descr)
PyArray_ISFLOAT (obj)
Type represents any floating point number.
PyTypeNum_ISCOMPLEX(num)
PyDataType_ISCOMPLEX(descr)
PyArray_ISCOMPLEX (obj)
Type represents any complex floating point number.
PYTypeNum_ISNUMBER(num)
PyDataType_ISNUMBER(descr)
PyArray_ISNUMBER(obj)
Type represents any integer, floating point, or complex floating point number.
PyTypeNum_ISSTRING(num)
PyDataType_ISSTRING (descr)

```
```

PyArray_ISSTRING (obj)
Type represents a string data type.
PyTypeNum_ISPYTHON(num)
PyDataType_ISPYTHON (descr)
PyArray_ISPYTHON(obj)
Type represents an enumerated type corresponding to one of the standard Python scalar (bool, int, float, or
complex).
PyTypeNum_ISFLEXIBLE (num)
PyDataType_ISFLEXIBLE (descr)
PyArray_ISFLEXIBLE (obj)
Type represents one of the flexible array types (NPY_STRING, NPY_UNICODE, or NPY_VOID ).
PyTypeNum_ISUSERDEF(num)
PyDataType_ISUSERDEF (descr)
PyArray_ISUSERDEF (obj)
Type represents a user-defined type.
PyTypeNum_ISEXTENDED (num)
PyDataType_ISEXTENDED (descr)
PyArray_ISEXTENDED(obj)
Type is either flexible or user-defined.
PyTypeNum_ISOBJECT (num)
PyDataType_ISOBJECT (descr)
PyArray_ISOBJECT(obj)
Type represents object data type.
PyTypeNum_ISBOOL (num)
PyDataType_ISBOOL (descr)
PyArray_ISBOOL (obj)
Type represents Boolean data type.
PyDataType_HASFIELDS (descr)
PyArray_HASFIELDS (obj)
Type has fields associated with it.

```

\section*{PyArray_ISNOTSWAPPED (m)}

Evaluates true if the data area of the ndarray \(m\) is in machine byte-order according to the array's data-type descriptor.

PyArray_ISBYTESWAPPED (m)
Evaluates true if the data area of the ndarray \(m\) is not in machine byte-order according to the array's data-type descriptor.

Bool PyArray_EquivTypes (PyArray_Descr* type1, PyArray_Descr* type2)
Return NPY_TRUE if typel and type2 actually represent equivalent types for this platform (the fortran member of each type is ignored). For example, on 32-bit platforms, NPY_LONG and NPY_INT are equivalent. Otherwise return NPY_FALSE.

Bool PyArray_EquivArrTypes (PyArrayObject* al, PyArrayObject * a2)
Return NPY_TRUE if \(a 1\) and \(a 2\) are arrays with equivalent types for this platform.
Bool PyArray_EquivTypenums (int typenum1, int typenum2)
Special case of PyArray_EquivTypes (...) that does not accept flexible data types but may be easier to call.
int PyArray_EquivByteorders (\{byteorder\} bl, \{byteorder\} b2)
True if byteorder characters ( NPY_LITTLE, NPY_BIG, NPY_NATIVE, NPY_IGNORE ) are either equal or equivalent as to their specification of a native byte order. Thus, on a little-endian machine NPY_LITTLE and NPY_NATIVE are equivalent where they are not equivalent on a big-endian machine.

\section*{Converting data types}

PyObject* PyArray_Cast (PyArrayObject* arr, int typenum)
Mainly for backwards compatibility to the Numeric C-API and for simple casts to non-flexible types. Return a new array object with the elements of arr cast to the data-type typenum which must be one of the enumerated types and not a flexible type.

PyObject* PyArray_CastToType (PyArrayObject* arr, PyArray_Descr* type, int fortran)
Return a new array of the type specified, casting the elements of arr as appropriate. The fortran argument specifies the ordering of the output array.
int PyArray_CastTo (PyArrayObject* out, PyArrayObject* in)
As of 1.6 , this function simply calls PyArray_CopyInto, which handles the casting.
Cast the elements of the array in into the array out. The output array should be writeable, have an integermultiple of the number of elements in the input array (more than one copy can be placed in out), and have a data type that is one of the builtin types. Returns 0 on success and -1 if an error occurs.

PyArray_VectorUnaryFunc* PyArray_GetCastFunc (PyArray_Descr* from, int totype)
Return the low-level casting function to cast from the given descriptor to the builtin type number. If no casting function exists return NULL and set an error. Using this function instead of direct access to from \(->f->\) cast will allow support of any user-defined casting functions added to a descriptors casting dictionary.
int PyArray_CanCastSafely (int fromtype, int totype)
Returns non-zero if an array of data type fromtype can be cast to an array of data type totype without losing information. An exception is that 64-bit integers are allowed to be cast to 64 -bit floating point values even though this can lose precision on large integers so as not to proliferate the use of long doubles without explict requests. Flexible array types are not checked according to their lengths with this function.
int PyArray_CanCastTo (PyArray_Descr* fromtype, PyArray_Descr* totype)
PyArray_CanCast TypeTo supercedes this function in NumPy 1.6 and later.
Equivalent to PyArray_CanCastTypeTo(fromtype, totype, NPY_SAFE_CASTING).
int PyArray_CanCastTypeTo (PyArray_Descr* fromtype, PyArray_Descr* totype, NPY_CASTING casting)
New in version 1.6. Returns non-zero if an array of data type fromtype (which can include flexible types) can be cast safely to an array of data type totype (which can include flexible types) according to the casting rule casting. For simple types with NPY_SAFE_CASTING, this is basically a wrapper around PyArray_CanCastSafely, but for flexible types such as strings or unicode, it produces results taking into account their sizes.
int PyArray_CanCastArrayTo (PyArrayObject* arr, PyArray_Descr* totype, NPY_CASTING casting)
New in version 1.6. Returns non-zero if arr can be cast to totype according to the casting rule given in casting. If arr is an array scalar, its value is taken into account, and non-zero is also returned when the value will not overflow or be truncated to an integer when converting to a smaller type.
PyArray_Descr* PyArray_MinScalarType (PyArrayObject* arr)
New in version 1.6. If arr is an array, returns its data type descriptor, but if arr is an array scalar (has 0 dimensions), it finds the data type of smallest kind and size to which the value may be converted without overflow or truncation to an integer.

PyArray_Descr* PyArray_PromoteTypes (PyArray_Descr* type1, PyArray_Descr* type2)
New in version 1.6. Finds the data type of smallest size and kind to which typel and type2 may be safely converted.

PyArray_Descr* PyArray_ResultType (npy_intp narrs, PyArrayObject**arrs, npy_intp ndtypes, PyArray_Descr**dtypes)
New in version 1.6. This applies PyArray_PromoteTypes to all the inputs, along with using the NumPy rules for combining scalars and arrays, to determine the output type of a set of operands. This is the same result type that ufuncs produce.
int PyArray_Object Type (PyObject* op, int mintype)
This function is superceded by PyArray_MinScalarType and/or PyArray_ResultType.
This function is useful for determining a common type that two or more arrays can be converted to. It only works for non-flexible array types as no itemsize information is passed. The mintype argument represents the minimum type acceptable, and \(o p\) represents the object that will be converted to an array. The return value is the enumerated typenumber that represents the data-type that \(o p\) should have.
void PyArray_ArrayType (PyObject* op, PyArray_Descr* mintype, PyArray_Descr* outtype)
This function is superceded by PyArray_ResultType.
This function works similarly to PyArray_ObjectType (...) except it handles flexible arrays. The mintype argument can have an itemsize member and the outtype argument will have an itemsize member at least as big but perhaps bigger depending on the object \(o p\).

PyArrayObject** PyArray_ConvertToCommonType (PyObject*op, int* \(n\) )
The functionality this provides is largely superceded by iterator NpyIter introduced in 1.6, with flag NPY_ITER_COMMON_DTYPE or with the same dtype parameter for all operands.
Convert a sequence of Python objects contained in \(o p\) to an array of ndarrays each having the same data type. The type is selected based on the typenumber (larger type number is chosen over a smaller one) ignoring objects that are only scalars. The length of the sequence is returned in \(n\), and an \(n\)-length array of PyArrayobject pointers is the return value (or NULL if an error occurs). The returned array must be freed by the caller of this routine (using PyDataMem_FREE ) and all the array objects in it DECREF 'd or a memory-leak will occur. The example template-code below shows a typically usage:
```

mps = PyArray_ConvertToCommonType(obj, \&n);
if (mps==NULL) return NULL;
{code}
<before return>
for (i=0; i<n; i++) Py_DECREF(mps[i]);

```

PyDataMem_FREE (mps);
\{return \}
char* PyArray_Zero (PyArrayObject* arr)
A pointer to newly created memory of size arr \(->\) itemsize that holds the representation of 0 for that type. The returned pointer, ret, must be freed using PyDataMem_FREE (ret) when it is not needed anymore.
char* PyArray_One (PyArrayObject* arr)
A pointer to newly created memory of size arr ->itemsize that holds the representation of 1 for that type. The returned pointer, ret, must be freed using PyDataMem_FREE (ret) when it is not needed anymore.
int PyArray_ValidType (int typenum)
Returns NPY_TRUE if typenum represents a valid type-number (builtin or user-defined or character code). Otherwise, this function returns NPY_FALSE.

\section*{New data types}
void PyArray_InitArrFuncs (PyArray_ArrFuncs* \(f\) )
Initialize all function pointers and members to NULL.
int PyArray_RegisterDataType (PyArray_Descr* dtype)
Register a data-type as a new user-defined data type for arrays. The type must have most of its entries filled in. This is not always checked and errors can produce segfaults. In particular, the typeobj member of the dtype structure must be filled with a Python type that has a fixed-size element-size that corresponds to the elsize member of dtype. Also the \(f\) member must have the required functions: nonzero, copyswap, copyswapn, getitem, setitem, and cast (some of the cast functions may be NULL if no support is desired). To avoid confusion, you should choose a unique character typecode but this is not enforced and not relied on internally.

A user-defined type number is returned that uniquely identifies the type. A pointer to the new structure can then be obtained from PyArray_DescrFromType using the returned type number. A -1 is returned if an error occurs. If this dtype has already been registered (checked only by the address of the pointer), then return the previously-assigned type-number.
int PyArray_RegisterCastFunc (PyArray_Descr* descr, int totype, PyArray_VectorUnaryFunc* castfunc)
Register a low-level casting function, castfunc, to convert from the data-type, descr, to the given data-type number, totype. Any old casting function is over-written. A 0 is returned on success or a -1 on failure.
int PyArray_RegisterCanCast (PyArray_Descr* descr, int totype, PyArray_SCALARKIND scalar)
Register the data-type number, totype, as castable from data-type object, descr, of the given scalar kind. Use scalar \(=\) NPY_NOSCALAR to register that an array of data-type descr can be cast safely to a data-type whose type_number is totype.

\section*{Special functions for PyArray_OBJECT}
int PyArray_INCREF (PyArrayObject*op)
Used for an array, op, that contains any Python objects. It increments the reference count of every object in the array according to the data-type of \(o p\). A -1 is returned if an error occurs, otherwise 0 is returned.
void PyArray_Item_INCREF (char* ptr, PyArray_Descr* dtype)
A function to INCREF all the objects at the location ptr according to the data-type dtype. If ptr is the start of a record with an object at any offset, then this will (recursively) increment the reference count of all object-like items in the record.
int PyArray_XDECREF (PyArrayObject* op)
Used for an array, \(o p\), that contains any Python objects. It decrements the reference count of every object in the array according to the data-type of \(o p\). Normal return value is 0 . A -1 is returned if an error occurs.
void PyArray_Item_XDECREF (char* ptr, PyArray_Descr* dtype)
A function to XDECREF all the object-like items at the loacation ptr as recorded in the data-type, dtype. This works recursively so that if dtype itself has fields with data-types that contain object-like items, all the object-like fields will be XDECREF \({ }^{\prime} \mathrm{d}\).
void PyArray_FillObjectArray (PyArrayObject* arr, PyObject* obj)
Fill a newly created array with a single value obj at all locations in the structure with object data-types. No checking is performed but arr must be of data-type PyArray_OBJECT and be single-segment and uninitialized (no previous objects in position). Use PyArray_DECREF (arr) if you need to decrement all the items in the object array prior to calling this function.

\subsection*{5.4.4 Array flags}

The flags attribute of the PyArrayObject structure contains important information about the memory used by the array (pointed to by the data member) This flag information must be kept accurate or strange results and even segfaults may result.

There are 6 (binary) flags that describe the memory area used by the data buffer. These constants are defined in arrayobject. h and determine the bit-position of the flag. Python exposes a nice attribute- based interface as well as a dictionary-like interface for getting (and, if appropriate, setting) these flags.

Memory areas of all kinds can be pointed to by an ndarray, necessitating these flags. If you get an arbitrary PyArrayObject in C-code, you need to be aware of the flags that are set. If you need to guarantee a certain kind of array (like NPY_C_CONTIGUOUS and NPY_BEHAVED), then pass these requirements into the PyArray_FromAny function.

\section*{Basic Array Flags}

An ndarray can have a data segment that is not a simple contiguous chunk of well-behaved memory you can manipulate. It may not be aligned with word boundaries (very important on some platforms). It might have its data in a different byte-order than the machine recognizes. It might not be writeable. It might be in Fortan-contiguous order. The array flags are used to indicate what can be said about data associated with an array.

\section*{NPY_C_CONTIGUOUS}

The data area is in C-style contiguous order (last index varies the fastest).

\section*{NPY_F_CONTIGUOUS}

The data area is in Fortran-style contiguous order (first index varies the fastest).
Notice that contiguous 1-d arrays are always both Fortran contiguous and C contiguous. Both of these flags can be checked and are convenience flags only as whether or not an array is NPY_C_CONTIGUOUS or NPY_F_CONTIGUOUS can be determined by the strides, dimensions, and itemsize attributes.

\section*{NPY_OWNDATA}

The data area is owned by this array.

\section*{NPY_ALIGNED}

The data area is aligned appropriately (for all strides).

\section*{NPY_WRITEABLE}

The data area can be written to.
Notice that the above 3 flags are are defined so that a new, well- behaved array has these flags defined as true.

\section*{NPY UPDATEIFCOPY}

The data area represents a (well-behaved) copy whose information should be transferred back to the original when this array is deleted.

This is a special flag that is set if this array represents a copy made because a user required certain flags in PyArray_FromAny and a copy had to be made of some other array (and the user asked for this flag to be set in such a situation). The base attribute then points to the "misbehaved" array (which is set read_only). When the array with this flag set is deallocated, it will copy its contents back to the "misbehaved" array (casting if necessary) and will reset the "misbehaved" array to NPY_WRITEABLE. If the "misbehaved" array was not NPY_WRITEABLE to begin with then PYArray_FromAny would have returned an error because NPY_UPDATEIFCOPY would not have been possible.

PyArray_UpdateFlags (obj, flags) will update the obj->flags for flags which can be any of NPY_C_CONTIGUOUS, NPY_F_CONTIGUOUS, NPY_ALIGNED, or NPY_WRITEABLE.

\section*{Combinations of array flags}

NPY_BEHAVED
NPY_ALIGNED I NPY_WRITEABLE

\section*{NPY_CARRAY}

NPY_C_CONTIGUOUS I NPY_BEHAVED
NPY_CARRAY_RO
NPY_C_CONTIGUOUS I NPY_ALIGNED

\section*{NPY_FARRAY}

NPY_F_CONTIGUOUS I NPY_BEHAVED

\section*{NPY_FARRAY_RO}

NPY_F_CONTIGUOUS I NPY_ALIGNED

\section*{NPY_DEFAULT}

NPY_CARRAY
NPY_UPDATE_ALL
NPY_C_CONTIGUOUS I NPY_F_CONTIGUOUS I NPY_ALIGNED

\section*{Flag-like constants}

These constants are used in PyArray_FromAny (and its macro forms) to specify desired properties of the new array.

\section*{NPY_FORCECAST}

Cast to the desired type, even if it can't be done without losing information.

\section*{NPY_ENSURECOPY}

Make sure the resulting array is a copy of the original.

\section*{NPY_ENSUREARRAY}

Make sure the resulting object is an actual ndarray (or bigndarray), and not a sub-class.

\section*{NPY_NOTSWAPPED}

Only used in PyArray_CheckFromAny to over-ride the byteorder of the data-type object passed in.

\section*{NPY_BEHAVED_NS}

NPY_ALIGNED I NPY_WRITEABLEINPY_NOTSWAPPED

\section*{Flag checking}

For all of these macros arr must be an instance of a (subclass of) PyArray_Type, but no checking is done.

\section*{PyArray_CHKFLAGS (arr, flags)}

The first parameter, arr, must be an ndarray or subclass. The parameter, flags, should be an integer consisting of bitwise combinations of the possible flags an array can have: NPY_C_CONTIGUOUS, NPY_F_CONTIGUOUS, NPY_OWNDATA, NPY_ALIGNED, NPY_WRITEABLE, NPY_UPDATEIFCOPY.

PyArray_ISCONTIGUOUS (arr) Evaluates true if arr is C-style contiguous.

\section*{PyArray_ISFORTRAN (arr)}

Evaluates true if arr is Fortran-style contiguous.

\section*{PyArray_ISWRITEABLE (arr)}

Evaluates true if the data area of arr can be written to

\section*{PyArray_ISALIGNED (arr)}

Evaluates true if the data area of \(a r r\) is properly aligned on the machine.

\section*{PyArray_ISBEHAVED (arr)}

Evalutes true if the data area of arr is aligned and writeable and in machine byte-order according to its descriptor.

\section*{PyArray_ISBEHAVED_RO (arr)}

Evaluates true if the data area of arr is aligned and in machine byte-order.

\section*{PyArray_ISCARRAY (arr)}

Evaluates true if the data area of \(\operatorname{arr}\) is C-style contiguous, and PyArray_ISBEHAVED (arr) is true.

\section*{PyArray_ISFARRAY (arr)}

Evaluates true if the data area of \(\operatorname{arr}\) is Fortran-style contiguous and PyArray_ISBEHAVED (arr) is true.

\section*{PyArray_ISCARRAY_RO (arr)}

Evaluates true if the data area of \(a r r\) is C-style contiguous, aligned, and in machine byte-order.
PyArray_ISFARRAY_RO (arr)
Evaluates true if the data area of arr is Fortran-style contiguous, aligned, and in machine byte-order .

\section*{PyArray_ISONESEGMENT (arr)}

Evaluates true if the data area of arr consists of a single (C-style or Fortran-style) contiguous segment.
void PyArray_UpdateFlags (PyArrayObject* arr, int flagmask)
The NPY_C_CONTIGUOUS, NPY_ALIGNED, and NPY_F_CONTIGUOUS array flags can be "calculated" from the array object itself. This routine updates one or more of these flags of arr as specified in flagmask by performing the required calculation.

Warning: It is important to keep the flags updated (using PyArray_UpdateFlags can help) whenever a manipulation with an array is performed that might cause them to change. Later calculations in NumPy that rely on the state of these flags do not repeat the calculation to update them.

\subsection*{5.4.5 Array method alternative API}

\section*{Conversion}

PyObject* PyArray_GetField (PyArrayObject* self, PyArray_Descr* dtype, int offset)
Equivalent to ndarray.getfield (self, dtype, offset). Return a new array of the given dtype using the data in the current array at a specified offset in bytes. The offset plus the itemsize of the new array type must be less than self \(->\) descr->elsize or an error is raised. The same shape and strides as the original array are used. Therefore, this function has the effect of returning a field from a record array. But, it can also be used to select specific bytes or groups of bytes from any array type.
int PyArray_SetField (PyArrayObject* self, PyArray_Descr* dtype, int offset, PyObject* val)
Equivalent to ndarray.setfield (self, val, dtype, offset). Set the field starting at offset in bytes and of the given dtype to val. The offset plus dtype ->elsize must be less than self ->descr->elsize or an error is raised. Otherwise, the val argument is converted to an array and copied into the field pointed to. If necessary, the elements of val are repeated to fill the destination array, But, the number of elements in the destination must be an integer multiple of the number of elements in val.

PyObject* PyArray_Byteswap (PyArrayObject* self, Bool inplace)
Equivalent to ndarray.byteswap (self, inplace). Return an array whose data area is byteswapped. If inplace is non-zero, then do the byteswap inplace and return a reference to self. Otherwise, create a byteswapped copy and leave self unchanged.

PyObject* PyArray_NewCopy (PyArrayObject* old, NPY_ORDER order)
Equivalent to ndarray.copy (self, fortran). Make a copy of the old array. The returned array is always aligned and writeable with data interpreted the same as the old array. If order is NPY_CORDER, then a C-style contiguous array is returned. If order is NPY_FORTRANORDER, then a Fortran-style contiguous array is returned. If order is NPY_ANYORDER, then the array returned is Fortran-style contiguous only if the old one is; otherwise, it is C-style contiguous.
PyObject* PyArray_ToList (PyArrayObject* self) Equivalent to ndarray.tolist (self). Return a nested Python list from self.

PyObject* PyArray_ToString (PyArrayObject* self, NPY_ORDER order)
Equivalent to ndarray.tostring (self, order). Return the bytes of this array in a Python string.
PyObject* PyArray_ToFile (PyArrayObject* self, FILE* fp, char* sep, char* format)
Write the contents of self to the file pointer \(f p\) in C -style contiguous fashion. Write the data as binary bytes if sep is the string ""or NULL. Otherwise, write the contents of self as text using the sep string as the item separator. Each item will be printed to the file. If the format string is not NULL or "", then it is a Python print statement format string showing how the items are to be written.
int PyArray_Dump (PyObject* self, PyObject* file, int protocol)
Pickle the object in self to the given file (either a string or a Python file object). If file is a Python string it is considered to be the name of a file which is then opened in binary mode. The given protocol is used (if protocol is negative, or the highest available is used). This is a simple wrapper around cPickle.dump(self, file, protocol).

PyObject* PyArray_Dumps (PyObject* self, int protocol)
Pickle the object in self to a Python string and return it. Use the Pickle protocol provided (or the highest available if protocol is negative).
int PyArray_FillWithScalar (PyArrayObject* arr, PyObject* obj)
Fill the array, arr, with the given scalar object, obj. The object is first converted to the data type of arr, and then copied into every location. A - 1 is returned if an error occurs, otherwise 0 is returned.

PyObject* PyArray_View (PyArrayObject* self, PyArray_Descr* dtype)
Equivalent to ndarray.view (self,dtype). Return a new view of the array self as possibly a different datatype, dtype. If dtype is NULL, then the returned array will have the same data type as self. The new data-type must be consistent with the size of self. Either the itemsizes must be identical, or self must be single-segment and the total number of bytes must be the same. In the latter case the dimensions of the returned array will be altered in the last (or first for Fortran-style contiguous arrays) dimension. The data area of the returned array and self is exactly the same.

\section*{Shape Manipulation}

PyObject* PyArray_Newshape (PyArrayObject* self, PyArray_Dims* newshape)
Result will be a new array (pointing to the same memory location as self if possible), but having a shape given by newshape. If the new shape is not compatible with the strides of self, then a copy of the array with the new specified shape will be returned.

PyObject* PyArray_Reshape (PyArrayObject* self, PyObject* shape)
Equivalent to ndarray.reshape (self, shape) where shape is a sequence. Converts shape to a PyArray_Dims structure and calls PyArray_Newshape internally.
PyObject* PyArray_Squeeze (PyArrayObject* self)
Equivalent to ndarray. squeeze (self). Return a new view of self with all of the dimensions of length 1 removed from the shape.

Warning: matrix objects are always 2-dimensional. Therefore, PyArray_Squeeze has no effect on arrays of matrix sub-class.

PyObject* PyArray_SwapAxes (PyArrayObject* self, int al, int a2)
Equivalent to ndarray. swapaxes (self, a1, a2). The returned array is a new view of the data in self with the given axes, al and a2, swapped.

PyObject* PyArray_Resize (PyArrayObject* self, PyArray_Dims* newshape, int refcheck, NPY_ORDER fortran)
Equivalent to ndarray.resize (self, newshape, refcheck = refcheck, order= fortran ). This function only works on single-segment arrays. It changes the shape of self inplace and will reallocate the memory for self if newshape has a different total number of elements then the old shape. If reallocation is necessary, then self must own its data, have self \(->\) base==NULL, have self \(->\) weakrefs \(==\) NULL, and (unless refcheck is 0 ) not be referenced by any other array. A reference to the new array is returned. The fortran argument can be NPY_ANYORDER, NPY_CORDER, or NPY_FORTRANORDER. It currently has no effect. Eventually it could be used to determine how the resize operation should view the data when constructing a differently-dimensioned array.

\section*{PyObject* PyArray_Transpose (PyArrayObject* self, PyArray_Dims* permute)}

Equivalent to ndarray.transpose (self, permute). Permute the axes of the ndarray object self according to the data structure permute and return the result. If permute is NULL, then the resulting array has its axes reversed. For example if self has shape \(10 \times 20 \times 30\), and permute .ptr is \((0,2,1)\) the shape of the result is \(10 \times 30 \times 20\). If permute is NULL, the shape of the result is \(30 \times 20 \times 10\).
PyObject* PyArray_Flatten (PyArrayObject* self, NPY_ORDER order)
Equivalent to ndarray.flatten (self, order). Return a 1-d copy of the array. If order is NPY_FORTRANORDER the elements are scanned out in Fortran order (first-dimension varies the fastest). If order is NPY_CORDER, the elements of self are scanned in C-order (last dimension varies the fastest). If order NPY_ANYORDER, then the result of PyArray_ISFORTRAN (self) is used to determine which order to flatten.

PyObject* PyArray_Ravel (PyArrayObject* self, NPY_ORDER order)
Equivalent to self.ravel(order). Same basic functionality as PyArray_Flatten (self, order) except if order is 0 and self is C-style contiguous, the shape is altered but no copy is performed.

\section*{Item selection and manipulation}

PyObject* PyArray_TakeFrom (PyArrayObject* self, PyObject* indices, int axis, PyArrayObject* ret, NPY_CLIPMODE clipmode)
Equivalent to ndarray.take (self, indices, axis, ret, clipmode) except axis =None in Python is obtained by setting axis \(=\) NPY_MAXDIMS in C. Extract the items from self indicated by the integer-valued indices along the given axis. The clipmode argument can be NPY_RAISE, NPY_WRAP, or NPY_CLIP to indicate what to do with out-of-bound indices. The ret argument can specify an output array rather than having one created internally.
```

PyObject* PyArray_PutTo (PyArrayObject* self, PyObject* values, PyObject* indices, NPY_CLIPMODE clipmode)

```

Equivalent to self.put(values, indices, clipmode ). Put values into self at the corresponding (flattened) indices. If values is too small it will be repeated as necessary.

PyObject* PyArray_PutMask (PyArrayObject* self, PyObject* values, PyObject* mask)
Place the values in self wherever corresponding positions (using a flattened context) in mask are true. The mask and self arrays must have the same total number of elements. If values is too small, it will be repeated as necessary.

PyObject* PyArray_Repeat (PyArrayObject* self, PyObject* op, int axis)
Equivalent to ndarray. repeat (self, op, axis). Copy the elements of self, op times along the given axis. Either \(o p\) is a scalar integer or a sequence of length self \(->\) dimensions[ axis ] indicating how many times to repeat each item along the axis.

PyObject* PyArray_Choose (PyArrayObject* self, PyObject* op, PyArrayObject* ret, NPY_CLIPMODE clipmode)
Equivalent to ndarray. choose (self, op, ret, clipmode). Create a new array by selecting elements from the sequence of arrays in \(o p\) based on the integer values in self. The arrays must all be broadcastable to the same shape and the entries in self should be between 0 and len \((o p)\). The output is placed in ret unless it is NULL in which case a new output is created. The clipmode argument determines behavior for when entries in self are not between 0 and len \((o p)\).

\section*{NPY_RAISE}
raise a ValueError;

\section*{NPY_WRAP}
wrap values \(<0\) by adding len \((o p)\) and values \(>=\operatorname{len}(o p)\) by subtracting len \((o p)\) until they are in range;
NPY_CLIP
all values are clipped to the region \([0, \operatorname{len}(o p))\).
PyObject* PyArray_Sort (PyArrayObject* self, int axis)
Equivalent to ndarray. sort (self, axis). Return an array with the items of self sorted along axis.
PyObject* PyArray_ArgSort (PyArrayObject* self, int axis)
Equivalent to ndarray. argsort (self, axis). Return an array of indices such that selection of these indices along the given axis would return a sorted version of self. If self \(->\) descr is a data-type with fields defined, then self->descr->names is used to determine the sort order. A comparison where the first field is equal will use the second field and so on. To alter the sort order of a record array, create a new data-type with a different order of names and construct a view of the array with that new data-type.
PyObject* PyArray_LexSort (PyObject* sort_keys, int axis)
Given a sequence of arrays (sort_keys) of the same shape, return an array of indices (similar to PyArray_ArgSort (...)) that would sort the arrays lexicographically. A lexicographic sort specifies that when two keys are found to be equal, the order is based on comparison of subsequent keys. A merge sort (which leaves equal entries unmoved) is required to be defined for the types. The sort is accomplished by sorting the indices first using the first sort_key and then using the second sort_key and so forth. This is equivalent to the lexsort(sort_keys, axis) Python command. Because of the way the merge-sort works, be sure to understand the order the sort_keys must be in (reversed from the order you would use when comparing two elements).

If these arrays are all collected in a record array, then PyArray_Sort (...) can also be used to sort the array directly.
PyObject* PyArray_SearchSorted (PyArrayObject* self, PyObject* values)
Equivalent to ndarray.searchsorted (self, values). Assuming self is a 1-d array in ascending order representing bin boundaries then the output is an array the same shape as values of bin numbers, giving the bin into which each item in values would be placed. No checking is done on whether or not self is in ascending order.

PyObject* PyArray_Diagonal (PyArrayObject* self, int offset, int axis1, int axis2)
Equivalent to ndarray. diagonal (self, offset, axisl, axis2 ). Return the offset diagonals of the 2-d arrays defined by axis 1 and axis 2 .
npy_intp PyArray_CountNonzero (PyArrayObject* self)
New in version 1.6. Counts the number of non-zero elements in the array object self.
PyObject* PyArray_Nonzero (PyArrayObject* self)
Equivalent to ndarray.nonzero (self). Returns a tuple of index arrays that select elements of self that are nonzero. If (nd= PyArray_NDIM ( self ))==1, then a single index array is returned. The index arrays have data type NPY_INTP. If a tuple is returned ( \(n d \neq 1\) ), then its length is nd.

PyObject* PyArray_Compress (PyArrayObject* self, PyObject* condition, int axis, PyArrayObject* out)
Equivalent to ndarray. compress (self, condition, axis ). Return the elements along axis corresponding to elements of condition that are true.

\section*{Calculation}

Tip: Pass in NPY_MAXDIMS for axis in order to achieve the same effect that is obtained by passing in axis = None in Python (treating the array as a 1-d array).

PyObject* PyArray_ArgMax (PyArrayObject* self, int axis)
Equivalent to ndarray. argmax (self, axis). Return the index of the largest element of self along axis.
PyObject* PyArray_ArgMin (PyArrayObject* self, int axis)
Equivalent to ndarray .argmin (self, axis). Return the index of the smallest element of self along axis.
PyObject* PyArray_Max (PyArrayObject* self, int axis, PyArrayObject* out)
Equivalent to ndarray.max (self, axis). Return the largest element of self along the given axis.
PyObject* PyArray_Min (PyArrayObject* self, int axis, PyArrayObject* out)
Equivalent to ndarray.min (self, axis). Return the smallest element of self along the given axis.
PyObject* PyArray_Ptp (PyArrayObject* self, int axis, PyArrayObject* out)
Equivalent to ndarray.ptp (self, axis). Return the difference between the largest element of self along axis and the smallest element of self along axis.

Note: The rtype argument specifies the data-type the reduction should take place over. This is important if the datatype of the array is not "large" enough to handle the output. By default, all integer data-types are made at least as large as NPY_LONG for the "add" and "multiply" ufuncs (which form the basis for mean, sum, cumsum, prod, and cumprod functions).

PyObject* PyArray_Mean (PyArrayObject* self, int axis, int rtype, PyArrayObject* out)
Equivalent to ndarray.mean (self, axis, rtype). Returns the mean of the elements along the given axis, using the enumerated type rtype as the data type to sum in. Default sum behavior is obtained using PyArray_NOTYPE for rtype.

PyObject* PyArray_Trace (PyArrayObject* self, int offset, int axis1, int axis2, int rtype, PyArrayObject* out)
Equivalent to ndarray.trace (self, offset, axis1, axis2, rtype). Return the sum (using rtype as the data type of summation) over the offset diagonal elements of the 2-d arrays defined by axis1 and axis2 variables. A positive offset chooses diagonals above the main diagonal. A negative offset selects diagonals below the main diagonal.

PyObject* PyArray_Clip (PyArrayObject* self, PyObject* min, PyObject* max)
Equivalent to ndarray.clip (self, min, max). Clip an array, self, so that values larger than max are fixed to max and values less than \(\min\) are fixed to min.

PyObject* PyArray_Conjugate (PyArrayObject* self)
Equivalent to ndarray. conjugate (self). Return the complex conjugate of self. If self is not of complex data type, then return self with an reference.

PyObject* PyArray_Round (PyArrayObject* self, int decimals, PyArrayObject* out)
Equivalent to ndarray. round (self, decimals, out). Returns the array with elements rounded to the nearest
decimal place. The decimal place is defined as the \(10^{- \text {decimals }}\) digit so that negative decimals cause rounding to the nearest 10 's, 100 's, etc. If out is NULL, then the output array is created, otherwise the output is placed in out which must be the correct size and type.
PyObject* PyArray_Std (PyArrayObject* self, int axis, int rtype, PyArrayObject* out)
Equivalent to ndarray.std (self, axis, rtype). Return the standard deviation using data along axis converted to data type rtype.

PyObject* PyArray_Sum (PyArrayObject* self, int axis, int rtype, PyArrayObject* out)
Equivalent to ndarray.sum (self, axis, rtype). Return 1-d vector sums of elements in self along axis. Perform the sum after converting data to data type rtype.

PyObject* PyArray_CumSum (PyArrayObject* self, int axis, int rtype, PyArrayObject* out)
Equivalent to ndarray. cumsum (self, axis, rtype). Return cumulative 1-d sums of elements in self along axis. Perform the sum after converting data to data type rtype.

PyObject* PyArray_Prod (PyArrayObject* self, int axis, int rtype, PyArrayObject* out)
Equivalent to ndarray.prod (self, axis, rtype). Return 1-d products of elements in self along axis. Perform the product after converting data to data type rtype.

PyObject* PyArray_CumProd (PyArrayObject* self, int axis, int rtype, PyArrayObject* out)
Equivalent to ndarray. cumprod (self, axis, rtype). Return 1-d cumulative products of elements in self along axis. Perform the product after converting data to data type rtype.

PyObject* PyArray_All (PyArrayObject* self, int axis, PyArrayObject* out)
Equivalent to ndarray.all (self, axis). Return an array with True elements for every 1-d sub-array of self defined by axis in which all the elements are True.

PyObject* PyArray_Any (PyArrayObject* self, int axis, PyArrayObject* out)
Equivalent to ndarray. any (self, axis). Return an array with True elements for every 1-d sub-array of self defined by axis in which any of the elements are True.

\subsection*{5.4.6 Functions}

\section*{Array Functions}
int PyArray_AsCArray (PyObject** op, void* ptr, npy_intp* dims, int nd, int typenum, int itemsize)
Sometimes it is useful to access a multidimensional array as a C-style multi-dimensional array so that algorithms can be implemented using C's a \([\mathrm{i}][\mathrm{j}][\mathrm{k}]\) syntax. This routine returns a pointer, ptr, that simulates this kind of C-style array, for 1-, 2-, and 3-d ndarrays.

\section*{Parameters}
- op - The address to any Python object. This Python object will be replaced with an equivalent well-behaved, C-style contiguous, ndarray of the given data type specifice by the last two arguments. Be sure that stealing a reference in this way to the input object is justified.
- ptr - The address to a (ctype* for 1-d, ctype** for 2-d or ctype*** for 3-d) variable where ctype is the equivalent C-type for the data type. On return, ptr will be addressable as a 1-d, 2-d, or 3-d array.
- dims - An output array that contains the shape of the array object. This array gives boundaries on any looping that will take place.
- nd - The dimensionality of the array ( 1,2 , or 3 ).
- typenum - The expected data type of the array.
- itemsize - This argument is only needed when typenum represents a flexible array. Otherwise it should be 0 .

Note: The simulation of a C-style array is not complete for 2-d and 3-d arrays. For example, the simulated arrays of pointers cannot be passed to subroutines expecting specific, statically-defined 2-d and 3-d arrays. To pass to functions requiring those kind of inputs, you must statically define the required array and copy data.
int PyArray_Free (PyObject* op, void* ptr)
Must be called with the same objects and memory locations returned from PyArray_AsCArray (...). This function cleans up memory that otherwise would get leaked.

PyObject* PyArray_Concatenate (PyObject* obj, int axis)
Join the sequence of objects in obj together along axis into a single array. If the dimensions or types are not compatible an error is raised.

PyObject* PyArray_InnerProduct (PyObject* obj1, PyObject* obj2)
Compute a product-sum over the last dimensions of obj1 and obj2. Neither array is conjugated.
PyObject* PyArray_MatrixProduct (PyObject* objl, PyObject*obj)
Compute a product-sum over the last dimension of obj1 and the second-to-last dimension of obj2. For 2-d arrays this is a matrix-product. Neither array is conjugated.

PyObject* PyArray_MatrixProduct2 (PyObject* obj1, PyObject* obj, PyObject* out)
New in version 1.6. Same as PyArray_MatrixProduct, but store the result in out. The output array must have the correct shape, type, and be C-contiguous, or an exception is raised.

PyObject* PyArray_EinsteinSum (char* subscripts, npy_intp nop, PyArrayObject** op_in, PyArray_Descr* dtype, NPY_ORDER order, NPY_CASTING casting, PyArrayObject* out)
New in version 1.6. Applies the einstein summation convention to the array operands provided, returning a new array or placing the result in out. The string in subscripts is a comma separated list of index letters. The number of operands is in nop, and op_in is an array containing those operands. The data type of the output can be forced with dtype, the output order can be forced with order (NPY_KEEPORDER is recommended), and when dtype is specified, casting indicates how permissive the data conversion should be.

See the einsum function for more details.
PyObject* PyArray_CopyAndTranspose (PyObject * op)
A specialized copy and transpose function that works only for 2-d arrays. The returned array is a transposed copy of \(o p\).
PyObject* PyArray_Correlate (PyObject* op1, PyObject* op2, int mode)
Compute the 1-d correlation of the 1-d arrays op1 and op2. The correlation is computed at each output point by multiplying opl by a shifted version of op2 and summing the result. As a result of the shift, needed values outside of the defined range of \(o p 1\) and \(o p 2\) are interpreted as zero. The mode determines how many shifts to return: 0 - return only shifts that did not need to assume zero- values; 1 - return an object that is the same size as opl, 2 - return all possible shifts (any overlap at all is accepted).

\section*{Notes}

This does not compute the usual correlation: if op2 is larger than op1, the arguments are swapped, and the conjugate is never taken for complex arrays. See PyArray_Correlate2 for the usual signal processing correlation.

PyObject* PyArray_Correlate2 (PyObject* op1, PyObject* op2, int mode)
Updated version of PyArray_Correlate, which uses the usual definition of correlation for 1d arrays. The correlation is computed at each output point by multiplying opl by a shifted version of op2 and summing the result. As a result of the shift, needed values outside of the defined range of opl and op2 are interpreted as zero. The mode determines how many shifts to return: 0 - return only shifts that did not need to assume zero- values; 1 return an object that is the same size as opl, 2 - return all possible shifts (any overlap at all is accepted).

\section*{Notes}

Compute z as follows:
```

z[k] = sum_n op1[n] * conj(op2[n+k])

```

PyObject* PyArray_Where (PyObject* condition, PyObject* \(x\), PyObject* y)
If both x and y are NULL, then return PyArray_Nonzero (condition). Otherwise, both \(x\) and \(y\) must be given and the object returned is shaped like condition and has elements of \(x\) and \(y\) where condition is respectively True or False.

\section*{Other functions}

Bool PyArray_CheckStrides (int elsize, int nd, npy_intp numbytes, npy_intp* dims, npy_intp* newstrides)
Determine if newstrides is a strides array consistent with the memory of an \(n d\)-dimensional array with shape dims and element-size, elsize. The newstrides array is checked to see if jumping by the provided number of bytes in each direction will ever mean jumping more than numbytes which is the assumed size of the available memory segment. If numbytes is 0 , then an equivalent numbytes is computed assuming nd, dims, and elsize refer to a single-segment array. Return NPY_TRUE if newstrides is acceptable, otherwise return NPY_FALSE.
npy_intp PyArray_MultiplyList (npy_intp* seq, int \(n\) )
int PyArray_MultiplyIntList (int* seq, int \(n\) )
Both of these routines multiply an \(n\)-length array, seq, of integers and return the result. No overflow checking is performed.
int PyArray_CompareLists (npy_intp* \(l l\), npy_intp* \(l 2\), int \(n\) )
Given two \(n\)-length arrays of integers, \(l l\), and \(l 2\), return 1 if the lists are identical; otherwise, return 0 .

\subsection*{5.4.7 Array Iterators}

As of Numpy 1.6, these array iterators are superceded by the new array iterator, Npy Iter.
An array iterator is a simple way to access the elements of an N -dimensional array quickly and efficiently. Section 2 provides more description and examples of this useful approach to looping over an array.

PyObject* PyArray_IterNew (PyObject* arr)
Return an array iterator object from the array, arr. This is equivalent to arr. flat. The array iterator object makes it easy to loop over an N -dimensional non-contiguous array in C -style contiguous fashion.

PyObject* PyArray_IterAllButAxis (PyObject* arr, int *axis)
Return an array iterator that will iterate over all axes but the one provided in *axis. The returned iterator cannot be used with PYArray_ITER_GOTO1D. This iterator could be used to write something similar to what ufuncs do wherein the loop over the largest axis is done by a separate sub-routine. If *axis is negative then *axis will be set to the axis having the smallest stride and that axis will be used.

PyObject *PyArray_BroadcastToShape (PyObject* arr, npy_intp *dimensions, int nd)
Return an array iterator that is broadcast to iterate as an array of the shape provided by dimensions and nd.
int PyArrayIter_Check (PyObject*op)
Evaluates true if \(o p\) is an array iterator (or instance of a subclass of the array iterator type).
void PyArray_ITER_RESET (PyObject* iterator)
Reset an iterator to the beginning of the array.
void PyArray_ITER_NEXT (PyObject* iterator)
Incremement the index and the dataptr members of the iterator to point to the next element of the array. If the array is not ( C -style) contiguous, also increment the N -dimensional coordinates array.
void *PyArray_ITER_DATA (PyObject* iterator)
A pointer to the current element of the array.
void PyArray_ITER_GOTO (PyObject* iterator, npy_intp* destination)
Set the iterator index, dataptr, and coordinates members to the location in the array indicated by the N -dimensional c-array, destination, which must have size at least iterator \(->\mathrm{nd}\) _m1+1.

PyArray_ITER_GOTO1D (PyObject* iterator, npy_intp index)
Set the iterator index and dataptr to the location in the array indicated by the integer index which points to an element in the C-styled flattened array.
int PyArray_ITER_NOTDONE (PyObject* iterator)
Evaluates TRUE as long as the iterator has not looped through all of the elements, otherwise it evaluates FALSE.

\subsection*{5.4.8 Broadcasting (multi-iterators)}

PyObject* PyArray_MultiIterNew (int num, ...)
A simplified interface to broadcasting. This function takes the number of arrays to broadcast and then num extra ( PyObject * ) arguments. These arguments are converted to arrays and iterators are created. PyArray_Broadcast is then called on the resulting multi-iterator object. The resulting, broadcasted mult-iterator object is then returned. A broadcasted operation can then be performed using a single loop and using PyArray_MultiIter_NEXT (..)
void PyArray_MultiIter_RESET (PyObject* multi)
Reset all the iterators to the beginning in a multi-iterator object, multi.
void PyArray_MultiIter_NEXT (PyObject* multi)
Advance each iterator in a multi-iterator object, multi, to its next (broadcasted) element.
void *PyArray_MultiIter_DATA (PyObject* multi, int \(i\) )
Return the data-pointer of the \(i^{\text {th }}\) iterator in a multi-iterator object.
void PyArray_MultiIter_NEXTi (PyObject* multi, int i)
Advance the pointer of only the \(i^{\text {th }}\) iterator.
void PyArray_MultiIter_GOTO (PyObject* multi, npy_intp* destination)
Advance each iterator in a multi-iterator object, multi, to the given \(N\)-dimensional destination where \(N\) is the number of dimensions in the broadcasted array.
void PyArray_MultiIter_GOTO1D (PyObject* multi, npy_intp index)
Advance each iterator in a multi-iterator object, multi, to the corresponding location of the index into the flattened broadcasted array.
int PyArray_MultiIter_NOTDONE (PyObject* multi)
Evaluates TRUE as long as the multi-iterator has not looped through all of the elements (of the broadcasted result), otherwise it evaluates FALSE.
int PyArray_Broadcast (PyArrayMultiIterObject* mit)
This function encapsulates the broadcasting rules. The mit container should already contain iterators for all the arrays that need to be broadcast. On return, these iterators will be adjusted so that iteration over each simultaneously will accomplish the broadcasting. A negative number is returned if an error occurs.
int PyArray_RemoveSmallest (PyArrayMultiIterObject* mit)
This function takes a multi-iterator object that has been previously "broadcasted," finds the dimension with the smallest "sum of strides" in the broadcasted result and adapts all the iterators so as not to iterate over that dimension (by effectively making them of length-1 in that dimension). The corresponding dimension is
returned unless mit \(->\) nd is 0 , then -1 is returned. This function is useful for constructing ufunc-like routines that broadcast their inputs correctly and then call a strided 1-d version of the routine as the inner-loop. This 1-d version is usually optimized for speed and for this reason the loop should be performed over the axis that won't require large stride jumps.

\subsection*{5.4.9 Neighborhood iterator}

New in version 1.4.0. Neighborhood iterators are subclasses of the iterator object, and can be used to iter over a neighborhood of a point. For example, you may want to iterate over every voxel of a 3d image, and for every such voxel, iterate over an hypercube. Neighborhood iterator automatically handle boundaries, thus making this kind of code much easier to write than manual boundaries handling, at the cost of a slight overhead.

PyObject* PyArray_NeighborhoodIterNew (PyArrayIterObject* iter, npy_intp bounds, int mode, PyArrayObject* fill_value)
This function creates a new neighborhood iterator from an existing iterator. The neighborhood will be computed relatively to the position currently pointed by iter, the bounds define the shape of the neighborhood iterator, and the mode argument the boundaries handling mode.

The bounds argument is expected to be a ( \(2 *\) iter->ao->nd \()\) arrays, such as the range bound \([2 * \mathrm{i}]->\) bounds \([2 * \mathrm{i}+1]\) defines the range where to walk for dimension \(i\) (both bounds are included in the walked coordinates). The bounds should be ordered for each dimension (bounds[ \(2 * \mathrm{i}]<=\) bounds \([2 * i+1]\) ).

The mode should be one of:
-NPY_NEIGHBORHOOD_ITER_ZERO_PADDING: zero padding. Outside bounds values will be 0 .
-NPY_NEIGHBORHOOD_ITER_ONE_PADDING: one padding, Outside bounds values will be 1.
-NPY_NEIGHBORHOOD_ITER_CONSTANT_PADDING: constant padding. Outside bounds values will be the same as the first item in fill_value.
-NPY_NEIGHBORHOOD_ITER_MIRROR_PADDING: mirror padding. Outside bounds values will be as if the array items were mirrored. For example, for the array \([1,2,3,4], x[-2]\) will be \(2, x[-2]\) will be 1 , \(x[4]\) will be 4 , \(x[5]\) will be 1 , etc...
-NPY_NEIGHBORHOOD_ITER_CIRCULAR_PADDING: circular padding. Outside bounds values will be as if the array was repeated. For example, for the array [1, 2, 3, 4], x[-2] will be 3 , \(x[-2]\) will be 4 , \(x[4]\) will be 1 , \(x[5]\) will be 2 , etc...

If the mode is constant filling (NPY_NEIGHBORHOOD_ITER_CONSTANT_PADDING), fill_value should point to an array object which holds the filling value (the first item will be the filling value if the array contains more than one item). For other cases, fill_value may be NULL.
-The iterator holds a reference to iter
-Return NULL on failure (in which case the reference count of iter is not changed)
-iter itself can be a Neighborhood iterator: this can be useful for .e.g automatic boundaries handling
-the object returned by this function should be safe to use as a normal iterator
-If the position of iter is changed, any subsequent call to PyArrayNeighborhoodIter_Next is undefined behavior, and PyArrayNeighborhoodIter_Reset must be called.
```

PyArrayIterObject \*iter;
PyArrayNeighborhoodIterObject \*neigh_iter;
iter = PyArray_IterNew(x);
//For a 3x3 kernel
bounds = {-1, 1, -1, 1};
neigh_iter = (PyArrayNeighborhoodIterObject*)PyArrayNeighborhoodIter_New(

```
```

    iter, bounds, NPY_NEIGHBORHOOD_ITER_ZERO_PADDING, NULL);
    for(i = 0; i < iter->size; ++i) {
for (j = 0; j < neigh_iter->size; ++j) {
// Walk around the item currently pointed by iter->dataptr
PyArrayNeighborhoodIter_Next(neigh_iter);
}
// Move to the next point of iter
PyArrayIter_Next(iter);
PyArrayNeighborhoodIter_Reset(neigh_iter);
}

```
int PyArrayNeighborhoodIter_Reset (PyArrayNeighborhoodIterObject* iter)
Reset the iterator position to the first point of the neighborhood. This should be called whenever the iter argument given at PyArray_NeighborhoodIterObject is changed (see example)
int PyArrayNeighborhoodIter_Next (PyArrayNeighborhoodIterObject* iter)
After this call, iter->dataptr points to the next point of the neighborhood. Calling this function after every point of the neighborhood has been visited is undefined.

\subsection*{5.4.10 Array Scalars}

\section*{PyObject* PyArray_Return (PyArrayObject* arr)}

This function checks to see if arr is a 0 -dimensional array and, if so, returns the appropriate array scalar. It should be used whenever 0-dimensional arrays could be returned to Python.

PyObject* PyArray_Scalar (void* data, PyArray_Descr* dtype, PyObject* itemsize)
Return an array scalar object of the given enumerated typenum and itemsize by copying from memory pointed to by data. If swap is nonzero then this function will byteswap the data if appropriate to the data-type because array scalars are always in correct machine-byte order.

PyObject* PyArray_ToScalar (void* data, PyArrayObject* arr)
Return an array scalar object of the type and itemsize indicated by the array object arr copied from the memory pointed to by data and swapping if the data in arr is not in machine byte-order.

PyObject* PyArray_FromScalar (PyObject* scalar, PyArray_Descr* outcode)
Return a 0-dimensional array of type determined by outcode from scalar which should be an array-scalar object. If outcode is NULL, then the type is determined from scalar.
void PyArray_ScalarAsCtype (PyObject* scalar, void* ctypeptr)
Return in ctypeptr a pointer to the actual value in an array scalar. There is no error checking so scalar must be an array-scalar object, and ctypeptr must have enough space to hold the correct type. For flexible-sized types, a pointer to the data is copied into the memory of ctypeptr, for all other types, the actual data is copied into the address pointed to by ctypeptr.
void PyArray_CastScalarToCtype (PyObject* scalar, void* ctypeptr, PyArray_Descr* outcode)
Return the data (cast to the data type indicated by outcode) from the array-scalar, scalar, into the memory pointed to by ctypeptr (which must be large enough to handle the incoming memory).

PyObject* PyArray_TypeObjectFromType (int type)
Returns a scalar type-object from a type-number, type . Equivalent to PyArray_DescrFromType (type)>typeobj except for reference counting and error-checking. Returns a new reference to the typeobject on success or NULL on failure.

NPY_SCALARKIND PyArray_ScalarKind (int typenum, PyArrayObject** arr)
Return the kind of scalar represented by typenum and the array in *arr (if arr is not NULL ). The array is assumed to be rank-0 and only used if typenum represents a signed integer. If arr is not NULL and the first
element is negative then NPY_INTNEG_SCALAR is returned, otherwise NPY_INTPOS_SCALAR is returned. The possible return values are NPY_\{kind \(\}\) SCALAR where \(\{\mathrm{k}\) ind \(\}\) can be INTPOS, INTNEG, FLOAT, COMPLEX, BOOL, or OBJECT. NPY_NOSCALAR is also an enumerated value NPY_SCALARKIND variables can take on.
int PyArray_CanCoerceScalar (char thistype, char neededtype, NPY_SCALARKIND scalar)
Implements the rules for scalar coercion. Scalars are only silently coerced from thistype to neededtype if this function returns nonzero. If scalar is NPY_NOSCALAR, then this function is equivalent to PyArray_CanCastSafely. The rule is that scalars of the same KIND can be coerced into arrays of the same KIND. This rule means that high-precision scalars will never cause low-precision arrays of the same KIND to be upcast.

\subsection*{5.4.11 Data-type descriptors}

\begin{abstract}
Warning: Data-type objects must be reference counted so be aware of the action on the data-type reference of different C-API calls. The standard rule is that when a data-type object is returned it is a new reference. Functions that take PyArray_Descr * objects and return arrays steal references to the data-type their inputs unless otherwise noted. Therefore, you must own a reference to any data-type object used as input to such a function.
\end{abstract}
int PyArrayDescr_Check (PyObject* obj)
Evaluates as true if \(o b j\) is a data-type object (PyArray_Descr *).
PyArray_Descr* PyArray_DescrNew (PyArray_Descr* obj)
Return a new data-type object copied from obj (the fields reference is just updated so that the new object points to the same fields dictionary if any).

PyArray_Descr* PyArray_DescrNewFromType (int typenum)
Create a new data-type object from the built-in (or user-registered) data-type indicated by typenum. All builtin types should not have any of their fields changed. This creates a new copy of the PyArray_Descr structure so that you can fill it in as appropriate. This function is especially needed for flexible data-types which need to have a new elsize member in order to be meaningful in array construction.

PyArray_Descr* PyArray_DescrNewByteorder (PyArray_Descr* obj, char newendian)
Create a new data-type object with the byteorder set according to newendian. All referenced data-type objects (in subdescr and fields members of the data-type object) are also changed (recursively). If a byteorder of NPY_IGNORE is encountered it is left alone. If newendian is NPY_SWAP, then all byte-orders are swapped. Other valid newendian values are NPY_NATIVE, NPY_LITTLE, and NPY_BIG which all cause the returned data-typed descriptor (and all it's referenced data-type descriptors) to have the corresponding byte- order.

PyArray_Descr* PyArray_DescrFromObject (PyObject* op, PyArray_Descr* mintype)
Determine an appropriate data-type object from the object \(o p\) (which should be a "nested" sequence object) and the minimum data-type descriptor mintype (which can be NULL ). Similar in behavior to array(op).dtype. Don't confuse this function with PyArray_DescrConverter. This function essentially looks at all the objects in the (nested) sequence and determines the data-type from the elements it finds.

PyArray_Descr* PyArray_DescrFromScalar (PyObject* scalar)
Return a data-type object from an array-scalar object. No checking is done to be sure that scalar is an array scalar. If no suitable data-type can be determined, then a data-type of NPY_OBJECT is returned by default.

PyArray_Descr* PyArray_DescrFromType (int typenum)
Returns a data-type object corresponding to typenum. The typenum can be one of the enumerated types, a character code for one of the enumerated types, or a user-defined type.
int PyArray_DescrConverter (PyObject* obj, PyArray_Descr** dtype)
Convert any compatible Python object, obj, to a data-type object in dtype. A large number of Python objects
can be converted to data-type objects. See Data type objects (dtype) for a complete description. This version of the converter converts None objects to a NPY_DEFAULT_TYPE data-type object. This function can be used with the "O\&" character code in PyArg_ParseTuple processing.
int PyArray_DescrConverter2 (PyObject* obj, PyArray_Descr** dtype)
Convert any compatible Python object, obj, to a data-type object in dtype. This version of the converter converts None objects so that the returned data-type is NULL. This function can also be used with the "O\&" character in PyArg_ParseTuple processing.
int Pyarray_DescrAlignConverter (PyObject* obj, PyArray_Descr** dtype)
Like PyArray_DescrConverter except it aligns C-struct-like objects on word-boundaries as the compiler would.
int Pyarray_DescrAlignConverter2 (PyObject* obj, PyArray_Descr** dtype)
Like PyArray_DescrConverter2 except it aligns C-struct-like objects on word-boundaries as the compiler would.

\section*{PyObject *PyArray_FieldNames (PyObject* dict)}

Take the fields dictionary, dict, such as the one attached to a data-type object and construct an ordered-list of field names such as is stored in the names field of the PyArray_Descr object.

\subsection*{5.4.12 Conversion Utilities}

\section*{For use with PyArg_ParseTuple}

All of these functions can be used in PyArg_ParseTuple (...) with the "O\&" format specifier to automatically convert any Python object to the required C-object. All of these functions return NPY_SUCCEED if successful and NPY_FAIL if not. The first argument to all of these function is a Python object. The second argument is the address of the C-type to convert the Python object to.

Warning: Be sure to understand what steps you should take to manage the memory when using these conversion functions. These functions can require freeing memory, and/or altering the reference counts of specific objects based on your use.
int PyArray_Converter (PyObject* obj, PyObject** address)
Convert any Python object to a PyArrayObject. If PyArray_Check (obj) is TRUE then its reference count is incremented and a reference placed in address. If obj is not an array, then convert it to an array using PyArray_FromAny. No matter what is returned, you must DECREF the object returned by this routine in address when you are done with it.
int PyArray_OutputConverter (PyObject* obj, PyArrayObject** address)
This is a default converter for output arrays given to functions. If obj is Py_None or NULL, then *address will be NULL but the call will succeed. If PyArray_Check (obj) is TRUE then it is returned in *address without incrementing its reference count.
int PyArray_IntpConverter (PyObject* obj, PyArray_Dims* seq)
Convert any Python sequence, obj, smaller than NPY_MAXDIMS to a C-array of npy_intp. The Python object could also be a single number. The seq variable is a pointer to a structure with members ptr and len. On successful return, seq \(->\) ptr contains a pointer to memory that must be freed to avoid a memory leak. The restriction on memory size allows this converter to be conveniently used for sequences intended to be interpreted as array shapes.
int PyArray_BufferConverter (PyObject* obj, PyArray_Chunk* buf)
Convert any Python object, obj, with a (single-segment) buffer interface to a variable with members that detail the object's use of its chunk of memory. The buf variable is a pointer to a structure with base, ptr, len, and flags members. The PyArray_Chunk structure is binary compatibile with the Python's buffer object (through its
len member on 32-bit platforms and its ptr member on 64-bit platforms or in Python 2.5). On return, the base member is set to obj (or its base if obj is already a buffer object pointing to another object). If you need to hold on to the memory be sure to INCREF the base member. The chunk of memory is pointed to by buf ->ptr member and has length buf ->len. The flags member of buf is NPY_BEHAVED_RO with the NPY_WRITEABLE flag set if obj has a writeable buffer interface.
int PyArray_AxisConverter (PyObject * obj, int* axis)
Convert a Python object, obj, representing an axis argument to the proper value for passing to the functions that take an integer axis. Specifically, if \(o b j\) is None, axis is set to NPY_MAXDIMS which is interpreted correctly by the C-API functions that take axis arguments.
int PyArray_BoolConverter (PyObject* obj, Bool* value)
Convert any Python object, obj, to NPY_TRUE or NPY_FALSE, and place the result in value.
int PyArray_ByteorderConverter (PyObject* obj, char* endian)
Convert Python strings into the corresponding byte-order character: '>', '<', 's', '=', or 'l'.
int PyArray_SortkindConverter (PyObject* obj, NPY_SORTKIND* sort)
Convert Python strings into one of NPY_QUICKSORT (starts with ' \(q\) ' or 'Q'), NPY_HEAPSORT (starts with ' \(h\) ' or 'H'), or NPY_MERGESORT (starts with ' \(m\) ' or 'M').
int PyArray_SearchsideConverter (PyObject* obj, NPY_SEARCHSIDE* side)
Convert Python strings into one of NPY_SEARCHLEFT (starts with 'l' or 'L'), or NPY_SEARCHRIGHT (starts with ' \(r\) ' or ' \(R\) ').
int PyArray_OrderConverter (PyObject* obj, NPY_ORDER* order)
Convert the Python strings 'C', ' F ', ' A ', and ' K ' into the NPY_ORDER enumeration NPY_CORDER, NPY_FORTRANORDER, NPY_ANYORDER, and NPY_KEEPORDER.
int PyArray_CastingConverter (PyObject* obj, NPY_CASTING* casting)
Convert the Python strings 'no', 'equiv', 'safe', 'same_kind', and 'unsafe' into the NPY_CASTING enumeration NPY_NO_CASTING, NPY_EQUIV_CASTING, NPY_SAFE_CASTING, NPY_SAME_KIND_CASTING, and NPY_UNSAFE_CASTING.
int PyArray_ClipmodeConverter (PyObject* object, NPY_CLIPMODE* val)
Convert the Python strings 'clip', 'wrap', and 'raise' into the NPY_CLIPMODE enumeration NPY_CLIP, NPY_WRAP, and NPY_RAISE.
int PyArray_ConvertClipmodeSequence (PyObject* object, NPY_CLIPMODE* modes, int \(n\) )
Converts either a sequence of clipmodes or a single clipmode into a C array of NPY_CLIPMODE values. The number of clipmodes \(n\) must be known before calling this function. This function is provided to help functions allow a different clipmode for each dimension.

\section*{Other conversions}
int PyArray_PyIntAsInt (PyObject* op)
Convert all kinds of Python objects (including arrays and array scalars) to a standard integer. On error, -1 is returned and an exception set. You may find useful the macro:
```

\#define error_converting(x) (((x) == -1) \&\& PyErr_Occurred()

```
npy_intp PyArray_PyIntAsIntp (PyObject* op)
Convert all kinds of Python objects (including arrays and array scalars) to a (platform-pointer-sized) integer. On error, -1 is returned and an exception set.
int PyArray_IntpFromSequence (PyObject* seq, npy_intp* vals, int maxvals)
Convert any Python sequence (or single Python number) passed in as seq to (up to) maxvals pointer-sized integers and place them in the vals array. The sequence can be smaller then maxvals as the number of converted objects is returned.
int PyArray_TypestrConvert (int itemsize, int gentype)
Convert typestring characters (with itemsize) to basic enumerated data types. The typestring character corresponding to signed and unsigned integers, floating point numbers, and complex-floating point numbers are recognized and converted. Other values of gentype are returned. This function can be used to convert, for example, the string 'f4' to NPY_FLOAT32.

\subsection*{5.4.13 Miscellaneous}

\section*{Importing the API}

In order to make use of the C-API from another extension module, the import_array () command must be used. If the extension module is self-contained in a single .c file, then that is all that needs to be done. If, however, the extension module involves multiple files where the C-API is needed then some additional steps must be taken.
```

void import_array(void)

```

This function must be called in the initialization section of a module that will make use of the C-API. It imports the module where the function-pointer table is stored and points the correct variable to it.
```

PY_ARRAY_UNIQUE_SYMBOL

```

\section*{NO_IMPORT_ARRAY}

Using these \#defines you can use the C-API in multiple files for a single extension module. In each file you must define PY_ARRAY_UNIQUE_SYMBOL to some name that will hold the C-API (e.g. myextension_ARRAY_API). This must be done before including the numpy/arrayobject.h file. In the module intialization routine you call import_array (). In addition, in the files that do not have the module initialization sub_routine define NO_IMPORT_ARRAY prior to including numpy/arrayobject.h.

Suppose I have two files coolmodule.c and coolhelper.c which need to be compiled and linked into a single extension module. Suppose coolmodule.c contains the required initcool module initialization function (with the import_array() function called). Then, coolmodule.c would have at the top:
\#define PY_ARRAY_UNIQUE_SYMBOL COOI_ARRAY_API
\#include numpy/arrayobject.h

On the other hand, coolhelper.c would contain at the top:
```

\#define PY_ARRAY_UNIQUE_SYMBOL COOI_ARRAY_API
\#define NO_IMPORT_ARRAY
\#include numpy/arrayobject.h

```

\section*{Checking the API Version}

Because python extensions are not used in the same way as usual libraries on most platforms, some errors cannot be automatically detected at build time or even runtime. For example, if you build an extension using a function available only for numpy \(>=1.3 .0\), and you import the extension later with numpy 1.2 , you will not get an import error (but almost certainly a segmentation fault when calling the function). That's why several functions are provided to check for numpy versions. The macros NPY_VERSION and NPY_FEATURE_VERSION corresponds to the numpy version used to build the extension, whereas the versions returned by the functions PyArray_GetNDArrayCVersion and PyArray_GetNDArrayCFeatureVersion corresponds to the runtime numpy's version.

The rules for ABI and API compatibilities can be summarized as follows:
- Whenever NPY_VERSION != PyArray_GetNDArrayCVersion, the extension has to be recompiled (ABI incompatibility)
- NPY_VERSION == PyArray_GetNDArrayCVersion and NPY_FEATURE_VERSION <= PyArray_GetNDArrayCFeatureVersion means backward compatible changes.
ABI incompatibility is automatically detected in every numpy's version. API incompatibility detection was added in numpy 1.4.0. If you want to supported many different numpy versions with one extension binary, you have to build your extension with the lowest NPY_FEATURE_VERSION as possible.
unsigned int PyArray_GetNDArrayCVersion (void)
This just returns the value NPY_VERSION. NPY_VERSION changes whenever a backward incompatible change at the ABI level. Because it is in the C-API, however, comparing the output of this function from the value defined in the current header gives a way to test if the C-API has changed thus requiring a re-compilation of extension modules that use the C-API. This is automatically checked in the function import_array.
unsigned int PyArray_GetNDArrayCFeatureVersion (void)
New in version 1.4.0. This just returns the value NPY_FEATURE_VERSION. NPY_FEATURE_VERSION changes whenever the API changes (e.g. a function is added). A changed value does not always require a recompile.

\section*{Internal Flexibility}
int PyArray_SetNumericOps (PyObject* dict)
NumPy stores an internal table of Python callable objects that are used to implement arithmetic operations for arrays as well as certain array calculation methods. This function allows the user to replace any or all of these Python objects with their own versions. The keys of the dictionary, dict, are the named functions to replace and the paired value is the Python callable object to use. Care should be taken that the function used to replace an internal array operation does not itself call back to that internal array operation (unless you have designed the function to handle that), or an unchecked infinite recursion can result (possibly causing program crash). The key names that represent operations that can be replaced are:
add, subtract, multiply, divide, remainder, power, square, reciprocal, ones_like, sqrt, negative, absolute, invert, left_shift, right_shift, bitwise_and, bitwise_xor, bitwise_or, less, less_equal, equal, not_equal, greater, greater_equal, floor_divide, true_divide, logical_or, logical_and, floor, ceil, maximum, minimum, rint.

These functions are included here because they are used at least once in the array object's methods. The function returns -1 (without setting a Python Error) if one of the objects being assigned is not callable.
```

PyObject* PyArray_GetNumericOps (void)
Return a Python dictionary containing the callable Python objects stored in the the internal arithmetic operation table. The keys of this dictionary are given in the explanation for PyArray_SetNumericops.
void PyArray_SetStringFunction (PyObject*op, int repr)
This function allows you to alter the tp_str and tp_repr methods of the array object to any Python function. Thus you can alter what happens for all arrays when $\operatorname{str}(\operatorname{arr})$ or repr(arr) is called from Python. The function to be called is passed in as $o p$. If repr is non-zero, then this function will be called in response to repr(arr), otherwise the function will be called in response to $\operatorname{str}(\operatorname{arr})$. No check on whether or not $o p$ is callable is performed. The callable passed in to $o p$ should expect an array argument and should return a string to be printed.

```

\section*{Memory management}
char* PyDataMem_NEW (size_t nbytes)

PyDataMem_FREE (char* ptr)
char* PyDataMem_RENEW (void * ptr, size_t newbytes)
Macros to allocate, free, and reallocate memory. These macros are used internally to create arrays.
```

npy_intp* PyDimMem_NEW (nd)

```
PyDimMem_FREE (npy_intp* ptr)
npy_intp* PyDimMem_RENEW (npy_intp* ptr, npy_intp newnd)
    Macros to allocate, free, and reallocate dimension and strides memory.
PyArray_malloc (nbytes)
PyArray_free (ptr)
PyArray_realloc (ptr, nbytes)

These macros use different memory allocators, depending on the constant NPY_USE_PYMEM. The system malloc is used when NPY_USE_PYMEM is 0 , if NPY_USE_PYMEM is 1 , then the Python memory allocator is used.

\section*{Threading support}

These macros are only meaningful if NPY_ALLOW_THREADS evaluates True during compilation of the extension module. Otherwise, these macros are equivalent to whitespace. Python uses a single Global Interpreter Lock (GIL) for each Python process so that only a single thread may excecute at a time (even on multi-cpu machines). When calling out to a compiled function that may take time to compute (and does not have side-effects for other threads like updated global variables), the GIL should be released so that other Python threads can run while the time-consuming calculations are performed. This can be accomplished using two groups of macros. Typically, if one macro in a group is used in a code block, all of them must be used in the same code block. Currently, NPY_ALLOW_THREADS is defined to the python-defined WITH_THREADS constant unless the environment variable NPY_NOSMP is set in which case NPY_ALLOW_THREADS is defined to be 0 .

\section*{Group 1}

This group is used to call code that may take some time but does not use any Python C-API calls. Thus, the GIL should be released during its calculation.

\section*{NPY_BEGIN_ALLOW_THREADS}

Equivalent to Py_BEGIN_ALLOW_THREADS except it uses NPY_ALLOW_THREADS to determine if the macro if replaced with white-space or not.

\section*{NPY_END_ALLOW_THREADS}

Equivalent to PY_END_ALLOW_THREADS except it uses NPY_ALLOW_THREADS to determine if the macro if replaced with white-space or not.

NPY_BEGIN_THREADS_DEF
Place in the variable declaration area. This macro sets up the variable needed for storing the Python state.

\section*{NPY_BEGIN_THREADS}

Place right before code that does not need the Python interpreter (no Python C-API calls). This macro saves the Python state and releases the GIL.

\section*{NPY_END_THREADS}

Place right after code that does not need the Python interpreter. This macro acquires the GIL and restores the Python state from the saved variable.

NPY_BEGIN_THREADS_DESCR (PyArray_Descr *dtype)
Useful to release the GIL only if dtype does not contain arbitrary Python objects which may need the Python interpreter during execution of the loop. Equivalent to
NPY_END_THREADS_DESCR (PyArray_Descr *dtype)
Useful to regain the GIL in situations where it was released using the BEGIN form of this macro.

\section*{Group 2}

This group is used to re-acquire the Python GIL after it has been released. For example, suppose the GIL has been released (using the previous calls), and then some path in the code (perhaps in a different subroutine) requires use of the Python C-API, then these macros are useful to acquire the GIL. These macros accomplish essentially a reverse of the previous three (acquire the LOCK saving what state it had) and then re-release it with the saved state.

\section*{NPY_ALLOW_C_API_DEF}

Place in the variable declaration area to set up the necessary variable.
NPY_ALLOW_C_API
Place before code that needs to call the Python C-API (when it is known that the GIL has already been released).

NPY_DISABLE_C_API
Place after code that needs to call the Python C-API (to re-release the GIL).
Tip: Never use semicolons after the threading support macros.

\section*{Priority}

\section*{NPY_PRIOIRTY}

Default priority for arrays.

\section*{NPY_SUBTYPE_PRIORITY}

Default subtype priority.

\section*{NPY_SCALAR_PRIORITY}

Default scalar priority (very small)
double PyArray_GetPriority (PyObject* obj, double def)
Return the __array_priority__ attribute (converted to a double) of obj or def if no attribute of that name exists. Fast returns that avoid the attribute lookup are provided for objects of type PyArray_Type.

\section*{Default buffers}

\section*{NPY_BUFSIZE}

Default size of the user-settable internal buffers.

\section*{NPY_MIN_BUFSIZE}

Smallest size of user-settable internal buffers.
NPY_MAX_BUFSIZE
Largest size allowed for the user-settable buffers.

\section*{Other constants}

\section*{NPY_NUM_FLOATTYPE}

The number of floating-point types

\section*{NPY_MAXDIMS}

The maximum number of dimensions allowed in arrays.

\section*{NPY VERSION}

The current version of the ndarray object (check to see if this variable is defined to guarantee the numpy/arrayobject.h header is being used).

\section*{NPY_FALSE}

Defined as 0 for use with Bool.

\section*{NPY_TRUE}

Defined as 1 for use with Bool.

\section*{NPY_FAIL}

The return value of failed converter functions which are called using the "O\&" syntax in PyArg_ParseTuple-like functions.

\section*{NPY SUCCEED}

The return value of successful converter functions which are called using the "O\&" syntax in PyArg_ParseTuple-like functions.

\section*{Miscellaneous Macros}

PyArray_SAMESHAPE (a1, a2)
Evaluates as True if arrays \(a 1\) and \(a 2\) have the same shape.
PyArray_MAX (a, b)
Returns the maximum of \(a\) and \(b\). If ( \(a\) ) or (b) are expressions they are evaluated twice.
PyArray_MIN (a, b)
Returns the minimum of \(a\) and \(b\). If ( \(a\) ) or ( \(b\) ) are expressions they are evaluated twice.
PyArray_CLT (a, b)

PyArray_CGT (a, b)

PyArray_CLE (a, b)

PyArray_CGE (a, b)

PyArray_CEQ (a, b)

PyArray_CNE (a, b)
Implements the complex comparisons between two complex numbers (structures with a real and imag member) using NumPy's definition of the ordering which is lexicographic: comparing the real parts first and then the complex parts if the real parts are equal.

PyArray_REFCOUNT (PyObject* op )
Returns the reference count of any Python object.
PyArray_XDECREF_ERR (PyObject *obj)
DECREF's an array object which may have the NPY_UPDATEIFCOPY flag set without causing the contents to be copied back into the original array. Resets the NPY_WRITEABLE flag on the base object. This is useful for recovering from an error condition when NPY_UPDATEIFCOPY is used.

\section*{Enumerated Types}

NPY_SORTKIND
A special variable-type which can take on the values NPY_\{KIND \} where \{KIND \} is

\section*{QUICKSORT, HEAPSORT, MERGESORT}

NPY_NSORTS
Defined to be the number of sorts.

\section*{NPY_SCALARKIND}

A special variable type indicating the number of "kinds" of scalars distinguished in determining scalar-coercion rules. This variable can take on the values NPY_\{KIND \} where \{KIND \} can be

\section*{NOSCALAR, BOOL_SCALAR, INTPOS_SCALAR, INTNEG_SCALAR, FLOAT_SCALAR, COMPLEX_SCALAR, OBJECT_SCALAR}

\section*{NPY_NSCALARKINDS}

Defined to be the number of scalar kinds (not including NPY_NOSCALAR).

\section*{NPY_ORDER}

An enumeration type indicating the element order that an array should be interpreted in. When a brand new array is created, generally only NPY_CORDER and NPY_FORTRANORDER are used, whereas when one or more inputs are provided, the order can be based on them.

NPY_ANYORDER
Fortran order if all the inputs are Fortran, C otherwise.

\section*{NPY_CORDER}

C order.

\section*{NPY_FORTRANORDER}

Fortran order.
NPY_KEEPORDER
An order as close to the order of the inputs as possible, even if the input is in neither C nor Fortran order.

\section*{NPY_CLIPMODE}

A variable type indicating the kind of clipping that should be applied in certain functions.

\section*{NPY_RAISE}

The default for most operations, raises an exception if an index is out of bounds.

\section*{NPY_CLIP}

Clips an index to the valid range if it is out of bounds.
NPY_WRAP
Wraps an index to the valid range if it is out of bounds.

\section*{NPY_CASTING}

New in version 1.6. An enumeration type indicating how permissive data conversions should be. This is used by the iterator added in NumPy 1.6, and is intended to be used more broadly in a future version.

\section*{NPY_NO_CASTING}

Only allow identical types.
NPY_EQUIV_CASTING
Allow identical and casts involving byte swapping.
NPY_SAFE_CASTING
Only allow casts which will not cause values to be rounded, truncated, or otherwise changed.

NPY_SAME_KIND_CASTING
Allow any safe casts, and casts between types of the same kind. For example, float64 -> float32 is permitted with this rule.

NPY_UNSAFE_CASTING
Allow any cast, no matter what kind of data loss may occur.

\subsection*{5.5 Array Iterator API}

New in version 1.6.

\subsection*{5.5.1 Array Iterator}

The array iterator encapsulates many of the key features in ufuncs, allowing user code to support features like output parameters, preservation of memory layouts, and buffering of data with the wrong alignment or type, without requiring difficult coding.

This page documents the API for the iterator. The C-API naming convention chosen is based on the one in the numpyrefactor branch, so will integrate naturally into the refactored code base. The iterator is named Npy Iter and functions are named NpyIter_*.

\subsection*{5.5.2 Converting from Previous NumPy Iterators}

The existing iterator API includes functions like PyArrayIter_Check, PyArray_Iter* and PyArray_ITER_*. The multiiterator array includes PyArray_MultiIter*, PyArray_Broadcast, and PyArray_RemoveSmallest. The new iterator design replaces all of this functionality with a single object and associated API. One goal of the new API is that all uses of the existing iterator should be replaceable with the new iterator without significant effort. In 1.6, the major exception to this is the neighborhood iterator, which does not have corresponding features in this iterator.

Here is a conversion table for which functions to use with the new iterator:
```

Iterator Functions
PyArray_IterNew
PyArray_IterAllButAxis
PyArray_BroadcastToShape
PyArrayIter_Check
PyArray_ITER_RESET
PyArray_ITER_NEXT
PyArray_ITER_DATA
PyArray_ITER_GOTO
PyArray_ITER_GOTO1D
PyArray_ITER_NOTDONE
Multi-iterator Functions
PyArray_MultiIterNew
PyArray_MultiIter_RESET
PyArray_MultiIter_NEXT
PyArray_MultiIter_DATA
PyArray_MultiIter_NEXTi
PyArray_MultiIter_GOTO
PyArray_MultiIter_GOTO1D
PyArray_MultiIter_NOTDONE
PyArray_Broadcast
PyArray_RemoveSmallest
Other Functions
PyArray_ConvertToCommonTypHerator flag NPY_ITER_COMMON_DTYPE

```

\subsection*{5.5.3 Simple Iteration Example}

The best way to become familiar with the iterator is to look at its usage within the NumPy codebase itself. For example, here is a slightly tweaked version of the code for PyArray_CountNonzero, which counts the number of non-zero elements in an array.
```

npy_intp PyArray_CountNonzero(PyArrayObject* self)
{
/* Nonzero boolean function */
PyArray_NonzeroFunc* nonzero = PyArray_DESCR(self)->f->nonzero;
NpyIter* iter;
NpyIter_IterNextFunc *iternext;
char** dataptr;
npy_intp* strideptr,* innersizeptr;
/* Handle zero-sized arrays specially */
if (PyArray_SIZE(self) == 0) {
return 0;
}
/*
* Create and use an iterator to count the nonzeros.
flag NPY_ITER_READONLY
- The array is never written to.
flag NPY_ITER_EXTERNAL_LOOP
- Inner loop is done outside the iterator for efficiency.
flag NPY_ITER_NPY_ITER_REFS_OK
* - Reference types are acceptable.

```
```

        order NPY KEEPORDER
            - Visit elements in memory order, regardless of strides.
        This is good for performance when the specific order
        elements are visited is unimportant.
    casting NPY_NO_CASTING
- No casting is required for this operation.
*/
iter = NpyIter_New(self, NPY_ITER_READONLY|
NPY_ITER_EXTERNAL_LOOP |
NPY_ITER_REFS_OK,
NPY_KEEPORDER, NPY_NO_CASTING,
NULL);
if (iter == NULL) {
return -1;
}
/*
* The iternext function gets stored in a local variable
* so it can be called repeatedly in an efficient manner.
*/
iternext = NpyIter_GetIterNext(iter, NULL);
if (iternext == NULL) {
NpyIter_Deallocate(iter);
return -1;
}
/* The location of the data pointer which the iterator may update */
dataptr = NpyIter_GetDataPtrArray(iter);
/* The location of the stride which the iterator may update */
strideptr = NpyIter_GetInnerStrideArray(iter);
/* The location of the inner loop size which the iterator may update */
innersizeptr = NpyIter_GetInnerLoopSizePtr(iter);
/* The iteration loop */
do {
/* Get the inner loop data/stride/count values */
char* data = *dataptr;
npy_intp stride = *strideptr;
npy_intp count = *innersizeptr;
/* This is a typical inner loop for NPY_ITER_EXTERNAL_LOOP */
while (count--) {
if (nonzero(data, self)) {
++nonzero_count;
}
data += stride;
}
/* Increment the iterator to the next inner loop */
} while(iternext(iter));
NpyIter_Deallocate(iter);
return nonzero_count;
}

```

\subsection*{5.5.4 Simple Multi-Iteration Example}

Here is a simple copy function using the iterator. The order parameter is used to control the memory layout of the allocated result, typically NPY_KEEPORDER is desired.
```

PyObject *CopyArray(PyObject *arr, NPY_ORDER order)
{
NpyIter *iter;
NpyIter_IterNextFunc *iternext;
PyObject *op[2], *ret;
npy_uint32 flags;
npy_uint32 op_flags[2];
npy_intp itemsize, *innersizeptr, innerstride;
char **dataptrarray;
/*
* No inner iteration - inner loop is handled by CopyArray code
*/
flags = NPY_ITER_EXTERNAL_LOOP;
/*
* Tell the constructor to automatically allocate the output.
* The data type of the output will match that of the input.
*/
op[0] = arr;
op[1] = NULL;
op_flags[0] = NPY_ITER_READONLY;
Op_flags[1] = NPY_ITER_WRITEONLY | NPY_ITER_ALLOCATE;
/* Construct the iterator */
iter = NpyIter_MultiNew(2, op, flags, order, NPY_NO_CASTING,
op_flags, NULL);
if (iter == NULL) {
return NULL;
}
/*
* Make a copy of the iternext function pointer and
* a few other variables the inner loop needs.
*/
iternext = NpyIter_GetIterNext(iter);
innerstride = NpyIter_GetInnerStrideArray(iter)[0];
itemsize = NpyIter_GetDescrArray(iter)[0]->elsize;
/*
* The inner loop size and data pointers may change during the
* loop, so just cache the addresses.
*/
innersizeptr = NpyIter_GetInnerLoopSizePtr(iter);
dataptrarray = NpyIter_GetDataPtrArray(iter);
/*
* Note that because the iterator allocated the output,
* it matches the iteration order and is packed tightly,
* so we don't need to check it like the input.
*/
if (innerstride == itemsize) {
do {
memcpy(dataptrarray[1], dataptrarray[0],
itemsize * (*innersizeptr));
} while (iternext(iter));

```
```

    } else {
        /* For efficiency, should specialize this based on item size... */
    npy_intp i;
    do {
                npy_intp size = *innersizeptr;
                char *src = dataaddr[0], *dst = dataaddr[1];
                for(i = 0; i < size; i++, src += innerstride, dst += itemsize) {
                    memcpy(dst, src, itemsize);
            }
    } while (iternext(iter));
    }
/* Get the result from the iterator object array */
ret = NpyIter_GetOperandArray(iter)[1];
Py_INCREF (ret);
if (NpyIter_Deallocate(iter) != NPY_SUCCEED) {
Py_DECREF(ret);
return NULL;
}
return ret;
}

```

\subsection*{5.5.5 Iterator Data Types}

The iterator layout is an internal detail, and user code only sees an incomplete struct.

\section*{NpyIter}

This is an opaque pointer type for the iterator. Access to its contents can only be done through the iterator API.

\section*{NpyIter_Type}

This is the type which exposes the iterator to Python. Currently, no API is exposed which provides access to the values of a Python-created iterator. If an iterator is created in Python, it must be used in Python and vice versa. Such an API will likely be created in a future version.

\section*{NpyIter_IterNextFunc}

This is a function pointer for the iteration loop, returned by NpyIter_GetIterNext.

\section*{NpyIter_GetMultiIndexFunc}

This is a function pointer for getting the current iterator multi-index, returned by NpyIter_GetGetMultiIndex.

\subsection*{5.5.6 Construction and Destruction}

NpyIter* NpyIter_New (PyArrayObject* op, npy_uint32 flags, NPY_ORDER order, NPY_CASTING casting, PyArray_Descr* dtype)
Creates an iterator for the given numpy array object op.
Flags that may be passed in flags are any combination of the global and per-operand flags documented in NpyIter_MultiNew, except for NPY_ITER_ALLOCATE.

Any of the NPY_ORDER enum values may be passed to order. For efficient iteration, NPY_KEEPORDER is the best option, and the other orders enforce the particular iteration pattern.

Any of the NPY_CASTING enum values may be passed to casting. The values include NPY_NO_CASTING, NPY_EQUIV_CASTING, NPY_SAFE_CASTING, NPY_SAME_KIND_CASTING, and

NPY_UNSAFE_CASTING. To allow the casts to occur, copying or buffering must also be enabled.
If dtype isn't NULL, then it requires that data type. If copying is allowed, it will make a temporary copy if the data is castable. If NPY_ITER_UPDATEIFCOPY is enabled, it will also copy the data back with another cast upon iterator destruction.
Returns NULL if there is an error, otherwise returns the allocated iterator.
To make an iterator similar to the old iterator, this should work.
```

iter = NpyIter_New(op, NPY_ITER_READWRITE,
NPY_CORDER, NPY_NO_CASTING, NULL);

```

If you want to edit an array with aligned double code, but the order doesn't matter, you would use this.
dtype = PyArray_DescrFromType(NPY_DOUBLE);
iter \(=\) NpyIter_New (op, NPY_ITER_READWRITE|
NPY_ITER_BUFFERED|
NPY_ITER_NBO|
NPY_ITER_ALIGNED,
NPY_KEEPORDER, NPY_SAME_KIND_CASTING, dtype);
Py_DECREF (dtype);
NpyIter* NpyIter_MultiNew (npy_intp nop, PyArrayObject** op, npy_uint32 flags, NPY_ORDER order, NPY_CASTING casting, npy_uint32* op_flags, PyArray_Descr** op_dtypes)
Creates an iterator for broadcasting the nop array objects provided in op, using regular NumPy broadcasting rules.

Any of the NPY_ORDER enum values may be passed to order. For efficient iteration, NPY_KEEPORDER is the best option, and the other orders enforce the particular iteration pattern. When using NPY_KEEPORDER, if you also want to ensure that the iteration is not reversed along an axis, you should pass the flag NPY_ITER_DONT_NEGATE_STRIDES.
Any of the NPY_CASTING enum values may be passed to casting. The values include NPY_NO_CASTING, NPY_EQUIV_CASTING, NPY_SAFE_CASTING, NPY_SAME_KIND_CASTING, and NPY_UNSAFE_CASTING. To allow the casts to occur, copying or buffering must also be enabled.

If op_dtypes isn't NULL, it specifies a data type or NULL for each op [i].
Returns NULL if there is an error, otherwise returns the allocated iterator.
Flags that may be passed in flags, applying to the whole iterator, are:
NPY_ITER_C_INDEX
Causes the iterator to track a raveled flat index matching C order. This option cannot be used with NPY_ITER_F_INDEX.

NPY_ITER_F_INDEX
Causes the iterator to track a raveled flat index matching Fortran order. This option cannot be used with NPY_ITER_C_INDEX.
NPY_ITER_MULTI_INDEX
Causes the iterator to track a multi-index. This prevents the iterator from coalescing axes to produce bigger inner loops.

\section*{NPY_ITER_EXTERNAL_LOOP}

Causes the iterator to skip iteration of the innermost loop, requiring the user of the iterator to handle it.

This flag is incompatible with NPY_ITER_C_INDEX, NPY_ITER_F_INDEX, and NPY_ITER_MULTI_INDEX.

NPY_ITER_DONT_NEGATE_STRIDES
This only affects the iterator when NPY_KEEPORDER is specified for the order parameter. By default with NPY_KEEPORDER, the iterator reverses axes which have negative strides, so that memory is traversed in a forward direction. This disables this step. Use this flag if you want to use the underlying memory-ordering of the axes, but don't want an axis reversed. This is the behavior of numpy. ravel ( \(a\), order=' \(\mathrm{K}^{\prime}\) ), for instance.

NPY_ITER_COMMON_DTYPE
Causes the iterator to convert all the operands to a common data type, calculated based on the ufunc type promotion rules. Copying or buffering must be enabled.

If the common data type is known ahead of time, don't use this flag. Instead, set the requested dtype for all the operands.

\section*{NPY ITER REFS OK}

Indicates that arrays with reference types (object arrays or structured arrays containing an object type) may be accepted and used in the iterator. If this flag is enabled, the caller must be sure to check whether :cfunc:'NpyIter_IterationNeedsAPI‘(iter) is true, in which case it may not release the GIL during iteration.

\section*{NPY_ITER_ZEROSIZE_OK}

Indicates that arrays with a size of zero should be permitted. Since the typical iteration loop does not naturally work with zero-sized arrays, you must check that the IterSize is non-zero before entering the iteration loop.

\section*{NPY_ITER_REDUCE_OK}

Permits writeable operands with a dimension with zero stride and size greater than one. Note that such operands must be read/write.
When buffering is enabled, this also switches to a special buffering mode which reduces the loop length as necessary to not trample on values being reduced.

Note that if you want to do a reduction on an automatically allocated output, you must use NpyIter_GetOperandArray to get its reference, then set every value to the reduction unit before doing the iteration loop. In the case of a buffered reduction, this means you must also specify the flag NPY_ITER_DELAY_BUFALLOC, then reset the iterator after initializing the allocated operand to prepare the buffers.

\section*{NPY_ITER_RANGED}

Enables support for iteration of sub-ranges of the full iterindex range [0, NpyIter_IterSize(iter)). Use the function NpyIter_ResetToIterIndexRange to specify a range for iteration.

This flag can only be used with NPY_ITER_EXTERNAL_LOOP when NPY_ITER_BUFFERED is enabled. This is because without buffering, the inner loop is always the size of the innermost iteration dimension, and allowing it to get cut up would require special handling, effectively making it more like the buffered version.

\section*{NPY_ITER_BUFFERED}

Causes the iterator to store buffering data, and use buffering to satisfy data type, alignment, and byte-order requirements. To buffer an operand, do not specify the NPY_ITER_COPY or NPY_ITER_UPDATEIFCOPY flags, because they will override buffering. Buffering is especially useful for Python code using the iterator, allowing for larger chunks of data at once to amortize the Python interpreter overhead.

If used with NPY_ITER_EXTERNAL_LOOP, the inner loop for the caller may get larger chunks than would be possible without buffering, because of how the strides are laid out.

Note that if an operand is given the flag NPY_ITER_COPY or NPY_ITER_UPDATEIFCOPY, a copy will be made in preference to buffering. Buffering will still occur when the array was broadcast so elements need to be duplicated to get a constant stride.
In normal buffering, the size of each inner loop is equal to the buffer size, or possibly larger if NPY_ITER_GROWINNER is specified. If NPY_ITER_REDUCE_OK is enabled and a reduction occurs, the inner loops may become smaller depending on the structure of the reduction.

\section*{NPY_ITER_GROWINNER}

When buffering is enabled, this allows the size of the inner loop to grow when buffering isn't necessary. This option is best used if you're doing a straight pass through all the data, rather than anything with small cache-friendly arrays of temporary values for each inner loop.

\section*{NPY_ITER_DELAY_BUFALLOC}

When buffering is enabled, this delays allocation of the buffers until NpyIter_Reset or another reset function is called. This flag exists to avoid wasteful copying of buffer data when making multiple copies of a buffered iterator for multi-threaded iteration.
Another use of this flag is for setting up reduction operations. After the iterator is created, and a reduction output is allocated automatically by the iterator (be sure to use READWRITE access), its value may be initialized to the reduction unit. Use NpyIter_GetoperandArray to get the object. Then, call NpyIter_Reset to allocate and fill the buffers with their initial values.

Flags that may be passed in op_flags [i], where \(0<=i<n o p:\)
```

NPY_ITER_READWRITE

```
```

NPY_ITER_READONLY

```

\section*{NPY_ITER_WRITEONLY}

Indicate how the user of the iterator will read or write to op [i]. Exactly one of these flags must be specified per operand.

\section*{NPY_ITER_COPY}

Allow a copy of op [i] to be made if it does not meet the data type or alignment requirements as specified by the constructor flags and parameters.

\section*{NPY_ITER_UPDATEIFCOPY}

Triggers NPY_ITER_COPY, and when an array operand is flagged for writing and is copied, causes the data in a copy to be copied back to op [i] when the iterator is destroyed.

If the operand is flagged as write-only and a copy is needed, an uninitialized temporary array will be created and then copied to back to op [i] on destruction, instead of doing the unecessary copy operation.
```

NPY_ITER_NBO

```

NPY_ITER_ALIGNED

\section*{NPY_ITER_CONTIG}

Causes the iterator to provide data for op [i] that is in native byte order, aligned according to the dtype requirements, contiguous, or any combination.
By default, the iterator produces pointers into the arrays provided, which may be aligned or unaligned, and with any byte order. If copying or buffering is not enabled and the operand data doesn't satisfy the constraints, an error will be raised.

The contiguous constraint applies only to the inner loop, successive inner loops may have arbitrary pointer changes.
If the requested data type is in non-native byte order, the NBO flag overrides it and the requested data type is converted to be in native byte order.

\section*{NPY_ITER_ALLOCATE}

This is for output arrays, and requires that the flag NPY_ITER_WRITEONLY be set. If op [i] is NULL, creates a new array with the final broadcast dimensions, and a layout matching the iteration order of the iterator.

When op [i] is NULL, the requested data type op_dtypes [i] may be NULL as well, in which case it is automatically generated from the dtypes of the arrays which are flagged as readable. The rules for generating the dtype are the same is for UFuncs. Of special note is handling of byte order in the selected dtype. If there is exactly one input, the input's dtype is used as is. Otherwise, if more than one input dtypes are combined together, the output will be in native byte order.

After being allocated with this flag, the caller may retrieve the new array by calling NpyIter_GetOperandArray and getting the i-th object in the returned C array. The caller must call Py_INCREF on it to claim a reference to the array.

\section*{NPY_ITER_NO_SUBTYPE}

For use with NPY_ITER_ALLOCATE, this flag disables allocating an array subtype for the output, forcing it to be a straight ndarray.

TODO: Maybe it would be better to introduce a function NpyIter_GetWrappedOutput and remove this flag?

NPY_ITER_NO_BROADCAST
Ensures that the input or output matches the iteration dimensions exactly.
NpyIter* NpyIter_AdvancedNew (npy_intp nop, PyArrayObject** op, npy_uint32 flags, NPY_ORDER order, NPY_CASTING casting, npy_uint32* op_flags, PyArray_Descr** op_dtypes, int oa_ndim, int** op_axes, npy_intp* itershape, npy_intp buffersize)
Extends NpyIter_MultiNew with several advanced options providing more control over broadcasting and buffering.

If 0/NULL values are passed to oa_ndim, op_axes, itershape, and buffersize, it is equivalent to NpyIter_MultiNew.

The parameter oa_ndim, when non-zero, specifies the number of dimensions that will be iterated with customized broadcasting. If it is provided, op_axes and/or itershape must also be provided. The op_axes parameter let you control in detail how the axes of the operand arrays get matched together and iterated. In op_axes, you must provide an array of nop pointers to oa_ndim-sized arrays of type npy_intp. If an entry in op_axes is NULL, normal broadcasting rules will apply. In op_axes [j] [i] is stored either a valid axis of op [j], or -1 which means newaxis. Within each op_axes [j] array, axes may not be repeated. The following example is how normal broadcasting applies to a 3-D array, a 2-D array, a 1-D array and a scalar.
```

int oa_ndim = 3; /* \# iteration axes */
int op0_axes[] = {0, 1, 2}; /* 3-D operand */
int op1_axes[] = {-1, 0, 1}; /* 2-D operand */
int op2_axes[] = {-1, -1, 0}; /* 1-D operand */
int op3_axes[] = {-1, -1, -1} /* O-D (scalar) operand */
int* op_axes[] = {op0_axes, op1_axes, op2_axes, op3_axes};

```

The itershape parameter allows you to force the iterator to have a specific iteration shape. It is an array of length oa_ndim. When an entry is negative, its value is determined from the operands. This parameter allows
automatically allocated outputs to get additional dimensions which don't match up with any dimension of an input.

If buffersize is zero, a default buffer size is used, otherwise it specifies how big of a buffer to use. Buffers which are powers of 2 such as 4096 or 8192 are recommended.

Returns NULL if there is an error, otherwise returns the allocated iterator.
NpyIter* NpyIter_Copy (NpyIter* iter)
Makes a copy of the given iterator. This function is provided primarily to enable multi-threaded iteration of the data.

TODO: Move this to a section about multithreaded iteration.
The recommended approach to multithreaded iteration is to first create an iterator with the flags NPY_ITER_EXTERNAL_LOOP, NPY_ITER_RANGED, NPY_ITER_BUFFERED, NPY_ITER_DELAY_BUFALLOC, and possibly NPY_ITER_GROWINNER. Create a copy of this iterator for each thread (minus one for the first iterator). Then, take the iteration index range [0, NpyIter_GetIterSize(iter)) and split it up into tasks, for example using a TBB parallel_for loop. When a thread gets a task to execute, it then uses its copy of the iterator by calling NpyIter_ResetToIterIndexRange and iterating over the full range.

When using the iterator in multi-threaded code or in code not holding the Python GIL, care must be taken to only call functions which are safe in that context. NpyIter_Copy cannot be safely called without the Python GIL, because it increments Python references. The Reset * and some other functions may be safely called by passing in the errmsg parameter as non-NULL, so that the functions will pass back errors through it instead of setting a Python exception.
int NpyIter_RemoveAxis (NpyIter* iter, int axis)"
Removes an axis from iteration. This requires that NPY_ITER_MULTI_INDEX was set for iterator creation, and does not work if buffering is enabled or an index is being tracked. This function also resets the iterator to its initial state.

This is useful for setting up an accumulation loop, for example. The iterator can first be created with all the dimensions, including the accumulation axis, so that the output gets created correctly. Then, the accumulation axis can be removed, and the calculation done in a nested fashion.

WARNING: This function may change the internal memory layout of the iterator. Any cached functions or pointers from the iterator must be retrieved again!

Returns NPY_SUCCEED or NPY_FAIL.
int NpyIter_RemoveMultiIndex (NpyIter* iter)
If the iterator is tracking a multi-index, this strips support for them, and does further iterator optimizations that are possible if multi-indices are not needed. This function also resets the iterator to its initial state.

WARNING: This function may change the internal memory layout of the iterator. Any cached functions or pointers from the iterator must be retrieved again!

After calling this function, :cfunc:'NpyIter_HasMultiIndex'(iter) will return false.
Returns NPY_SUCCEED or NPY_FAIL.
int NpyIter_EnableExternalLoop (NpyIter* iter)
If NpyIter_RemoveMultiIndex was called, you may want to enable the flag NPY_ITER_EXTERNAL_LOOP. This flag is not permitted together with NPY_ITER_MULTI_INDEX, so this function is provided to enable the feature after NpyIter_RemoveMultiIndex is called. This function also resets the iterator to its initial state.

WARNING: This function changes the internal logic of the iterator. Any cached functions or pointers from the iterator must be retrieved again!

Returns NPY_SUCCEED or NPY_FAIL.
int NpyIter_Deallocate (NpyIter*iter)
Deallocates the iterator object. This additionally frees any copies made, triggering UPDATEIFCOPY behavior where necessary.

Returns NPY_SUCCEED or NPY_FAIL.
int NpyIter_Reset (NpyIter* iter, char** errmsg)
Resets the iterator back to its initial state, at the beginning of the iteration range.
Returns NPY_SUCCEED or NPY_FAIL. If errmsg is non-NULL, no Python exception is set when NPY_FAIL is returned. Instead, *errmsg is set to an error message. When errmsg is non-NULL, the function may be safely called without holding the Python GIL.
int NpyIter_ResetToIterIndexRange (NpyIter* iter, npy_intp istart, npy_intp iend, char** errmsg)
Resets the iterator and restricts it to the iterindex range [istart, iend). See NpyIter_Copy for an explanation of how to use this for multi-threaded iteration. This requires that the flag NPY_ITER_RANGED was passed to the iterator constructor.

If you want to reset both the iterindex range and the base pointers at the same time, you can do the following to avoid extra buffer copying (be sure to add the return code error checks when you copy this code).
```

/* Set to a trivial empty range */
NpyIter_ResetToIterIndexRange(iter, 0, 0);
/* Set the base pointers */
NpyIter_ResetBasePointers(iter, baseptrs);
/* Set to the desired range */
NpyIter_ResetToIterIndexRange(iter, istart, iend);

```

Returns NPY_SUCCEED or NPY_FAIL. If errmsg is non-NULL, no Python exception is set when NPY_FAIL is returned. Instead, *errmsg is set to an error message. When errmsg is non-NULL, the function may be safely called without holding the Python GIL.
int NpyIter_ResetBasePointers (NpyIter *iter, char** baseptrs, char** errmsg)
Resets the iterator back to its initial state, but using the values in baseptrs for the data instead of the pointers from the arrays being iterated. This functions is intended to be used, together with the op_axes parameter, by nested iteration code with two or more iterators.

Returns NPY_SUCCEED or NPY_FAIL. If errmsg is non-NULL, no Python exception is set when NPY_FAIL is returned. Instead, *errmsg is set to an error message. When errmsg is non-NULL, the function may be safely called without holding the Python GIL.
\(T O D O\) : Move the following into a special section on nested iterators.
Creating iterators for nested iteration requires some care. All the iterator operands must match exactly, or the calls to NpyIter_ResetBasePointers will be invalid. This means that automatic copies and output allocation should not be used haphazardly. It is possible to still use the automatic data conversion and casting features of the iterator by creating one of the iterators with all the conversion parameters enabled, then grabbing the allocated operands with the NpyIter_GetOperandArray function and passing them into the constructors for the rest of the iterators.

WARNING: When creating iterators for nested iteration, the code must not use a dimension more than once in the different iterators. If this is done, nested iteration will produce out-of-bounds pointers during iteration.

WARNING: When creating iterators for nested iteration, buffering can only be applied to the innermost iterator. If a buffered iterator is used as the source for baseptrs, it will point into a small buffer instead of the array and the inner iteration will be invalid.

The pattern for using nested iterators is as follows.
```

NpyIter *iter1, *iter1;
NpyIter_IterNextFunc *iternext1, *iternext2;
char **dataptrs1;
/*
* With the exact same operands, no copies allowed, and
* no axis in op_axes used both in iterl and iter2.
* Buffering may be enabled for iter2, but not for iter1.
*/
iter1 = ...; iter2 = ...;
iternext1 = NpyIter_GetIterNext(iter1);
iternext2 = NpyIter_GetIterNext(iter2);
dataptrs1 = NpyIter_GetDataPtrArray(iter1);
do {
NpyIter_ResetBasePointers(iter2, dataptrs1);
do {
/* Use the iter2 values */
} while (iternext2(iter2));
} while (iternextl(iterl));

```
int NpyIter_GotoMultiIndex (NpyIter* iter, npy_intp* multi_index)
Adjusts the iterator to point to the ndim indices pointed to by multi_index. Returns an error if a multi-index is not being tracked, the indices are out of bounds, or inner loop iteration is disabled.

Returns NPY_SUCCEED or NPY_FAIL.
int NpyIter_GotoIndex (NpyIter* iter, npy_intp index)
Adjusts the iterator to point to the index specified. If the iterator was constructed with the flag NPY_ITER_C_INDEX, index is the C-order index, and if the iterator was constructed with the flag NPY_ITER_F_INDEX, index is the Fortran-order index. Returns an error if there is no index being tracked, the index is out of bounds, or inner loop iteration is disabled.

Returns NPY_SUCCEED or NPY_FAIL.
npy_intp NpyIter_GetIterSize (NpyIter* iter)
Returns the number of elements being iterated. This is the product of all the dimensions in the shape.
npy_intp NpyIter_GetIterIndex (NpyIter* iter)
Gets the iterindex of the iterator, which is an index matching the iteration order of the iterator.
void NpyIter_GetIterIndexRange (NpyIter* iter, npy_intp* istart, npy_intp* iend)
Gets the iterindex sub-range that is being iterated. If NPY_ITER_RANGED was not specified, this always returns the range [0, NpyIter_IterSize(iter)).
int NpyIter_GotoIterIndex (NpyIter* iter, npy_intp iterindex)
Adjusts the iterator to point to the iterindex specified. The IterIndex is an index matching the iteration order of the iterator. Returns an error if the iterindex is out of bounds, buffering is enabled, or inner loop iteration is disabled.

Returns NPY_SUCCEED or NPY_FAIL.
npy_bool NpyIter_HasDelayedBufAlloc (NpyIter* iter)
Returns 1 if the flag NPY_ITER_DELAY_BUFALLOC was passed to the iterator constructor, and no call to one of the Reset functions has been done yet, 0 otherwise.
npy_bool NpyIter_HasExternalLoop (NpyIter* iter)
Returns 1 if the caller needs to handle the inner-most 1-dimensional loop, or 0 if the iterator handles all looping. This is controlled by the constructor flag NPY_ITER_EXTERNAL_LOOP or

NpyIter_EnableExternalLoop.
npy_bool NpyIter_HasMultiIndex (NpyIter* iter)
Returns 1 if the iterator was created with the NPY_ITER_MULTI_INDEX flag, 0 otherwise.

\section*{npy_bool NpyIter_HasIndex (NpyIter* iter)}

Returns 1 if the iterator was created with the NPY_ITER_C_INDEX or NPY_ITER_F_INDEX flag, 0 otherwise.

\section*{npy_bool NpyIter_RequiresBuffering (NpyIter* iter)}

Returns 1 if the iterator requires buffering, which occurs when an operand needs conversion or alignment and so cannot be used directly.
```

npy_bool NpyIter_IsBuffered (NpyIter* iter)

```

Returns 1 if the iterator was created with the NPY_ITER_BUFFERED flag, 0 otherwise.
npy_bool NpyIter_IsGrowInner (NpyIter* iter)
Returns 1 if the iterator was created with the NPY_ITER_GROWINNER flag, 0 otherwise.
npy_intp NpyIter_GetBufferSize (NpyIter* iter)
If the iterator is buffered, returns the size of the buffer being used, otherwise returns 0 .
int NpyIter_GetNDim (NpyIter* iter)
Returns the number of dimensions being iterated. If a multi-index was not requested in the iterator constructor, this value may be smaller than the number of dimensions in the original objects.
int NpyIter_GetNOp (NpyIter* iter)
Returns the number of operands in the iterator.
npy_intp* NpyIter_GetAxisStrideArray (NpyIter* iter, int axis)
Gets the array of strides for the specified axis. Requires that the iterator be tracking a multi-index, and that buffering not be enabled.

This may be used when you want to match up operand axes in some fashion, then remove them with NpyIter_RemoveAxis to handle their processing manually. By calling this function before removing the axes, you can get the strides for the manual processing.

Returns NULL on error.
int NpyIter_GetShape (NpyIter* iter, npy_intp* outshape)
Returns the broadcast shape of the iterator in outshape. This can only be called on an iterator which is tracking a multi-index.

Returns NPY_SUCCEED or NPY_FAIL.
PyArray_Descr** NpyIter_GetDescrArray (NpyIter* iter)
This gives back a pointer to the nop data type Descrs for the objects being iterated. The result points into iter, so the caller does not gain any references to the Descrs.

This pointer may be cached before the iteration loop, calling iternext will not change it.
PyObject** NpyIter_GetOperandArray (NpyIter* iter)
This gives back a pointer to the nop operand PyObjects that are being iterated. The result points into iter, so the caller does not gain any references to the PyObjects.

PyObject* NpyIter_GetIterView (NpyIter* iter, npy_intp \(i\) )
This gives back a reference to a new ndarray view, which is a view into the i-th object in the array :cfunc: \({ }^{\text {N NpyIter_GetOperandArray }}\) (), whose dimensions and strides match the internal optimized iteration pattern. A C-order iteration of this view is equivalent to the iterator's iteration order.

For example, if an iterator was created with a single array as its input, and it was possible to rearrange all its axes and then collapse it into a single strided iteration, this would return a view that is a one-dimensional array.
void NpyIter_GetReadFlags (NpyIter* iter, char* outreadflags)
Fills nop flags. Sets outreadflags [i] to 1 if op [i] can be read from, and to 0 if not.
void NpyIter_GetWriteFlags (NpyIter* iter, char* outwriteflags)
Fills nop flags. Sets outwriteflags [i] to 1 if op [i] can be written to, and to 0 if not.
int NpyIter_CreateCompatibleStrides (NpyIter* iter, npy_intp itemsize, npy_intp* outstrides)
Builds a set of strides which are the same as the strides of an output array created using the NPY_ITER_ALLOCATE flag, where NULL was passed for op_axes. This is for data packed contiguously, but not necessarily in C or Fortran order. This should be used together with NpyIter_GetShape and NpyIter_GetNDim with the flag NPY_ITER_MULTI_INDEX passed into the constructor.
A use case for this function is to match the shape and layout of the iterator and tack on one or more dimensions. For example, in order to generate a vector per input value for a numerical gradient, you pass in ndim*itemsize for itemsize, then add another dimension to the end with size ndim and stride itemsize. To do the Hessian matrix, you do the same thing but add two dimensions, or take advantage of the symmetry and pack it into 1 dimension with a particular encoding.
This function may only be called if the iterator is tracking a multi-index and if NPY_ITER_DONT_NEGATE_STRIDES was used to prevent an axis from being iterated in reverse order.

If an array is created with this method, simply adding 'itemsize' for each iteration will traverse the new array matching the iterator.

Returns NPY_SUCCEED or NPY_FAIL.

\subsection*{5.5.7 Functions For Iteration}

NpyIter_IterNextFunc* NpyIter_GetIterNext (NpyIter* iter, char** errmsg)
Returns a function pointer for iteration. A specialized version of the function pointer may be calculated by this function instead of being stored in the iterator structure. Thus, to get good performance, it is required that the function pointer be saved in a variable rather than retrieved for each loop iteration.

Returns NULL if there is an error. If errmsg is non-NULL, no Python exception is set when NPY_FAIL is returned. Instead, *errmsg is set to an error message. When errmsg is non-NULL, the function may be safely called without holding the Python GIL.
The typical looping construct is as follows.
```

NpyIter_IterNextFunc *iternext = NpyIter_GetIterNext(iter, NULL);
char** dataptr = NpyIter_GetDataPtrArray(iter);
do {
/* use the addresses dataptr[0], ... dataptr[nop-1] */
} while(iternext(iter));

```

When NPY_ITER_EXTERNAL_LOOP is specified, the typical inner loop construct is as follows.
```

NpyIter_IterNextFunc *iternext = NpyIter_GetIterNext(iter, NULL);
char** dataptr = NpyIter_GetDataPtrArray(iter);
npy_intp* stride = NpyIter_GetInnerStrideArray(iter);
npy_intp* size_ptr = NpyIter_GetInnerLoopSizePtr(iter), size;
npy_intp iop, nop = NpyIter_GetNOp(iter);
do {
size = *size_ptr;
while (size--) {
/* use the addresses dataptr[0], ... dataptr[nop-1] */

```
```

        for (iop = 0; iop < nop; ++iop) {
        dataptr[iop] += stride[iop];
        }
    }
    } while (iternext());

```

Observe that we are using the dataptr array inside the iterator, not copying the values to a local temporary. This is possible because when iternext () is called, these pointers will be overwritten with fresh values, not incrementally updated.

If a compile-time fixed buffer is being used (both flags NPY_ITER_BUFFERED and NPY_ITER_EXTERNAL_LOOP), the inner size may be used as a signal as well. The size is guaranteed to become zero when iternext () returns false, enabling the following loop construct. Note that if you use this construct, you should not pass NPY_ITER_GROWINNER as a flag, because it will cause larger sizes under some circumstances.
```

/* The constructor should have buffersize passed as this value */
\#define FIXED_BUFFER_SIZE 1024
NpyIter_IterNextFunc *iternext = NpyIter_GetIterNext(iter, NULL);
char **dataptr = NpyIter_GetDataPtrArray(iter);
npy_intp *stride = NpyIter_GetInnerStrideArray(iter);
npy_intp *size_ptr = NpyIter_GetInnerLoopSizePtr(iter), size;
npy_intp i, iop, nop = NpyIter_GetNOp(iter);
/* One loop with a fixed inner size */
size = *size_ptr;
while (size == FIXED_BUFFER_SIZE) {
/*
* This loop could be manually unrolled by a factor
* which divides into FIXED_BUFFER_SIZE
*/
for (i = 0; i < FIXED_BUFFER_SIZE; ++i) {
/* use the addresses dataptr[0], ... dataptr[nop-1] */
for (iop = 0; iop < nop; ++iop) {
dataptr[iop] += stride[iop];
}
}
iternext();
size = *size_ptr;
}
/* Finish-up loop with variable inner size */
if (size > 0) do {
size = *size_ptr;
while (size--) {
/* use the addresses dataptr[0], ... dataptr[nop-1] */
for (iop = 0; iop < nop; ++iop) {
dataptr[iop] += stride[iop];
}
}
} while (iternext());

```

NpyIter_GetMultiIndexFunc *NpyIter_GetGetMultiIndex (NpyIter* iter, char** errmsg)
Returns a function pointer for getting the current multi-index of the iterator. Returns NULL if the iterator is not tracking a multi-index. It is recommended that this function pointer be cached in a local variable before the iteration loop.

Returns NULL if there is an error. If errmsg is non-NULL, no Python exception is set when NPY_FAIL is
returned. Instead, *errmsg is set to an error message. When errmsg is non-NULL, the function may be safely called without holding the Python GIL.
char** NpyIter_GetDataPtrArray (NpyIter* iter)
This gives back a pointer to the nop data pointers. If NPY_ITER_EXTERNAL_LOOP was not specified, each data pointer points to the current data item of the iterator. If no inner iteration was specified, it points to the first data item of the inner loop.

This pointer may be cached before the iteration loop, calling iternext will not change it. This function may be safely called without holding the Python GIL.
char** NpyIter_GetInitialDataPtrArray (NpyIter* iter)
Gets the array of data pointers directly into the arrays (never into the buffers), corresponding to iteration index 0.

These pointers are different from the pointers accepted by NpyIter_ResetBasePointers, because the direction along some axes may have been reversed.

This function may be safely called without holding the Python GIL.
npy_intp* NpyIter_GetIndexPtr (NpyIter* iter)
This gives back a pointer to the index being tracked, or NULL if no index is being tracked. It is only useable if one of the flags NPY_ITER_C_INDEX or NPY_ITER_F_INDEX were specified during construction.

When the flag NPY_ITER_EXTERNAL_LOOP is used, the code needs to know the parameters for doing the inner loop. These functions provide that information.
npy_intp* NpyIter_GetInnerStrideArray (NpyIter* iter)
Returns a pointer to an array of the nop strides, one for each iterated object, to be used by the inner loop.
This pointer may be cached before the iteration loop, calling iternext will not change it. This function may be safely called without holding the Python GIL.
npy_intp* NpyIter_GetInnerLoopSizePtr (NpyIter* iter)
Returns a pointer to the number of iterations the inner loop should execute.
This address may be cached before the iteration loop, calling iternext will not change it. The value itself may change during iteration, in particular if buffering is enabled. This function may be safely called without holding the Python GIL.
void NpyIter_GetInnerFixedStrideArray (NpyIter* iter, npy_intp* out_strides)
Gets an array of strides which are fixed, or will not change during the entire iteration. For strides that may change, the value NPY_MAX_INTP is placed in the stride.
Once the iterator is prepared for iteration (after a reset if NPY_DELAY_BUFALLOC was used), call this to get the strides which may be used to select a fast inner loop function. For example, if the stride is 0 , that means the inner loop can always load its value into a variable once, then use the variable throughout the loop, or if the stride equals the itemsize, a contiguous version for that operand may be used.

This function may be safely called without holding the Python GIL.

\subsection*{5.6 UFunc API}

\subsection*{5.6.1 Constants}

UFUNC_ERR_\{ HANDLER\}
\{HANDLER\} can be IGNORE, WARN, RAISE, or CALL

UFUNC_\{THING\}_\{ERR\}
\(\{T H I N G\}\) can be MASK, SHIFT, or FPE, and \(\{E R R\}\) can be DIVIDEBYZERO, OVERFLOW, UNDERFLOW, and INVALID.

PyUFunc_\{VALUE \}
\{VALUE \} can be One (1), Zero (0), or None (-1)

\subsection*{5.6.2 Macros}

\section*{NPY_LOOP_BEGIN_THREADS}

Used in universal function code to only release the Python GIL if loop->obj is not true (i.e. this is not an OBJECT array loop). Requires use of NPY_BEGIN_THREADS_DEF in variable declaration area.

\section*{NPY_LOOP_END_THREADS}

Used in universal function code to re-acquire the Python GIL if it was released (because loop->obj was not true).

\section*{UFUNC_CHECK_ERROR (loop)}

A macro used internally to check for errors and goto fail if found. This macro requires a fail label in the current code block. The loop variable must have at least members (obj, errormask, and errorobj). If loop \(->\) obj is nonzero, then PyErr_Occurred () is called (meaning the GIL must be held). If loop ->obj is zero, then if loop ->errormask is nonzero, PyUFunc_checkfperr is called with arguments loop ->errormask and loop \(->\) errobj. If the result of this check of the IEEE floating point registers is true then the code redirects to the fail label which must be defined.

\section*{UFUNC_CHECK_STATUS (ret)}

A macro that expands to platform-dependent code. The ret variable can can be any integer. The UFUNC_FPE_\{ERR\} bits are set in ret according to the status of the corresponding error flags of the floating point processor.

\subsection*{5.6.3 Functions}
```

PyObject* PyUFunc_FromFuncAndData(PyUFuncGenericFunction* func,
void** data, char* types, int ntypes, int nin, int nout, int identity,
char* name, char* doc, int check_return)

```

Create a new broadcasting universal function from required variables. Each ufunc builds around the notion of an element-by-element operation. Each ufunc object contains pointers to 1-d loops implementing the basic functionality for each supported type.

Note: The func, data, types, name, and doc arguments are not copied by PyUFunc_FromFuncAndData. The caller must ensure that the memory used by these arrays is not freed as long as the ufunc object is alive.

\section*{Parameters}
- func - Must to an array of length ntypes containing PyUFuncGenericFunction items. These items are pointers to functions that actually implement the underlying (element-byelement) function \(N\) times.
- data - Should be NULL or a pointer to an array of size ntypes. This array may contain arbitrary extra-data to be passed to the corresponding 1-d loop function in the func array.
- types - Must be of length \((\) nin + nout \() *\) ntypes, and it contains the data-types (built-in only) that the corresponding function in the func array can deal with.
- ntypes - How many different data-type "signatures" the ufunc has implemented.
- nin - The number of inputs to this operation.
- nout - The number of outputs
- name - The name for the ufunc. Specifying a name of 'add' or 'multiply' enables a special behavior for integer-typed reductions when no dtype is given. If the input type is an integer (or boolean) data type smaller than the size of the int_ data type, it will be internally upcast to the int_ (or uint) data type.
- doc - Allows passing in a documentation string to be stored with the ufunc. The documentation string should not contain the name of the function or the calling signature as that will be dynamically determined from the object and available when accessing the __doc attribute of the ufunc.
- check_return - Unused and present for backwards compatibility of the C-API. A corresponding check_return integer does exist in the ufunc structure and it does get set with this value when the ufunc object is created.
```

int PyUFunc_RegisterLoopForType(PyUFuncObject* ufunc,
int usertype, PyUFuncGenericFunction function, int* arg_types, void* data)

```

This function allows the user to register a 1-d loop with an already- created ufunc to be used whenever the ufunc is called with any of its input arguments as the user-defined data-type. This is needed in order to make ufuncs work with built-in data-types. The data-type must have been previously registered with the numpy system. The loop is passed in as function. This loop can take arbitrary data which should be passed in as data. The data-types the loop requires are passed in as arg_types which must be a pointer to memory at least as large as ufunc->nargs.

\section*{int PyUFunc_ReplaceLoopBySignature (PyUFuncObject* ufunc,}
```

PyUFuncGenericFunction newfunc, int* signature,

```

\section*{PyUFuncGenericFunction* oldfunc)}

Replace a 1-d loop matching the given signature in the already-created ufunc with the new 1-d loop newfunc. Return the old 1-d loop function in oldfunc. Return 0 on success and -1 on failure. This function works only with built-in types (use PyUFunc_RegisterLoopForType for user-defined types). A signature is an array of data-type numbers indicating the inputs followed by the outputs assumed by the 1-d loop.
int PyUFunc_GenericFunction (PyUFuncObject* self,
PyObject* args, PyObject* kwds, PyArrayObject** mps)
A generic ufunc call. The ufunc is passed in as self, the arguments to the ufunc as args and kwds. The mps argument is an array of PyArrayObject pointers whose values are discarded and which receive the converted input arguments as well as the ufunc outputs when success is returned. The user is responsible for managing this array and receives a new reference for each array in \(m p s\). The total number of arrays in mps is given by self \(->\) nin + self \(->\) nout.

Returns 0 on success, -1 on error.
int PyUFunc_checkfperr (int errmask, PyObject* errobj)
A simple interface to the IEEE error-flag checking support. The errmask argument is a mask of UFUNC_MASK_\{ERR\} bitmasks indicating which errors to check for (and how to check for them). The errobj must be a Python tuple with two elements: a string containing the name which will be used in any communication of error and either a callable Python object (call-back function) or Py_None. The callable object will only be used if UFUNC_ERR_CALL is set as the desired error checking method. This routine manages the GIL and is safe to call even after releasing the GIL. If an error in the IEEE-compatibile hardware is determined a -1 is returned, otherwise a 0 is returned.
void PyUFunc_clearfperr ()
Clear the IEEE error flags.
```

void PyUFunc_GetPyValues (char* name, int* bufsize,

```
int* errmask, PyObject** errobj)
Get the Python values used for ufunc processing from the thread-local storage area unless the defaults have been set in which case the name lookup is bypassed. The name is placed as a string in the first element of *errobj. The second element is the looked-up function to call on error callback. The value of the looked-up buffer-size to use is passed into bufsize, and the value of the error mask is placed into errmask.

\subsection*{5.6.4 Generic functions}

At the core of every ufunc is a collection of type-specific functions that defines the basic functionality for each of the supported types. These functions must evaluate the underlying function \(N \geq 1\) times. Extra-data may be passed in that may be used during the calculation. This feature allows some general functions to be used as these basic looping functions. The general function has all the code needed to point variables to the right place and set up a function call. The general function assumes that the actual function to call is passed in as the extra data and calls it with the correct values. All of these functions are suitable for placing directly in the array of functions stored in the functions member of the PyUFuncObject structure.
```

void PyUFunc_f_f_As_d_d(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_d_d(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_f_f(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_g_g(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_F_F_As_D_D(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_F_F(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_D_D(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_G_G(char** args, npy_intp* dimensions,

```
```

npy_intp* steps, void* func)
void PyUFunc_e_e(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_e_e_As_f_f(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_e_e_As_d_d(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
Type specific, core 1-d functions for ufuncs where each calculation is obtained by calling a function taking
one input argument and returning one output. This function is passed in func. The letters correspond to
dtypechar's of the supported data types ( e - half, f - float, d - double, g-long double, F - cfloat, D - cdouble, G
- clongdouble). The argument func must support the same signature. The _As_X_X variants assume ndarray's
of one data type but cast the values to use an underlying function that takes a different data type. Thus,
PyUFunc_f_f_As_d_d uses ndarrays of data type NPY_FLOAT but calls out to a C-function that takes
double and returns double.
void PyUFunc_ff_f_As_dd_d(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_ff_f(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_dd_d(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_gg_g(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_FF_F_As_DD_D(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_DD_D(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_FF_F(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)

```
```

void PyUFunc_GG_G(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_ee_e(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_ee_e_As_ff_f(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_ee_e_As_dd_d(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)

```

Type specific, core 1-d functions for ufuncs where each calculation is obtained by calling a function taking two input arguments and returning one output. The underlying function to call is passed in as func. The letters correspond to dtypechar's of the specific data type supported by the general-purpose function. The argument func must support the corresponding signature. The _As_XX_X variants assume ndarrays of one data type but cast the values at each iteration of the loop to use the underlying function that takes a different data type.
```

void PyUFunc_O_O(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
void PyUFunc_OO_O(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)

```
    One-input, one-output, and two-input, one-output core 1-d functions for the NPY_OBJECT data type. These
    functions handle reference count issues and return early on error. The actual function to call is func
    and it must accept calls with the signature (PyObject*) (PyObject*) for PyUFunc_O_O or
    (PyObject*) (PyObject *, PyObject *) for PyUFunc_Oo_O.
void PyUFunc_O_O_method(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)

This general purpose 1-d core function assumes that func is a string representing a method of the input object. For each iteration of the loop, the Python obejct is extracted from the array and its func method is called returning the result to the output array.
void PyUFunc_00_O_method(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
This general purpose 1-d core function assumes that func is a string representing a method of the input object that takes one argument. The first argument in args is the method whose function is called, the second argument in args is the argument passed to the function. The output of the function is stored in the third entry of args.
void PyUFunc_On_Om(char** args, npy_intp* dimensions,
npy_intp* steps, void* func)
This is the 1-d core function used by the dynamic ufuncs created by umath.frompyfunc(function, nin, nout). In this case func is a pointer to a PyUFunc_PyFuncData structure which has definition

PyUFunc_PyFuncData
```

typedef struct {
int nin;
int nout;
PyObject *callable;
} PyUFunc_PyFuncData;

```

At each iteration of the loop, the nin input objects are exctracted from their object arrays and placed into an argument tuple, the Python callable is called with the input arguments, and the nout outputs are placed into their object arrays.

\subsection*{5.6.5 Importing the API}

PY_UFUNC_UNIQUE_SYMBOL

\section*{NO_IMPORT_UFUNC}
```

void import_ufunc (void)

```

These are the constants and functions for accessing the ufunc C-API from extension modules in precisely the same way as the array C-API can be accessed. The import_ufunc () function must always be called (in the initialization subroutine of the extension module). If your extension module is in one file then that is all that is required. The other two constants are useful if your extension module makes use of multiple files. In that case, define PY_UFUNC_UNIQUE_SYMBOL to something unique to your code and then in source files that do not contain the module initialization function but still need access to the UFUNC API, define PY_UFUNC_UNIQUE_SYMBOL to the same name used previously and also define NO_IMPORT_UFUNC.
The C-API is actually an array of function pointers. This array is created (and pointed to by a global variable) by import_ufunc. The global variable is either statically defined or allowed to be seen by other files depending on the state of Py_UFUNC_UNIQUE_SYMBOL and NO_IMPORT_UFUNC.

\subsection*{5.7 Generalized Universal Function API}

There is a general need for looping over not only functions on scalars but also over functions on vectors (or arrays), as explained on http://scipy.org/scipy/numpy/wiki/GeneralLoopingFunctions. We propose to realize this concept by generalizing the universal functions (ufuncs), and provide a C implementation that adds \(\sim 500\) lines to the numpy code base. In current (specialized) ufuncs, the elementary function is limited to element-by-element operations, whereas the generalized version supports "sub-array" by "sub-array" operations. The Perl vector library PDL provides a similar functionality and its terms are re-used in the following.
Each generalized ufunc has information associated with it that states what the "core" dimensionality of the inputs is, as well as the corresponding dimensionality of the outputs (the element-wise ufuncs have zero core dimensions). The list of the core dimensions for all arguments is called the "signature" of a ufunc. For example, the ufunc numpy.add has signature (), () -> () defining two scalar inputs and one scalar output.

Another example is (see the GeneralLoopingFunctions page) the function innerld \((a, b)\) with a signature of (i), (i) \(->\) (). This applies the inner product along the last axis of each input, but keeps the remaining indices intact. For example, where \(a\) is of shape \((3,5, N)\) and \(b\) is of shape \((5, N)\), this will return an output of shape \((3,5)\). The underlying elementary function is called \(3 * 5\) times. In the signature, we specify one core dimension (i) for each input and zero core dimensions () for the output, since it takes two 1-d arrays and returns a scalar. By using the same name \(i\), we specify that the two corresponding dimensions should be of the same size (or one of them is of size 1 and will be broadcasted).

The dimensions beyond the core dimensions are called "loop" dimensions. In the above example, this corresponds to \((3,5)\).

The usual numpy "broadcasting" rules apply, where the signature determines how the dimensions of each input/output object are split into core and loop dimensions:
1. While an input array has a smaller dimensionality than the corresponding number of core dimensions, 1's are pre-pended to its shape.
2. The core dimensions are removed from all inputs and the remaining dimensions are broadcasted; defining the loop dimensions.
3. The output is given by the loop dimensions plus the output core dimensions.

\subsection*{5.7.1 Definitions}

\section*{Elementary Function}

Each ufunc consists of an elementary function that performs the most basic operation on the smallest portion of array arguments (e.g. adding two numbers is the most basic operation in adding two arrays). The ufunc applies the elementary function multiple times on different parts of the arrays. The input/output of elementary functions can be vectors; e.g., the elementary function of innerld takes two vectors as input.

\section*{Signature}

A signature is a string describing the input/output dimensions of the elementary function of a ufunc. See section below for more details.

\section*{Core Dimension}

The dimensionality of each input/output of an elementary function is defined by its core dimensions (zero core dimensions correspond to a scalar input/output). The core dimensions are mapped to the last dimensions of the input/output arrays.

\section*{Dimension Name}

A dimension name represents a core dimension in the signature. Different dimensions may share a name, indicating that they are of the same size (or are broadcastable).

\section*{Dimension Index}

A dimension index is an integer representing a dimension name. It enumerates the dimension names according to the order of the first occurrence of each name in the signature.

\subsection*{5.7.2 Details of Signature}

The signature defines "core" dimensionality of input and output variables, and thereby also defines the contraction of the dimensions. The signature is represented by a string of the following format:
- Core dimensions of each input or output array are represented by a list of dimension names in parentheses, (i_1, ...,i_N) ; a scalar input/output is denoted by (). Instead of i_1, i_2, etc, one can use any valid Python variable name.
- Dimension lists for different arguments are separated by ", ". Input/output arguments are separated by "->".
- If one uses the same dimension name in multiple locations, this enforces the same size (or broadcastable size) of the corresponding dimensions.

The formal syntax of signatures is as follows:
```

<Signature> ::= <Input arguments> "->" <Output arguments>
<Input arguments> ::= <Argument list>
<Output arguments> ::= <Argument list>
<Argument list> ::= nil | <Argument> | <Argument> "," <Argument list>

```
```

<Argument> ::= "(" <Core dimension list> ")"
<Core dimension list> ::= nil | <Dimension name> |
<Dimension name> "," <Core dimension list>
<Dimension name> ::= valid Python variable name

```

Notes:
1. All quotes are for clarity.
2. Core dimensions that share the same name must be broadcastable, as the two \(i\) in our example above. Each dimension name typically corresponding to one level of looping in the elementary function's implementation.
3. White spaces are ignored.

Here are some examples of signatures:
\begin{tabular}{|l|l|l|}
\hline add & ()\(,()->()\) & \\
inner1d & \((i),(i)->()\) \\
sum1d & \((i)->()\) \\
dot2d & \((m, n),(n, p) \rightarrow>(m\), & pmatrix multiplication \\
outer_inner & \((i, t),(j, t) \rightarrow>(i\), & \begin{tabular}{l} 
jinner over the last dimension, outer over the second to last, and \\
loop/broadcast over the rest.
\end{tabular} \\
\hline
\end{tabular}

\subsection*{5.7.3 C-API for implementing Elementary Functions}

The current interface remains unchanged, and PyUFunc_FromFuncAndData can still be used to implement (specialized) ufuncs, consisting of scalar elementary functions.

One can use PyUFunc_FromFuncAndDataAndSignature to declare a more general ufunc. The argument list is the same as PyUFunc_FromFuncAndData, with an additional argument specifying the signature as C string.

Furthermore, the callback function is of the same type as before, void (*foo) (char **args, intp *dimensions, intp *steps, void *func). When invoked, args is a list of length nargs containing the data of all input/output arguments. For a scalar elementary function, steps is also of length nargs, denoting the strides used for the arguments. dimensions is a pointer to a single integer defining the size of the axis to be looped over.

For a non-trivial signature, dimensions will also contain the sizes of the core dimensions as well, starting at the second entry. Only one size is provided for each unique dimension name and the sizes are given according to the first occurrence of a dimension name in the signature.

The first nargs elements of steps remain the same as for scalar ufuncs. The following elements contain the strides of all core dimensions for all arguments in order.

For example, consider a ufunc with signature (i,j), (i) -> (). In this case, args will contain three pointers to the data of the input/output arrays \(a, b, c\). Furthermore, dimensions will be [N, I, J] to define the size of \(N\) of the loop and the sizes I and \(J\) for the core dimensions \(i\) and \(j\). Finally, steps will be [a_N, b_N, c_N, a_i, a_j, b_i], containing all necessary strides.

\subsection*{5.8 Numpy core libraries}

New in version 1.3.0. Starting from numpy 1.3.0, we are working on separating the pure C, "computational" code from the python dependent code. The goal is twofolds: making the code cleaner, and enabling code reuse by other extensions outside numpy (scipy, etc...).

\subsection*{5.8.1 Numpy core math library}

The numpy core math library ('npymath') is a first step in this direction. This library contains most math-related C99 functionality, which can be used on platforms where C99 is not well supported. The core math functions have the same API as the C99 ones, except for the npy_* prefix.
The available functions are defined in <numpy/npy_math.h> - please refer to this header when in doubt.

\section*{Floating point classification}

\section*{NPY_NAN}

This macro is defined to a NaN (Not a Number), and is guaranteed to have the signbit unset ('positive' NaN ). The corresponding single and extension precision macro are available with the suffix F and L .

\section*{NPY_INFINITY}

This macro is defined to a positive inf. The corresponding single and extension precision macro are available with the suffix F and L .

\section*{NPY_PZERO}

This macro is defined to positive zero. The corresponding single and extension precision macro are available with the suffix F and L .

\section*{NPY NZERO}

This macro is defined to negative zero (that is with the sign bit set). The corresponding single and extension precision macro are available with the suffix \(F\) and \(L\).
int npy_isnan (x)
This is a macro, and is equivalent to C99 isnan: works for single, double and extended precision, and return a non 0 value is x is a NaN .
int npy_isfinite(x)
This is a macro, and is equivalent to C99 isfinite: works for single, double and extended precision, and return a non 0 value is x is neither a NaN nor an infinity.
int npy_isinf(x)
This is a macro, and is equivalent to C99 isinf: works for single, double and extended precision, and return a non 0 value is x is infinite (positive and negative).
int npy_signbit (x)
This is a macro, and is equivalent to C99 signbit: works for single, double and extended precision, and return a non 0 value is x has the signbit set (that is the number is negative).
double npy_copysign (double \(x\), double \(y\) )
This is a function equivalent to C99 copysign: return x with the same sign as y . Works for any value, including inf and nan. Single and extended precisions are available with suffix \(f\) and 1 . New in version 1.4.0.

\section*{Useful math constants}

The following math constants are available in npy_math.h. Single and extended precision are also available by adding the F and L suffixes respectively.

\section*{NPY_E}

Base of natural logarithm (e)

\section*{NPY LOG2E}

Logarithm to base 2 of the Euler constant \(\left(\frac{\ln (e)}{\ln (2)}\right)\)

\section*{NPY_LOG10E}

Logarithm to base 10 of the Euler constant \(\left(\frac{\ln (e)}{\ln (10)}\right)\)

\section*{NPY_LOGE2}

Natural logarithm of \(2(\ln (2))\)

\section*{NPY_LOGE10}

Natural logarithm of \(10(\ln (10))\)

\section*{NPY_PI}

Pi ( \(\pi\) )
```

NPY_PI_2

```

Pi divided by \(2\left(\frac{\pi}{2}\right)\)
```

NPY_PI_4

```

Pi divided by \(4\left(\frac{\pi}{4}\right)\)

\section*{NPY_1_PI}

Reciprocal of pi \(\left(\frac{1}{\pi}\right)\)

\section*{NPY_2_PI}

Two times the reciprocal of pi \(\left(\frac{2}{\pi}\right)\)
```

NPY_EULER

```

The Euler constant
\[
\lim _{n \rightarrow \infty}\left(\sum_{k=1}^{n} \frac{1}{k}-\ln n\right)
\]

\section*{Low-level floating point manipulation}

Those can be useful for precise floating point comparison.
double npy_nextafter (double \(x\), double \(y\) )
This is a function equivalent to C 99 nextafter: return next representable floating point value from x in the direction of \(y\). Single and extended precisions are available with suffix f and 1 . New in version 1.4.0.
double npy_spacing (double \(x\) )
This is a function equivalent to Fortran intrinsic. Return distance between x and next representable floating point value from \(x\), e.g. spacing \((1)==\) eps. spacing of nan and \(+/-\) inf return nan. Single and extended precisions are available with suffix \(f\) and 1 . New in version 1.4.0.

\section*{Complex functions}

New in version 1.4.0. C99-like complex functions have been added. Those can be used if you wish to implement portable C extensions. Since we still support platforms without C99 complex type, you need to restrict to C90compatible syntax, e.g.:
```

/* a = 1 + 2i \*/
npy_complex a = npy_cpack(1, 2);
npy_complex b;
b = npy_log(a);

```

\section*{Linking against the core math library in an extension}

New in version 1.4.0. To use the core math library in your own extension, you need to add the npymath compile and link options to your extension in your setup.py:
```

>>> from numpy.distutils.misc_utils import get_info
>>> info = get_info('npymath')
>>> config.add_extension('foo', sources=['foo.c'], extra_info=**info)

```

In other words, the usage of info is exactly the same as when using blas_info and co.

\section*{Half-precision functions}

New in version 2.0.0. The header file <numpy/halffloat.h> provides functions to work with IEEE 754-2008 16-bit floating point values. While this format is not typically used for numerical computations, it is useful for storing values which require floating point but do not need much precision. It can also be used as an educational tool to understand the nature of floating point round-off error.
Like for other types, NumPy includes a typedef npy_half for the 16 bit float. Unlike for most of the other types, you cannot use this as a normal type in C, since is is a typedef for npy_uint16. For example, 1.0 looks like \(0 \times 3 \mathrm{c} 00\) to C , and if you do an equality comparison between the different signed zeros, you will get \(-0.0!=0.0(0 \times 8000!=0 \times 0000)\), which is incorrect.

For these reasons, NumPy provides an API to work with npy_half values accessible by including <numpy/halffloat.h> and linking to 'npymath'. For functions that are not provided directly, such as the arithmetic operations, the preferred method is to convert to float or double and back again, as in the following example.
```

npy_half sum(int n, npy_half *array) {
float ret = 0;
while(n--) {
ret += npy_half_to_float(*array++);
}
return npy_float_to_half(ret);
}

```

External Links:
- 754-2008 IEEE Standard for Floating-Point Arithmetic
- Half-precision Float Wikipedia Article.
- OpenGL Half Float Pixel Support
- The OpenEXR image format.

\section*{NPY_HALF_ZERO}

This macro is defined to positive zero.

\section*{NPY_HALF_PZERO}

This macro is defined to positive zero.

\section*{NPY_HALF_NZERO}

This macro is defined to negative zero.

\section*{NPY_HALF_ONE}

This macro is defined to 1.0 .

\section*{NPY_HALF_NEGONE}

This macro is defined to -1.0.

\section*{NPY_HALF_PINF}

This macro is defined to +inf.
NPY_HALF_NINF
This macro is defined to -inf.

\section*{NPY_HALF_NAN}

This macro is defined to a NaN value, guaranteed to have its sign bit unset.
float npy_half_to_float (npy_half \(h\) )
Converts a half-precision float to a single-precision float.
double npy_half_to_double (npy_half \(h\) )
Converts a half-precision float to a double-precision float.
npy_half npy_float_to_half(float \(f\) )
Converts a single-precision float to a half-precision float. The value is rounded to the nearest representable half, with ties going to the nearest even. If the value is too small or too big, the system's floating point underflow or overflow bit will be set.
npy_half npy_double_to_half (double \(d\) )
Converts a double-precision float to a half-precision float. The value is rounded to the nearest representable half, with ties going to the nearest even. If the value is too small or too big, the system's floating point underflow or overflow bit will be set.
int npy_half_eq (npy_half \(h 1\), npy_half \(h 2\) )
Compares two half-precision floats ( \(\mathrm{h} 1=\mathrm{h} 2\) ).
int npy_half_ne (npy_half \(h 1\), npy_half \(h 2\) )
Compares two half-precision floats (h1 != h2).
int npy_half_le (npy_half \(h 1\), npy_half \(h 2\) )
Compares two half-precision floats ( \(\mathrm{h} 1<=\mathrm{h} 2\) ).
int npy_half_lt (npy_half \(h 1\), npy_half \(h 2\) )
Compares two half-precision floats (h1<h2).
int npy_half_ge (npy_half \(h 1\), npy_half \(h 2\) )
Compares two half-precision floats ( \(\mathrm{h} 1>=\mathrm{h} 2\) ).
int npy_half_gt (npy_half \(h 1\), npy_half \(h 2\) )
Compares two half-precision floats ( \(\mathrm{h} 1>\mathrm{h} 2\) ).
int npy_half_eq_nonan (npy_half \(h 1\), npy_half \(h 2\) )
Compares two half-precision floats that are known to not be \(\mathrm{NaN}(\mathrm{h} 1=\mathrm{h} 2\) ). If a value is NaN , the result is undefined.
int npy_half_lt_nonan (npy_half \(h 1\), npy_half \(h 2\) )
Compares two half-precision floats that are known to not be \(\mathrm{NaN}(\mathrm{h} 1<\mathrm{h} 2\) ). If a value is NaN , the result is undefined.
int npy_half_le_nonan (npy_half \(h 1\), npy_half \(h 2\) )
Compares two half-precision floats that are known to not be \(\mathrm{NaN}(\mathrm{h} 1<=\mathrm{h} 2)\). If a value is NaN , the result is undefined.
int npy_half_iszero (npy_half \(h\) )
Tests whether the half-precision float has a value equal to zero. This may be slightly faster than calling npy_half_eq(h, NPY_ZERO).
int npy_half_isnan (npy_half \(h\) )
Tests whether the half-precision float is a NaN .
int npy_half_isinf(npy_half \(h\) )
Tests whether the half-precision float is plus or minus Inf.
int npy_half_isfinite (npy_half \(h\) )
Tests whether the half-precision float is finite (not NaN or Inf).
int npy_half_signbit (npy_half \(h\) )
Returns 1 is h is negative, 0 otherwise.
npy_half npy_half_copysign (npy_half \(x\), npy_half \(y\) )
Returns the value of \(x\) with the sign bit copied from \(y\). Works for any value, including Inf and NaN .
npy_half npy_half_spacing (npy_half \(h\) )
This is the same for half-precision float as npy_spacing and npy_spacingf described in the low-level floating point section.
npy_half npy_half_nextafter (npy_half \(x\), npy_half \(y\) )
This is the same for half-precision float as npy_nextafter and npy_nextafterf described in the low-level floating point section.
npy_uint16 npy_floatbits_to_halfbits (npy_uint \(32 f\) )
Low-level function which converts a 32-bit single-precision float, stored as a uint 32, into a 16-bit half-precision float.
npy_uint16 npy_doublebits_to_halfbits (npy_uint64 d)
Low-level function which converts a 64-bit double-precision float, stored as a uint64, into a 16-bit half-precision float.
npy_uint32 npy_halfbits_to_floatbits (npy_uint16 \(h\) )
Low-level function which converts a 16-bit half-precision float into a 32-bit single-precision float, stored as a uint32.
npy_uint64 npy_halfbits_to_doublebits (npy_uint16 \(h\) )
Low-level function which converts a 16-bit half-precision float into a 64-bit double-precision float, stored as a uint64.

\title{
NUMPY INTERNALS
}

\subsection*{6.1 Numpy C Code Explanations}

> Fanaticism consists of redoubling your efforts when you have forgotten your aim. - George Santayana

An authority is a person who can tell you more about something than you really care to know. - Unknown
This Chapter attempts to explain the logic behind some of the new pieces of code. The purpose behind these explanations is to enable somebody to be able to understand the ideas behind the implementation somewhat more easily than just staring at the code. Perhaps in this way, the algorithms can be improved on, borrowed from, and/or optimized.

\subsection*{6.1.1 Memory model}

One fundamental aspect of the ndarray is that an array is seen as a "chunk" of memory starting at some location. The interpretation of this memory depends on the stride information. For each dimension in an \(N\)-dimensional array, an integer (stride) dictates how many bytes must be skipped to get to the next element in that dimension. Unless you have a single-segment array, this stride information must be consulted when traversing through an array. It is not difficult to write code that accepts strides, you just have to use (char \({ }^{*}\) ) pointers because strides are in units of bytes. Keep in mind also that strides do not have to be unit-multiples of the element size. Also, remember that if the number of dimensions of the array is 0 (sometimes called a rank-0 array), then the strides and dimensions variables are NULL.

Besides the structural information contained in the strides and dimensions members of the PyArrayObject, the flags contain important information about how the data may be accessed. In particular, the NPY_ALIGNED flag is set when the memory is on a suitable boundary according to the data-type array. Even if you have a contiguous chunk of memory, you cannot just assume it is safe to dereference a data- type-specific pointer to an element. Only if the NPY_ALIGNED flag is set is this a safe operation (on some platforms it will work but on others, like Solaris, it will cause a bus error). The NPY_WRITEABLE should also be ensured if you plan on writing to the memory area of the array. It is also possible to obtain a pointer to an unwriteable memory area. Sometimes, writing to the memory area when the NPY_WRITEABLE flag is not set will just be rude. Other times it can cause program crashes ( e.g. a data-area that is a read-only memory-mapped file).

\subsection*{6.1.2 Data-type encapsulation}

The data-type is an important abstraction of the ndarray. Operations will look to the data-type to provide the key functionality that is needed to operate on the array. This functionality is provided in the list of function pointers pointed to by the ' f ' member of the PyArray_Descr structure. In this way, the number of data-types can be extended simply by providing a PyArray_Descr structure with suitable function pointers in the ' \(f\) ' member. For built-in types there are some optimizations that by-pass this mechanism, but the point of the data- type abstraction is to allow new data-types to be added.

One of the built-in data-types, the void data-type allows for arbitrary records containing 1 or more fields as elements of the array. A field is simply another data-type object along with an offset into the current record. In order to support arbitrarily nested fields, several recursive implementations of data-type access are implemented for the void type. A common idiom is to cycle through the elements of the dictionary and perform a specific operation based on the data-type object stored at the given offset. These offsets can be arbitrary numbers. Therefore, the possibility of encountering mis- aligned data must be recognized and taken into account if necessary.

\subsection*{6.1.3 N-D Iterators}

A very common operation in much of NumPy code is the need to iterate over all the elements of a general, strided, N -dimensional array. This operation of a general-purpose N -dimensional loop is abstracted in the notion of an iterator object. To write an N-dimensional loop, you only have to create an iterator object from an ndarray, work with the dataptr member of the iterator object structure and call the macro PyArray_ITER_NEXT (it) on the iterator object to move to the next element. The "next" element is always in C-contiguous order. The macro works by first special casing the C-contiguous, 1-D, and 2-D cases which work very simply.

For the general case, the iteration works by keeping track of a list of coordinate counters in the iterator object. At each iteration, the last coordinate counter is increased (starting from 0 ). If this counter is smaller then one less than the size of the array in that dimension (a pre-computed and stored value), then the counter is increased and the dataptr member is increased by the strides in that dimension and the macro ends. If the end of a dimension is reached, the counter for the last dimension is reset to zero and the dataptr is moved back to the beginning of that dimension by subtracting the strides value times one less than the number of elements in that dimension (this is also pre-computed and stored in the backstrides member of the iterator object). In this case, the macro does not end, but a local dimension counter is decremented so that the next-to-last dimension replaces the role that the last dimension played and the previouslydescribed tests are executed again on the next-to-last dimension. In this way, the dataptr is adjusted appropriately for arbitrary striding.

The coordinates member of the PyArrayIterObject structure maintains the current N -d counter unless the underlying array is C-contiguous in which case the coordinate counting is by-passed. The index member of the PyArrayiterObject keeps track of the current flat index of the iterator. It is updated by the PyArray_ITER_NEXT macro.

\subsection*{6.1.4 Broadcasting}

In Numeric, broadcasting was implemented in several lines of code buried deep in ufuncobject.c. In NumPy, the notion of broadcasting has been abstracted so that it can be performed in multiple places. Broadcasting is handled by the function PyArray_Broadcast. This function requires a PyArrayMultiIterObject (or something that is a binary equivalent) to be passed in. The PyArrayMultiIterObject keeps track of the broadcasted number of dimensions and size in each dimension along with the total size of the broadcasted result. It also keeps track of the number of arrays being broadcast and a pointer to an iterator for each of the arrays being broadcasted.

The PyArray_Broadcast function takes the iterators that have already been defined and uses them to determine the broadcast shape in each dimension (to create the iterators at the same time that broadcasting occurs then use the PyMultiIter_New function). Then, the iterators are adjusted so that each iterator thinks it is iterating over an array with the broadcasted size. This is done by adjusting the iterators number of dimensions, and the shape in each dimension. This works because the iterator strides are also adjusted. Broadcasting only adjusts (or adds) length-1 dimensions. For these dimensions, the strides variable is simply set to 0 so that the data-pointer for the iterator over that array doesn't move as the broadcasting operation operates over the extended dimension.

Broadcasting was always implemented in Numeric using 0 -valued strides for the extended dimensions. It is done in exactly the same way in NumPy. The big difference is that now the array of strides is kept track of in a PyArrayIterObject, the iterators involved in a broadcasted result are kept track of in a PyArrayMultiIterobject, and the PyArray_BroadCast call implements the broad-casting rules.

\subsection*{6.1.5 Array Scalars}

The array scalars offer a hierarchy of Python types that allow a one- to-one correspondence between the data-type stored in an array and the Python-type that is returned when an element is extracted from the array. An exception to this rule was made with object arrays. Object arrays are heterogeneous collections of arbitrary Python objects. When you select an item from an object array, you get back the original Python object (and not an object array scalar which does exist but is rarely used for practical purposes).

The array scalars also offer the same methods and attributes as arrays with the intent that the same code can be used to support arbitrary dimensions (including 0-dimensions). The array scalars are read-only (immutable) with the exception of the void scalar which can also be written to so that record-array field setting works more naturally (a[0]['f1'] = value ).

\subsection*{6.1.6 Advanced ("Fancy") Indexing}

The implementation of advanced indexing represents some of the most difficult code to write and explain. In fact, there are two implementations of advanced indexing. The first works only with 1-D arrays and is implemented to handle expressions involving a.flat[obj]. The second is general-purpose that works for arrays of "arbitrary dimension" (up to a fixed maximum). The one-dimensional indexing approaches were implemented in a rather straightforward fashion, and so it is the general-purpose indexing code that will be the focus of this section.

There is a multi-layer approach to indexing because the indexing code can at times return an array scalar and at other times return an array. The functions with "_nice" appended to their name do this special handling while the function without the _nice appendage always return an array (perhaps a 0 -dimensional array). Some special-case optimizations (the index being an integer scalar, and the index being a tuple with as many dimensions as the array) are handled in array_subscript_nice function which is what Python calls when presented with the code "a[obj]." These optimizations allow fast single-integer indexing, and also ensure that a 0-dimensional array is not created only to be discarded as the array scalar is returned instead. This provides significant speed-up for code that is selecting many scalars out of an array (such as in a loop). However, it is still not faster than simply using a list to store standard Python scalars, because that is optimized by the Python interpreter itself.

After these optimizations, the array_subscript function itself is called. This function first checks for field selection which occurs when a string is passed as the indexing object. Then, \(0-\mathrm{D}\) arrays are given special-case consideration. Finally, the code determines whether or not advanced, or fancy, indexing needs to be performed. If fancy indexing is not needed, then standard view-based indexing is performed using code borrowed from Numeric which parses the indexing object and returns the offset into the data-buffer and the dimensions necessary to create a new view of the array. The strides are also changed by multiplying each stride by the step-size requested along the corresponding dimension.

\section*{Fancy-indexing check}

The fancy_indexing_check routine determines whether or not to use standard view-based indexing or new copy-based indexing. If the indexing object is a tuple, then view-based indexing is assumed by default. Only if the tuple contains an array object or a sequence object is fancy-indexing assumed. If the indexing object is an array, then fancy indexing is automatically assumed. If the indexing object is any other kind of sequence, then fancy-indexing is assumed by default. This is over-ridden to simple indexing if the sequence contains any slice, newaxis, or Ellipsis objects, and no arrays or additional sequences are also contained in the sequence. The purpose of this is to allow the construction of "slicing" sequences which is a common technique for building up code that works in arbitrary numbers of dimensions.

\section*{Fancy-indexing implementation}

The concept of indexing was also abstracted using the idea of an iterator. If fancy indexing is performed, then a PyArrayMapIterObject is created. This internal object is not exposed to Python. It is created in order to handle
the fancy-indexing at a high-level. Both get and set fancy-indexing operations are implemented using this object. Fancy indexing is abstracted into three separate operations: (1) creating the PyArrayMapIterObject from the indexing object, (2) binding the PyArrayMapIterObject to the array being indexed, and (3) getting (or setting) the items determined by the indexing object. There is an optimization implemented so that the PyArrayIterObject (which has it's own less complicated fancy-indexing) is used for indexing when possible.

\section*{Creating the mapping object}

The first step is to convert the indexing objects into a standard form where iterators are created for all of the index array inputs and all Boolean arrays are converted to equivalent integer index arrays (as if nonzero(arr) had been called). Finally, all integer arrays are replaced with the integer 0 in the indexing object and all of the index-array iterators are "broadcast" to the same shape.

\section*{Binding the mapping object}

When the mapping object is created it does not know which array it will be used with so once the index iterators are constructed during mapping-object creation, the next step is to associate these iterators with a particular ndarray. This process interprets any ellipsis and slice objects so that the index arrays are associated with the appropriate axis (the axis indicated by the iteraxis entry corresponding to the iterator for the integer index array). This information is then used to check the indices to be sure they are within range of the shape of the array being indexed. The presence of ellipsis and/or slice objects implies a sub-space iteration that is accomplished by extracting a sub-space view of the array (using the index object resulting from replacing all the integer index arrays with 0 ) and storing the information about where this sub-space starts in the mapping object. This is used later during mapping-object iteration to select the correct elements from the underlying array.

\section*{Getting (or Setting)}

After the mapping object is successfully bound to a particular array, the mapping object contains the shape of the resulting item as well as iterator objects that will walk through the currently-bound array and either get or set its elements as needed. The walk is implemented using the PyArray_MapIterNext function. This function sets the coordinates of an iterator object into the current array to be the next coordinate location indicated by all of the indexing-object iterators while adjusting, if necessary, for the presence of a sub- space. The result of this function is that the dataptr member of the mapping object structure is pointed to the next position in the array that needs to be copied out or set to some value.

When advanced indexing is used to extract an array, an iterator for the new array is constructed and advanced in phase with the mapping object iterator. When advanced indexing is used to place values in an array, a special "broadcasted" iterator is constructed from the object being placed into the array so that it will only work if the values used for setting have a shape that is "broadcastable" to the shape implied by the indexing object.

\subsection*{6.1.7 Universal Functions}

Universal functions are callable objects that take \(N\) inputs and produce \(M\) outputs by wrapping basic 1-D loops that work element-by-element into full easy-to use functions that seamlessly implement broadcasting, type-checking and buffered coercion, and output-argument handling. New universal functions are normally created in C, although there is a mechanism for creating ufuncs from Python functions (frompyfunc). The user must supply a 1-D loop that implements the basic function taking the input scalar values and placing the resulting scalars into the appropriate output slots as explaine n implementation.

\section*{Setup}

Every ufunc calculation involves some overhead related to setting up the calculation. The practical significance of this overhead is that even though the actual calculation of the ufunc is very fast, you will be able to write array and type-specific code that will work faster for small arrays than the ufunc. In particular, using ufuncs to perform many calculations on 0-D arrays will be slower than other Python-based solutions (the silently-imported scalarmath
module exists precisely to give array scalars the look-and-feel of ufunc-based calculations with significantly reduced overhead).
When a ufunc is called, many things must be done. The information collected from these setup operations is stored in a loop-object. This loop object is a C-structure (that could become a Python object but is not initialized as such because it is only used internally). This loop object has the layout needed to be used with PyArray_Broadcast so that the broadcasting can be handled in the same way as it is handled in other sections of code.

The first thing done is to look-up in the thread-specific global dictionary the current values for the buffer-size, the error mask, and the associated error object. The state of the error mask controls what happens when an error-condiction is found. It should be noted that checking of the hardware error flags is only performed after each 1-D loop is executed. This means that if the input and output arrays are contiguous and of the correct type so that a single 1-D loop is performed, then the flags may not be checked until all elements of the array have been calcluated. Looking up these values in a thread- specific dictionary takes time which is easily ignored for all but very small arrays.

After checking, the thread-specific global variables, the inputs are evaluated to determine how the ufunc should proceed and the input and output arrays are constructed if necessary. Any inputs which are not arrays are converted to arrays (using context if necessary). Which of the inputs are scalars (and therefore converted to 0-D arrays) is noted.

Next, an appropriate 1-D loop is selected from the 1-D loops available to the ufunc based on the input array types. This 1-D loop is selected by trying to match the signature of the data-types of the inputs against the available signatures. The signatures corresponding to built-in types are stored in the types member of the ufunc structure. The signatures corresponding to user-defined types are stored in a linked-list of function-information with the head element stored as a COb ject in the userloops dictionary keyed by the data-type number (the first user-defined type in the argument list is used as the key). The signatures are searched until a signature is found to which the input arrays can all be cast safely (ignoring any scalar arguments which are not allowed to determine the type of the result). The implication of this search procedure is that "lesser types" should be placed below "larger types" when the signatures are stored. If no 1-D loop is found, then an error is reported. Otherwise, the argument_list is updated with the stored signature - in case casting is necessary and to fix the output types assumed by the 1-D loop.
If the ufunc has 2 inputs and 1 output and the second input is an Object array then a special-case check is performed so that NotImplemented is returned if the second input is not an ndarray, has the __array_priority__ attribute, and has an __r \(\left\{\begin{array}{l}\text { op }\}\end{array}\right.\) _ special method. In this way, Python is signaled to give the other object a chance to complete the operation instead of using generic object-array calculations. This allows (for example) sparse matrices to override the multiplication operator 1-D loop.

For input arrays that are smaller than the specified buffer size, copies are made of all non-contiguous, mis-aligned, or out-of- byteorder arrays to ensure that for small arrays, a single-loop is used. Then, array iterators are created for all the input arrays and the resulting collection of iterators is broadcast to a single shape.

The output arguments (if any) are then processed and any missing return arrays are constructed. If any provided output array doesn't have the correct type (or is mis-aligned) and is smaller than the buffer size, then a new output array is constructed with the special UPDATEIFCOPY flag set so that when it is DECREF'd on completion of the function, it's contents will be copied back into the output array. Iterators for the output arguments are then processed.
Finally, the decision is made about how to execute the looping mechanism to ensure that all elements of the input arrays are combined to produce the output arrays of the correct type. The options for loop execution are one-loop (for contiguous, aligned, and correct data- type), strided-loop (for non-contiguous but still aligned and correct data-type), and a buffered loop (for mis-aligned or incorrect data- type situations). Depending on which execution method is called for, the loop is then setup and computed.

\section*{Function call}

This section describes how the basic universal function computation loop is setup and executed for each of the three different kinds of execution possibilities. If NPY_ALLOW_THREADS is defined during compilation, then the Python Global Interpreter Lock (GIL) is released prior to calling all of these loops (as long as they don't involve object arrays).

It is re-acquired if necessary to handle error conditions. The hardware error flags are checked only after the 1-D loop is calcluated.

\section*{One Loop}

This is the simplest case of all. The ufunc is executed by calling the underlying 1-D loop exactly once. This is possible only when we have aligned data of the correct type (including byte-order) for both input and output and all arrays have uniform strides (either contiguous, \(0-\mathrm{D}\), or \(1-\mathrm{D}\) ). In this case, the \(1-\mathrm{D}\) computational loop is called once to compute the calculation for the entire array. Note that the hardware error flags are only checked after the entire calculation is complete.

\section*{Strided Loop}

When the input and output arrays are aligned and of the correct type, but the striding is not uniform (non-contiguous and 2-D or larger), then a second looping structure is employed for the calculation. This approach converts all of the iterators for the input and output arguments to iterate over all but the largest dimension. The inner loop is then handled by the underlying 1-D computational loop. The outer loop is a standard iterator loop on the converted iterators. The hardware error flags are checked after each 1-D loop is completed.

\section*{Buffered Loop}

This is the code that handles the situation whenever the input and/or output arrays are either misaligned or of the wrong data-type (including being byte-swapped) from what the underlying 1-D loop expects. The arrays are also assumed to be non-contiguous. The code works very much like the strided loop except for the inner 1-D loop is modified so that pre-processing is performed on the inputs and post- processing is performed on the outputs in bufsize chunks (where bufsize is a user-settable parameter). The underlying 1-D computational loop is called on data that is copied over (if it needs to be). The setup code and the loop code is considerably more complicated in this case because it has to handle:
- memory allocation of the temporary buffers
- deciding whether or not to use buffers on the input and output data (mis-aligned and/or wrong data-type)
- copying and possibly casting data for any inputs or outputs for which buffers are necessary.
- special-casing Object arrays so that reference counts are properly handled when copies and/or casts are necessary.
- breaking up the inner 1-D loop into bufsize chunks (with a possible remainder).

Again, the hardware error flags are checked at the end of each 1-D loop.

\section*{Final output manipulation}

Ufuncs allow other array-like classes to be passed seamlessly through the interface in that inputs of a particular class will induce the outputs to be of that same class. The mechanism by which this works is the following. If any of the inputs are not ndarrays and define the __array_wrap__ method, then the class with the largest __array_priority__ attribute determines the type of all the outputs (with the exception of any output arrays passed in). The __array_wrap__ method of the input array will be called with the ndarray being returned from the ufunc as it's input. There are two calling styles of the __array_wrap__ function supported. The first takes the ndarray as the first argument and a tuple of "context" as the second argument. The context is (ufunc, arguments, output argument number). This is the first call tried. If a TypeError occurs, then the function is called with just the ndarray as the first argument.

\section*{Methods}

Their are three methods of ufuncs that require calculation similar to the general-purpose ufuncs. These are reduce, accumulate, and reduceat. Each of these methods requires a setup command followed by a loop. There are four loop
styles possible for the methods corresponding to no-elements, one-element, strided-loop, and buffered- loop. These are the same basic loop styles as implemented for the general purpose function call except for the no-element and oneelement cases which are special-cases occurring when the input array objects have 0 and 1 elements respectively.

\section*{Setup}

The setup function for all three methods is construct_reduce. This function creates a reducing loop object and fills it with parameters needed to complete the loop. All of the methods only work on ufuncs that take 2-inputs and return 1 output. Therefore, the underlying 1-D loop is selected assuming a signature of [ otype, otype, otype ] where otype is the requested reduction data-type. The buffer size and error handling is then retrieved from (perthread) global storage. For small arrays that are mis-aligned or have incorrect data-type, a copy is made so that the un-buffered section of code is used. Then, the looping strategy is selected. If there is 1 element or 0 elements in the array, then a simple looping method is selected. If the array is not mis-aligned and has the correct data-type, then strided looping is selected. Otherwise, buffered looping must be performed. Looping parameters are then established, and the return array is constructed. The output array is of a different shape depending on whether the method is reduce, accumulate, or reduceat. If an output array is already provided, then it's shape is checked. If the output array is not C-contiguous, aligned, and of the correct data type, then a temporary copy is made with the UPDATEIFCOPY flag set. In this way, the methods will be able to work with a well-behaved output array but the result will be copied back into the true output array when the method computation is complete. Finally, iterators are set up to loop over the correct axis (depending on the value of axis provided to the method) and the setup routine returns to the actual computation routine.

\section*{Reduce}

All of the ufunc methods use the same underlying 1-D computational loops with input and output arguments adjusted so that the appropriate reduction takes place. For example, the key to the functioning of reduce is that the 1-D loop is called with the output and the second input pointing to the same position in memory and both having a step- size of 0 . The first input is pointing to the input array with a step- size given by the appropriate stride for the selected axis. In this way, the operation performed is
\[
\begin{array}{lrr}
o= & & i[0] \\
o= & i[k]<\mathrm{op}>o & k=1 \ldots N
\end{array}
\]
where \(N+1\) is the number of elements in the input, \(i, o\) is the output, and \(i[k]\) is the \(k^{\text {th }}\) element of \(i\) along the selected axis. This basic operations is repeated for arrays with greater than 1 dimension so that the reduction takes place for every 1-D sub-array along the selected axis. An iterator with the selected dimension removed handles this looping.

For buffered loops, care must be taken to copy and cast data before the loop function is called because the underlying loop expects aligned data of the correct data-type (including byte-order). The buffered loop must handle this copying and casting prior to calling the loop function on chunks no greater than the user-specified bufsize.

\section*{Accumulate}

The accumulate function is very similar to the reduce function in that the output and the second input both point to the output. The difference is that the second input points to memory one stride behind the current output pointer. Thus, the operation performed is
\[
\begin{array}{lrr}
o[0] & = & i[0] \\
o[k] & = & i[k]<\text { op }>o[k-1]
\end{array} \begin{aligned}
& k=1 \ldots N .
\end{aligned}
\]

The output has the same shape as the input and each 1-D loop operates over \(N\) elements when the shape in the selected axis is \(N+1\). Again, buffered loops take care to copy and cast the data before calling the underlying 1-D computational loop.

\section*{Reduceat}

The reduceat function is a generalization of both the reduce and accumulate functions. It implements a reduce over ranges of the input array specified by indices. The extra indices argument is checked to be sure that every input
is not too large for the input array along the selected dimension before the loop calculations take place. The loop implementation is handled using code that is very similar to the reduce code repeated as many times as there are elements in the indices input. In particular: the first input pointer passed to the underlying 1-D computational loop points to the input array at the correct location indicated by the index array. In addition, the output pointer and the second input pointer passed to the underlying 1-D loop point to the same position in memory. The size of the 1-D computational loop is fixed to be the difference between the current index and the next index (when the current index is the last index, then the next index is assumed to be the length of the array along the selected dimension). In this way, the 1-D loop will implement a reduce over the specified indices.

Mis-aligned or a loop data-type that does not match the input and/or output data-type is handled using buffered code where-in data is copied to a temporary buffer and cast to the correct data-type if necessary prior to calling the underlying 1-D function. The temporary buffers are created in (element) sizes no bigger than the user settable buffer-size value. Thus, the loop must be flexible enough to call the underlying 1-D computational loop enough times to complete the total calculation in chunks no bigger than the buffer-size.

\subsection*{6.2 Internal organization of numpy arrays}

It helps to understand a bit about how numpy arrays are handled under the covers to help understand numpy better. This section will not go into great detail. Those wishing to understand the full details are referred to Travis Oliphant's book "Guide to Numpy".

Numpy arrays consist of two major components, the raw array data (from now on, referred to as the data buffer), and the information about the raw array data. The data buffer is typically what people think of as arrays in C or Fortran, a contiguous (and fixed) block of memory containing fixed sized data items. Numpy also contains a significant set of data that describes how to interpret the data in the data buffer. This extra information contains (among other things):
1. The basic data element's size in bytes
2. The start of the data within the data buffer (an offset relative to the beginning of the data buffer).
3. The number of dimensions and the size of each dimension
4. The separation between elements for each dimension (the 'stride'). This does not have to be a multiple of the element size
5. The byte order of the data (which may not be the native byte order)
6. Whether the buffer is read-only
7. Information (via the dtype object) about the interpretation of the basic data element. The basic data element may be as simple as a int or a float, or it may be a compound object (e.g., struct-like), a fixed character field, or Python object pointers.
8. Whether the array is to interpreted as C-order or Fortran-order.

This arrangement allow for very flexible use of arrays. One thing that it allows is simple changes of the metadata to change the interpretation of the array buffer. Changing the byteorder of the array is a simple change involving no rearrangement of the data. The shape of the array can be changed very easily without changing anything in the data buffer or any data copying at all

Among other things that are made possible is one can create a new array metadata object that uses the same data buffer to create a new view of that data buffer that has a different interpretation of the buffer (e.g., different shape, offset, byte order, strides, etc) but shares the same data bytes. Many operations in numpy do just this such as slices. Other operations, such as transpose, don't move data elements around in the array, but rather change the information about the shape and strides so that the indexing of the array changes, but the data in the doesn't move.

Typically these new versions of the array metadata but the same data buffer are new 'views' into the data buffer. There is a different ndarray object, but it uses the same data buffer. This is why it is necessary to force copies through use of the .copy() method if one really wants to make a new and independent copy of the data buffer.

New views into arrays mean the the object reference counts for the data buffer increase. Simply doing away with the original array object will not remove the data buffer if other views of it still exist.

\subsection*{6.3 Multidimensional Array Indexing Order Issues}

What is the right way to index multi-dimensional arrays? Before you jump to conclusions about the one and true way to index multi-dimensional arrays, it pays to understand why this is a confusing issue. This section will try to explain in detail how numpy indexing works and why we adopt the convention we do for images, and when it may be appropriate to adopt other conventions.

The first thing to understand is that there are two conflicting conventions for indexing 2-dimensional arrays. Matrix notation uses the first index to indicate which row is being selected and the second index to indicate which column is selected. This is opposite the geometrically oriented-convention for images where people generally think the first index represents \(x\) position (i.e., column) and the second represents y position (i.e., row). This alone is the source of much confusion; matrix-oriented users and image-oriented users expect two different things with regard to indexing.

The second issue to understand is how indices correspond to the order the array is stored in memory. In Fortran the first index is the most rapidly varying index when moving through the elements of a two dimensional array as it is stored in memory. If you adopt the matrix convention for indexing, then this means the matrix is stored one column at a time (since the first index moves to the next row as it changes). Thus Fortran is considered a Column-major language. C has just the opposite convention. In C, the last index changes most rapidly as one moves through the array as stored in memory. Thus C is a Row-major language. The matrix is stored by rows. Note that in both cases it presumes that the matrix convention for indexing is being used, i.e., for both Fortran and C, the first index is the row. Note this convention implies that the indexing convention is invariant and that the data order changes to keep that so.

But that's not the only way to look at it. Suppose one has large two-dimensional arrays (images or matrices) stored in data files. Suppose the data are stored by rows rather than by columns. If we are to preserve our index convention (whether matrix or image) that means that depending on the language we use, we may be forced to reorder the data if it is read into memory to preserve our indexing convention. For example if we read row-ordered data into memory without reordering, it will match the matrix indexing convention for C, but not for Fortran. Conversely, it will match the image indexing convention for Fortran, but not for C. For C, if one is using data stored in row order, and one wants to preserve the image index convention, the data must be reordered when reading into memory.

In the end, which you do for Fortran or C depends on which is more important, not reordering data or preserving the indexing convention. For large images, reordering data is potentially expensive, and often the indexing convention is inverted to avoid that.

The situation with numpy makes this issue yet more complicated. The internal machinery of numpy arrays is flexible enough to accept any ordering of indices. One can simply reorder indices by manipulating the internal stride information for arrays without reordering the data at all. Numpy will know how to map the new index order to the data without moving the data.

So if this is true, why not choose the index order that matches what you most expect? In particular, why not define row-ordered images to use the image convention? (This is sometimes referred to as the Fortran convention vs the C convention, thus the ' C ' and 'FORTRAN' order options for array ordering in numpy.) The drawback of doing this is potential performance penalties. It's common to access the data sequentially, either implicitly in array operations or explicitly by looping over rows of an image. When that is done, then the data will be accessed in non-optimal order. As the first index is incremented, what is actually happening is that elements spaced far apart in memory are being sequentially accessed, with usually poor memory access speeds. For example, for a two dimensional image 'im' defined so that \(\mathrm{im}[0,10]\) represents the value at \(\mathrm{x}=0, \mathrm{y}=10\). To be consistent with usual Python behavior then im[0] would represent a column at \(\mathrm{x}=0\). Yet that data would be spread over the whole array since the data are stored in row order. Despite the flexibility of numpy's indexing, it can't really paper over the fact basic operations are rendered inefficient because of data order or that getting contiguous subarrays is still awkward (e.g., im[:,0] for the first row, vs im[0]), thus one can't use an idiom such as for row in im; for col in im does work, but doesn't yield contiguous column data.

As it turns out, numpy is smart enough when dealing with ufuncs to determine which index is the most rapidly varying one in memory and uses that for the innermost loop. Thus for ufuncs there is no large intrinsic advantage to either approach in most cases. On the other hand, use of .flat with an FORTRAN ordered array will lead to non-optimal memory access as adjacent elements in the flattened array (iterator, actually) are not contiguous in memory.

Indeed, the fact is that Python indexing on lists and other sequences naturally leads to an outside-to inside ordering (the first index gets the largest grouping, the next the next largest, and the last gets the smallest element). Since image data are normally stored by rows, this corresponds to position within rows being the last item indexed.

If you do want to use Fortran ordering realize that there are two approaches to consider: 1) accept that the first index is just not the most rapidly changing in memory and have all your I/O routines reorder your data when going from memory to disk or visa versa, or use numpy's mechanism for mapping the first index to the most rapidly varying data. We recommend the former if possible. The disadvantage of the latter is that many of numpy's functions will yield arrays without Fortran ordering unless you are careful to use the 'order' keyword. Doing this would be highly inconvenient.

Otherwise we recommend simply learning to reverse the usual order of indices when accessing elements of an array. Granted, it goes against the grain, but it is more in line with Python semantics and the natural order of the data.

\title{
NUMPY AND SWIG
}

\subsection*{7.1 Numpy.i: a SWIG Interface File for NumPy}

\subsection*{7.1.1 Introduction}

The Simple Wrapper and Interface Generator (or SWIG) is a powerful tool for generating wrapper code for interfacing to a wide variety of scripting languages. SWIG can parse header files, and using only the code prototypes, create an interface to the target language. But SWIG is not omnipotent. For example, it cannot know from the prototype:
double rms (double* seq, int \(n\) );
what exactly seq is. Is it a single value to be altered in-place? Is it an array, and if so what is its length? Is it input-only? Output-only? Input-output? SWIG cannot determine these details, and does not attempt to do so.

If we designed rms, we probably made it a routine that takes an input-only array of length \(n\) of double values called seq and returns the root mean square. The default behavior of SWIG, however, will be to create a wrapper function that compiles, but is nearly impossible to use from the scripting language in the way the C routine was intended.

For Python, the preferred way of handling contiguous (or technically, strided) blocks of homogeneous data is with NumPy, which provides full object-oriented access to multidimensial arrays of data. Therefore, the most logical Python interface for the rms function would be (including doc string):
```

def rms(seq):
"" "
rms: return the root mean square of a sequence
rms(numpy.ndarray) -> double
rms(list) -> double
rms(tuple) -> double
"""

```
where seq would be a NumPy array of double values, and its length \(n\) would be extracted from seq internally before being passed to the C routine. Even better, since NumPy supports construction of arrays from arbitrary Python sequences, seq itself could be a nearly arbitrary sequence (so long as each element can be converted to a double) and the wrapper code would internally convert it to a NumPy array before extracting its data and length.
SWIG allows these types of conversions to be defined via a mechanism called typemaps. This document provides information on how to use numpy.i, a SWIG interface file that defines a series of typemaps intended to make the type of array-related conversions described above relatively simple to implement. For example, suppose that the rms function prototype defined above was in a header file named rms.h. To obtain the Python interface discussed above, your SWIG interface file would need the following:
```

%{
\#define SWIG_FILE_WITH_INIT

```
```

\#include "rms.h"
%}
%include "numpy.i"
%init %{
import_array();
%}
%apply (double* IN_ARRAY1, int DIM1) {(double* seq, int n)};
%include "rms.h"

```

Typemaps are keyed off a list of one or more function arguments, either by type or by type and name. We will refer to such lists as signatures. One of the many typemaps defined by numpy.i is used above and has the signature (double* IN_ARRAY1, int DIM1). The argument names are intended to suggest that the double* argument is an input array of one dimension and that the int represents that dimension. This is precisely the pattern in the rms prototype.

Most likely, no actual prototypes to be wrapped will have the argument names IN_ARRAY1 and DIM1. We use the \%apply directive to apply the typemap for one-dimensional input arrays of type double to the actual prototype used by rms. Using numpy. i effectively, therefore, requires knowing what typemaps are available and what they do.

A SWIG interface file that includes the SWIG directives given above will produce wrapper code that looks something like:
```

PyObject *_wrap_rms(PyObject *args) {
PyObject *resultobj = 0;
double *arg1 = (double *) 0 ;
int arg2 ;
double result;
PyArrayObject *array1 = NULL ;
int is_new_object1 = 0 ;
PyObject * obj0 = 0 ;
if (!PyArg_ParseTuple(args,(char *)"O:rms", \&obj0)) SWIG_fail;
{
array1 = obj_to_array_contiguous_allow_conversion(
obj0, NPY_DOUBLE, \&is_new_object1);
npy_intp size[1] = {
-1
};
if (!array1 || !require_dimensions(array1, 1) ||
!require_size(array1, size, 1)) SWIG_fail;
arg1 = (double*) array1->data;
arg2 = (int) array1->dimensions[0];
}
result = (double)rms(arg1,arg2);
resultobj = SWIG_From_double((double)(result));
{
if (is_new_object1 \&\& array1) Py_DECREF(array1);
}
return resultobj;
fail:
{
if (is_new_object1 \&\& array1) Py_DECREF(array1);
}
return NULL;
}

```

The typemaps from numpy.i are responsible for the following lines of code: 12-20, 25 and 30 . Line 10 parses the input to the rms function. From the format string " \(\mathrm{O}: \mathrm{rms}\) ", we can see that the argument list is expected to be a single Python object (specified by the O before the colon) and whose pointer is stored in obj0. A number of functions, supplied by numpy.i, are called to make and check the (possible) conversion from a generic Python object to a NumPy array. These functions are explained in the section Helper Functions, but hopefully their names are selfexplanatory. At line 12 we use objo to construct a NumPy array. At line 17, we check the validity of the result: that it is non-null and that it has a single dimension of arbitrary length. Once these states are verified, we extract the data buffer and length in lines 19 and 20 so that we can call the underlying \(C\) function at line 22 . Line 25 performs memory management for the case where we have created a new array that is no longer needed.

This code has a significant amount of error handling. Note the SWIG_fail is a macro for goto fail, refering to the label at line 28. If the user provides the wrong number of arguments, this will be caught at line 10 . If construction of the NumPy array fails or produces an array with the wrong number of dimensions, these errors are caught at line 17. And finally, if an error is detected, memory is still managed correctly at line 30.

Note that if the C function signature was in a different order:
```

double rms(int n, double* seq)

```
that SWIG would not match the typemap signature given above with the argument list for rms. Fortunately, numpy.i has a set of typemaps with the data pointer given last:
\%apply (int DIM1, double* IN_ARRAY1) \{(int \(n\), double* seq) \};
This simply has the effect of switching the definitions of arg1 and arg2 in lines 3 and 4 of the generated code above, and their assignments in lines 19 and 20.

\subsection*{7.1.2 Using numpy.i}

The numpy.i file is currently located in the numpy/docs/swig sub-directory under the numpy installation directory. Typically, you will want to copy it to the directory where you are developing your wrappers. If it is ever adopted by SWIG developers, then it will be installed in a standard place where SWIG can find it.

A simple module that only uses a single SWIG interface file should include the following:
```

% {
\#define SWIG_FILE_WITH_INIT
% }
%include "numpy.i"
%init %{
import_array();
% }

```

Within a compiled Python module, import_array () should only get called once. This could be in a C/C++ file that you have written and is linked to the module. If this is the case, then none of your interface files should \#define SWIG_FILE_WITH_INIT or call import_array (). Or, this initialization call could be in a wrapper file generated by SWIG from an interface file that has the \%init block as above. If this is the case, and you have more than one SWIG interface file, then only one interface file should \#define SWIG_FILE_WITH_INIT and call import_array().

\subsection*{7.1.3 Available Typemaps}

The typemap directives provided by numpy. i for arrays of different data types, say double and int, and dimensions of different types, say int or long, are identical to one another except for the C and NumPy type specifications. The typemaps are therefore implemented (typically behind the scenes) via a macro:
\%numpy_typemaps (DATA_TYPE, DATA_TYPECODE, DIM_TYPE)
that can be invoked for appropriate (DATA_TYPE, DATA_TYPECODE, DIM_TYPE) triplets. For example:
\%numpy_typemaps(double, NPY_DOUBLE, int)
\%numpy_typemaps(int, NPY_INT , int)
The numpy.i interface file uses the \%numpy_typemaps macro to implement typemaps for the following C data types and int dimension types:
- signed char
- unsigned char
- short
- unsigned short
- int
- unsigned int
- long
- unsigned long
- long long
- unsigned long long
- float
- double

In the following descriptions, we reference a generic DATA_TYPE, which could be any of the C data types listed above, and DIM_TYPE which should be one of the many types of integers.
The typemap signatures are largely differentiated on the name given to the buffer pointer. Names with FARRAY are for FORTRAN-ordered arrays, and names with ARRAY are for C-ordered (or 1D arrays).

\section*{Input Arrays}

Input arrays are defined as arrays of data that are passed into a routine but are not altered in-place or returned to the user. The Python input array is therefore allowed to be almost any Python sequence (such as a list) that can be converted to the requested type of array. The input array signatures are

1D:
- ( DATA_TYPE IN_ARRAY1[ANY] )
- ( DATA_TYPE* IN_ARRAY1, int DIM1 )
- ( int DIM1, DATA_TYPE* IN_ARRAY1 )

2D:
- ( DATA_TYPE IN_ARRAY2[ANY][ANY] )
- ( DATA_TYPE* IN_ARRAY2, int DIM1, int DIM2 )
- ( int DIM1, int DIM2, DATA_TYPE* IN_ARRAY2 )
- ( DATA_TYPE* IN_FARRAY2, int DIM1, int DIM2 )
- ( int DIM1, int DIM2, DATA_TYPE* IN_FARRAY2 )

3D:
- ( DATA_TYPE IN_ARRAY3[ANY][ANY][ANY] )
- ( DATA_TYPE* IN_ARRAY3, int DIM1, int DIM2, int DIM3 )
- ( int DIM1, int DIM2, int DIM3, DATA_TYPE* IN_ARRAY3 )
- ( DATA_TYPE* IN_FARRAY3, int DIM1, int DIM2, int DIM3 )
- ( int DIM1, int DIM2, int DIM3, DATA_TYPE* IN_FARRAY3 )

The first signature listed, ( DATA_TYPE IN_ARRAY [ANY] ) is for one-dimensional arrays with hard-coded dimensions. Likewise, ( DATA_TYPE IN_ARRAY2 [ANY] [ANY] ) is for two-dimensional arrays with hard-coded dimensions, and similarly for three-dimensional.

\section*{In-Place Arrays}

In-place arrays are defined as arrays that are modified in-place. The input values may or may not be used, but the values at the time the function returns are significant. The provided Python argument must therefore be a NumPy array of the required type. The in-place signatures are
1D:
- ( DATA_TYPE INPLACE_ARRAY1[ANY] )
- ( DATA_TYPE* INPLACE_ARRAY1, int DIM1 )
- ( int DIM1, DATA_TYPE* INPLACE_ARRAY1 )

2D:
- ( DATA_TYPE INPLACE_ARRAY2[ANY][ANY] )
- ( DATA_TYPE* INPLACE_ARRAY2, int DIM1, int DIM2 )
- ( int DIM1, int DIM2, DATA_TYPE* INPLACE_ARRAY2 )
- ( DATA_TYPE* INPLACE_FARRAY2, int DIM1, int DIM2 )
- ( int DIM1, int DIM2, DATA_TYPE* INPLACE_FARRAY2 )

3D:
- ( DATA_TYPE INPLACE_ARRAY3[ANY][ANY][ANY] )
- ( DATA_TYPE* INPLACE_ARRAY3, int DIM1, int DIM2, int DIM3 )
- ( int DIM1, int DIM2, int DIM3, DATA_TYPE* INPLACE_ARRAY3 )
- ( DATA_TYPE* INPLACE_FARRAY3, int DIM1, int DIM2, int DIM3 )
- ( int DIM1, int DIM2, int DIM3, DATA_TYPE* INPLACE_FARRAY3 )

These typemaps now check to make sure that the INP LACE_ARRAY arguments use native byte ordering. If not, an exception is raised.

\section*{Argout Arrays}

Argout arrays are arrays that appear in the input arguments in C, but are in fact output arrays. This pattern occurs often when there is more than one output variable and the single return argument is therefore not sufficient. In Python, the convential way to return multiple arguments is to pack them into a sequence (tuple, list, etc.) and return the sequence. This is what the argout typemaps do. If a wrapped function that uses these argout typemaps has more than one return argument, they are packed into a tuple or list, depending on the version of Python. The Python user does not pass
these arrays in, they simply get returned. For the case where a dimension is specified, the python user must provide that dimension as an argument. The argout signatures are
1D:
- ( DATA_TYPE ARGOUT_ARRAY1[ANY] )
- ( DATA_TYPE* ARGOUT_ARRAY1, int DIM1 )
- ( int DIM1, DATA_TYPE* ARGOUT_ARRAY1 )

2D:
- ( DATA_TYPE ARGOUT_ARRAY2[ANY][ANY] )

3D:
- ( DATA_TYPE ARGOUT_ARRAY3[ANY][ANY][ANY] )

These are typically used in situations where in \(\mathrm{C} / \mathrm{C}++\), you would allocate \(\mathrm{a}(\mathrm{n})\) array(s) on the heap, and call the function to fill the array(s) values. In Python, the arrays are allocated for you and returned as new array objects.
Note that we support DATA_TYPE* argout typemaps in 1D, but not 2D or 3D. This is because of a quirk with the SWIG typemap syntax and cannot be avoided. Note that for these types of 1D typemaps, the Python function will take a single argument representing DIM1.

\section*{Argoutview Arrays}

Argoutview arrays are for when your \(C\) code provides you with a view of its internal data and does not require any memory to be allocated by the user. This can be dangerous. There is almost no way to guarantee that the internal data from the C code will remain in existence for the entire lifetime of the NumPy array that encapsulates it. If the user destroys the object that provides the view of the data before destroying the NumPy array, then using that array my result in bad memory references or segmentation faults. Nevertheless, there are situations, working with large data sets, where you simply have no other choice.

The C code to be wrapped for argoutview arrays are characterized by pointers: pointers to the dimensions and double pointers to the data, so that these values can be passed back to the user. The argoutview typemap signatures are therefore

1D:
- ( DATA_TYPE** ARGOUTVIEW_ARRAY1, DIM_TYPE* DIM1 )
- ( DIM_TYPE* DIM1, DATA_TYPE** ARGOUTVIEW_ARRAY1 )

2D:
- ( DATA_TYPE** ARGOUTVIEW_ARRAY2, DIM_TYPE* DIM1, DIM_TYPE* DIM2 )
- ( DIM_TYPE* DIM1, DIM_TYPE* DIM2, DATA_TYPE** ARGOUTVIEW_ARRAY2 )
- ( DATA_TYPE** ARGOUTVIEW_FARRAY2, DIM_TYPE* DIM1, DIM_TYPE* DIM2 )
- ( DIM_TYPE* DIM1, DIM_TYPE* DIM2, DATA_TYPE** ARGOUTVIEW_FARRAY2 )

3D:
- ( DATA_TYPE** ARGOUTVIEW_ARRAY3, DIM_TYPE* DIM1, DIM_TYPE* DIM2, DIM_TYPE* DIM3)
- ( DIM_TYPE* DIM1, DIM_TYPE* DIM2, DIM_TYPE* DIM3, DATA_TYPE** ARGOUTVIEW_ARRAY3)
- ( DATA_TYPE** ARGOUTVIEW_FARRAY3, DIM_TYPE* DIM1, DIM_TYPE* DIM2, DIM_TYPE* DIM3)
```

•( DIM_TYPE* DIM1, DIM_TYPE* DIM2, DIM_TYPE* DIM3, DATA_TYPE**
ARGOUTVIEW_FARRAY3)

```

Note that arrays with hard-coded dimensions are not supported. These cannot follow the double pointer signatures of these typemaps.

\section*{Output Arrays}

The numpy.i interface file does not support typemaps for output arrays, for several reasons. First, C/C++ return arguments are limited to a single value. This prevents obtaining dimension information in a general way. Second, arrays with hard-coded lengths are not permitted as return arguments. In other words:
```

double[3] newVector(double x, double y, double z);

```
is not legal C/C++ syntax. Therefore, we cannot provide typemaps of the form:
\%typemap (out) (TYPE[ANY]);
If you run into a situation where a function or method is returning a pointer to an array, your best bet is to write your own version of the function to be wrapped, either with \%extend for the case of class methods or \%ignore and \%rename for the case of functions.

\section*{Other Common Types: bool}

Note that C++ type bool is not supported in the list in the Available Typemaps section. NumPy bools are a single byte, while the C++ bool is four bytes (at least on my system). Therefore:
```

%numpy_typemaps(bool, NPY_BOOL, int)

```
will result in typemaps that will produce code that reference improper data lengths. You can implement the following macro expansion:
\%numpy_typemaps(bool, NPY_UINT, int)
to fix the data length problem, and Input Arrays will work fine, but In-Place Arrays might fail type-checking.

\section*{Other Common Types: complex}

Typemap conversions for complex floating-point types is also not supported automatically. This is because Python and NumPy are written in C, which does not have native complex types. Both Python and NumPy implement their own (essentially equivalent) struct definitions for complex variables:
```

/* Python */
typedef struct {double real; double imag;} Py_complex;
/* NumPy */
typedef struct {float real, imag;} npy_cfloat;
typedef struct {double real, imag;} npy_cdouble;

```

We could have implemented:
```

%numpy_typemaps(Py_complex , NPY_CDOUBLE, int)
%numpy_typemaps(npy_cfloat , NPY_CFLOAT , int)
%numpy_typemaps(npy_cdouble, NPY_CDOUBLE, int)

```
which would have provided automatic type conversions for arrays of type Py_complex, npy_cfloat and npy_cdouble. However, it seemed unlikely that there would be any independent (non-Python, non-NumPy) application code that people would be using SWIG to generate a Python interface to, that also used these definitions for complex types. More likely, these application codes will define their own complex types, or in the case of C++, use std: : complex. Assuming these data structures are compatible with Python and NumPy complex types, \%numpy_typemap expansions as above (with the user's complex type substituted for the first argument) should work.

\subsection*{7.1.4 NumPy Array Scalars and SWIG}

SWIG has sophisticated type checking for numerical types. For example, if your \(\mathrm{C} / \mathrm{C}++\) routine expects an integer as input, the code generated by SWIG will check for both Python integers and Python long integers, and raise an overflow error if the provided Python integer is too big to cast down to a C integer. With the introduction of NumPy scalar arrays into your Python code, you might conceivably extract an integer from a NumPy array and attempt to pass this to a SWIG-wrapped C/C++ function that expects an int, but the SWIG type checking will not recognize the NumPy array scalar as an integer. (Often, this does in fact work - it depends on whether NumPy recognizes the integer type you are using as inheriting from the Python integer type on the platform you are using. Sometimes, this means that code that works on a 32-bit machine will fail on a 64-bit machine.)

If you get a Python error that looks like the following:
```

TypeError: in method 'MyClass_MyMethod', argument 2 of type 'int'

```
and the argument you are passing is an integer extracted from a NumPy array, then you have stumbled upon this problem. The solution is to modify the SWIG type conversion system to accept ' \({ }^{\text {Numpy }}{ }^{6}\) _ array scalars in addition to the standard integer types. Fortunately, this capabilitiy has been provided for you. Simply copy the file:
```

pyfragments.swg

```
to the working build directory for you project, and this problem will be fixed. It is suggested that you do this anyway, as it only increases the capabilities of your Python interface.

\section*{Why is There a Second File?}

The SWIG type checking and conversion system is a complicated combination of C macros, SWIG macros, SWIG typemaps and SWIG fragments. Fragments are a way to conditionally insert code into your wrapper file if it is needed, and not insert it if not needed. If multiple typemaps require the same fragment, the fragment only gets inserted into your wrapper code once.

There is a fragment for converting a Python integer to a C long. There is a different fragment that converts a Python integer to a C int, that calls the rountine defined in the long fragment. We can make the changes we want here by changing the definition for the long fragment. SWIG determines the active definition for a fragment using a "first come, first served" system. That is, we need to define the fragment for long conversions prior to SWIG doing it internally. SWIG allows us to do this by putting our fragment definitions in the file pyfragments.swg. If we were to put the new fragment definitions in numpy. \(i\), they would be ignored.

\subsection*{7.1.5 Helper Functions}

The numpy. i file containes several macros and routines that it uses internally to build its typemaps. However, these functions may be useful elsewhere in your interface file. These macros and routines are implemented as fragments, which are described briefly in the previous section. If you try to use one or more of the following macros or functions, but your compiler complains that it does not recognize the symbol, then you need to force these fragments to appear in your code using:
```

%fragment("NumPy_Fragments");

```
in your SWIG interface file.

\section*{Macros}

\section*{is_array(a)}

Evaluates as true if a is non-NULL and can be cast to a PyArrayObject*.
array_type(a)
Evaluates to the integer data type code of a, assuming a can be cast to a PyArrayObject *.
array_numdims(a)
Evaluates to the integer number of dimensions of \(a\), assuming \(a\) can be cast to \(a\) PyArrayObject*.
array_dimensions(a)
Evaluates to an array of type npy_intp and length array_numdims (a), giving the lengths of all of the dimensions of a, assuming a can be cast to a PyArrayObject*.
array_size \((\mathbf{a}, \mathbf{i})\)
Evaluates to the i-th dimension size of a, assuming a can be cast to a PyArrayObject*.
array_data(a)
Evaluates to a pointer of type void \(\star\) that points to the data buffer of a, assuming a can be cast to a PyArrayObject*.

\section*{array_is_contiguous(a)}

Evaluates as true if a is a contiguous array. Equivalent to (PyArray_ISCONTIGUOUS (a)).
array_is_native(a)
Evaluates as true if the data buffer of a uses native byte order. Equivalent to (PyArray_ISNOTSWAPPED (a)).
array_is_fortran(a)
Evaluates as true if a is FORTRAN ordered.

\section*{Routines}

\section*{pytype_string()}

Return type: char*
Arguments:
- PyObject* py_obj, a general Python object.

Return a string describing the type of py_obj.
typecode_string()
Return type: char*
Arguments:
- int typecode, a NumPy integer typecode.

Return a string describing the type corresponding to the NumPy typecode.
type_match()

Return type: int
Arguments:
- int actual_type, the NumPy typecode of a NumPy array.
- int desired_type, the desired NumPy typecode.

Make sure that actual_type is compatible with desired_type. For example, this allows character and byte types, or int and long types, to match. This is now equivalent to PyArray_EquivTypenums().
obj_to_array_no_conversion()
Return type: PyArrayObject*
Arguments:
- PyObject* input, a general Python object.
- int typecode, the desired NumPy typecode.

Cast input to a PyArrayobject* if legal, and ensure that it is of type typecode. If input cannot be cast, or the typecode is wrong, set a Python error and return NULL.
obj_to_array_allow_conversion()
Return type: PyArrayObject*
Arguments:
- PyObject* input, a general Python object.
- int typecode, the desired NumPy typecode of the resulting array.
- int* is_new_object, returns a value of 0 if no conversion performed, else 1.

Convert input to a NumPy array with the given typecode. On success, return a valid PyArrayObject* with the correct type. On failure, the Python error string will be set and the routine returns NULL.

\section*{make_contiguous()}

Return type: PyArrayObject*
Arguments:
- PyArrayObject* ary, a NumPy array.
- int* is_new_object, returns a value of 0 if no conversion performed, else 1.
- int min_dims, minimum allowable dimensions.
- int max_dims, maximum allowable dimensions.

Check to see if ary is contiguous. If so, return the input pointer and flag it as not a new object. If it is not contiguous, create a new PyArrayObject* using the original data, flag it as a new object and return the pointer.

\section*{obj_to_array_contiguous_allow_conversion()}

Return type: PyArrayObject*
Arguments:
- PyObject* input, a general Python object.
- int typecode, the desired NumPy typecode of the resulting array.
- int* is_new_object, returns a value of 0 if no conversion performed, else 1.

Convert input to a contiguous PyArrayObject * of the specified type. If the input object is not a contiguous PyArrayObject*, a new one will be created and the new object flag will be set.
require_contiguous()
Return type: int
Arguments:
- PyArrayObject* ary, a NumPy array.

Test whether ary is contiguous. If so, return 1. Otherwise, set a Python error and return 0 .
require_native()
Return type: int
Arguments:
- PyArray_Object* ary, a NumPy array.

Require that ary is not byte-swapped. If the array is not byte-swapped, return 1. Otherwise, set a Python error and return 0.
require_dimensions()
Return type: int
Arguments:
- PyArrayObject* ary, a NumPy array.
- int exact_dimensions, the desired number of dimensions.

Require ary to have a specified number of dimensions. If the array has the specified number of dimensions, return 1. Otherwise, set a Python error and return 0.
require_dimensions_n()
Return type: int
Arguments:
- PyArrayObject* ary, a NumPy array.
- int* exact_dimensions, an array of integers representing acceptable numbers of dimensions.
- int \(n\), the length of exact_dimensions.

Require ary to have one of a list of specified number of dimensions. If the array has one of the specified number of dimensions, return 1. Otherwise, set the Python error string and return 0 .
require_size()
Return type: int
Arguments:
- PyArrayObject* ary, a NumPy array.
- npy_int* size, an array representing the desired lengths of each dimension.
- int \(n\), the length of size.

Require ary to have a specified shape. If the array has the specified shape, return 1. Otherwise, set the Python error string and return 0 .

\section*{require_fortran()}

Return type: int
Arguments:
- PyArrayObject* ary, a NumPy array.

Require the given PyArrayObject to to be FORTRAN ordered. If the the PyArrayObject is already FORTRAN ordered, do nothing. Else, set the FORTRAN ordering flag and recompute the strides.

\subsection*{7.1.6 Beyond the Provided Typemaps}

There are many C or C++ array/NumPy array situations not covered by a simple \%include "numpy.i" and subsequent \%apply directives.

\section*{A Common Example}

Consider a reasonable prototype for a dot product function:
```

double dot(int len, double* vec1, double* vec2);

```

The Python interface that we want is:
```

def dot(vec1, vec2):
"""
dot(PyObject, PyObject) -> double
"""

```

The problem here is that there is one dimension argument and two array arguments, and our typemaps are set up for dimensions that apply to a single array (in fact, SWIG does not provide a mechanism for associating len with vec2 that takes two Python input arguments). The recommended solution is the following:
```

%apply (int DIM1, double* IN_ARRAY1) {(int len1, double* vec1),
(int len2, double* vec2)}
%rename (dot) my_dot;
%exception my_dot {
\$action
if (PyErr_Occurred()) SWIG_fail;
}
%inline %{
double my_dot(int len1, double* vec1, int len2, double* vec2) {
if (len1 != len2) {
PyErr_Format(PyExc_ValueError,
"Arrays of lengths (%d,%d) given",
len1, len2);
return 0.0;
}
return dot(len1, vec1, vec2);
}
%}

```

If the header file that contains the prototype for double \(\operatorname{dot}()\) also contains other prototypes that you want to wrap, so that you need to \%include this header file, then you will also need a \%ignore dot; directive, placed
after the \%rename and before the \%include directives. Or, if the function in question is a class method, you will want to use \%extend rather than \%inline in addition to \%ignore.

A note on error handling: Note that my_dot returns a double but that it can also raise a Python error. The resulting wrapper function will return a Python float representation of 0.0 when the vector lengths do not match. Since this is not NULL, the Python interpreter will not know to check for an error. For this reason, we add the \%exception directive above for my_dot to get the behavior we want (note that \(\$\) action is a macro that gets expanded to a valid call to my_dot). In general, you will probably want to write a SWIG macro to perform this task.

\section*{Other Situations}

There are other wrapping situations in which numpy.i may be helpful when you encounter them.
- In some situations, it is possible that you could use the \%numpy_templates macro to implement typemaps for your own types. See the Other Common Types: bool or Other Common Types: complex sections for examples. Another situation is if your dimensions are of a type other than int (say long for example):
```

%numpy_typemaps(double, NPY_DOUBLE, long)

```
- You can use the code in numpy. i to write your own typemaps. For example, if you had a four-dimensional array as a function argument, you could cut-and-paste the appropriate three-dimensional typemaps into your interface file. The modifications for the fourth dimension would be trivial.
- Sometimes, the best approach is to use the \%extend directive to define new methods for your classes (or overload existing ones) that take a PyObject * (that either is or can be converted to a PyArrayObject*) instead of a pointer to a buffer. In this case, the helper routines in numpy. i can be very useful.
- Writing typemaps can be a bit nonintuitive. If you have specific questions about writing SWIG typemaps for NumPy, the developers of numpy.i do monitor the Numpy-discussion and Swig-user mail lists.

\section*{A Final Note}

When you use the \%apply directive, as is usually necessary to use numpy.i, it will remain in effect until you tell SWIG that it shouldn't be. If the arguments to the functions or methods that you are wrapping have common names, such as length or vector, these typemaps may get applied in situations you do not expect or want. Therefore, it is always a good idea to add a \%clear directive after you are done with a specific typemap:
```

%apply (double* IN_ARRAY1, int DIM1) {(double* vector, int length)}
%include "my_header.h"
%clear (double* vector, int length);

```

In general, you should target these typemap signatures specifically where you want them, and then clear them after you are done.

\subsection*{7.1.7 Summary}

Out of the box, numpy.i provides typemaps that support conversion between NumPy arrays and C arrays:
- That can be one of 12 different scalar types: signed char, unsigned char, short, unsigned short, int, unsigned int, long, unsigned long, long long, unsigned long long, float and double.
- That support 41 different argument signatures for each data type, including:
- One-dimensional, two-dimensional and three-dimensional arrays.
- Input-only, in-place, argout and argoutview behavior.
- Hard-coded dimensions, data-buffer-then-dimensions specification, and dimensions-then-data-buffer specification.
- Both C-ordering ("last dimension fastest") or FORTRAN-ordering ("first dimension fastest") support for 2D and 3D arrays.

The numpy. i interface file also provides additional tools for wrapper developers, including:
- A SWIG macro (\%numpy_typemaps) with three arguments for implementing the 41 argument signatures for the user's choice of (1) C data type, (2) NumPy data type (assuming they match), and (3) dimension type.
- Nine C macros and 13 C functions that can be used to write specialized typemaps, extensions, or inlined functions that handle cases not covered by the provided typemaps.

\subsection*{7.2 Testing the numpy.i Typemaps}

\subsection*{7.2.1 Introduction}

Writing tests for the numpy.i SWIG interface file is a combinatorial headache. At present, 12 different data types are supported, each with 23 different argument signatures, for a total of 276 typemaps supported "out of the box". Each of these typemaps, in turn, might require several unit tests in order to verify expected behavior for both proper and improper inputs. Currently, this results in 1,020 individual unit tests that are performed when make test is run in the numpy/docs / swig subdirectory.

To facilitate this many similar unit tests, some high-level programming techniques are employed, including C and SWIG macros, as well as Python inheritance. The purpose of this document is to describe the testing infrastructure employed to verify that the numpy. i typemaps are working as expected.

\subsection*{7.2.2 Testing Organization}

There are three indepedent testing frameworks supported, for one-, two-, and three-dimensional arrays respectively. For one-dimensional arrays, there are two C++ files, a header and a source, named:

Vector.h
Vector.cxx
that contain prototypes and code for a variety of functions that have one-dimensional arrays as function arguments. The file:

Vector.i
is a SWIG interface file that defines a python module Vector that wraps the functions in Vector. h while utilizing the typemaps in numpy. i to correctly handle the C arrays.

The Makefile calls swig to generate Vector.py and Vector_wrap.cxx, and also executes the setup.py script that compiles Vector_wrap.cxx and links together the extension module _Vector.so or _Vector. dylib, depending on the platform. This extension module and the proxy file Vector.py are both placed in a subdirectory under the build directory.
The actual testing takes place with a Python script named:
testVector.py
that uses the standard Python library module unittest, which performs several tests of each function defined in Vector. \(h\) for each data type supported.

Two-dimensional arrays are tested in exactly the same manner. The above description applies, but with Matrix substituted for Vector. For three-dimensional tests, substitute Tensor for Vector. For the descriptions that follow, we will reference the Vector tests, but the same information applies to Matrix and Tensor tests.

The command make test will ensure that all of the test software is built and then run all three test scripts.

\subsection*{7.2.3 Testing Header Files}

Vector.h is a C++ header file that defines a C macro called TEST_FUNC_PROTOS that takes two arguments: TYPE, which is a data type name such as unsigned int; and SNAME, which is a short name for the same data type with no spaces, e.g. uint. This macro defines several function prototypes that have the prefix SNAME and have at least one argument that is an array of type TYPE. Those functions that have return arguments return a TYPE value.

TEST_FUNC_PROTOS is then implemented for all of the data types supported by numpy.i:
- signed char
- unsigned char
- short
- unsigned short
- int
- unsigned int
- long
- unsigned long
- long long
- unsigned long long
- float
- double

\subsection*{7.2.4 Testing Source Files}

Vector.cxx is a C++ source file that implements compilable code for each of the function prototypes specified in Vector.h. It defines a C macro TEST_FUNCS that has the same arguments and works in the same way as TEST_FUNC_PROTOS does in Vector.h. TEST_FUNCS is implemented for each of the 12 data types as above.

\subsection*{7.2.5 Testing SWIG Interface Files}

Vector.i is a SWIG interface file that defines python module Vector. It follows the conventions for using numpy.i as described in this chapter. It defines a SWIG macro \%apply_numpy_typemaps that has a single argument TYPE. It uses the SWIG directive \%apply to apply the provided typemaps to the argument signatures found in Vector.h. This macro is then implemented for all of the data types supported by numpy.i. It then does a \%include "Vector.h" to wrap all of the function prototypes in Vector.h using the typemaps in numpy.i.

\subsection*{7.2.6 Testing Python Scripts}

After make is used to build the testing extension modules, testVector.py can be run to execute the tests. As with other scripts that use unittest to facilitate unit testing, testVector.py defines a class that inherits from unittest.TestCase:
```

class VectorTestCase(unittest.TestCase):

```

However, this class is not run directly. Rather, it serves as a base class to several other python classes, each one specific to a particular data type. The VectorTestCase class stores two strings for typing information:

\section*{self.typeStr}

A string that matches one of the SNAME prefixes used in Vector.h and Vector.cxx. For example, "double".

\section*{self.typeCode}

A short (typically single-character) string that represents a data type in numpy and corresponds to self.typeStr. For example, if self.typeStr is "double", then self.typeCode should be "d".

Each test defined by the VectorTestCase class extracts the python function it is trying to test by accessing the Vect or module's dictionary:
length = Vector.__dict__[self.typeStr + "Length"]
In the case of double precision tests, this will return the python function Vector. doubleLength.
We then define a new test case class for each supported data type with a short definition such as:
```

class doubleTestCase(VectorTestCase):
def __init__(self, methodName="runTest")
VectorTestCase.__init__(self, methodName)
self.typeStr = "double"
self.typeCode = "d"

```

Each of these 12 classes is collected into a unittest. TestSuite, which is then executed. Errors and failures are summed together and returned as the exit argument. Any non-zero result indicates that at least one test did not pass.

\section*{ACKNOWLEDGEMENTS}

Large parts of this manual originate from Travis E. Oliphant's book Guide to Numpy (which generously entered Public Domain in August 2008). The reference documentation for many of the functions are written by numerous contributors and developers of Numpy, both prior to and during the Numpy Documentation Marathon.

Please help to improve NumPy's documentation! Instructions on how to join the ongoing documentation marathon can be found on the scipy.org website

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[^0]:    ${ }^{1}$ However, array scalars are immutable, so none of the array scalar attributes are settable.

[^1]:    setbufsize(size) Set the size of the buffer used in ufuncs.
    numpy.setbufsize (size)

[^2]:    maximum(x1) Element-wise maximum of array elements.

[^3]:    numpy. random. rand $(d 0, d l, \ldots, d n)$

[^4]:    ma.MaskType Numpy's Boolean type. Character code: ?. Alias: bool8
    numpy.ma.MaskType
    alias of bool_

[^5]:    info([object, maxwidth, output, toplevel]) Get help information for a function, class, or module. source(object[, output]) Print or write to a file the source code for a Numpy object.

